

Design and Stabilization of a One Legged Hopper

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Guide

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Co-guide

B.Tech. Project

Outline

- 1 Introduction
- 2 Design
- 3 Modeling
- 4 Gaits
- 5 Attitude Estimation
- 6 Conclusion

Springy Leg Offset Mass

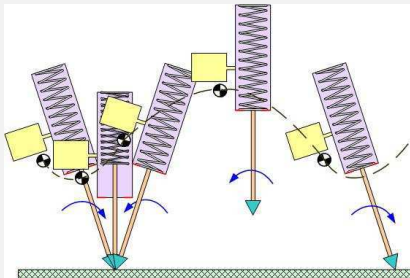


Figure: SLOM motion

Stages

- Lift-off
- Free fall
- Touch-down
- Stance

Terms

- Energy Pumping Mechanism
- Constraint
- Energy Release

Design of robot

- Efficient EPM
- Reaction wheel
- Onboard electronics

Theory

- Non-linear model
- Initial conditions
- In-place hopping
- Running gait

Experiments

- Attitude estimation
- Fabrication and interfacing of electronics

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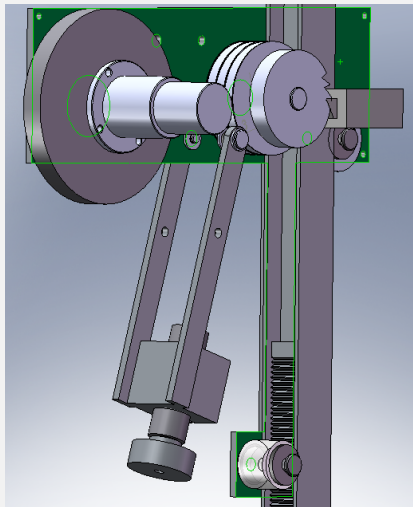
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Final Design



Features

- **EPM :**
 - Motor travels down on rack
 - Dual springs, helical gears and slant rack
- **Constraint :**
 - Ratchet and Paul
 - Band drive
 - Disengage motor sleeve

Figure: Detached motor sleeve

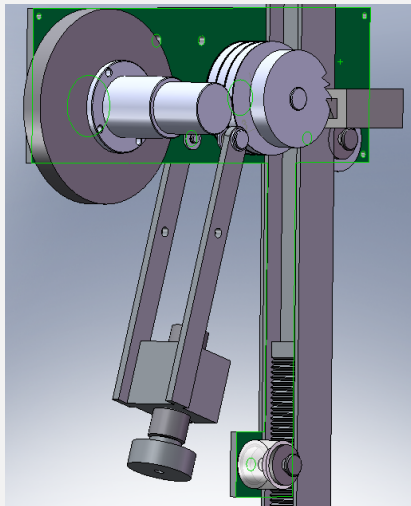


Figure: Detached motor sleeve

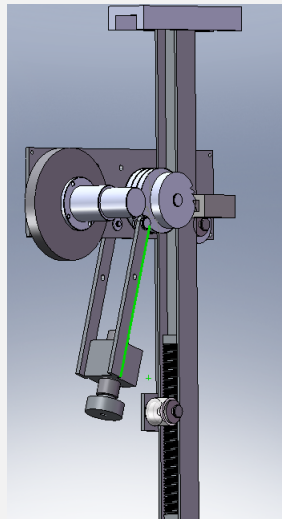


Figure: Full Robot

Final Design

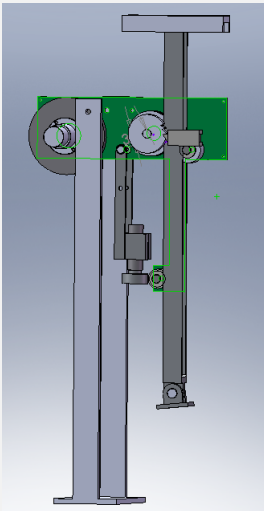


Figure: Test Rig

Features

- Test-rig :
 - Pivoted near the C.G.
 - Attitude re-orientation
 - Simulated hopping
- Overall :
 - Height : ~ 500 mm
 - Leg ~ 0.7 kg
 - Total ~ 4.7 kg
 - Disengage motor sleeve

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Equations of motion

Euler–Lagrangian equations

$$T = \frac{1}{2} \left[m_w (\dot{x}_w^2 + \dot{y}_w^2) + m_p (\dot{x}_p^2 + \dot{y}_p^2) + m_l (\dot{x}_l^2 + \dot{y}_l^2) + J_w (\dot{\phi} + \dot{\theta})^2 + J_b \dot{\theta}^2 \right]$$

$$V = g [m_l y_l + m_w y_w + m_p y_p] + \frac{1}{2} K (l - l_0)^2$$

$$L = T - V$$

$$q = [x \quad y \quad l \quad \theta \quad \phi]$$

$$\frac{d}{dt} \left(\frac{\partial L}{\partial \dot{q}_A} \right) - \frac{\partial L}{\partial q_A} = Q_A$$

$$Q_A = \sum_{r=1}^m \lambda_r \frac{\partial \psi_r}{\partial q_A}$$

Stance Phase

Stance Phase

- Foot touches the ground when,

$$y(t) = (l_{impact} - l_0) \cos \theta_{impact} + d \sin \theta_{impact}$$

- Constraint equations,

$$y(t) = (l(t) - l_0) \cos \theta + d \sin \theta$$

$$x(t) = x_{f-impact} - (l(t) - l_0) \sin \theta - d \cos \theta$$

where

$$x_{f-impact} = x_{impact} + (l_{impact} - l_0) \sin \theta_{impact} + d \cos \theta_{impact}$$

- Phase ends when

$$l(t) = l_0$$

Flight Phase

Spring Controller

$$\ddot{I}(t) = \begin{cases} 0 & I(t) \leq (I_0 - \epsilon) \text{ OR } I(t) \geq (I_{max} + \epsilon) \\ I_{accel} & I_0 \leq I(t) \leq \frac{(I_{max} + I_0)}{2} \\ -I_{accel} & \frac{(I_{max} + I_0)}{2} \leq I(t) \leq I_{max} \end{cases}$$

- Convert $\ddot{I}(t)$ control law to implementable $\dot{I}(t)$ form
- Sense $\omega(t)$ with encoders,

$$e(t) = \omega(t) - \omega_d(t)$$

$$U_I(t) = K_w \omega_d(t) + K_p e(t) + K_d \frac{d e(t)}{dt} + K_i \int e(t) dt$$

Spring Phase

Constrained flight phase

- Constraint is,

$$l(t) = l_{max}$$

- Solver stops when,

$$y(t) = (l(t) - l_0) \cos \theta + d \sin \theta$$

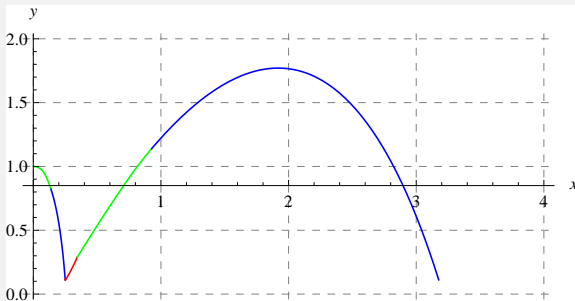


Figure: Equations of motion propagation

Initial Conditions

- Topmost point of the trajectory,
i.e. $x = 0$, $\dot{x} = 1$, $\dot{y} = 0$, $y = 1$, ϕ is constrained
- Calculate the amount of energy lost in the impact to give $I_{max} = 0.37m$
- Vary θ_0 and $\dot{\theta}_0$ to minimize norm
- Define norm as,

$$norm = \sum_{i=1, i \neq 1, 5, 10}^{10} ||q_{A_i} - q_{B_i}||$$

Remove $x(t)$, $\phi(t)$ and $\dot{\phi}(t)$ from the norm

- Problems with optimizing algorithm, hence manual search
- $\theta_0 = 0$ and $\dot{\theta}_0 = -0.5$ rad/s

Outline

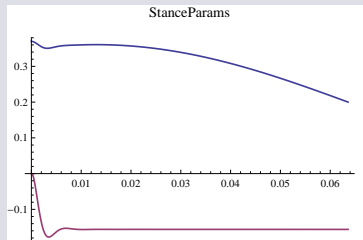
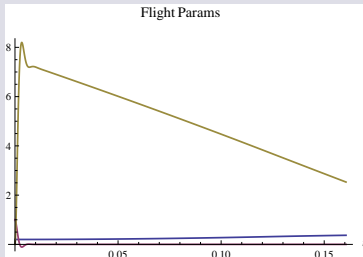
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In-place hopping

Controller

- Impact torque destabilizing, control robot attitude
- Flight, spring phases : $\theta_d = 0$
- Stance phase,

$$\theta_d = \tan^{-1} \left(\frac{x_{impact}}{h_{max}} \right)$$



- $I(t)$ - Blue, $\theta(t)$ - Pink, $\phi(t)$ - Yellow, t = secs

Inplace : Trajectory

- Start at $y = 1\text{m}$, $\theta = 1\text{ rad}$, $\dot{\theta} = -1\text{ rad/s}$

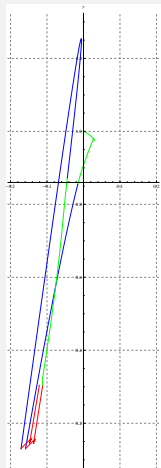


Figure: Inplace : Trajectory

Stance controller

Details

- Most important phase for control
- Generate $\theta_G(t)$ using good initial conditions
- PID torque controller for $e = \theta - \theta_G$



Figure: Good - Blue, Perturbed - Pink, distances in meters

Flight, Spring phases

Control

- Large time-scales
- Solve attitude reorientation to impact attitude

$$\Delta \theta(t) = \theta_{impact} - \theta(t)$$

$$\ddot{\phi}_d(t) = \left(\frac{-2 J_b}{J_w} \right) \left(\frac{\Delta \theta - \dot{\theta}(t) t_{left}}{t_{left}^2} \right)$$

$$e(t) = \ddot{\phi}(t) - \ddot{\phi}_d(t)$$

$$U_{\phi}(t) = \ddot{\phi}_d(t) + K_p e(t) + K_d \ddot{\phi}(t) + K_i \int \phi dt$$

Controlled trajectory

- Perturb attitude at liftoff

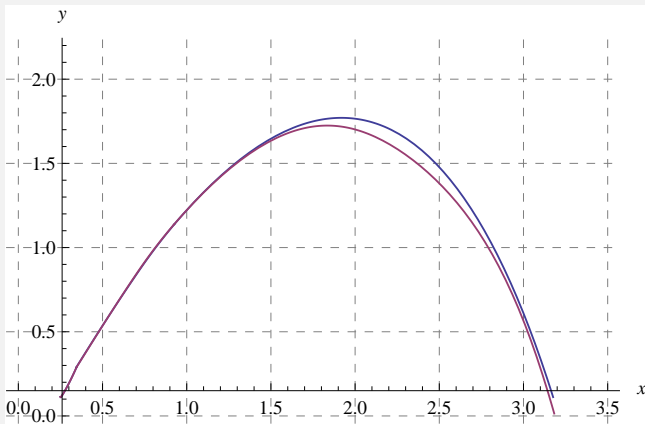


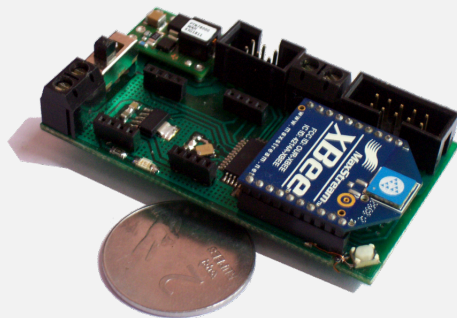
Figure: Trajectory Controller : Good - Blue, Perturbed - Pink

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ReWac Board Hardware

- Microchip dsPIC33F
16 bit, 40 MIPS
- Accelerometer
2.162 LSB/mg
- Gyroscope (50 Hz)
 $0.07326^{\circ}/s/LSB$
- Self-made MOSFET
motor driver
- XBee module



Kalman Filter

Why

- Pitch attitude estimate
- Computing power

How

$$\mathbf{x} = [x_1 \ x_2]^T = [\theta \ \dot{\theta}]^T$$

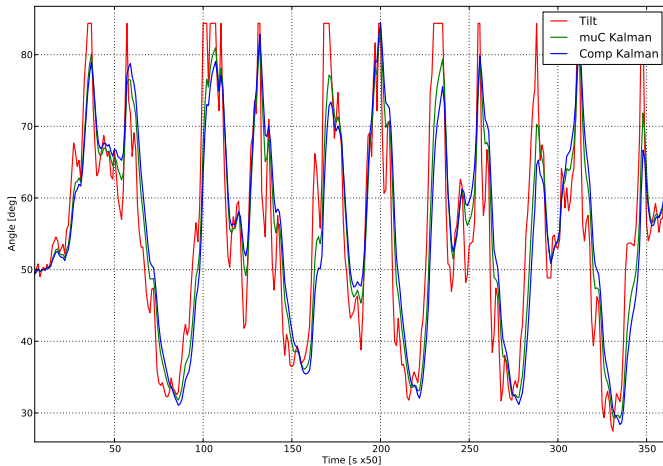
$$\mathbf{x}_{k+1} = \mathbf{A} \mathbf{x}_k + \mathbf{B} \mathbf{u}_k + \mathbf{w}_k$$

$$y_{k+1} = \mathbf{C} \mathbf{x}_{k+1} + z_{k+1}$$

Tricks

- Sparse covariance matrix
- Remove matrix operations
- Fixed point arithmetic

High Frequency Input sampled at 50 Hz



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Summary

Fabrication

- Robot fabrication almost done
- Electronics ready

Controller

- In-place hopping solved
- More work on trajectory following

Future Work

- Assisted test-rig control
- Running on treadmill