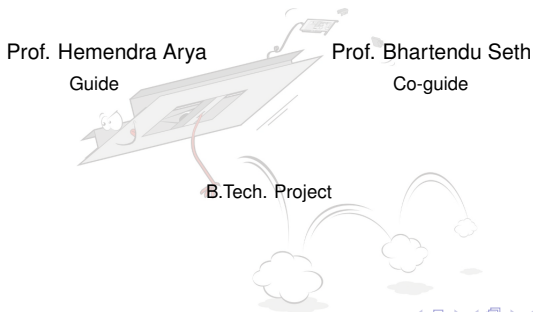


Design and Stabilization of a One Legged Hopper

Pratik Chaudhari

06D01015



Outline

- 1 Introduction
- 2 SLOM
- 3 Mechanical Design
- 4 Analysis
- 5 Embedded System

Springy Leg Offset Mass

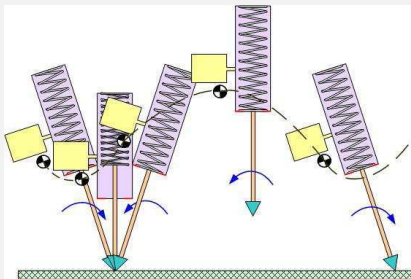


Figure: SLOM motion

Stages

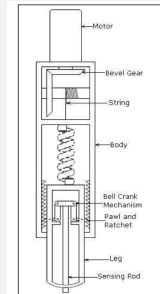
- Lift-off
- Free fall
- Touch-down
- Stance

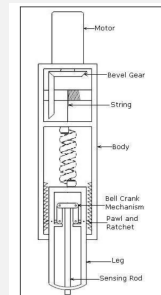
Terms

- Energy Pumping Mechanism
- Constraint
- Energy Release

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- Compression spring
- Ratchet and pawl activated by voice coil
- Large leg mass : Small hopping height
- In-place hopping : Feed forward control law

- Spring compressed by a motor
- Bell-crank constraint mechanism
- Use of impact to release energy

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Problem Definition

Features

- SLOM concept, 2D / 3D hopping
- Tension springs instead of compression spring
- Reduce leg mass, higher hopping heights
- Reaction wheel
 - Necessary for inplace hopping
 - Stable running gait
- Onboard embedded system

Design 1

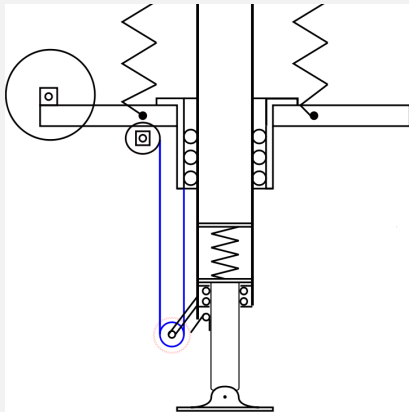


Figure: Winch pulley design

Features

- **EPM :**
 - Motor pulls itself down
 - Moves twice the extension
- **Constraint :**
 - Toothed pulley constrained by the hatch
 - Impact pushes hatch inside
 - Momentum transfer

Design 1

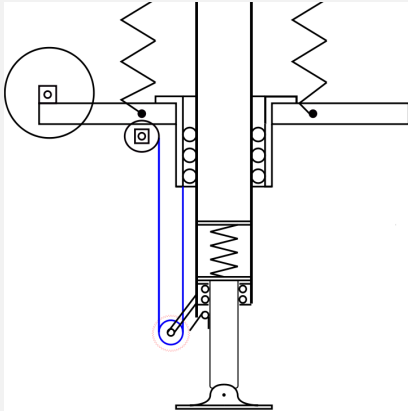


Figure: Winch pulley design

Evaluation

- Pros :

- Simple constraint mechanism
- Easier to make a light leg

- Cons :

- Winch can slide off the pulley
- Torsion spring : potential point of failure
- Torques on roller bearings

Design 2

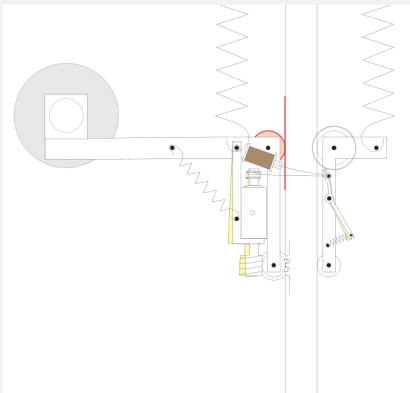


Figure: Rack and pinion design

Features

- **EPM :**
 - Rack worm-worm wheel
 - Band drive
 - Main spring can push the worm onto the rack
- **Constraint :**
 - Friction pulley
 - Ratchet with paul
 - Motor sleeve moves left

Design 2

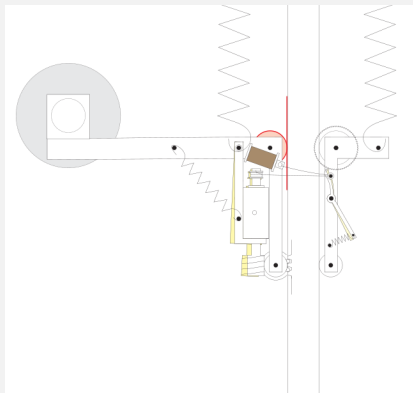


Figure: Rack and pinion design

Evaluation

● Pros :

- Mechanical advantage
- Less moving parts, easier to build

● Cons :

- Friction pulley
- Lower resolution

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Objectives

Objective

- Estimate masses, dimensions
- Choose motors and electronics

Design 1

- Reaction wheel
- Springs
- Winding motor
- Platform
- Lower leg, main leg masses

Design 2

- Reaction wheel
- Springs
- Rack-pinion drive and motor
- Platform and leg mass

Objectives

Objective

- Estimate masses, dimensions
- Choose motors and electronics

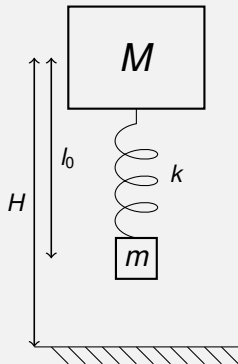
Design 1

- Reaction wheel
- Springs
- Winding motor
- Platform
- Lower leg, main leg masses

Design 2

- Reaction wheel
- Springs
- Rack-pinion drive and motor
- Platform and leg mass

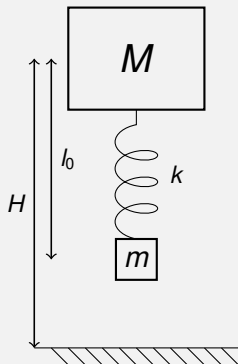
Two Mass Problem



$$h_n = \frac{Mh_{n-1} + ml_0}{M + m}$$

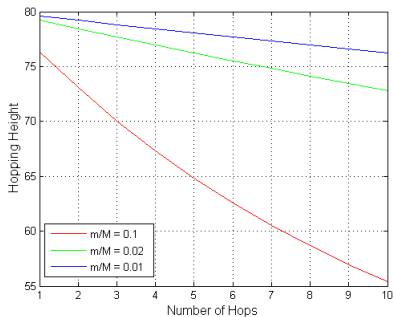
$$E_{loss} = \frac{Mg(H - l_0)}{1 + M/m}$$

Two Mass Problem

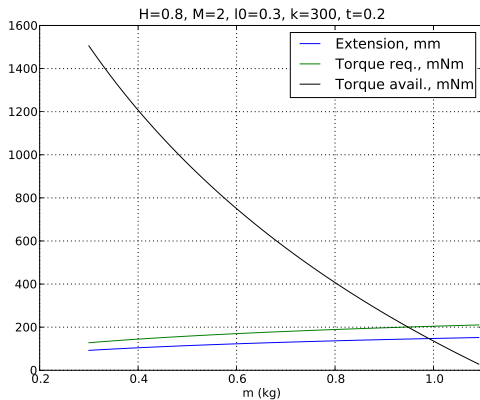


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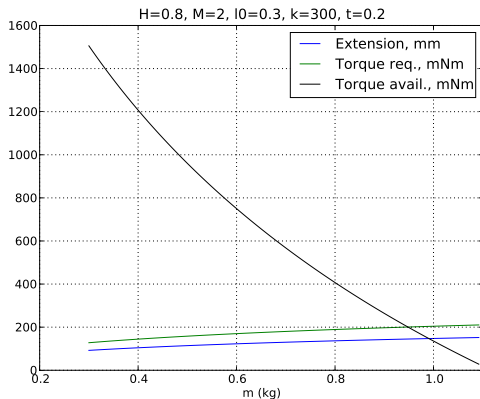
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Torque Requirements



Torque Requirements



Results

- $m \sim 0.5 \text{ kg}$
- $k \sim 300 \text{ N}$
- $M \sim 2 \text{ kg}$
- Lower leg $\sim 12 \text{ cms}$
- Standard rack-pinion
- Faulhaber 2342 motor
- 43 : 1 gearbox

ReWac : Idea and Advantages

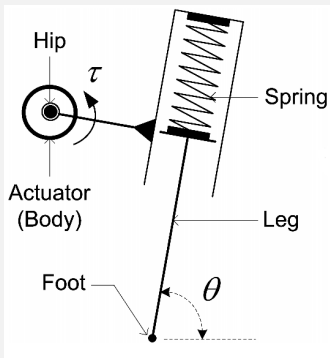


Figure: ReWac : Schematic

Inertia Wheel Assembly

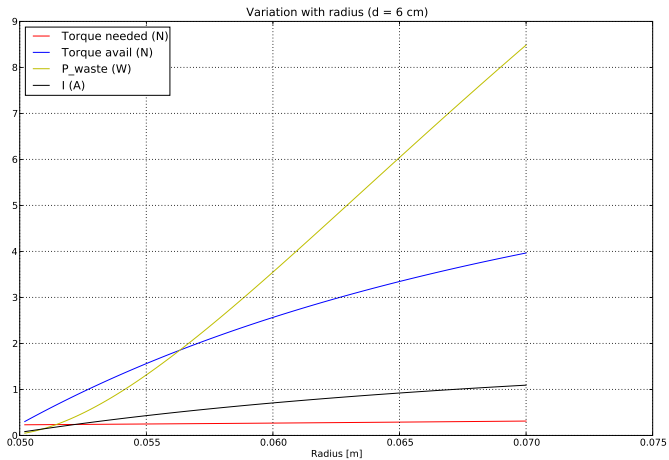
Conserve angular momentum

$$\dot{\theta}_b = -\frac{J_w}{J_b + J_w} \dot{\theta}_w$$

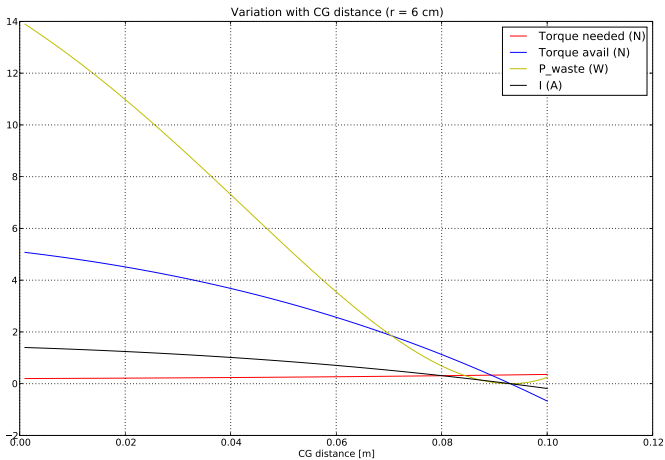
Uses

- Initial condition
- Changing hopping height online
- Change from an **arbitrary** pitch to **steady state** pitch within one hop

ReWac : Radius



ReWac : CG distance



Impact Analysis

Concept

- Desired hopping height dictates impact frequency
- Masses dictate energy loss
- **Natural frequency** of the system should be much **higher** than hopping frequency

Results

- Hopping frequency is a weak function of hopping height and M
- **Leg mass** consideration is important

Impact Analysis

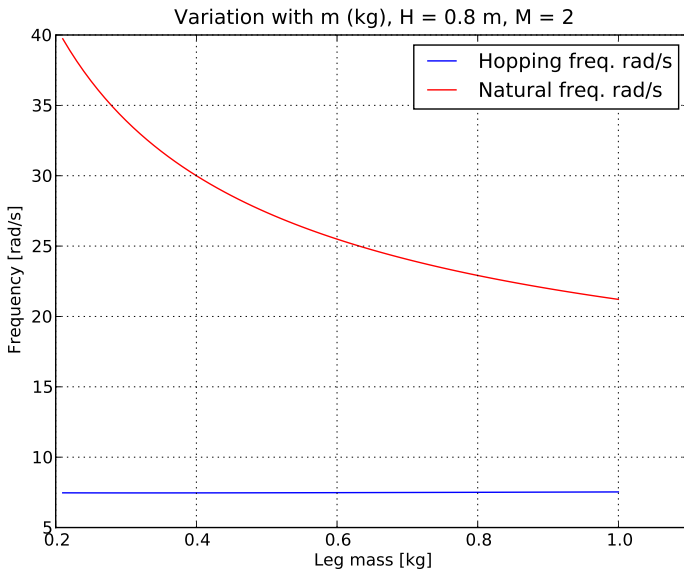
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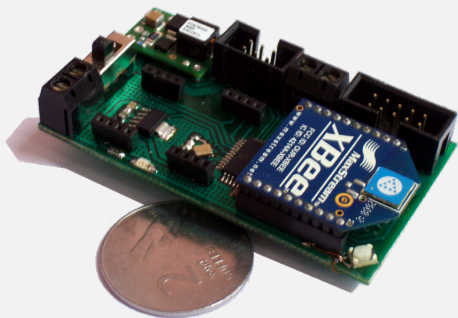
Impact : Leg mass



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ReWac Board Hardware



- Microchip dsPIC33F
16 bit, 40 MIPS
- Accelerometer
2.162 LSB/mg
- Gyroscope (50 Hz)
 $0.07326^{\circ}/s/LSB$
- 5A motor driver
- XBee module

Kalman Filter

Why

- Pitch attitude estimate
- Computing power

How

$$\mathbf{x} = [x_1 \ x_2]^T = [\theta \ \dot{\theta}]^T$$

$$\mathbf{x}_{k+1} = \mathbf{A} \mathbf{x}_k + \mathbf{B} \mathbf{u}_k + \mathbf{w}_k$$

$$y_{k+1} = \mathbf{C} \mathbf{x}_{k+1} + z_{k+1}$$

Tricks

- Sparse covariance matrix
- Remove matrix operations
- Fixed point arithmetic

Attitude Estimation

Accelerometer

- Slow, absolute reading
- **Body accelerations** - Noise
- High frequency noise

Gyroscope

- Fast
- Drifts slowly, randomly

- After liftoff ~ **250 ms**
 - Only force is gravity
 - Both sensors used
- Free fall ~ **250 ms**
 - No accelerometer reading
 - Propagate using rate only
- Stance ~ **150 ms**
 - **Ankle potentiometer**

High Frequency Input sampled at 50 Hz

