

Recursion

1) Base case condition

2) Recursive

function call itself

call

Fibonacci Series

0	1	2	3	4	5	6	7
0	1	1	2	3	5	8	13

$$\text{fib}(n) \Rightarrow \begin{cases} n & n \leq 1 \\ \text{fib}(n-1) + \text{fib}(n-2) & n > 1 \end{cases}$$

Method
name

fib(n)

① Base case condition

if ($n \leq 1$)

return n;

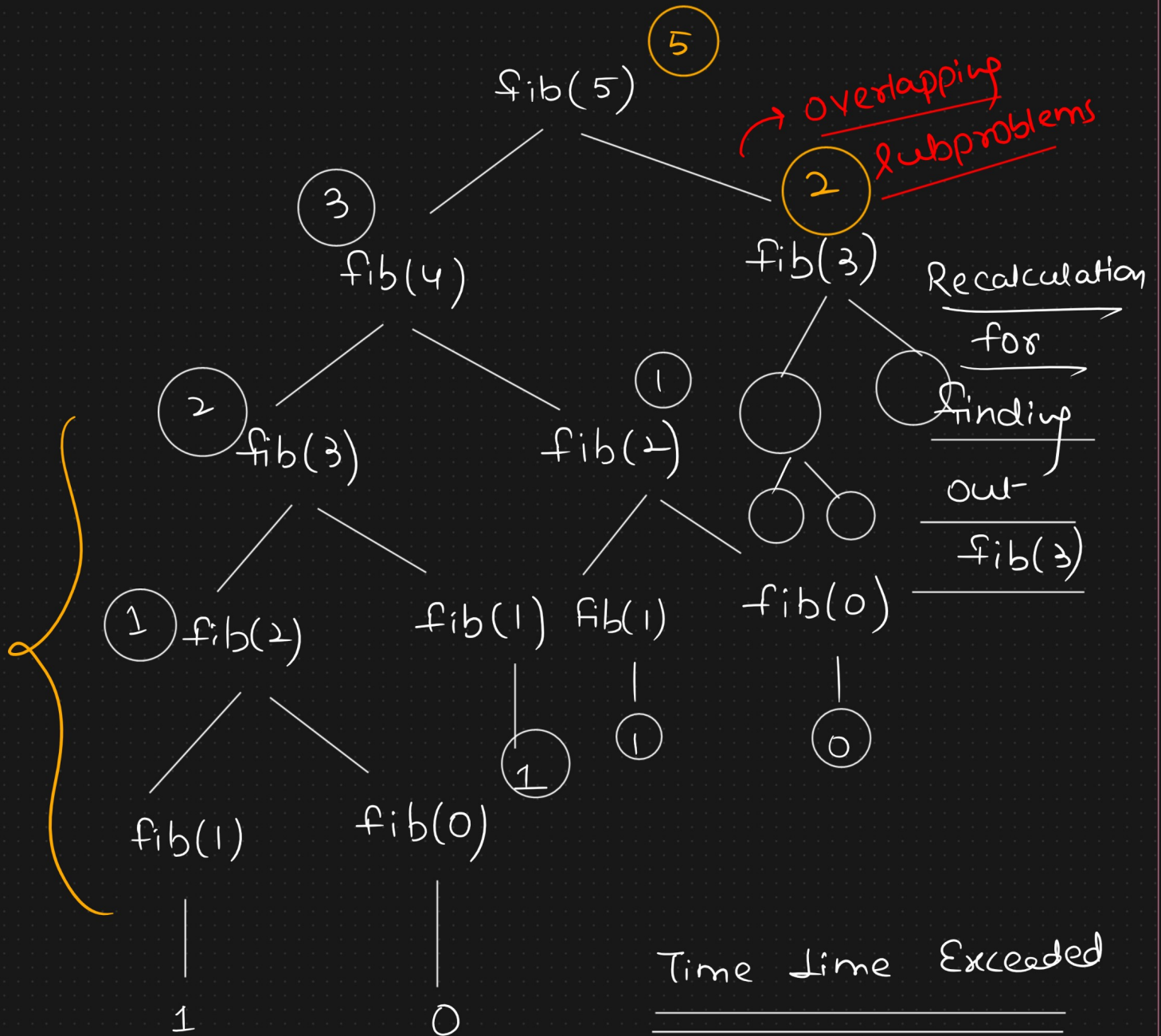
else

return fib(n-1) + fib(n-2);

different
set of
parameters

$O(2^n)$

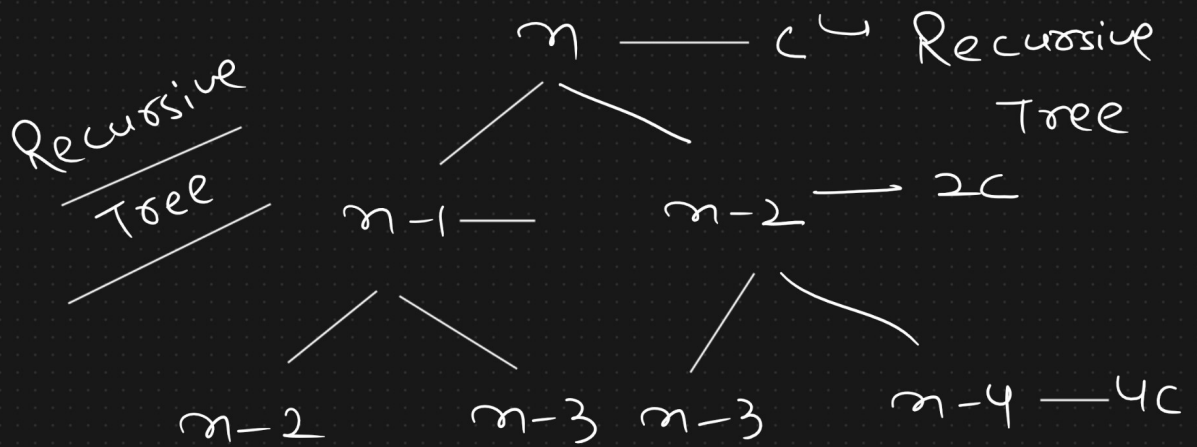
② Recursion



Dynamic Programming

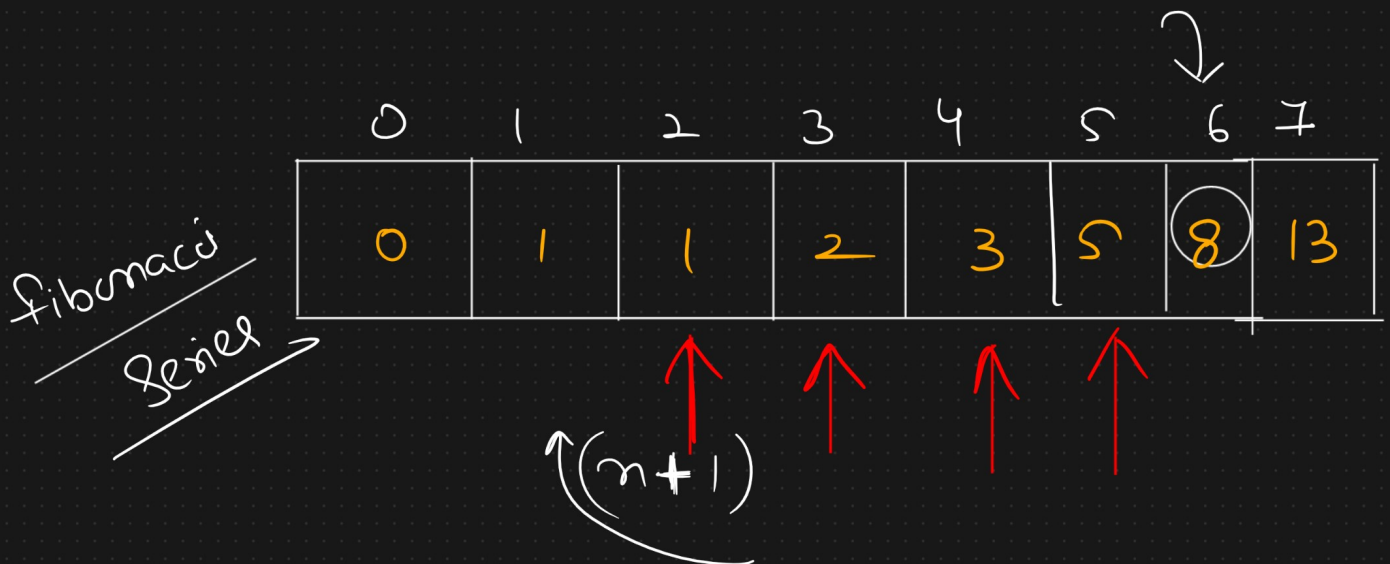
$\text{fib}(2)$	
$\text{fib}(3)$	
$\text{fib}(4)$	
$\text{fib}(5)$	<u>Stack</u>

$$T(n) = \underline{T(n-1)} + \underline{T(n-2)} + c$$



$$\underline{\underline{O(2^n)}}$$

$n=5$



Climbing a Stairs ——— (n)

n=1
↳ 1 way 1 step

n=2
↳ 2 ways 1 step, 1 step
2 steps

n=3 1 step, 1 step, 1 step
↳ 3 ways 1 step, 2 step
2 step, 1 step

n=4 1 step, 1 step, 1 step,
1 step
↳ 5 ways 1 step, 2 step,
1 step

2 step, 1 step,
2 step

2 step, 1 step,
1 step
1 step, 1 step,
2 step

$$n = 5$$

→ 8 ways

1 | 1 | 1 | 1 | 1 | _____

1 2 2 _____

2 1 2 _____

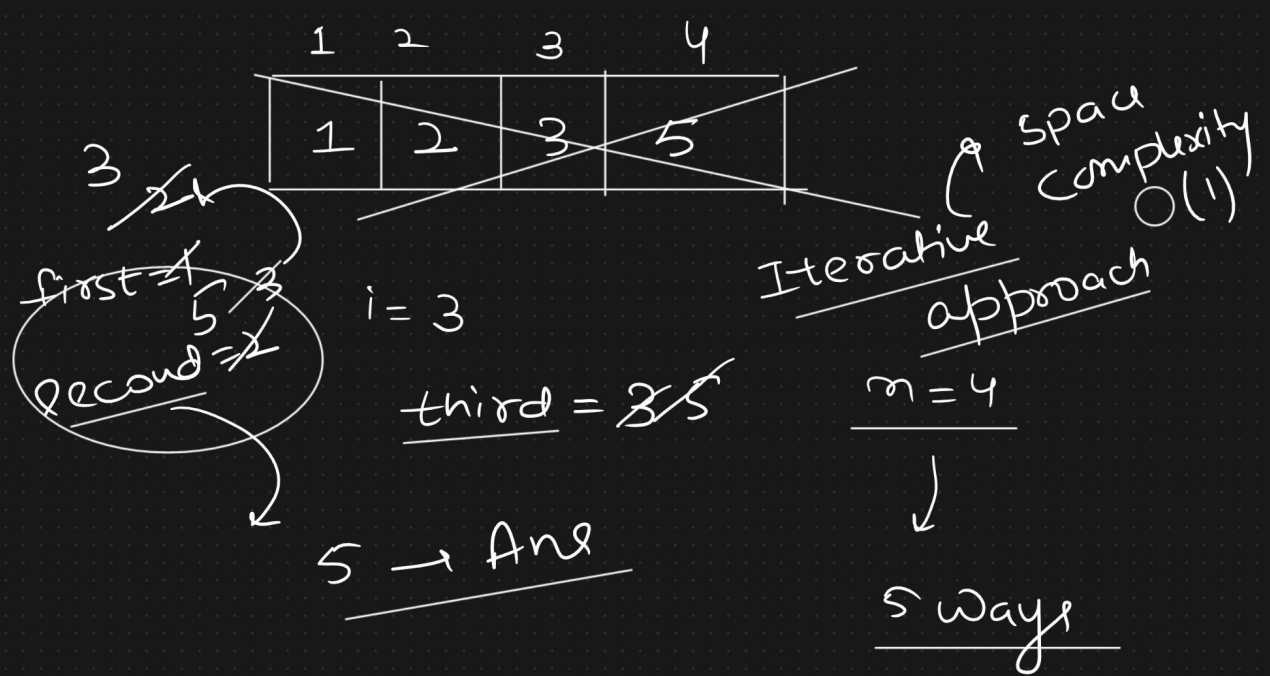
2 2 1 _____

2 1 1 1 _____

1 2 1 1 _____

1 1 2 1 _____

1 1 1 2 _____



Time complexity $\rightarrow O(n)$
Space complexity $\rightarrow O(1)$