Assignment 8

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Abstract—This document finds the solutions of given Now, we can apply Row Reduction Methodology: matrix by row reduction.

Download python codes from

https://github.com/priya6971/ matrix theory EE5609/tree/master/ Assignment8/codes

Download latex-tikz codes from

https://github.com/priya6971/ matrix theory EE5609/tree/master/ Assignment8

1 Problem

If

$$A = \begin{pmatrix} 3 & -1 & 2 \\ 2 & 1 & 1 \\ 1 & -3 & 0 \end{pmatrix} \tag{1.0.1}$$

Find all solutions of AX = 0 by row reducing A.

2 Solution

For the given equation AX = 0 can be defined as follows:

$$\begin{pmatrix} 3 & -1 & 2 \\ 2 & 1 & 1 \\ 1 & -3 & 0 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$
 (2.0.1)

$$\begin{pmatrix} 3 & -1 & 2 \\ 2 & 1 & 1 \\ 1 & -3 & 0 \end{pmatrix} \xrightarrow{R_1 = R_1 + R_2} \begin{pmatrix} 5 & 0 & 3 \\ 2 & 1 & 1 \\ 1 & -3 & 0 \end{pmatrix}$$
 (2.0.2)

$$\stackrel{R_2=R_2-2R_3}{\longleftrightarrow} \begin{pmatrix} 5 & 0 & 3\\ 0 & 7 & 1\\ 1 & -3 & 0 \end{pmatrix}$$
 (2.0.3)

$$\xrightarrow{R_3 = R_3 - \frac{1}{5}R_1} \begin{pmatrix} 5 & 0 & 3 \\ 0 & 7 & 1 \\ 0 & -3 & -\frac{3}{5} \end{pmatrix}$$
 (2.0.4)

$$\stackrel{R_1 = \frac{1}{5}R_1}{\longleftrightarrow} \begin{pmatrix} 1 & 0 & \frac{3}{5} \\ 0 & 7 & 1 \\ 0 & -3 & -\frac{3}{5} \end{pmatrix}$$
(2.0.5)

$$\stackrel{R_2 = \frac{1}{7}R_2}{\longleftrightarrow} \begin{pmatrix} 1 & 0 & \frac{3}{5} \\ 0 & 1 & \frac{1}{7} \\ 0 & -3 & -\frac{3}{5} \end{pmatrix}$$
(2.0.6)

$$\stackrel{R_3 = R_3 + 3R_2}{\longleftrightarrow} \begin{pmatrix} 1 & 0 & \frac{3}{5} \\ 0 & 1 & \frac{1}{7} \\ 0 & 0 & -\frac{6}{25} \end{pmatrix}$$
(2.0.7)