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Assignment 10

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Abstract—This document gives an explicit description of the vectors in R^5 which are linear combination of the vectors.

Download latex-tikz codes from

https://github.com/priya6971/ matrix theory EE5609/tree/master/ Assignment10

Download python codes from

https://github.com/priya6971/ matrix theory EE5609/tree/master/ Assignment10/codes

1 Problem

Give an explicit description of the type b_i = $\sum_{i=1}^{r} b_{ki} R_{ij}$ for the vectors

$$\beta = (b_1, b_2, b_3, b_4, b_5)$$

in R^5 which are linear combinations of the vectors

$$\alpha_1 = (1, 0, 2, 1, -1),$$
 (1.0.1)

$$\alpha_2 = (-1, 2, -4, 2, 0),$$
 (1.0.2)

$$\alpha_3 = (2, -1, 5, 2, 1),$$
 (1.0.3)

$$\alpha_4 = (2, 1, 3, 5, 2)$$
 (1.0.4)

2 Solution

Above matrix represented as: $Ax = \beta$

$$\begin{pmatrix} 1 & -1 & 2 & 2 \\ 0 & 2 & -1 & 1 \\ 2 & -4 & 5 & 3 \\ 1 & 2 & 2 & 5 \\ -1 & 0 & 1 & 2 \end{pmatrix} x = \beta$$
 (2.0.1)

$$\begin{pmatrix} 1 & -1 & 2 & 2 \\ 0 & 2 & -1 & 1 \\ 2 & -4 & 5 & 3 \\ 1 & 2 & 2 & 5 \\ -1 & 0 & 1 & 2 \end{pmatrix} x = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \\ b_4 \\ b_5 \end{pmatrix}$$
(2.0.2)

Now finding row space of A is equivalent to finding column space of A^{T} . So, here we do elementary

matrix multiplication of the A^T matrix whose rows are given by $\alpha'_i s$, consider matrix X and Y which is equal to A^T , we get row reduced echelon form XY defined below:

$$X = \begin{pmatrix} 0.67 & -1.67 & -2 & 1.33 \\ 0.5 & -1.5 & -2.5 & 1.5 \\ -0.167 & 1.17 & 1.5 & -0.83 \\ -0.5 & -0.5 & -0.5 & 0.5 \end{pmatrix}$$
 (2.0.3)

$$X = \begin{pmatrix} 0.67 & -1.67 & -2 & 1.33 \\ 0.5 & -1.5 & -2.5 & 1.5 \\ -0.167 & 1.17 & 1.5 & -0.83 \\ -0.5 & -0.5 & -0.5 & 0.5 \end{pmatrix}$$
(2.0.3)
$$Y = \begin{pmatrix} 1 & 0 & 2 & 1 & -1 \\ -1 & 2 & -4 & 2 & 0 \\ 2 & -1 & 5 & 2 & 1 \\ 2 & 1 & 3 & 5 & 2 \end{pmatrix}$$
(2.0.4)

$$XY = \begin{pmatrix} 1 & 0 & 2 & 0 & 0 \\ 0 & 1 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$
 (2.0.5)

Now since the columns of the above matrix are linearly independent, b is described by (2.0.2)