Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

# 1 Introduction

MATLAB is a *prototyping* environment, meaning it focuses on the ease of development with language flexibility, interactive debugging, and other conveniences lacking in performance-oriented languages like C and FORTRAN. While MATLAB may not be as fast as C, there are ways to bring it closer.

**Disclaimer** This is not a beginner's tutorial to MATLAB, but a tutorial on performance. The methods discussed here are generally fast, but *no claim is made* on what is fastest. Use at your own risk.

Before beginning our main topic, let's step back for a moment and ask ourselves what we really want. Do we want the fastest possible code?—if so, we should switch to a performance language like C. Probably more accurately, we want to spend less time *total* from developing, debugging, running, and until finally obtaining results. This section gives some tips on working smart, not hard.

## Assignment Project Exam Help

#### M-Lint Messages

In more recent versions of MASAB/the Delword of the flat call fire feedback on possible code errors and suggested optimizations. These messages are helpful in improving a program and in learning more about MATLAB.

Hold the mouse cursor over underlined code to read a message. Or, see all M-Lint messages at once with Tools  $\rightarrow$  M-Lint  $\rightarrow$  Show M-Lint Report.

#### **Organization**

• Use a separate folder for each project.

A separate folder for each project keeps related things together and simplifies making copies and backups of project files.

• Write header comments, especially H1.

The first line of the header comment is called the H1 comment. Type help(cd) to get a listing of all project files and their H1 comments.

#### • Save frequent console commands as a script.

If you find yourself repeating certain commands on the console, save them as a script. Less typing means fewer opportunities for typos.

#### Avoid losing data

#### • Don't use clear all in a script.

This is an unfortunate common practice—any important variables in the base workspace will be irretrievably lost.

#### • Beware of clobber.

"File clobber" refers to the kind of data loss when a file is accidentally overwritten with another one having the same filename. This phenomenon can occur with variables as well:

>>> result = big\_operation(input1); % Store the result of a time\_consuming operation
...Assignment.Project.ExampHelp

Variable result was clobbered and the first output was lost.

### Beware of what types by MOWCOder.com

While MATLAB is generally reliable, crashes are possible when using third-party MEX functions or extremely memory-intensive operations, for example, with video and very large arrays.

Now with good working habits covered, we begin our discussion of writing fast MATLAB code. The rest of this article is organized by topic, first on techniques that are useful in general application, and next on specific computational topics (table of contents is on the first page).

# 2 The Profiler

MATLAB 5.0 (R10) and newer versions include a tool called the profiler that helps identify bottlenecks in a program. Use it with the profile command:

For example, consider profiling the following function:

```
function result = example1(Count)

for k = 1:Count
    result(k) = sin(k/50);

    if result(k) < -0.9
        real SSISTIMENT Project Exam Help
end</pre>
```

To analyze the efficiency this function, first enable and dear the profiler, run the function, and then view the profile report 100 S.//powcoder.com

```
>> profile on, profile clear  
>> example1(5000);  
>> profile report Add\ WeChat\ powcoder
```

There is a slight parsing overhead when running code for the first time; run the test code twice and time the second run. The profiler report command shows a report. Depending on the system, profiler results may differ from this example.

### MATLAB Profile Report: Summary

Report generated 30-Jul-2004 16:57:01

Total recorded time: 3.09 s Number of M-functions: 4 Clock precision: 0.016 s

#### **Function List**

Name	Time		Time	Time/call	Self time		Location	
example1	3.09	100.0%	1	3.094000	2.36	76.3%	~/example1.m	
gammaln	0.73	23.7%	3562	0.000206	0.73	23.7%	/toolbox/matlab/specfun/gammaln.m	
profile	0.00	0.0%	1	0.000000	0.00	0.0%	/toolbox/matlab/general/profile.m	
profreport	0.00	0.0%	1	0.000000	0.00	0.0%	/toolbox/matlab/general/profreport.m	

Clicking the "example1" link gives more details:

#### Lines where the most time was spent

Line Number	Code	Calls	Total Time	% Time
4	result(k) = sin(k/50);	5000	2.11 s	68%
<u>7</u>	<pre>result(k) = gammaln(k);</pre>	721	$0.84~\mathrm{s}$	27%
<u>6</u>	if result(k) $< -0.9$	5000	$0.14 \mathrm{\ s}$	5%
Totals			$3.09 \; s$	100%

The most time-consuming lines are displayed, along with time time percentage, and line number. The most costly lines are the computations on lines Pane 7. LX and TEP

Another helpful section of the profile report is "M-Lint Results," which gives feedback from the M-Lint code analyzer. Possil in trop and suggestion we discorded the code analyzer.

#### M-Lint results

<del></del>				
Line number	Message			
4	'result might be growing inside bloopt Consider preallocating for speed.  'result' might be growing inside a loop. Consider preallocating for speed.			
<u>7</u>	'result' might be growing inside a loop. Consider preallocating for speed.			

(Preallocation is discussed in the next section.)

The profiler has limited time resolution, so to profile a piece of code that runs too quickly, run the test code multiple times with a loop. Adjust the number of loop iterations so that the time it takes to run is noticeable. More iterations yields better time resolution.

The profiler is an essential tool for identifying bottlenecks and per-statement analysis, however, for more accurate timing of a piece of code, use the tic/toc stopwatch timer.

```
>> tic; example1(5000); toc;
Elapsed time is 3.082055 seconds
```

For serious benchmarking, also close your web browser, anti-virus, and other background processes that may be taking CPU cycles.



### **Array Preallocation**

MATLAB's matrix variables have the ability to dynamically augment rows and columns. For example,

MATLAB automatically resizes the matrix. Internally, the matrix data memory must be reallocated with larger size. If a matrix is resized repeatedly—like within a loop—this overhead can be significant. To avoid frequent reallocations, *preallocate* the matrix with the zeros command.

## Consider the Sessignment Project Exam Help

```
a(1) = 1;
b(1) = 0;
for k = 2:8000 https://powcoder.com
a(k) = 0.99803 * a(k-1) + 0.99803 * b(k-1);
b(k) = 0.06279 * a(k-1) + 0.99803 * b(k-1);
```

This code takes 0.47 second to run. After the late of Dohart sale frectors of length 8000, thus to preallocate, create empty a and b row vectors each with 8000 elements.

With this modification, the code takes only 0.14 seconds (over three times faster). Preallocation is often easy to do, in this case it was only necessary to determine the right preallocation size and add two lines.

What if the final array size can vary? Here is an example:

The average run time of this program is 0.42 seconds without preallocation and 0.18 seconds with it.

Preallocation is also beneficial for cell arrays, using the cell command to create a cell array of the desired siz Assignment Project Exam Help

https://powcoder.com

Add WeChat powcoder

# 4 JIT Acceleration

MATLAB 6.5 (R13) and later feature the Just-In-Time (JIT) Accelerator for improving the speed of M-functions, particularly with loops. By knowing a few things about the accelerator, you can improve its performance.

The JIT Accelerator is enabled by default. To disable it, type "feature accel off" in the console, and "feature accel on" to enable it again.

As of Matlab R2008b, only a subset of the Matlab language is supported for acceleration. Upon encountering an unsupported feature, acceleration processing falls back to non-accelerated evaluation. Acceleration is most effective when significant contiguous portions of code are supported.

- Data types: Code must use supported data types for acceleration: double (both real and complex), logical, char, int8-32, uint8-32. Some struct, cell, classdef, and function handle usage is supported. Sparse arrays are not accelerated.
- Array shapes A ray Three of any size (i) in the tever final rays are accelerated.

  A few limited situations with 4D arrays are accelerated.
- Function calls Male Suilt-In the New and Great of the Colling MEX functions and Java interrupts acceleration. (See also page 14 on inlining simple functions.)
- Conditionals and loops: The conditional statements if, elseif, and simple switch statements are supported if the conditional expression explicitly to a water of the form for k=a:b, for k=a:b:c, and while loops are accelerated if all code within the loop is supported.

#### In-place computation

Introduced in Matlab 7.3 (R2006b), the element-wise operators (+, .\*, etc.) and some other functions can be computed in-place. That is, a computation like

```
x = 5*sqrt(x.^2 + 1);
```

is handled internally without needing temporary storage for accumulating the result. An M-function can also be computed in-place if its output argument matches one of the input arguments.

```
x = myfun(x);
function x = myfun(x)
x = 5*sqrt(x.^2 + 1);
return;
```

To enable in-place computation, the in-place operation must be within an M-function (and for an inplace function, the function itself must be called within an M-function). Currently, there is no support for in-place computation with MEX-functions.

#### **Multithreaded Computation**

MATLAB 7.4 (R2007a) introduced multithreaded computation for multicore and multiprocessor computers. Multithreaded computation accelerates some per-element functions when applied to large arrays (for example, .^, sin, exp) and certain linear algebra functions in the BLAS library. To enable it, select File  $\rightarrow$  Preferences  $\rightarrow$  General  $\rightarrow$  Multithreading and select "Enable multithreaded computation." Further control over parallel computation is possible with the Parallel Computing Toolbox<sup>TM</sup> using parfor and spmd.

#### JIT-Accelerated Example

For example, the following loop-heavy code is supported for acceleration:

```
function B = bilateral(A, sd, sr, R)
% The bilateral image denoising filter
      Assignment Project Exam Help
   for j = 1:size(A, 2)
       zsum = 0;
               https://powcoder.com
          if i+m >= 1 && i+m <= size(A,1)</pre>
                         \exp(-(m^2 + n^2)/(2*sr^2));
                    zsum = zsum + z;
                    B(i,j) = B(i,j) + z*A(i+m,j+n);
                 end
             end
          end
      end
      B(i,j) = B(i,j)/zsum;
   end
end
```

For a  $128 \times 128$  input image and R = 3, the run time is 53.3 seconds without acceleration and 0.68 seconds with acceleration.

# 5 Vectorization

A computation is *vectorized* by taking advantage of vector operations. A variety of programming situations can be vectorized, and often improving speed to 10 times faster or even better. Vectorization is one of the most general and effective techniques for writing fast M-code.

#### 5.1 Vectorized Computations

Many standard Matlab functions are "vectorized": they can operate on an array as if the function had been applied individually to every element.

## Consider the following innerion: Project Exam Help

For every point, its distance from the origin is computed and stored in d. For speed, array d is preallocated (see Section 3). The minimum distance is then found with min. To vectorize the distance computation, replace the for loop with vector operations:

The modified code performs the distance computation with vector operations. The x, y and z arrays are first squared using the per-element power operator, .^ (the per-element operators for multiplication and division are .\* and ./). The squared components are added with vector addition. Finally, the square root of the vector sum is computed per element, yielding an array of distances. (A further improvement: it is equivalent to compute  $d = sqrt(min(x.^2 + y.^2 + z.^2))$ ).

The first version of the minDistance program takes 0.73 seconds on 50000 points. The vectorized version takes less than 0.04 seconds, more than 18 times faster.

Some useful functions for vectorizing computations:

```
min, max, repmat, meshgrid, sum, cumsum, diff, prod, cumprod, accumarray
```

#### 5.2 Vectorized Logic

The previous section shows how to vectorize pure computation. But bottleneck code often involves conditional logic. Like computations, Matlab's logic operators are vectorized:

```
>>> [1,5,3] < [2,2,4]
ans =
```

Two arrays are compared per-element. Logic operations return "logical" arrays with binary values. How is this useful? MATLAB has a few powerful functions for operating on logical arrays:

```
» find Assignment of Project Exam Help
```

Vectorized logic also works on arrays.

By default, find returns element locations as indices (see page 16 for indices vs. subscripts).

#### **Example 1: Vector Normalization**

To normalize a single vector  $\mathbf{v}$  to unit length, one can use  $\mathbf{v} = \mathbf{v/norm}(\mathbf{v})$ . However, to use norm for set of vectors  $\mathbf{v}(:,1)$ ,  $\mathbf{v}(:,2)$ , ... requires computing  $\mathbf{v}(:,k)/norm(\mathbf{v}(:,k))$  in a loop. Alternatively,

```
vMag = sqrt(sum(v.^2));
v = v./vMag(ones(1,size(v,1)),:);
```

#### Example 2: Removing elements

The situation often arises where array elements must be removed on some per-element condition. For example, this code removes all NaN and infinite elements from an array x:

```
i = find(isnan(x) \mid isinf(x)); % Find bad elements in x x(i) = []; % and delete them
```

Alternatively,

```
i = find(\tilde{\text{risnan}}(x) & \tilde{\text{risinf}}(x)); % Find elements that are not NaN and not infinite x = x(i) Assignment Project Exam Help
```

Both of these solutions can be further streamlined by using logical indexing:

## Example 3: Picade full ie Chat powcoder

The sinc function has a piecewise definition,

$$\operatorname{sinc}(x) = \begin{cases} \sin(x)/x, & x \neq 0 \\ 1, & x = 0 \end{cases}$$

This code uses find with vectorized computation to handle the two cases separately:

A concise alternative is  $y = (\sin(x) + (x == 0))./(x + (x == 0)).$ 

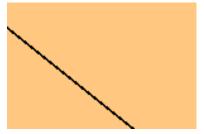
#### Example 4: Drawing images with meshgrid

The meshgrid function takes two input vectors and converts them to matrices by replicating the first over the rows and the second over the columns.

The matrices above work like a map for a width 5, height 3 image. For each pixel, the x-location can be read from x and the y-location from y. This may seem like a gratuitous use of memory as x and y simply record the column and row positions, but this is useful. For example, to draw an ellipse,

Drawing lines is just Ahargan Wella: hat powcoder

```
[x,y] = meshgrid(1:150,1:100);
% The line y = x*0.8 + 20
Img = (abs((x*0.8 + 20) - y) > 1);
imagesc(Img); colormap(copper);
axis image, axis off
```



Polar functions can be drawn by first converting x and y variables with the cart2pol function.

```
[x,y] = meshgrid(1:150,1:100);
[th,r] = cart2pol(x - 75,y - 50); % Convert to polar
% Spiral centered at (75,50)
Img = sin(r/3 + th);
imagesc(Img); colormap(hot);
axis image, axis off
```



#### Example 5: Polynomial interpolation

Given n points  $x_1, \ldots x_n$  and corresponding function values  $y_1, \ldots y_n$ , the coefficients  $c_0, \ldots, c_{n-1}$  of the interpolating polynomial

$$P(x) = c_{n-1}x^{n-1} + \dots + c_1x + c_0$$

can be found by solving

$$\begin{bmatrix} x_1^{n-1} & x_1^{n-2} & \cdots & x_1^2 & x_1 & 1 \\ x_2^{n-1} & x_2^{n-2} & \cdots & x_2^2 & x_2 & 1 \\ \vdots & & & & \vdots \\ x_n^{n-1} & x_n^{n-2} & \cdots & x_n^2 & x_n & 1 \end{bmatrix} \begin{bmatrix} c_{n-1} \\ c_{n-2} \\ \vdots \\ c_0 \end{bmatrix} = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}$$

```
function c = polyint(x,y)
% Given a set of points and function values x and y,
% computes the interpolating polynomial.

x = x(:)Assignment Project ac xanon chreveters
y = y(:);
n = length(x);
% n = Number of points

% Construct the manifecture of points

% Make another n by n matrix of exponents
A = xMatrix .^ powMatrix;
% Compute the powers

c = A\y;

Add Wechaet matrix of conficients
```

The strategy to construct the left-hand side matrix is to first make two n×n matrices of bases and exponents and then put them together using the per element power operator, . ^ . The repmat function ("replicate matrix") is used to make the base matrix xMatrix and the exponent matrix powMatrix.

$$\mathtt{xMatrix} = \left[ \begin{array}{cccc} \mathtt{x}(1) & \mathtt{x}(1) & \cdots & \mathtt{x}(1) \\ \mathtt{x}(2) & \mathtt{x}(2) & \cdots & \mathtt{x}(2) \\ \vdots & & & \vdots \\ \mathtt{x}(\mathtt{n}) & \mathtt{x}(\mathtt{n}) & \cdots & \mathtt{x}(\mathtt{n}) \end{array} \right] \qquad \mathsf{powMatrix} = \left[ \begin{array}{cccc} \mathtt{n} - \mathtt{1} & \mathtt{n} - \mathtt{2} & \cdots & \mathtt{0} \\ \mathtt{n} - \mathtt{1} & \mathtt{n} - \mathtt{2} & \cdots & \mathtt{0} \\ \vdots & & & \vdots \\ \mathtt{n} - \mathtt{1} & \mathtt{n} - \mathtt{2} & \cdots & \mathtt{0} \end{array} \right]$$

The xMatrix is made by repeating the column vector  $\mathbf{x}$  over the columns  $\mathbf{n}$  times. The powMatrix is a row vector with elements  $n-1, n-2, n-3, \ldots, 0$  repeated down the rows  $\mathbf{n}$  times. The two matrices could also have been created with [powMatrix, xMatrix] = meshgrid(n-1:-1:0, x).

The code above is only an example—use the standard polyfit function for serious use.



### **Inlining Simple Functions**

Every time an M-file function is called, the MATLAB interpreter incurs some overhead. Additionally, many M-file functions begin with conditional code that checks the input arguments for errors or determines the mode of operation.

Of course, this overhead is negligible for a single function call. It should only be considered when the function being called is an M-file, the function itself is "simple," that is, implemented with only a few lines, and called frequently from within a loop.

For example, this code calls the M-file function median repeatedly to perform median filtering:

```
% Apply the median filter of size 5 to signal x y = zeros(size(x)); % Preallocate for k = 3:length(x)-2 y(k) = median(x(k-2:k+2)); end Assignment Project Exam Help
```

Given a 2500-sample array for x, the overall run time is 0.42 seconds.

"Inlining a function" nears to seplect path to the function with the function code itself. Beware that inlining should not be confused with NATLAB's "inline" function datatype. Studying median.m (type "edit median" on the console) reveals that most of the work is done using the built-in sort function.

The median call can be inlined as WeChat powcoder

```
% Apply the median filter of size 5 to signal x
y = zeros(size(x)); % Preallocate

for k = 3:length(x)-2
   tmp = sort(x(k-2:k+2));
   y(k) = tmp(3); % y(k) = median(x(k-2:k+2));
end
```

Now the overall run time is 0.047 seconds, nearly 9 times faster. Furthermore, by inlining median, it can be specifically tailored to evaluating 5-sample medians. But this is only an example; if the Signal Processing Toolbox<sup>TM</sup> is available, y = medfilt1(x,5) is much faster.

A surprising number of MATLAB's functions are implemented as M-files, of which many can be inlined in just a few lines. In MATLAB 5.3 (R11), the following functions are worth inlining:

conv, cross, fft2, fliplr, flipud, ifft, ifft2, ifftn, ind2sub, ismember, linspace, logspace, mean, median, meshgrid, poly, polyval, repmat, roots, rot90, setdiff, setxor, sortrows, std, sub2ind, union, unique, var

The list above is for MATLAB R11; some of these functions have since become built-in. Use the which command or try "edit function name" to determine whether a function is implemented as an M-file.

For example, in MATLAB R11 and earlier, ifft was implemented by simply calling fft and conj. If x is a one-dimensional array, y = ifft(x) can be inlined with y = conj(fft(conj(x)))/length(x).

Another example: b = unique(a) can be inlined with

```
b = sort(a(:)); b(b((1:end-1)') == b((2:end)')) = [];
```

While repmat has the generality to operate on matrices, it is often only necessary to tile a vector or just a scalar. To repeat a column vector y over the columns n times,

```
A = y(:, ones(1,n)); % Equivalent to A = repmat(y,1,n);
```

To repeat a row vector x over the rows m times,

```
A = x(ones(1,m),:); % Equivalent to A = repmat(x,m,1);
```

To repeat a scalar s into an  $m \times n$  matrix,

```
A = s(ones(m,n)); % Equivalent to A = repmat(s,m,n);
```

This method avoids the overhead of calling an M-file function. It is never slower than repmat (critics should note the Sregnal of the little than the little constructing matrices with constant value, there are other efficient methods, for example, s+zeros(m,n).

Don't go overboard. Inlining functions is only beneficial when the function is simple and when it is called frequently. Doing it unnecessarily objustates the order.

## Add WeChat powcoder

# 7

### **Referencing Operations**

Referencing in MATLAB is varied and powerful enough to deserve a section of discussion. Good understanding of referencing enables vectorizing a broader range of programming situations.

#### 7.1 Subscripts vs. Indices

Subscripts are the most common method used to refer to matrix elements, for example, A(3,9) refers to row 3, column 9. Indices are an alternative referencing method. Consider a  $10 \times 10$  matrix A. Internally, MATLAB stores the matrix data linearly as a one-dimensional, 100-element array of data in column-major order.

An index refers to an element's position in this one-dimensional array. Using an index, A(83) also refers to the element on rollar polyments. //powcoder.com

It is faster to scan down columns than over rows. Column-major order means that elements along a column are sequential in memory while elements along a row are further apart. Scanning down columns promotes cache efficiency WeChat powcoder

Conversion between subscripts and indices can be done with the sub2ind and ind2sub functions. However, because these are M-file functions rather than fast built-in operations, it is more efficient to compute conversions directly (also see Section 6). For a two-dimensional matrix A of size  $M \times N$ , the conversions between subscript (i,j) and index (index) are

```
\begin{array}{lll} \texttt{A(i,j)} & \leftrightarrow & \texttt{A(i + (j-1)*M)} \\ \texttt{A(index)} & \leftrightarrow & \texttt{A(rem(index-1,M)+1, floor((index-1)/M)+1)} \end{array}
```

Indexing extends to N-D matrices as well, with indices increasing first through the columns, then through the rows, through the third dimension, and so on. Subscript notation extends intuitively,

$$A(..., dim4, dim3, row, col)$$
.

#### 7.2 Vectorized Subscripts

It is useful to work with submatrices rather than individual elements. This is done with a vector of indices or subscripts. If A is a two-dimensional matrix, a vector subscript reference has the syntax

where row and colv are vectors. Both may be of any length and their elements may be in any order. If either is a matrix, it is reshaped to a vector. There is no difference between using row vectors or column vectors in vector subscripts.

Let M = length(rowv) and N = length(colv). Then a vector subscripted matrix on the right-hand side\* returns a submatrix of size  $M \times N$ :

```
 \begin{bmatrix} \texttt{A}(\texttt{rowv}(1),\texttt{colv}(1)) & \texttt{A}(\texttt{rowv}(1),\texttt{colv}(2)) & \texttt{A}(\texttt{rowv}(1),\texttt{colv}(3)) & \cdots & \texttt{A}(\texttt{rowv}(1),\texttt{colv}(N)) \\ \texttt{A}(\texttt{rowv}(2),\texttt{colv}(1)) & \texttt{A}(\texttt{rowv}(2),\texttt{colv}(2)) & \texttt{A}(\texttt{rowv}(2),\texttt{colv}(3)) & \cdots & \texttt{A}(\texttt{rowv}(2),\texttt{colv}(N)) \\ \vdots & & & \vdots & & \vdots \\ \texttt{A}(\texttt{rowv}(\texttt{M}),\texttt{colv}(1)) & \texttt{A}(\texttt{rowv}(\texttt{M}),\texttt{colv}(2)) & \texttt{A}(\texttt{rowv}(\texttt{M}),\texttt{colv}(3)) & \cdots & \texttt{A}(\texttt{rowv}(\texttt{M}),\texttt{colv}(N)) \end{bmatrix}
```

A vector subscripted matrix can also appear on the left-hand side as

```
A(rowv, colv) = scalar or M \times N matrix
```

If any elements in the destination reference are repeated, the source element with the greater index dominates Forexample 2011

Vector subscript references extend intuitively in higher dimensions.

## 7.3 Vector Indeeddd WeChat powcoder

Multiple elements can also be referenced with vector indices.

#### A(indexv)

where indexv is an array of indices. On the right-hand side, a vector index reference returns a matrix the same size and shape as indexv. If indexv is a  $3 \times 4$  matrix, then A(indexv) is the  $3 \times 4$  matrix

$$\texttt{A}(\texttt{indexv}) = \left[ \begin{array}{cccc} \texttt{A}(\texttt{indexv}(1,1)) & \texttt{A}(\texttt{indexv}(1,2)) & \texttt{A}(\texttt{indexv}(1,3)) & \texttt{A}(\texttt{indexv}(1,4)) \\ \texttt{A}(\texttt{indexv}(2,1)) & \texttt{A}(\texttt{indexv}(2,2)) & \texttt{A}(\texttt{indexv}(2,3)) & \texttt{A}(\texttt{indexv}(2,4)) \\ \texttt{A}(\texttt{indexv}(3,1)) & \texttt{A}(\texttt{indexv}(3,2)) & \texttt{A}(\texttt{indexv}(3,3)) & \texttt{A}(\texttt{indexv}(3,4)) \end{array} \right]$$

While vector subscripts are limited to referring to block-shaped submatrices, vector indices can refer to any subset of elements.

If a vector index reference is on the left-hand side, the right-hand side must return a matrix of the same size as indexv or a scalar. As with vector subscripts, ambiguous duplicate assignments use the value with greater source index.

<sup>\*</sup>The left- and right-hand sides (LHS and RHS) refer to the two sides of an assignment, "LHS = RHS."

#### 7.4 Reference Wildcards

Using the wildcard, :, in a subscript refers to an entire row or column. For example, A(:,1) refers to every row in column one—the entire first column. This can be combined with vector subscripts, A([2,4],:) refers to the second and fourth rows.

When the wildcard is used in a vector index, the entire matrix is referenced. On the right-hand side, this always returns a column vector.

A(:) = column vector

This is frequently useful: for example, if a function input must be a row vector, the user's input can be quickly reshaped into row vector with A(:).' (make a column vector and transpose to a row vector).

A(:) on the left-hand side assigns all the elements of A, but does not change its size. For example, A(:) = 8 changes all elements of matrix A to 8.

#### 7.5 Logical Indexing

## Given a la Sassignmenta Project Exam Help

A(mask)

refers to all elements of A where the corresponding element of mask is 1 (true). It is equivalent to A(find(mask)). A common usage of logical valuesing is to refer to elements based on a per-element condition, for example,

sets all elements with magnitude less than to be to zero power also useful to select non-

sets all elements with magnitude less than 10<sup>-18</sup> to zero. Logical indexing is also useful to select non-rectangular sets of elements, for example,

```
A(logical(eye(size(A))))
```

references the diagonal elements of A. Note that for a right-hand side reference, it is faster to use diag(A) to get the diagonal of A.

#### 7.6 Deleting Submatrices with []

Elements in a matrix can be deleted by assigning the empty matrix. For example, A([3,5]) = [] deletes the third and fifth element from A. If this is done with index references, the matrix is reshaped into a row vector.

It is also possible to delete with subscripts if all but one subscript are the wildcard. A(2,:) = [] deletes the second row. Deletions like A(2,1) = [] or even A(2,1:end) = [] are illegal.

# Solving Ax = b

Many problems involve solving a linear system, that is, solving the Ax = b problem

$$\begin{bmatrix} a_{1,1} & a_{1,2} & \cdots & a_{1,n} \\ a_{2,1} & a_{2,2} & \cdots & a_{2,n} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n,1} & a_{n,2} & \cdots & a_{n,n} \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix} = \begin{bmatrix} b_1 \\ b_2 \\ \vdots \\ b_n \end{bmatrix}.$$

The condition number cond(A) describes how sensitive the problem is to small perturbations. MATLAB can efficiently approximate cond(A) with condest. Smaller condition number is better, and in this case A is said to be well-conditioned. An infinite condition number implies that A is singular—the problem cannot be solved, though it may be solved approximately with the pseudoinverse (x = pinv(A)\*b).

Small- to moderately-sized problems are solved efficiently by the backslash operator:

# \*\* Assignment Project Exam Help

# 8.1 Iterative Methods://powcoder.com For large problems, MATLAB is well-equipped with iterative solvers: bicg, bicgstab, cgs, gmres, lsqr,

minres, pcg, symmlq, qmr. The general calling syntax (except for gmres) is

## [x,flag,relres,iArdeceWeedhatl,powcoder

where the required arguments are the matrix A, the right-hand side b, and the solution x. The minres, pcg, and symmlq methods require A to be symmetric (A = A') and pcg additionally requires positive definiteness (all eigenvalues are positive). The optional input variables are

```
accuracy tolerance (default 10^{-6})
tol
```

maximum number of iterations (default 20) maxit

the method uses preconditioner M = M1\*M2; it solves  $M^{-1}Ax = M^{-1}b$ M1, M2

x0initial guess

The optional output variables are

convergence flag (0 = success, nonzero values are error codes)flag

relative residual ||b - Ax||/||b||relres

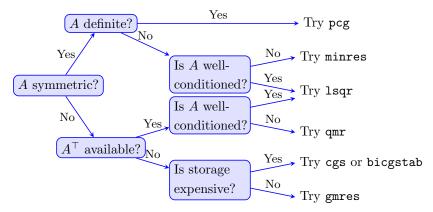
iter number of iterations

a vector listing the residual norm ||b - Ax|| at each iteration

The gmres method includes one additional input,

The method restarts every restart iterations, or if restart=[], the method does not restart.

Which method works best depends on the particular problem. This diagram (adapted from Demmel [3]) provides a reasonable starting point.



**Functional Representation** 

Rather than SS1 generality it is of each enter ent X defreent A S1 pear function acting on x. For example,

$$https://powcoder com$$

can be expressed as A\*\* = tursum(V). In addition to being conceptually envenient, functional representation avoids the memory overhead of storing the matrix.

All the iterative solvers support functional representation, where a function handle afun is given in place of matrix A. The function afun(x) should accept a vector x and return A\*x. The help for lsqr ("help lsqr") has a functional example where A is the central differencing operator. The bicg, lsqr, and qmr methods also require the transpose: afun(x,'notransp') should return A\*x and afun(x,'transp') should return A\*x. Similarly, the preconditioner may be given as a function handle mfun.

#### **Special Matrices**

For certain special matrix structures, the Ax = b problem can be solved very quickly.

- Circulant matrices. Matrices corresponding to cyclic convolution Ax = h \* x are diagonalized in the Fourier domain, and can be solved by x = ifft(fft(b)./fft(h));
- Triangular and banded. Triangular matrices and diagonally-dominant banded matrices are solved efficiently by sparse LU factorization: [L,U] = lu(sparse(A)); x = U\(L\b);
- Poisson problem. If A is a finite difference approximation of the Laplacian, the problem is efficiently solved by multigrid methods (e.g., web search for "matlab multigrid").

#### 8.2 Inlined PCG

As discussed in Section 6, it is sometimes advantageous to inline a simple piece of code to tailor it to a specific application. While most iterative methods are too lengthy for inlining, conjugate gradients has a short implementation. The value of inlining pcg is that calls to afun and mfun may be inlined. Beware that in the following code, A must be symmetric positive definite—otherwise, it will not work!

```
%% Use PCG to solve Ax = b %%
tol = 1e-6; % Convergence tolerance
maxit = 20; % Maximum number of iterations
            % Set x to initial guess (if no guess is available, use x0 = 0)
x = x0;
Compute w = A x
r = b - w;
                   % r = residual vector
Set p = r, or if using a preconditioner, p = M^{-1} r
         ssignment Project Exam Help
   if norm(p) < tol</pre>
                   % PCG converged successfully (small change in x)
       break:
               https://powcoder.com
   Compute w = Ap
   alpha = e/(p'*waidd WeChat powcoder
   Set w = r, or if using a preconditioner, w = M^{-1} r
   if norm(w) < tol && norm(r) < tol
                % PCG converged successfully (small residual)
   end
   dlast = d;
   d = r' *w;
   p = w + (d/dlast) *p;
```

After the loop, the final solution is in x. The method converged successfully with accuracy tol if it encountered a break statement, otherwise, it failed or needed more iterations. The relative residual may be computed by relres = norm(r)/norm(b) after the loop and resvec by storing the value of norm(r) each iteration.



### **Numerical Integration**

Quadrature formulas are numerical approximation of integrals of the form

$$\int_{a}^{b} f(x) \, \mathrm{d}x \approx \sum_{k} w_{k} f(x_{k}),$$

where the  $x_k$  are called the *nodes* or *abscissas* and  $w_k$  are the associated weights. Simpson's rule is

$$\int_{a}^{b} f(x) dx \approx \frac{h}{3} [f(a) + 4f(a+h) + f(b)], \qquad h = \frac{b-a}{2}.$$

Simpson's rule is a quadrature formula with nodes a, a + h, b and node weights  $\frac{h}{3}$ ,  $\frac{4h}{3}$ ,  $\frac{h}{3}$ .

Matlab has several functions for quadrature in one dimension:

```
quad adaptive Simpson Better for low accuracy and nonsmooth integrands quadl adaptive Gauss-Lobatto Higher accuracy with smoother integrands quadgk adaptive Gauss-Kronrod Quadro Vectorized Graditiva Led Xueriands Help
```

The quad- functions are robust and precise, however, they are not very efficient. They use an adaptive refinement procedure, and while this reduces the number of function calls, they gain little from vectorization and including strong work of the control of the

If an application requires approximating an integral whose integrand can be efficiently vectorized, using nonadaptive quadrature may improve speed.

```
for n = -20:20 % Compute Fourier series coefficients OWCOGER c(n + 21) = quad(@(x)(exp(sin(x).^6).*exp(-li*x*n)),0,pi,1e-4); end
```

This code runs in 5.16 seconds. In place of quad, using Simpson's composite rule with N = 199 nodes yields results with comparable accuracy and allows for vectorized computation. Since the integrals are all over the same interval, the nodes and weights only need to be constructed once.

This version of the code runs in 0.02 seconds (200 times faster). The quadrature is performed by the dot product multiplication with w. It can be further optimized by replacing the for loop with one vector-matrix multiply:

```
[n,x] = meshgrid(-20:20, 0:h:pi);
c = w * (exp(sin(x).^6).*exp(-1i*x.*n));
```

For this example, quadv can be used on a multi-valued integrand with similar accuracy and speed,

```
n = -20:20;
c = quadv(@(x)exp(sin(x).^6).*exp(-1i.*x.*n),0,pi,1e-4);
```

#### 9.1 One-Dimensional Integration

 $\int_a^b f(x) dx$  is approximated by composite Simpson's rule with

```
\begin{array}{lll} h = & (b-a)/(N-1); \\ x = & (a:h:b).'; \\ w = & ones(1,N); & w(2:2:N-1) = 4; & w(3:2:N-2) = 2; & w = w*h/3; \\ I = & w + f(x); & & Approximately evaluate the integral \\ \end{array}
```

where N is an odd integer specifying the number of nodes.

A good higher-order choice is 4th-order Gauss-Lobatto [4] (as used by quad1), based on

The number of nodes N must be such that (N-1)/3 is an integer. If not, the first line adjusts N to the closest valid choice. It is usually more accurate than Simpson's rule when f has six continuous derivatives,  $f \in C^6(a,b)$ .

A disadvantage of this nonadaptive approach is that the accuracy of the result is only indirectly controlled by the parameter N. To guarantee a desired accuracy, either use a generously large value for N or, if possible, determine the error bounds [6, 7]

$$\begin{array}{lll} \textit{Simpson's rule error} & \leq & \frac{(b-a)h^4}{180} \max_{a \leq \eta \leq b} \left| f^{(4)}(\eta) \right| & \text{provided } f \in C^4(a,b), \\ \\ \textit{4th-order Gauss-Lobatto error} & \leq & \frac{27(b-a)h^6}{56000} \max_{a \leq \eta \leq b} \left| f^{(6)}(\eta) \right| & \text{provided } f \in C^6(a,b), \end{array}$$

where  $h = \frac{b-a}{N-1}$ . Note that these bounds are valid only when the integrand is sufficiently differentiable: f must have four continuous derivatives for the Simpson's rule error bound, and six continuous derivatives for 4th-order Gauss-Lobatto.

Composite Simpson's rule is a fast and effective default choice. But depending on the situation, other methods may be faster and more accurate:

- If the integrand is expensive to evaluate, or if high accuracy is required and the error bounds above are too difficult to compute, use one of Matlab's adaptive methods. Otherwise, consider composite methods.
- Use higher-order methods (like Gauss-Lobatto/quad1) for very smooth integrands and lower-order methods for less smooth integrands.
- Use the substitution  $u = \frac{1}{1-x}$  or Gauss-Laguerre quadrature for infinite-domain integrals like  $\int_0^\infty$ .

#### 9.2 Multidimensional Integration

An approach for evaluating double integrals of the form  $\int_a^b \int_c^d f(x,y) \, \mathrm{d}y \, \mathrm{d}x$  is to apply one-dimensional quadrature to the outer integral  $\int_a^b F(x) \, \mathrm{d}x$  and then for each x use one-dimensional quadrature over the inner danger to parameter f(x) by the following to the

Similarly for three-dimensional integrals, the weights are combined with

```
[x,y,z] = meshgrid(x,y,z); x = x(:); y = y(:); z = z(:); w = wy.'*wx; w = w(:)*wz; w = w(:).';
```

When the integration region is complicated or of high dimension, Monte Carlo integration techniques are appropriate. The disadvantage is that an N-point Monte Carlo quadrature has error on the order  $O(\frac{1}{\sqrt{N}})$ , so many points are necessary even for moderate accuracy. Suppose that N points,  $x_1, x_2, \ldots, x_N$ , are uniformly randomly selected in a multidimensional region (or volume)  $\Omega$ . Then

$$\int_{\Omega} f \, dV \approx \frac{\int_{\Omega} dV}{N} \sum_{n=1}^{N} f(x_n).$$

To integrate a complicated region W that is difficult to sample uniformly, find an easier region  $\Omega$  that contains W and can be sampled [5]. Then

$$\int\limits_{W} f \, \mathrm{d}V = \int\limits_{\Omega} f \cdot \chi_{W} \, \mathrm{d}V \approx \frac{\int_{\Omega} \mathrm{d}V}{N} \sum_{n=1}^{N} f(x_{n}) \chi_{W}(x_{n}), \qquad \chi_{W}(x) = \left\{ \begin{array}{ll} 1, & x \in W, \\ 0, & x \notin W. \end{array} \right.$$

 $\chi_W(x)$  is the indicator function of W:  $\chi_W(x) = 1$  when x is within region W and  $\chi_W(x) = 0$  otherwise. Multiplying the integrand by  $\chi_W$  sets contributions from outside of W to zero.

For example, consider finding the center of mass of the shape W defined by  $\cos\left(2\sqrt{x^2+y^2}\right)x\leq y$  and  $x^2+y^2\leq 4$ . Given the integrals  $M=\int_W \mathrm{d}A$ ,  $M_x=\int_W x\,\mathrm{d}A$ , and  $M_y=\int_W y\,\mathrm{d}A$ , the center of mass is  $(\frac{M_x}{M},\frac{M_y}{M})$ . The region is contained in the rectangle  $\Omega$  defined by  $-2\leq x\leq 2$  and  $-2\leq y\leq 2$ . The following code estimates M,  $M_x$ , and  $M_y$ :



More generally, if W is a two-dimensional region contained in the rectangle defined by  $a \le x \le b$  and  $c \le y \le d$ , the following code approximates  $\int_W f \, dA$ :

```
x = a + (b-a)*rand(N,1);
y = c + (d-c)*rand(N,1);
i = logical(indicatorW(x,y));
x = x(i); y = y(i);
area = (b-a)*(d-c);
I = (area/N) * sum(f(x,y)); % Approximately evaluate the integral
```

where indicator W(x,y) is the indicator function  $\chi_W(x,y)$  for region W.

For refinements and variations of Monte Carlo integration, see for example [1].

# 10 Signal Processing

Even without the Signal Processing Toolbox, MATLAB is quite capable in signal processing computations. This section lists code snippets to perform several common operations efficiently.

#### Moving-average filter

To compute an N-sample moving average of x with zero padding:

```
y = filter(ones(N,1)/N,1,x);
For large N, it is faster to use y = cumsum(x)/N;
y(N+1:end) = y(N+1:end) - y(1:end-N);
```

#### Locating zero-crossings and extrema

To obtain the indices where signal x cross perocepts and Help is a final (diff signs)). The kth zero-crossing lies between x(i(k)) and x(i(k)+1)

Linear interpolation can be used for subsample estimates of zero-crossing locations:

```
i = find(diff(sign(A)ttps://powcoder.com)); % Linear interpolation
```

Since local maximum and minimum points of a signal have zero derivative, their locations can be estimated from the zero-crossings of der (x) provided the sixual is satisfied with sufficiently fine resolution. For a coarsely sampled signal, a better estimate is

```
 i \text{Max} = \text{find} (\text{sign}(x(2:\text{end-1})-x(1:\text{end-2})) \dots \\ + \text{sign}(x(2:\text{end-1})-x(3:\text{end})) > 0) + 1; \\ i \text{Min} = \text{find} (\text{sign}(x(2:\text{end-1})-x(1:\text{end-2})) \dots \\ + \text{sign}(x(2:\text{end-1})-x(3:\text{end})) < 0) + 1; \\
```

#### FFT-based convolution

This line performs FFT-based circular convolution, equivalent to y = filter(b,1,x) except near the boundaries, provided that length(b) < length(x):

```
For FFT-based zero-padded convolution, equivalent to y = filter(b,1,x),

N = length(x)+length(b)-1;
```

```
N = length(x) + length(b) - 1;
y = ifft(fft(b, N) .*fft(x, N));
y = y(1:length(x));
```

y = ifft(fft(b, length(x)).\*fft(x));

In both code snippets above, y will be complex-valued, even if x and b are both real. To force y to be real, follow the computation with y = real(y). If you have the Signal Processing Toolbox, it is faster to use fftfilt for FFT-based, zero-padded filtering.

#### Noncausal filtering and other boundary extensions

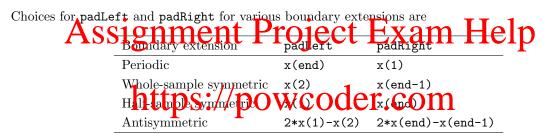
For its intended use, the filter command is limited to causal filters, that is, filters that do not involve "future" values to the right of the current sample. Furthermore, filter is limited to zero-padded boundary extension; data beyond the array boundaries are assumed zero as if the data were padded with zeros.

For two-tap filters, noncausal filtering and other boundary extensions are possible through filter's fourth initial condition argument. Given a boundary extension value padLeft for x(0), the filter  $y_n = b_1 x_n + b_2 x_{n-1}$  may be implemented as

```
y = filter(b, 1, x, padLeft*b(2));
```

Similarly, given a boundary extension value padRight for x(end+1), the filter  $y_n = b_1 x_{n+1} + b_2 x_n$  is implemented as

```
y = filter(b, 1, [x(2:end), padRight], x(1) *b(2));
```



It is in principle possible to the a single proof ar long fifty of in all, computing the initial condition itself requires filtering. To implement noncausal filtering and filtering with other boundary handling, it is usually fastest to pad the input signal, apply filter, and then truncate the result.

#### **Upsampling and Downsampling**

```
Upsample x (insert zeros) by factor p:
```

```
y = zeros(length(x)*p-p+1,1); % For trailing zeros, use y = zeros(length(x)*p,1); y(1:p:length(x)*p) = x;
```

Downsample x by factor p, where  $1 \le q \le p$ :

```
y = x(q:p:end);
```

#### Haar Wavelet

This code performs K stages of the Haar wavelet transform on the input data x to produce wavelet coefficients y. The input array x must have length divisible by  $2^{K}$ .

Forward transform:

```
y = x(:); N = length(y);
for k = 1:K
  tmp = y(1:2:N) + y(2:2:N);
  y([1:N/2,N/2+1:N]) = ...
  [tmp;y(1:2:N) - 0.5*tmp]/sqrt(2);
  N = N/2;
end
```

Inverse transform:

```
x = y(:); N = length(x)*pow2(-K);
for k = 1:K
   N = N*2;
   tmp = x(N/2+1:N) + 0.5*x(1:N/2);
   x([1:2:N,2:2:N]) = ...
   [tmp;x(1:N/2) - tmp]*sqrt(2);
end
```

#### Daubechies 4-Tap Wavelet

This code implements the Daubechies 4-tap wavelet in lifting scheme form [2]. The input array x must have length disastly at 17 Hiller gif done with principle roux and hadding C 10

Forward transform:

Inverse transform:

```
U = 0.25*[2-sqrt(3), -sqrt(3)];
                                              U = 0.25 * [2-sqrt(3), -sqrt(3)];
x = y(:); N = length(x)*pow2(-K);
y = x(:); N = length(y);
                Add WeChat power
for k = 1:K
  N = N/2;
  y1 = y(1:2:2*N);
                                                 y2 = x(1:N)/ScaleS + y1([min(2,N),1:N-1]);
  y2 = y(2:2:2*N) + sqrt(3)*y1;
                                                 y1 = y1 - filter(U, 1, ...
  y1 = y1 + filter(U,1,...
                                                    y2([2:N, max(N-1,1)]), y2(1)*U(2));
                                                 x([1:2:2*N,2:2:2*N]) = [y1;y2 - sqrt(3)*y1];
     y2([2:N, max(N-1,1)]), y2(1)*U(2));
  y(1:2*N) = [ScaleS*...
                                                 N = 2 * N;
      (y2 - y1([min(2,N),1:N-1]));ScaleD*y1];
                                              end
end
```

To use periodic boundary handling rather than symmetric boundary handling, change appearances of  $[2:N,\max(N-1,1)]$  to [2:N,1] and  $[\min(2,N),1:N-1]$  to [N,1:N-1].



#### Clip a value without using if statements

To clip (or clamp, bound, or saturate) a value to within a range, the straightforward implementation is

```
if x < lowerBound
    x = lowerBound;
elseif x > upperBound
    x = upperBound;
end
```

Unfortunately, this is slow. A faster method is to use the min and max functions:

```
x = max(x, lowerBound); % Clip elements from below, force x >= lowerBound

x = min(x, upperBound); % Clip elements from above, force x <= upperBound
```

Moreover, it works per-element if x a matrix of any size.

### Convertes Signimentul Project Exam Help

It is often useful to force an array to be a column vector, for example, when writing a function expecting a column vector as an input. This simple trick will convert the input array of any shape and number of dimensions to a column vector, even in the writing tenth is column vector.

```
x = x(:); % Convert x to a column vector
```

Similarly, x = x(:,:) reduces an N-d array to 2D, where the number of rows stays the same.

### Add WeChat powcoder

#### Find the min/max of a matrix or N-d array

Given a matrix input (with no other inputs), the min and max functions operate along the columns, finding the extreme element in each column. To find the extreme element over the entire matrix, one way for a two-dimensional matrix is min(min(A)). A better method that works regardless of the number of dimensions and determines the extreme element's location is

The minimum element is A(MinIndex) or A(MinSub(1), MinSub(2), ...) as a subscript reference. (Similarly, replace min with max for maximum value.)

#### Flood filling

Flood filling, like the "bucket" tool in image editors, can be elegantly written as a recursive function:

Being a highly recursive function, this is inefficient in MATLAB. The following code is faster:

```
function I = flood2(I,c,x,y)
% Flood fills image I from point (x,y) with color c.

LastFlood Scignment Project Exam Help
Flood = LastFlood Help
Flood(y,x) = 1;
Mask = (I == I(y,x));
FloodFilter = [0,1] https://powcoder.com
while any(LastFlood(:) ~= Flood(:))
    LastFlood = Flood;
    Flood = conv2(Flood, FloodFilter, 'same hank;
end Add WeChat powcoder

I(find(Flood)) = c;
```

The key is the conv2 two-dimensional convolution function. Flood filling a  $40 \times 40$ -pixel region takes 1.168 seconds with flood1 and 0.067 seconds with flood2.

#### Vectorized use of set on GUI objects

While not a speed improvement, a trick for cleaner code is vectorized use of set on GUI objects. A serious graphical user interface (GUI) can have dozens of objects and many properties to configure. For example, to define three edit boxes with white text background and left text alignment:

```
uicontrol('Units', 'normalized', 'Position', [0.1,0.9,0.7,0.05], ...
   'HorizontalAlignment', 'left', 'Style', 'edit', 'BackgroundColor', [1,1,1]);
uicontrol('Units', 'normalized', 'Position', [0.1,0.8,0.7,0.05], ...
   'HorizontalAlignment', 'left', 'Style', 'edit', 'BackgroundColor', [1,1,1]);
uicontrol('Units', 'normalized', 'Position', [0.1,0.7,0.7,0.05], ...
   'HorizontalAlignment', 'left', 'Style', 'edit', 'BackgroundColor', [1,1,1]);
```

A vectorized call to set reduces this to

```
h(1) = uicontrol('Units', 'normalized', 'Position', [0.1,0.9,0.7,0.05]);
h(2) = uicontrol('Units', 'normalized', 'Position', [0.1,0.8,0.7,0.05]);
h(3) = uicontrol('Units', 'normalized', 'Position', [0.1,0.7,0.7,0.05]);
set(h, 'HorizontalAlignment', 'left', 'Style', 'edit', 'BackgroundColor', [1,1,1]);
```

# 12

### **Further Reading**

For more reading on vectorization, see the MathWorks vectorization guide:

http://www.mathworks.com/support/tech-notes/1100/1109.shtml

For further details and examples on JIT Acceleration, see for example

http://www.mathworks.com/access/helpdesk\_r13/help/techdoc/matlab\_prog/ch7\_perf.html For a thorough guide on efficient array manipulation, see MATLAB array manipulation ips and tricks:

http://home.online.no/~pjacklam/matlab/doc/mtt

For numerical methods with MATLAB, see Numerical Computing with MATLAB:

http://www.mathttps://pOWCOder.com

#### **MEX**

In a coding situation the Cantot Continue of the Cantot Continue of the Matlab language is intended primarily for easy prototyping rather than high-speed computation. In some cases, an appropriate solution is Matlab Executable (MEX) external interface functions. With a C or Fortran compiler, it is possible to produce a MEX function that can be called from within Matlab in the same as an M-function. The typical speed improvement over equivalent M-code is easily ten-fold.

Installations of MATLAB include an example of MEX under directory <MATLAB>/extern/examples/mex. In this directory, a function "yprime" is written as M-code (yprime.m) and equivalent C (yprime.c) and Fortran (yprime.f) MEX source code. For more information, see the MathWorks MEX-files guide http://www.mathworks.com/support/tech-notes/1600/1605.html

For information on compiling MEX files with the GNU compiler collection (GCC), see

http://gnumex.sourceforge.net

Beware, MEX is an ambitious alternative to M-code. Writing MEX files requires learning some low-level details about MATLAB, and takes more time to develop than M-code.

#### Matlab Compiler

The Matlab Compiler generates a standalone executable from M-code. For product information and documentation, see

http://www.mathworks.com/access/helpdesk/help/toolbox/compiler

#### References

- [1] A. BIELAJEW. "The Fundamentals of the Monte Carlo Method for Neutral and Charged Particle Transport." *University of Michigan, class notes.* Available online at http://www-personal.engin.umich.edu/~bielajew/MCBook/book.pdf
- [2] I. Daubechies and W. Sweldens. "Factoring Wavelet Transforms into Lifting Steps." Sep. 1996.
- [3] J. WASSIGNMENT Project Exam Help
- [4] W. GANDER AND W. GAUTSCHI. "Adaptive Quadrature-Revisited," BIT, vol. 40, pp. 84-101, 2000.
- [5] W. Press, B. Francisco S. Tropos With October 15 Press, 1986. Cambridge University Press, 1986.
- [6] E. WEISSTEIN. "Lobatto Quadrature." From MathWorld-A Wolfram Web Resource. http://mathworld-wilffam.cvm/Lobatto Quadrature." from MathWorld-A Wolfram Web Resource.
- [7] E. WEISSTEIN. "Simpson's Rule." From MathWorld—A Wolfram Web Resource. http://mathworld.wolfram.com/SimpsonsRule.html