Assignment 3

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Abstract—This document solves a problem based on the congruency of a triangles.

Download latex-tikz codes from

https://github.com/priya6971/ matrix_theory_EE5609/tree/master/ Assignment3

1 Problem

In right triangle ABC, right angled at C, M is the mid-point of hypotenuse AB.C is joined to M and produced to a point D such that DM = CM. Point D is joined to point D. Show that:

a)
$$\triangle AMC \cong \triangle BMD$$
 (1.0.1)

$$b) \quad \angle DBC = 90^{\circ} \tag{1.0.2}$$

c)
$$\triangle DBC \cong \triangle ACB$$
 (1.0.3)

d)
$$CM = \frac{1}{2}AB$$
 (1.0.4)

2 Solution

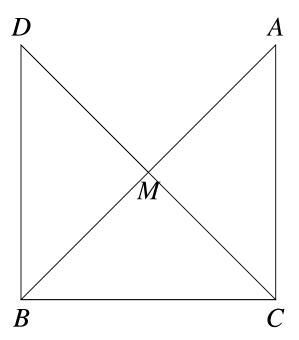


Fig. 1: Triangle ABC and DBC

In $\triangle ABC$, **M** is midpoint of hypotenuse AB, thus

$$\mathbf{M} = \frac{\mathbf{A} + \mathbf{B}}{2} \tag{2.0.1}$$

$$\mathbf{M} = \frac{\mathbf{C} + \mathbf{D}}{2} \tag{2.0.2}$$

Now it is given that $AC \perp BC$

$$\implies (\mathbf{A} - \mathbf{C})^T (\mathbf{B} - \mathbf{C}) = 0 \tag{2.0.3}$$