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Completeness

The ability to write complete code is a core competence of software developers, and it is also a key factor impacting interview results. Code is complete when it fulfills basic functional requirements, performs well on boundary inputs, and handles invalid input gracefully.

Test Cases for Completeness

In order to prevent bugs from occurring during interviews, it is a good practice for candidates to figure out a complete set of unit test cases before they begin to write code. After finishing coding, the candidate can test the code with the test cases in mind, which include functional test cases, boundary test cases, and negative test cases (Figure 5-2). If all cases pass, the candidate should feel confident in handing his or her code to the interviewer.

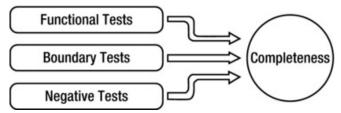


Figure 5-2. Three types of tests to guarantee complete code

The first type of test case is about functionality because candidates' code has to fulfill basic functional requirements. For example, if a candidate is asked to convert a string to a number, he or she may test with input strings "123", "0", and "-123". The function is expected to be able to convert strings for positive and negative numbers as well as zero.

Candidates have to break through the limit of conventional thinking while designing functional test cases. Sometimes functional requirements are ignored because of conventional thinking. For example, many candidates think the coding interview problem to print from 1 to the maximal numbers with n digits is quite easy—or is it? The maximum with three digits is 999, and the maximum with four digits is 9999. These maximal values are not difficult to calculate. However, the int or long type cannot accommodate numbers with n digits when n is large. If it is required that the program is able to handle arbitrarily large n, some data structures for big numbers, such as strings or arrays, may be utilized to solve this problem.

Boundary values should also be covered during unit tests. It is not rare to utilize iteration and recursion in code. What are the boundary values to end loops or recursion? Candidates may design some test cases based on these boundary values. Take the problem to convert a string to a number as an example again. Candidates should make sure their code can convert the maximal and minimal integers as expected.

Invalid inputs should also be considered while designing test cases. Cases about negative tests should be included to make sure that the program handles errors gracefully when given invalid inputs. When developing a function to convert a string to a number, strings with non-digit characters such as "1a2b3c" should be taken into consideration.

The points above are presented to consider all possible inputs according to the current requirements. In software engineering, what never changes is the fact that the requirements always change. If candidates take potential requirement changes into consideration to reduce risks in the future, they demonstrate their understanding of scalability and maintainability. Scalability and maintainability will be discussed in detail later for the question "Partition Numbers in Arrays" (Question 45).

Strategies to Handle Errors

When given inputs are invalid, they cause errors and the normal execution flow in a function cannot continue. It is necessary to handle errors in the function and pass error messages to the function caller. There are three common strategies to pass error messages to the caller of a function.

The first strategy is to use the return value. Many Windows APIs return 0 when they execute smoothly and return non-zero values when they fail. Microsoft defines different return values for different types of errors, so API callers have the opportunity to know the reason for failure according to the return values. The disadvantage is that the calculation result cannot be assigned to variables or passed to other functions as a parameter directly.

The second strategy is to pass calculation results via return values and set a global variable when an error occurs. Callers may assign results to variables or pass results to other functions directly with this strategy. When errors occur in many Windows APIs, they update a global variable that is accessible by the function GetLastError . It leaves in risks if a caller forgets to check the global variable and fails to handle the corresponding errors.

The third strategy is to throw exceptions when errors occur. Different types of exceptions are defined for different types of errors, so callers are able to handle the specific error according to the type of a caught exception. Additionally, code structure looks clear because the exception mechanism partitions a function into a try block for normal execution, a catch block to handle errors,

and a finally block to make sure resources are cleaned up whether an exception happens or not. Some programming languages, such as C, do not support the exception mechanism. The execution flow is interrupted when an exception is thrown, and it has a negative impact on performance.

Every error-handling mechanism has its own pros and cons (Table 5-1). Which one is suitable for interviews? It depends on interviewers' requirements. When candidates are asked to solve a certain coding problem, they should figure out all possible invalid inputs and discuss how to handle errors with their interviewers.

Table 5-1. Pros and Cons of Three Strategies to Handle Errors via Return Values, Global Variables, and Exceptions

| | Advantages | Disadvantages |
|------------------|---|---|
| Return Values | Consistent with system APIs | Inconvenient to use results |
| Global Variables | Convenient to use results | Possible for callers to forget to check the variable |
| Exceptions | Clear code structure isolating blocks for normal execution and error handling | Some languages don't support exceptions, and exceptions impact performance negatively |

Power of Integers

Question 40 Please implement the function double Power(double base, int exponent) to raise a number base to power of exponent. You are not allowed to call library functions, and it is not necessary to take care of overflow issues.

As we know, there is a pow function in the C/C++ library for power calculation. You will try to simulate the functionality of pow here. Similarly, there are many interview questions simulating library functions, especially functions about numeric calculations and string operations. In order to solve such problems, candidates should not only be familiar with the usages of library functions, but also understand the functional implementation inside of them.

Incomplete

It looks like a simple problembecause it does not require taking care of overflow issues. Some candidates finish writing code in a minute, as shown in Listing 5-1.

Listing 5-1. C++ Code to Calculate Power (Version 1)

```
double Power(double baseNumber, int exponent) {
  double result = 1.0;
  for(int i = 1; i <= exponent; ++i)
    result *= baseNumber;
  return result;
}</pre>
```

A fast solution is not necessarily a good one. The code in Listing 5-1 underestimates the complexity of the problem because it only handles cases where an exponent is positive. What happens when it is negative? Or zero? Incomplete solutions are not acceptable to almost all interviewers.

Complete but Inefficient

When the exponent is negative, it calculates power with absolute value of the exponent first and then gets the reciprocal of the power result. It raises an error when it tries to get the reciprocal of zero. Therefore, the scenario with a negative base and zero as the exponent should be handled specially. How do you handle the error in such scenarios? As discussed before, there are three choices available. Candidates can describe the pros and cons of each choice to the interviewers and select a solution based on the requirements. The solution in Listing 5-2 sets the global variable error when an error occurs, which is defined in the standard C library.

```
Listing 5-2. C++ Code to Calculate Power (Version 2)
```

```
double Power(double base, int exponent) {
   if(Equal(base, 0.0) && exponent < 0) {
       errno = EDOM;
       return 0.0;
   unsigned int absExponent = (unsigned int)(exponent);
       absExponent = (unsigned int)(-exponent);
   double result = PowerWithUnsignedExponent(base, absExponent);
   if(exponent < 0)
       result = 1.0 / result;
   return result;
double PowerWithUnsignedExponent(double base, unsigned int exponent) {
   double result = 1.0:
   for(int i = 1; i <= exponent; ++i)
       result *= base;
   return result:
bool Equal(double num1, double num2) {
   if((num1 - num2 > -0.0000001)
       && (num1 - num2 < 0.0000001))
       return false;
```

A corner case is worthy of attention: it is undefined in mathematics when both base and exponent are zero, so the corresponding power result is acceptable if it is one or zero. Candidates should explain this to interviewers to show that they have considered such a boundary value.

A function Equal is defined to check whether the base is equal to zero. Comparing float numbers with the == operator can be problematic because of the precision issue of the floating-point representation. When the difference between two float numbers is in a narrow range, these two numbers are equal to each other.

Tip Checking the equality of decimals (including float and double numbers) with the = operator is error-prone. Two decimals are treated as equal when the difference between them is in a narrow range, such as a range between 0 and 0.0000001.

The solution is already comprehensive and it is acceptable to many interviewers. However, if an interviewer is very passionate about performance, he or she may give you some hints that the efficiency of the function PowerWithUnsignedExponent can be improved.

Complete and Efficient

When the parameters baseNumber and exponent of the function PowerWithUnsignedExponent are n and 32 respectively, it requires 31 multiplications to get n^{32} . However, it only requires five multiplications with another strategy: it calculates n^2 first, and then calculates $n^4 = n^2 \times n^2$, and similarly calculates n^8 , n^{16} , and finally n^{32} .

That is to say, a^n can be calculated with the following equation efficiently:

$$a^n = \begin{cases} a^{n/2} \cdot a^{n/2} & n \text{ is even} \\ a^{(n-1)/2} \cdot a^{(n-1)/2} & n \text{ is odd} \end{cases}$$

It is easy to implement such an equation recursively, so the function PowerWithUnsignedExponent can be updated, as shown in Listing 5-3.

```
Listing 5-3, C++ Code to Calculate Power (Version 3)
```

```
double PowerWithUnsignedExponent(double base, unsigned int exponent) {
  if(exponent == 0)
    return 1;
  if(exponent == 1)
    return base;

double result = PowerWithUnsignedExponent(base, exponent >> 1);
  result *= result;
  if((exponent & 0x1) == 1)
    result *= base;

return result;
}
```

Some details are worthy of attention. This programreplaces a division operation (/) with a right-shift (>>), and replaces a modulo operation (%) with a bitwise AND (&). Right-shift and bitwise AND operations are more efficient than arithmetic division and modulo operations.

Source Code:

040 Davian em

Test Cases:

- · The exponent is positive/negative/zero
- · The base is positive/negative/zero

Big Numbers as Strings

Question 41 Given a number n, please print all numbers from 1 to the maximum n digit number in order. For example, if the input is 3, it prints 1, 2, 3, ..., 999, which is the maximum number with three digits.

Underestimating Complexity

This problem looks simple. An intuitive solution is to get the maximum number with n digits, which is 10^{n} -1, and print numbers from 1 one by one. Many candidates can create the code in Listing 5-4 in a very short time.

Listing 5-4. C++ Code to Print Numbers (Version 1)

```
void Print1ToMaxOfMDigits_1(int n) {
  int number = 1;
  int i = 0;
  while(i++ < n)
      number *= 10;

for(i = 1; i < number; ++i)
  printf("Md\t", i);</pre>
```

If candidates scrutinize the requirement carefully, they may find that the range of n is unspecified. When the input n is quite large, it causes overflow on the variable of n is declared as n long n long. Therefore, it is necessary to handle big numbers.

Tip If the range of input numbers is not specified explicitly in an interview question, it might be necessary to handle big numbers. Candidates can ask for more clarification on the requirement. Utilizing strings or arrays is a simple solution to handling big numbers.

Simulating Increment on a String

There are many methods available to express big numbers. The most common method, also the simplest one, is to utilize arrays or strings to express big numbers. The following solution is based on strings.

When a number is expressed as a string, each character in the string is in the range '0' to '9'. A string with length n+1 is created to accommodate numbers with n digits at most (there is a '0' and the end of string). When the number of digits is less than n, some leading characters are set to '0'. For example, when the input n is 3, the number 98 is expressed as the string "098".

First, all characters in the string are set as '0', and then a number in the string is increased by 1 and printed in each step of an iteration. There are two tasks to be finished: simulating addition on a string and printing a number in a string. Therefore, the skeleton function to solve this problemcan be implemented as shown in Listing 5-5.

Listing 5-5. C++ Code to Print Numbers (Version 2)

```
void PrintITOMaxOfNDigits_2(int n) {
  if(n <= 0)
    return;

char *number = new char[n + 1];
  memset(number, '0', n);
  number[n] = '\0';</pre>
```

```
while(!Increment(number, n))
    PrintNumber(number);

delete []number;
```

This solution increases a number in a string by one in the function Increment and prints the number in the function PrintNumber . Let's consider the implementation details of these two functions

The return type of the function Increment is bool . It returns true when it reaches the maximum number with n digits to stop the while loop in its caller. Otherwise, it returns false . How do you check if it reaches the maximum number? A straightforward method is to compare the string with "999...99"(n 9s) with the library function strcmp . It is done if they are equal. It costs O(n) time to compare two strings with length n.

There is a more efficient solution available for the Increment function. It carries the first digit (with index 0) when it adds 1 to the number "999...99", but it does not carry the first digit for other numbers. Therefore, it reaches the maximal number with n digits when it carries the first digit during an increment. The sample code of Increment is shown in Listing 5-6.

Listing 5-6. C++ Code to Increase on a String

 $It only takes O(1) time to check whether a number is increased to "999...99" in the function \\ Increment , which is faster than utilizing the function \\ strcmp \\ ...$

Now let's consider how to print the number in a string. The library function print is a handy tool to print a string, but it is not the best choice for this scenario. As mentioned earlier, the leading characters are 0s when the number of digits is less than n. The leading 0s in a number usually are not printed. Therefore, the function PrintNumber skips the leading 0s, as shown in Listing 5-7.

Listing 5-7. C++ Code to Increase on a String

```
void PrintNumber(char* number) {
  char* pChar = number;
  while(*pChar == '0')
    ++pChar;

if(*pChar != '\0')
    printf("%s\t*, pChar);
}
```

Simulating Permutation

The permutations of n digits ranging from 0 to 9 compose all numbers between 1 and 10^n -1. It is easy to implement the permutation recursively. Each digit is set as a value between 0 and 9, and then the next digit is set. It exits the recursion when all digits are set, as shown in Listing 5-8.

Listing 5-8. C++ Code to Print Numbers (Version 3)

```
void PrintIToMaxOfNDigits_3(int n) {
   if(n <= 0)
      return;

char* number = new char[n + 1];
   number[n] = '\0';

PrintIToMaxOfNDigitsCore(number, n, -1);

delete(1 number);
</pre>
```

```
void Print1ToMaxOfNDigitsCore(char* number, int length, int index) {
   if(index == length - 1) {
      PrintNumber(number);
      return;
   for(int i = 0; i < 10; ++i) {
      number[index + 1] = i + '0';
      Print1ToMaxOfNDigitsCore(number, length, index + 1);
   The function PrintNumber is the same as before, which skips the leading 0s and prints a number in a string.
```

 $More\ discussion\ about\ permutation\ is\ available\ in\ the\ section\ \textit{Permutation\ and\ Combination}.$

Source Code:

041_Print1ToMaxOfNDigits.cpp

Test Cases:

- Functional Cases (2, 3, 4, ...)
- Boundary Cases (1, 0, -1)

Question 42 Please design a function to add two arbitrary positive integers.

The problem requires you to add two arbitrary positive numbers, of which ranges are not specified. Therefore, you have to handle huge numbers beyond the range of the type int and even long long . Inspired by the solution of the preceding problem, strings are employed to express huge numbers.

What is the signature of the function? Your intuition might suggest that you pass the addition result in the return value, and the signature is defined as char* add(char* num1, char* num2). It $returns \ a \quad \text{NULL} \quad pointer \ for invalid inputs (including strings \ with non-digital characters \ and \quad \text{NULL} \quad pointers \ for numbers). Otherwise, it returns \ a string \ containing \ the \ addition \ result.$

The problem with this solution is that the add function allocates a string containing the addition result on the heap, and it expects its caller to release the memory. However, it is highly possible that the caller will forget to release memory because the memory is allocated by others. Usually, a function that allocates memory is responsible for release.

Therefore, the signature of the function can be defined as int add(char* num1, char* num2, char* sum) . It returns a non-zero value such as -1 when given invalid inputs; otherwise, it returns 0. It takes a pointer to a string for the addition result as the last parameter, which is passed from the caller. Therefore, the caller is responsible for allocating sufficient memory to accommodate the result and to release it afterward.

After the signature is figured out, it is time to implement the addition functionality. The sample code is shown in Listing 5-9.

```
Listing 5-9. C Code to Add Two Numbers in Strings
```

```
/* It returns -1 if the input invalid, otherwise returns 0. */
int add(char* num1, char* num2, char* sum) {
   int index1, index2, indexSum;
   int sumDigit, carry, digit1, digit2;
   if(checkInvalidInput(num1, num2, sum) != 0)
   reverse(num1):
   reverse(num2);
   index1 = index2 = indexSum = 0;
   carry = 0;
   while(num1[index1] != '\0' || num2[index2] != '\0') {
        digit1 = (num1[index1] == '\0') ? 0 : num1[index1] - '0';
        digit2 = (num2[index2] == '\0') ? 0 : num2[index2] - '0';
        sumDigit = digit1 + digit2 + carry;
        carry = (sumDigit >= 10) ? 1 : 0;
        sumDigit = (sumDigit >= 10) ? sumDigit - 10 : sumDigit;
        sum[indexSum++] = sumDigit + '0';
        if(num2[index2] != '\0')
           ++index2:
   if(carry != 0)
```

```
sum[indexSum++] = carry + '0';
sum[indexSum] = '\0';
```

Usually, addition begins from the last digits (also the least significant digits). However, it reverses numbers at first in the previous code and then adds numbers from the first digits. The reason is about simplicity. If it begins to add from the last digit, the index of the last digit in the sum is unknown before addition completes. For example, the sum of two numbers with two digits 33 and 44 is 77, which also has two digits. However, the sum of two other numbers with two digits 88 and 99 is 187, which has three digits. The index of the least significant digit is different even if it adds two numbers with two digits in both cases. When numbers are reversed, it begins to add from the first digit and set the first digit in the sum, no matter how many digits the sum will have finally.

Strings with non-digital characters are treated as invalid inputs. Additionally, NULL pointers to numbers should also be excluded from inputs in order to avoid execution crashes. The helper function checkInvalidInput in Listing 5-10 is defined to validate inputs.

Listing 5-10. C Code to Validate Inputs

```
int checkInvalidInput(char* num1, char* num2, char* sum) {
int length1, length2, i;
if(num1 == NULL \ | \ | \ num2 == NULL \ | \ | \ sum == NULL)
length1 = strlen(num1);
for(i = 0; i < length1; ++i) {
   if(num1[i] < '0' || num1[i] > '9')
   if(num2[i] < '0' || num2[i] > '9')
       return -1:
return 0;
The use of the following reverse function in Listing 5-11 reverses a given string.
```

Listing 5-11. C Code to Validate Inputs

```
void reverse(char* str) {
int i, length;
char temp;
   length = strlen(str);
for(i = 0; i < length / 2; ++i) {
   temp = str[i];
   str[i] = str[length - 1 - i];
    str[length - 1 - i] = temp;
```

Source Code:

042 AddNumericStrings.c

Test Cases:

- · Add numbers with/without a carry
- One or two numbers are very large
- . One or two numbers are invalid inputs (with non-numeric characters, or NULL pointers)

Delete Nodes from a List

Question 43 How to delete a given node from a single-linked list in O(1) time?

The most straightforward way to delete a node from a single-linked list is to scan all nodes in it and to find the target node to be deleted. It updates the next pointer in the preceding node and deletes the target.

Suppose node i in the list in Figure 5-3(a) is going to be deleted. It scans the list from its head node a. When it reaches node h (the preceding node of the target node i), the next pointer is updated to reference to node j (the next node of i). After reconnecting the link, node i is deleted. Nodes in the list remain connected, as shown in Figure 5-3(b). It costs O(n) time on a list with n nodes because it has to scan the list.

The reason it has to scan the list from its head is that it needs to get the node preceding the target. There is not a pointer to the preceding node in a single-linked list, so it has to traverse the list.

Is it absolutely necessary to get the preceding node of the target to be removed? The answer is no. It is easy to get the next node of the target in a single-linked list. If the target node data is replaced with the data in the next node and then the next node is deleted, it is equivalent to deleting the target node. Only the data in the target node gets removed, and the data in the next node is stored.

Let's take the list in Figure 5-3(a) as an example again. The node i is the target node to be removed. The new solution copies the data in node j, pastes it into node i, and then sets the next node of

node j as the next node of node i. When node j is deleted, it looks like node i is deleted, as shown in Figure 5-3(c).

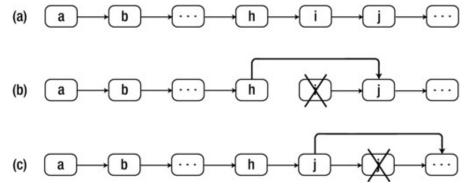


Figure 5-3. Two methods to remove a node from a list. (a) A sample list. (b) It scans the list from its head node. When it reaches node h, the preceding node of the target node i, it updates the next pointer in h to node j, which is the next node of node i. And then node i is deleted. (c) It replaces the data in node i with the data in node j and then deletes node j.

Notice that the tail node of the list does not have a next node. How do you delete it? We have to traverse the whole list, get the preceding node of the tail, and then delete the tail.

The last scenario is worthy of consideration when there is only one node in the list. When the only node is deleted, the pointer for the head node should be set as a NULL pointer, as shown in Listing 5-12.

```
Listing 5-12. C++ Code to Delete a Node from a List
```

```
void DeleteNode(ListNode** pListHead, ListNode* pToBeDeleted) {
if(!pListHead || !pToBeDeleted)
    return;
// The node to be deleted is not the tail of the list
if(pToBeDeleted->m_pNext != NULL) {
    ListNode* pNext = pToBeDeleted->m_pNext;
    pToBeDeleted->m nValue = pNext->m nValue:
    pToBeDeleted->m_pNext = pNext->m_pNext;
    delete pNext;
       pNext = NULL;
/\!/ The list has only one note. Delete the only node
else if(*pListHead == pToBeDeleted) {
    delete pToBeDeleted;
    pToBeDeleted = NULL;
    *pListHead = NULL:
// Delete the tail node of a list with multiple nodes
else {
    listNode* nNode = *nlistHead:
        pNode = pNode->m_pNext;
    pNode->m_pNext = NULL;
    delete pToBeDeleted;
    pToBeDeleted = NULL;
```

Now let's analyze the time efficiency of this solution. It only costs O(1) time to copy the data from the next node and delete the next node for the n-1 nodes, which are not at the end of the list. It costs O(n) time to delete the tail node because it has to scan the whole list. Therefore, the time efficiency on average is $[(n-1)\times O(1)+O(n)]/n$, and so is O(1). Source Code:

043_DeleteNodeInList.cpp

Test Cases:

- Functional Cases (Delete the head/tail node from a list or delete a node inside a list)
- Boundary Cases (Delete the only node in a list)
- Cases about Robustness (The pointer to the head node is NULL , or the pointer to the target node is NULL)

Question 44 Given a sorted linked list, please delete all duplicated numbers and leave only distinct numbers from the original list. For example, when the duplicated numbers in the list in Figure 5-4(a) are removed, it becomes the list in Figure 5-4(b).

The first step to solve this problem to figure out the signature of the required function. The head of the original list will be deleted if it is duplicated in the following nodes. Therefore, the function should be declared as void deleteDuplication(ListNode** pHead) rather than void deleteDuplication(ListNode** pHead).

We traverse the list beginning from the head of the list. When the value in the current visited node (pNode in the node below) is the same as the value in the next node, the current visited node

and its duplicate will be deleted. In order to make sure the list is still connected, the node prior to the current visited node (prenode in the code) is linked to the node with value greater than the current visited value. It should be guaranteed that prenode always points to the last node having a distinct value in the visited list so far.

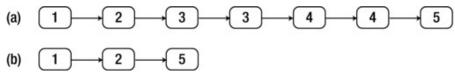


Figure 5-4. Remove duplicate numbers in a list. (a) A list with seven elements. (b) Three elements are left when duplications are removed.

Take the sample list as an example. When it visits the first node with value 3, prenode points to the node with value 2. Since the next node also has value 3, both nodes with value 3 should be deleted, and then the node pointed to by prenode is linked to the first node with value 4. Since the node with value 4 also has a duplicate, the node pointed by prenode is linked to the node with value 5 after nodes with value 4 are deleted. (See Listing 5-13.)

Listing 5-13. C++ Code to Delete Duplicated Nodes

```
void deleteDuplication(ListNode** pHead) {
   if(pHead == NULL || *pHead == NULL)
   ListNode* pPreNode = NULL;
   ListNode* pNode = *pHead:
    while(pNode != NULL) {
       bool needDelete = false;
       if(pNext != NULL && pNext->m_nValue == pNode->m_nValue)
            needDelete = true:
       if(!needDelete) {
           pPreNode = pNode;
            pNode = pNode->m pNext;
           ListNode* pToBeDeleted = pNode;
            while(pToBeDeleted != NULL && pToBeDeleted->m_nValue == value) {
               pNext = pToBeDeleted->m_pNext;
               delete pToBeDeleted;
               pToBeDeleted = NULL:
           if(pPreNode == NULL)
               pPreNode->m pNext = pNext;
Source Code:
```

Source Code:

044_DeleteDuplicationInList.cpp

Test Cases:

- Functional Cases (Groups of duplicated nodes are at the head/tail of a list, or groups of duplicated nodes are inside a list, or groups of duplicated nodes are continuous)
- Boundary Cases (All nodes in a list are duplicated, either in a duplication group or in multiple duplication groups)
- Cases Involving Robustness (The pointer to the head node is NULL)

Partition Numbers in Arrays

Question 45 Please reorder an input array to place all odds before evens. For example, after numbers in the array {1, 2, 3, 4, 5} are reordered, it looks like {1, 5, 3, 4, 2}. The result is not unique, and there are multiple arrays meeting the reordering criteria.

The brute-force solution is to scan the array sequentially and relocate every even number. Move all numbers behind the even number backward and then place it at the end of array. Since it has to shift O(n) numbers for an even number, the overall time complexity is $O(n^2)$.

Workable but Not Scalable

The problem asks you to place all odd numbers before even numbers. Therefore, we have to swap all pairs of numbers in which an even number is before an odd one.

Two pointers are defined to find such pairs. The first pointer P_1 is initialized at the first number, which moves forward, and the second one P_2 is initialized at the last number, which moves backward. When the number pointed to by P_1 is even and the number pointed by P_2 is odd, we have to swap these two numbers.

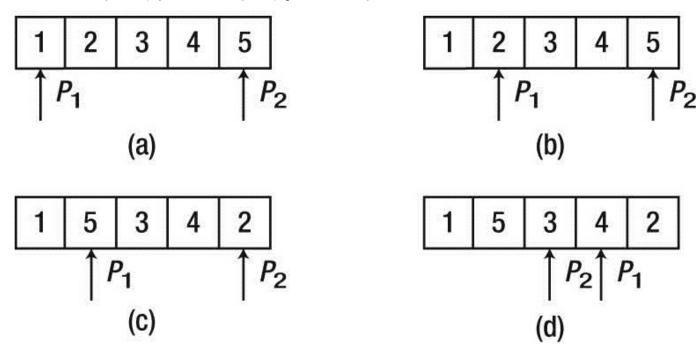


Figure 5-5. The process to place all odd numbers before even numbers in an array {1, 2, 3, 4, 5}. (a) P₁ points to the first number, and P₂ points to the last one in the array. (b) P₁ moves forward until it reaches the first even number, 2. Since P₂ already points to an odd number, it does not move. (c) Numbers pointed to by P₁ and P₂ are swapped. (d) P₁ moves forward until it reaches an even number, 4, and P₂ moves backward until it reaches an odd number, and P₂ moves backward until it reaches an odd number, and P₂ moves backward until it reaches an odd number, and P₂ moves backward until it reaches an odd number, and P₂ moves backward until it reaches an odd number, and P₂ moves backward until it reaches an odd number, and P₂ moves backward until it reaches an odd number, and P₂ moves backward until it reaches an odd number, and P₂ moves backward until it reaches an odd number, and P₂ moves backward until it reaches an odd number, and P₂ moves backward until it reaches an odd number, and P₂ moves backward until it reaches an odd number.

Let's take the sample array $\{1, 2, 3, 4, 5\}$ as an example to simulate the process to reorder numbers step-by-step. During the initialization phase, P_1 points to the first number in the array, and P_2 points to the last one (Figure 5-5(a)). The pointer P_1 moves forward until it reaches an even number 2, but P_2 does not move because it already points to an odd number 5 (Figure 5-5(b)). A pair of numbers in which an even number is before an odd one has been found. The state of the array is shown in Figure 5-5(c) after swapping.

It continues to move P_1 forward until reaching another even number, 4, and moves P_2 backward until reaching another odd number, 3 (Figure 5-5(d)). Since P_2 is now before P_1 , all odd numbers have been placed before even numbers in the array $\{1, 5, 3, 4, 2\}$.

We are able to implement this solution in Java with the step-by-step analysis above, as shown in Listing 5-14.

Listing 5-14. Java Code to Reorder Numbers in an Array (Version 1)

```
void reorderOddEven_solution1(int nums[]) {
  int begin = 0;
  int end = nums.length - 1;
  while(begin < end) {
    // Move begin forward until it meets an even number
    while(begin < end && (nums[begin] & 0x1) != 0)
        begin++;

    // Move end backward until it meets an odd number
    while(begin < end && (nums[end] & 0x1) == 0)
        end--;

    if(begin < end) {
        int temp = nums[begin];
        nums[begin] = rums[end];
        nums[end] = temp;
    }
}</pre>
```

Scalable to Handle Similar Scenarios

The solution in Listing 5-13 is acceptable for a graduate or a junior engineer. However, an interviewer may follow up with more questions if the candidate applies for a senior position as demonstrated in the following dialogue:

Interviewer:

Let's change the requirement to place all negative numbers before non-negative ones. How do you do it?

Candidate:

It's easy. Just define a method similar to before and modify the conditions in the second and third while loop.

Interviewer: Let's change the requirement again. We are going to partition an array into two parts where primes are placed before others.

Candidate: Define another new method of which the conditions ...

Interviewer: (Interrupting the candidate's words): Are there any better choices?

The candidate should get the interviewer's point: what he or she expects is a scalable solution to a series of similar problems.

Let's take a close look at those two new problems. In order to solve them, it is only necessary to modify conditions in the second and third while loop and leave the overall code structure untouched. Therefore, we can decouple the method into two parts: one is the criterion to place an element and the other is about how to partition an array into two sub-arrays. Let's define an interface criterion and a method reorder corresponding to these two purposes, as shown in Listing 5-15.

Listing 5-15. Java Code to Decouple Partitioning Criterion and Process

```
public interface Criterion{
  boolean check(int num);
```

```
void reorder(int nums[], Criterion criterion) {
  int begin = 0;
  int end = nums.length - 1;
  while(begin < end) {
    while(begin < end && !criterion.check(nums[begin]))
        begin++;

  while(begin < end && criterion.check(nums[end]))
        end--;

  if(begin < end) {
        int temp = nums[begin];
        nums[begin] = nums[end];
        nums[end] = temp;
    }
}</pre>
```

In order to place odd numbers before even ones, a specific criterion is Even is defined, as shown in Listing 5-16.

Listing 5-16. Java Code to Reorder Numbers in an Array (Version 2)

```
void reorderOddEven_solution2(int nums[]) {
Criterion isEven = new Criterion() {
   public boolean check(int num) {
      if((num & 0x1) == 0)
            return true;

   return false;
   }
};
reorder(nums, isEven);
```

If you must reorder numbers with other criteria, it is only necessary to implement new classes from the interface Criterion, but keep the method reorder untouched. Therefore, our decoupling strategy minimizes modification and potential risks to fulfill new requirements.

Source Code:

045_ReorderNumbers.java

Test Cases:

- Functional Cases (Including cases where all odd numbers are before even numbers in the original array, or all even numbers are before odd numbers, or numbers do not appear in any particular order)
- Boundary Cases (There is only an odd/even number in the array)

Question 46 Given an array and a value, how do you implement a function to remove all instances of that value in place and return the new length of the array? It is not required that you keep the order of the remaining numbers. It doesn't matter what you leave beyond the new length.

For example, if the input array is {4,3,2,1,2,3,6}, the resulting array after removing value 2 contains the numbers {4,3,1,3,6}, and the new length of the remaining array is 5.

Move Numbers for O(n) Times

The most straightforward solution for this problem is to scan the whole array from the beginning to the end. When a target number is scanned, it is skipped and numbers behind it are moved backward, as shown in Listing 5-17.

Listing 5-17. Java Code to Remove Numbers in an Array (Version 1)

```
int remove_solution1(int numbers[], int n) {
  int i = 0;
  for (int j = 0; j < numbers.length; j++) {
    if (numbers[j] != n)
        numbers[i++] = numbers[j];
}
return i;</pre>
```

Obviously, the time complexity of this solution is O(n). It is also noticeable that it has to move numbers for O(n) times even if the target number occurs only once in the original array because there are O(n) numbers behind it. Is it possible to reduce the times needed to move numbers? Let's explore alternatives.

Move Numbers for O(k) Times

Notice that it is not required to keep the order for the remaining numbers, and the problemdoes not care about what numbers are left except the new length. Therefore, this problem is essentially the same as the previous one. We partition the array into two parts: the left part contains all non-target values, and the right part contains target values to be removed.

Two pointers are defined to solve this problem. The first pointer (denoted as P_1) moves forward until it reaches a number equal to the target value, which is initialized at the beginning of the array. The other pointer (denoted as P_2) moves backward until it reaches a number different from the target value, which is initialized at the end of the array. Two numbers pointed to by P_1 and P_2 are swapped. We repeat the moving and swapping operations until all target numbers are scanned.

The sample code is shown in Listing 5-18.

Listing 5-18. Java Code to Remove Numbers in an Array (Version 2)

Since it is only necessary to scan the whole array once and it costs O(1) time to swap a target value, the overall time complexity is O(n) for an array with n numbers. Additionally, it swaps a pair of numbers only when a target number to be removed is scanned. If there are k target numbers in the array, it swaps O(k) times. Therefore, it is more efficient in terms of data moving.

Source Code:

046_RemoveNumbers.java

Test Cases:

- Functional Cases (There is a single target number to be removed in the array, there are multiple target numbers in the array, or there are no target numbers in the array)
- Boundary Cases (There is only one number in the array, which is/is not the target number to be removed; all numbers in the array are to be removed; the first/last number is/is not the target number)