

Assignment 10

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Abstract—This document gives an explicit description of the vectors in R^5 which are linear combination of the vectors.

Download latex-tikz codes from

[https://github.com/priya6971/
matrix_theory_EE5609/tree/master/
Assignment10](https://github.com/priya6971/matrix_theory_EE5609/tree/master/Assignment10)

Download python codes from

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matrix multiplication of the A^T matrix whose rows are given by α'_i s and we evaluate that row reduced echelon form of the above matrix is:

$$\begin{pmatrix} 0.67 & -1.67 & -2 & 1.33 \\ 0.5 & -1.5 & -2.5 & 1.5 \\ -0.167 & 1.17 & 1.5 & -0.83 \\ -0.5 & -0.5 & -0.5 & 0.5 \end{pmatrix} \begin{pmatrix} 1 & 0 & 2 & 1 & -1 \\ -1 & 2 & -4 & 2 & 0 \\ 2 & -1 & 5 & 2 & 1 \\ 2 & 1 & 3 & 5 & 2 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 2 & 0 & 0 \\ 0 & 1 & -1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} \quad (2.0.3)$$

Now since the columns of the above matrix are linearly independent, b is described by (2.0.2)

1 PROBLEM

Give an explicit description of the type $b_j = \sum_{i=1}^r b_{ki} R_{ij}$ for the vectors

$$\beta = (b_1, b_2, b_3, b_4, b_5)$$

in R^5 which are linear combinations of the vectors

$$\alpha_1 = (1, 0, 2, 1, -1), \quad (1.0.1)$$

$$\alpha_2 = (-1, 2, -4, 2, 0), \quad (1.0.2)$$

$$\alpha_3 = (2, -1, 5, 2, 1), \quad (1.0.3)$$

$$\alpha_4 = (2, 1, 3, 5, 2) \quad (1.0.4)$$

2 SOLUTION

Above matrix represented as: $Ax = \beta$

$$\begin{pmatrix} 1 & -1 & 2 & 2 \\ 0 & 2 & -1 & 1 \\ 2 & -4 & 5 & 3 \\ 1 & 2 & 2 & 5 \\ -1 & 0 & 1 & 2 \end{pmatrix} x = \beta \quad (2.0.1)$$

$$\begin{pmatrix} 1 & -1 & 2 & 2 \\ 0 & 2 & -1 & 1 \\ 2 & -4 & 5 & 3 \\ 1 & 2 & 2 & 5 \\ -1 & 0 & 1 & 2 \end{pmatrix} x = \begin{pmatrix} b_1 \\ b_2 \\ b_3 \\ b_4 \\ b_5 \end{pmatrix} \quad (2.0.2)$$

Now finding row space of A is equivalent to finding column space of A^T . So, here we do elementary