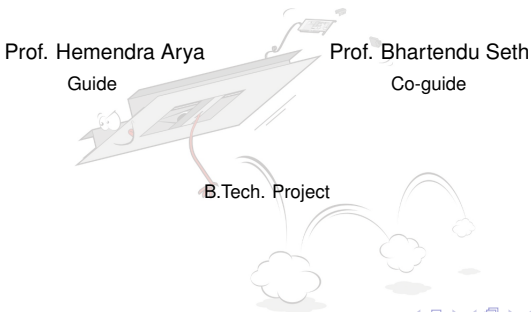


# Design and Stabilization of a One Legged Hopper

Pratik Chaudhari

06D01015



# Outline

- 1 Introduction
- 2 SLOM
- 3 Mechanical Design
- 4 Analysis
- 5 Embedded System

# Springy Leg Offset Mass

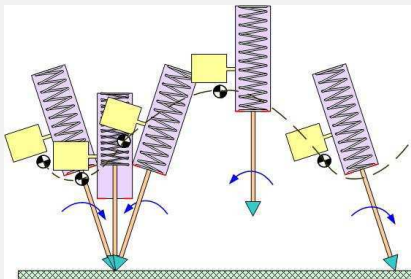


Figure: SLOM motion

## Stages

- Lift-off
- Free fall
- Touch-down
- Stance

## Terms

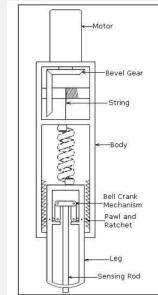
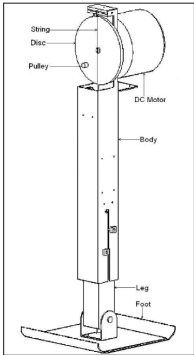
- Energy Pumping Mechanism
- Constraint
- Energy Release

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Introduction	SECM	Mechanical Design	Analysis	Embedded System
○	●	○○○○○	○○○○○○○	○○○○○

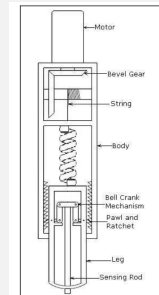
## Previous Work



- Compression spring
- Ratchet and pawl activated by voice coil
- Large leg mass : Small hopping height
- In-place hopping : Feed forward control law

- Compression spring
- Ratchet and pawl activated by voice coil
- Large leg mass : Small hopping height
- In-place hopping : Feed forward control law

Diagram of a DC Motor Driven Pendulum Apparatus. The diagram shows a vertical assembly. At the top, a DC Motor is connected to a Disc. A String is wound around the Disc and passes over a Pulley. The string is attached to a pendulum bob. The main vertical structure is labeled Body. The base is labeled Leg and Foot.



- Spring compressed by a motor
- Bell-crank constraint mechanism
- Use of impact to release energy

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# Problem Definition

## Features

- SLOM concept, 2D / 3D hopping
- Tension springs instead of compression spring
- Reduce leg mass, higher hopping heights
- Reaction wheel
  - Necessary for inplace hopping
  - Stable running gait
- Onboard embedded system



# Design 1

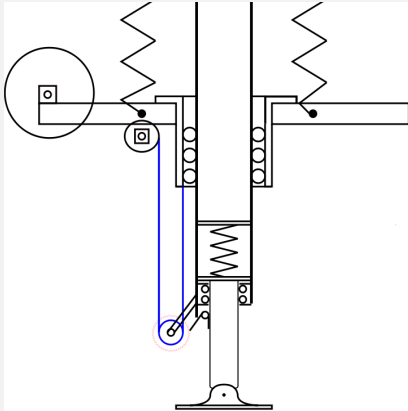


Figure: Winch pulley design

## Features

- EPM :
  - Motor pulls itself down
  - Moves twice the extension
- Constraint :
  - Toothed pulley constrained by the hatch
  - Impact pushes hatch inside
  - Momentum transfer

# Design 1

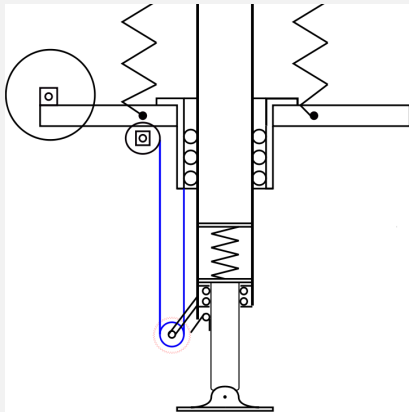


Figure: Winch pulley design

## Evaluation

- Pros :

- Simple constraint mechanism
- Easier to make a light leg

- Cons :

- Winch can slide off the pulley
- Torsion spring : potential point of failure
- Torques on roller bearings

# Design 2

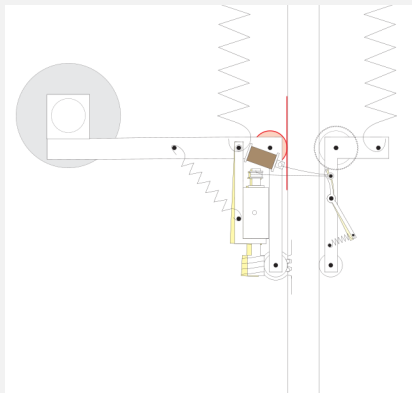


Figure: Rack and pinion design

## Features

- **EPM :**
  - Rack worm-worm wheel
  - Band drive
  - Main spring can push the worm onto the rack
- **Constraint :**
  - Friction pulley
  - Ratchet with paul
  - Motor sleeve moves left

# Design 2

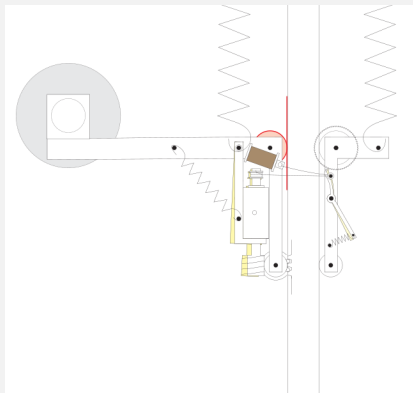


Figure: Rack and pinion design

## Evaluation

### ● Pros :

- Mechanical advantage
- Less moving parts, easier to build

### ● Cons :

- Friction pulley
- Lower resolution

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# Objectives

## Objective

- Estimate masses, dimensions
- Choose motors and electronics

## Design 1

- Reaction wheel
- Springs
- Winding motor
- Platform
- Lower leg, main leg masses

## Design 2

- Reaction wheel
- Springs
- Rack-pinion drive and motor
- Platform and leg mass

# Objectives

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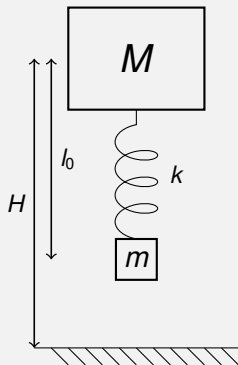
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- Reaction wheel
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- Reaction wheel
- Springs
- Rack-pinion drive and motor
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# Two Mass Problem

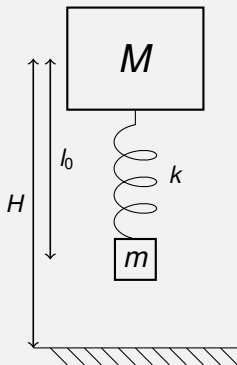


$$h_n = \frac{Mh_{n-1} + ml_0}{M + m}$$

$$E_{loss} = \frac{Mg(H - l_0)}{1 + M/m}$$

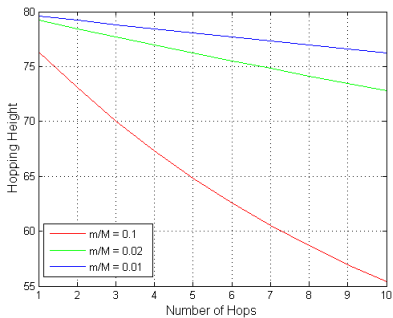


# Two Mass Problem

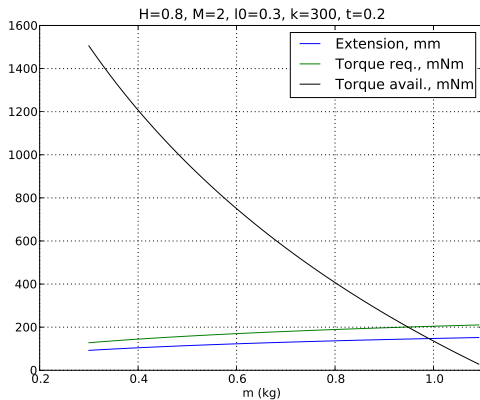


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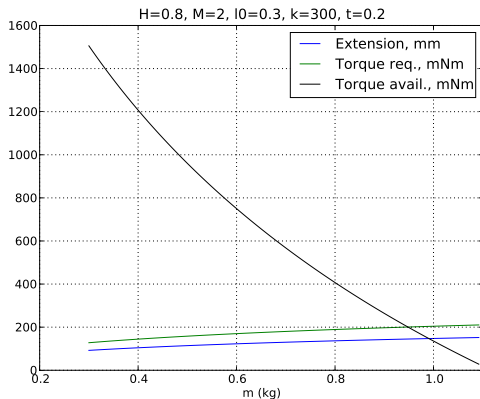
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# Torque Requirements



# Torque Requirements



## Results

- $m \sim 0.5 \text{ kg}$
- $k \sim 300 \text{ N}$
- $M \sim 2 \text{ kg}$
- Lower leg  $\sim 12 \text{ cms}$
- Standard rack-pinion
- Faulhaber 2342 motor
- 43 : 1 gearbox

# ReWac : Idea and Advantages

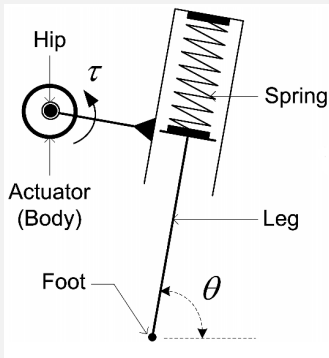


Figure: ReWac : Schematic

## Inertia Wheel Assembly

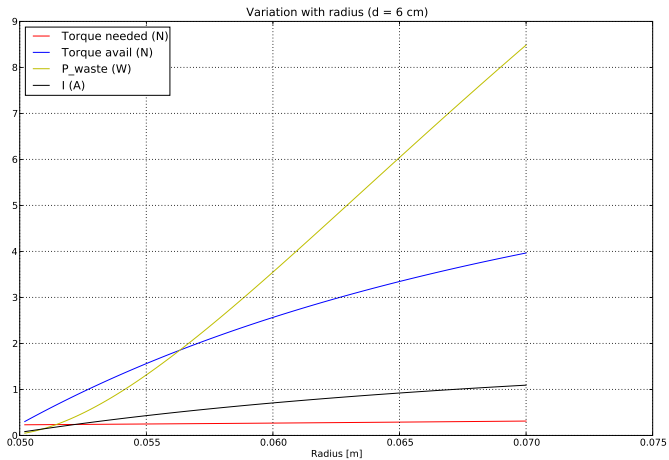
Conserve angular momentum

$$\dot{\theta}_b = -\frac{J_w}{J_b + J_w} \dot{\theta}_w$$

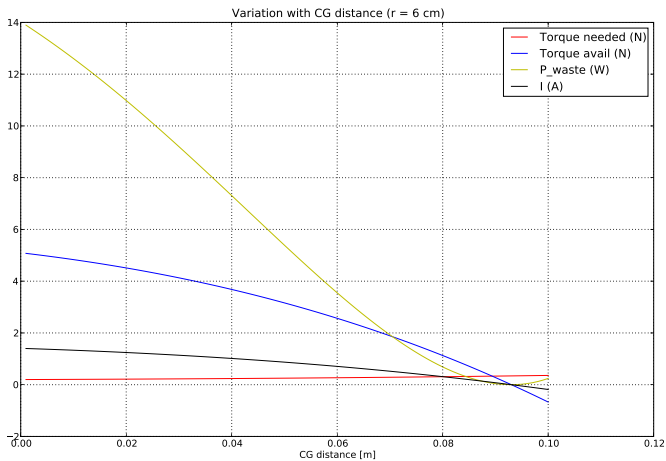
## Uses

- Initial condition
- Changing hopping height online
- Change from an **arbitrary** pitch to **steady state** pitch within one hop

# ReWac : Radius



# ReWac : CG distance



# Impact Analysis

## Concept

- Desired hopping height dictates impact frequency
- Masses dictate energy loss
- **Natural frequency** of the system should be much **higher** than hopping frequency

## Results

- Hopping frequency is a weak function of hopping height and M
- A large **dependence** on **leg mass**

# Impact Analysis

## Concept

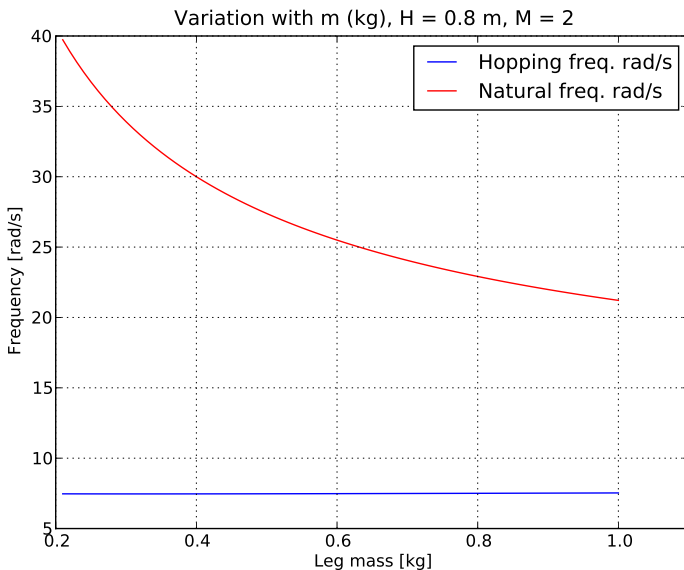
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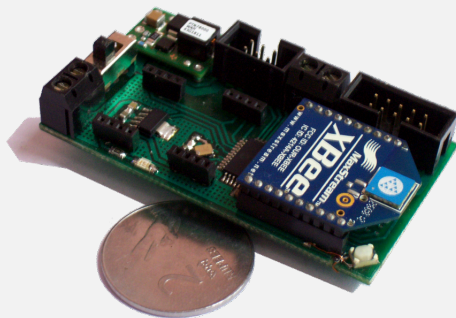
# Impact : Leg mass



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# ReWac Board Hardware



- Microchip dsPIC33F  
40 MIPS
- Accelerometer  
2.162 LSB/mg
- Gyroscope (50 Hz)  
 $0.07326^{\circ}/s/LSB$
- Quadrature Encoders
- XBee module

# Kalman Filter

## Why

- Pitch attitude estimate
- Computing power

## How

$$\mathbf{x} = [x_1 \ x_2]^T = [\theta \ \dot{\theta}]^T$$

$$\mathbf{x}_{k+1} = \mathbf{A} \mathbf{x}_k + \mathbf{B} \mathbf{u}_k + \mathbf{w}_k$$

$$y_{k+1} = \mathbf{C} \mathbf{x}_{k+1} + z_{k+1}$$

## Tricks

- Sparse covariance matrix
- Remove matrix operations
- Fixed point arithmetic

# Attitude Estimation

## Accelerometer

- Slow, absolute reading
- **Body accelerations** - Noise
- High frequency noise

## Gyroscope

- Fast
- Drifts slowly, randomly

- After liftoff ~ **250 ms**
  - Only force is gravity
  - Both sensors used
- Free fall ~ **250 ms**
  - No accelerometer reading
  - Propagate using rate only
- Stance ~ **150 ms**
  - **Ankle potentiometer**



# High Frequency Input sampled at 50 Hz

