Critical slowing down anticipates emergence and elimination of measles in Niger

Andrew T. Tredennick^{1,2*}, Eamon O'Dea^{1,2}, TBD^{1,2}, Pejman Rohani^{1,2}, & John M. Drake^{1,2}

¹ Odum School of Ecology, University of Georgia, Athens, GA, USA

² Center for the Ecology of Infectious Diseases, University of Georgia, Athens, GA, USA

Abstract

Introduction

- 2 Forecasts of the emergence and re-emergence of infectious diseases have the potential to save lives,
- money, and human productivity by allowing for proactive, rather than reactive, preparedness
- measures (1). Similarly, indicators of the elimination of infectious diseases can signal the
- effectiveness of "end game" strategies aimed at disease eradication (2). Predicting (re)emergence
- and elimination is possible with complex mathematical models of disease transmission, but their
- ₇ success relies on detailed understanding of the underlying transmission and pathogen dynamics. We
- often do not have enough information to parameterize such models. An alternative approach is to
- 9 use model-independent statistical signals that portend infectious disease (re)emergence and
- elimination by detecting critical slowing down as the system approaches a critical transition (3).

^{*}Corresponding author: atredenn@gmail.com

- Emergence and elimination of an infectious disease both involve a critical transition. The transition
- typically occurs at the critical point where the basic reproduction number (R_0 , the number of
- secondary cases that arise from a single infected case in a fully susceptible population) is equal to
- one (4). Thus, subcritical ($R_0 < 1$) and supercritical ($R_0 \ge 1$) systems represent alternative modes
- of fluctuation (5, 6).
- 16 Critical transitions in stochastic systems, such as disease transmission systems, are often associated
- with critical slowing down, a reduction in the resilience of a system to perturbations (7). Critical
- slowing down (CSD), in turn, is associated with changes in the dynamical features of the system,
- so-called early warning signals (EWS) such as an increase in the variance and autocorrelation (5, 8).
- Recent theoretical work suggests that CSD occurs as disease dynamics approach $R_0 = 1$ from
- below (emergence) (3, 9) and from above (elimination) (2, 3, 10), and that several EWS anticipate
- the critical transition (11-13). Empirical tests of EWS and associated CSD are, however, scarce.
- 23 Documenting CSD in real disease dynamics is an essential first step toward the development of
- 24 model-independent outbreak detection systems (1).
- ²⁵ Here, we use empirically-based model simulations of measles dynamics to test whether CSD
- ²⁶ anticipates critical transitions in real disease dynamics. We focus on two scenarios: (1) the
- 27 re-emergence of measles following a large outbreak, a situation typical of measles dynamics in
- sub-Saharan Africa, and (2) the elimination of measles by a vaccination campaign. We seek to
- ²⁹ answer two related questions. First, can CSD distinguish between time series of disease incidence
- when the underlying dynamics are far from and near to a critical transition? If so, then CSD can
- anticipate disease re-emergence and elimination. Second, how does the distance to and the rate of
- ³² approaching the threshold impact the anticipatory skill of CSD?
- To answer these questions, we fit mechanistic models of disease transmission to time series of
- measles incidence in four Nigerien cities. We then use the fitted models to perform model
- experiments designed to test the performance of several EWS, which quantify CSD, at anticipating
- ₃₆ re-emergence and elimination. Our results confirm theoretical expectations about several EWS and

- associated CSD. In particular, we show that CSD before a critical transition is detectable by several
- ³⁸ EWS in realistic scenarios, and they do so using much shorter time series than used in theoretical
- 39 studies. However, our study highlights the limitations of EWS in situations where disease
- re-emergence and elimination occurs rapidly. Moreoever, and contrary to theoretical expectations
- (3), we find that EWS perform better at detecting CSD before re-emergence than before elimination.

42 Materials and Methods

43 Data

- We used weekly measles case report data from four Nigerien cities: Agadez, Maradi, Niamey, and
- ⁴⁵ Zinder. The data were collected over an 11 year period from 1995-2005 (Figure 1). These data are
- ideal for testing theory on CSD in disease dynamics because each city has different population
- sizes, has different dynamics in terms of size of outbreaks and length of inter-epidemic periods, and
- each time series has different amounts of demographic stochasticity due to differences in population
- size. Such differences provide a natural gradient of "noise" that may obscure CSD (citation?). The
- data come from [somewhere/someone], and used here with permission from [somewhere/someone].

51 Stochastic SEIR model

- The model is a discrete-time approximation of a continuous-time SEIR model with limited
- demography, specified as a set of difference equations,

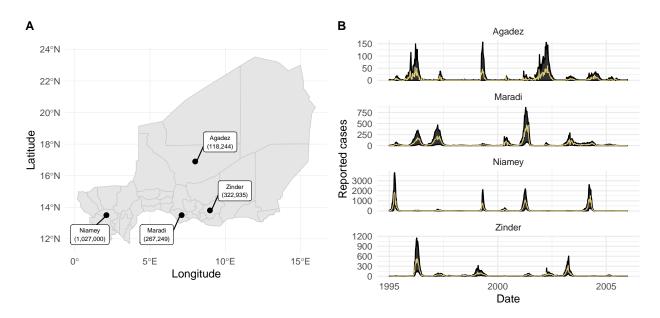


Fig. 1. Locations of data sources and observed and predicted measles dynamics. (A) Locations and population sizes (in parantheses) of our four focal cities in Niger. (B) Time series of weekly reported cases (yellow solid lines) and the 95% prediction intervals (black ribbons) for one-step-ahead predictions from our fitted SEIR models for each city.

$$S_{t+dt} = n_{S,t} - n_{E,t} \tag{1}$$

$$E_{t+dt} = n_{E,t} - n_{I,t} \tag{2}$$

$$I_{t+dt} = n_{I,t} + n_{O,t} - n_{R,t}, (3)$$

where \mathbf{n}_t are random variables representing the number of individuals transitioning into or out of

each class at each timestep $t \to t + dt$. n_S is the number of births, n_E is the number of newly

infected individuals that have the disease but are not infectious, n_I is the number of newly

infectious indiviuals, n_O is the number of imported infections, and n_R is the number of newly

recovered individuals who are no longer infectious and have life-long immunity. The stochastic

random variables are specified as follows:

$$n_{S,t} \sim \text{Poisson}(\mu_t N_t \times dt)$$
 (4)

$$n_{E,t} \sim \text{Binomial}(\lambda_{E,t}, S_t)$$
 (5)

$$n_{I,t} \sim \text{Binomial}(\lambda_{I,t}, E_t)$$
 (6)

$$n_{O,t} \sim \text{Poisson}(\psi \times dt)$$
 (7)

$$n_{R,t} \sim \text{Binomial}(\lambda_{R,t}, I_t),$$
 (8)

where μ_t is the birth rate at time t, ψ is the rate of imported infections, and λ_E , λ_I , and λ_R are the probabilities of exposure, becoming infectious, and recovery, respectively. These probabilities reflect the processes of transission, transition from the latent period to the infectious period, and recovery, which we model as:

$$\lambda_{E,t} = 1 - e^{-\frac{\beta_t I_t dt}{N_t}} \tag{9}$$

$$\lambda_{I,t} = 1 - e^{-\eta E_t dt} \tag{10}$$

$$\lambda_{R,t} = 1 - e^{-\gamma I_t dt},\tag{11}$$

where β_t is time-varying rate of transmission, η is time-invariant rate from the exposed class to the infectious class, and γ is time-invariant recovery rate. We model rate of transmission as:

$$\beta_t = \beta \left(1 + \sum_{i=1}^6 q_i \xi_{i_t} \right) \Gamma_t. \tag{12}$$

 β is the mean transmission rate, ψ accounts for measles infections from external sources that are not part of the local dynamics, and the term $\sum_{i=1}^{6} q_i \xi_{i_t}$ is a B-spline to model seasonality in transmission. The B-spline bases (ξ_{i_t}) are periodic with a 1 year period. The transmission rate (β_t)

- is also subject to stochastic process noise at each time step, Γ_t , which we model as
- gamma-distributed white (temporally uncorrelated) noise with mean 1 and variance σ^2 (14).
- We do not include a death process in the model because the rate of infection is much faster than the
- rate of death. Excluding deaths means we can avoid making further assumptions about demographic
- rates we are already making assumptions about birth rates (e.g., the rate is the same across cities,
- but with city-specific population size). We model demographic stochasticity in births and imported
- ⁷⁵ infections by drawing time-specific values from Poisson distributions. Transitions in the model are
- shown in Table 1. In this model, the effective reproductive ratio at time t is: $R_E(t) = \frac{\beta_t}{\gamma} \frac{S_t}{N_t}$.
- We assume observed case reports (y) are drawn from a Negative Binomial distribution subject to a
- constant reporting fraction (ρ) and dispersion parameter τ ,

$$y_t \sim \text{Negative Binomial}(\rho I_t, \tau)$$
. (13)

Table 1. Transitions in the SEIR model. We show the determinstic transmission rate for clarity, but our model uses the stochastic transmission rate.

Transition	$(\Delta S, \Delta E, \Delta I)$	Propensity
birth	(1,0,0)	$N_t \mu_t$
transmission	(-1, 1, 0)	$SIeta_t/N_t$
(deterministic)		
transmission (stochastic)	(-k, k, 0)	$\frac{S}{k} \sum_{j=0}^{k} \binom{k}{j} (-1)^{k-j+1} \tau_{f}^{-1} \ln(1 + (\beta_{t} I/N_{t})) \tau_{f}(S-j)$
symptomatic	(0, -1, 1)	$E\eta$
(infectious)		
imported	(0,0,1)	ψ_t
infections		

Transition	$(\Delta S, \Delta E, \Delta I)$	Propensity
recovery	(0,0,-1)	Ιγ

79 Model fitting and inference

We fit the SEIR model to time series of case reports from each of our focal cities using Maximization by Iterated particle Filtering (MIF). We estimated 14 parameters for each city: six seasonal transmission parameters (q_i) , mean transmission rate (β) , three initial conditions $\left(S_{(t=0)}, E_{(t=0)}, I_{(t=0)}\right)$, the number of imported infections (ψ) , reporting fraction (ρ) , one parameter accounting for process noise (σ) , and one parameter accounting for measurement noise (τ) . To ensure identifiability, and to make the model easier to fit, we assumed the infectious period was fixed at $1/\eta = 8$ days and the recovery period was fixed at $1/\gamma = 5$ days. The birth rate (μ_t) was multiplied by 0.3 to account for the reported 70% vaccination coverage (15). 87 MIF relies on particle filtering, which estimates the likelihood of fixed parameters by integrating state variables of a stochastic system. To narrow in on the maximum likelihood estimates, MIF lets 89 parameters take a random walk during the filtering process and selectively propagates forward parameter sets (i.e., particles) with the highest likelihood. The variance of the random walk 91 decreases at each iteration of MIF, where a MIF iteration means one filtering pass through the time series. This procedure converges toward the maximimum likelihood estimates (MLEs), in theory. We used the IF2 algorithm (16) implemented in the R (17) package pomp (18, 19) to conduct the MIF procedure. To initialize MIF, we generated 5000 parameter sets using Latin Hypercube Sampling over large ranges of the parameter values. We then performed two rounds of MIF, each for 100 iterations, with 10000 particles, and geometric cooling. For the first round of MIF we set 97 cooling.facter = 1. For the second round, which was initialized using the collection of parameter sets from the end of the first round, we set cooling.factor = 0.9. We computed the log likelihood of 5000 final MIF parameter sets (i.e., parameter sets collected after 200 MIF

iterations) as the log of the mean likelihoods of 50 replicate particle filters with 10000 particles each. At this stage, we assume the parameter set with highest log likelihood is the MLE. 102 We used a bootstrapping approach to estimate approximate 95% confidence intervals for all 103 parameters. The procedure, which was conducted for each city independently, is as follows. First, 104 we simulated 100 realizations from the fitted model using the MLE parameters. Second, we fitted the SEIR model to each of the 100 bootstrap simulations using the same MIF procedure described above, except we initiated the parameter search from 50 parameter sets rather then 5000. We 107 reduced the number of parameter sets due to the computational constraints of fitting 100 simulated 108 data sets for each of the four cities. Third, we identified the MLE parameter set for each of the 100 109 bootstrap simulations from among the 50 MIF paramete sets. Last, we calculated summary 110 statistics (mean, median, quantiles) from the distribution of 100 MLE parameters (SI text). 111

112 Model simulations

113 Model-data comparisons

We used the MLE parameter sets to make one-step-ahead predictions and to test the ability of early warning signals to anticipate the critical transition at $R_E(t)=1$. To make one-step-ahead predictions, we used particle filtering with 50000 particles and retained the mean and standard deviation of all latent states across all particles before they were filtered at each time step. We used these predictions ($\mathbb{E}(\text{cases}_t)$) to assess model fit using a generalized coefficient of determination, calculated as: $R^2=1-\frac{\sum_{t}[\mathbb{E}(\text{cases}_t)-\text{cases}_t]^2}{\sum_{t}[\text{mean}(\text{cases})-\text{cases}_t]^2}$ (20).

Simulating re-emergence

To simulate re-emergence of measles, we manipulated the initial size of the susceptible pool to simulate an increase from low $R_E(t)$ to high $R_E(t)$. Doing so allows us to test whether EWS can distinguish between windows of time when $R_E(t)$ is far from a critical transition and when $R_E(t)$ is near a critical transition. We reduced the initial fraction of susceptible individuals by multplying the MLE for $S_{(t=0)}$ by six discounting factors: 1e-4, 0.1, 0.2, 0.3, 0.4, and 0.5. These discounting factors represent situations of susceptible depletion after outbreaks of various size. We then simulated the model forward for thirty years using mean birth and death rates for the entire country. Thirty years was long enough for yearly average $R_E(t)$ to reach 1 for each city. Because the model is stochastic, we repeated these simulations 500 times for each city-susceptible discount combination.

Next, we split each simulated time series into null and test intervals. First, across all simulations for a city-susceptible discount combination, we found the simulation year in which $R_E(t)$ reaches or exceeds 1, and excluded years past that year (SI text). We split the remaining time series into two windows of equal length (Fig. S2). The null interval is the first window, where $R_E(t)$ is increasing but far from 1. The test interval is the second window, where $R_E(t)$ is increasing and approaching 1. We did this for each city and for each level of susceptible depletion. We calculated EWS over null and test intervals separately.

138 Simulating elimination

To simulate elimination, we simulated a vaccine campaign in which vaccination coverage linearly increased over time to eventually reach 100%, i.e. eradication (Fig. S3). We ran simulations for 100 years, starting with 50 years of dynamics at the baseline vaccine coverage reported for Niger of 70%, p = 0.7 (15). Note that vaccination coverage is included in our model by discounting the birth rate of susceptibles by 1 - p. At year 50, we initiated the vaccination campaign and let the model run for another 50 years. We ran simulations across six vaccination "speeds" (the rate at which $p \rightarrow 1$; SI text), simulating situations of slow and fast approaches to elimination.

We then split each time series into null and test intervals for calculating EWS. We define the test interval as the window of time between the start of the vaccination campaign (year 50) and the time at which vaccination coverage reached the vaccination threshold of $1 - 1/R_0$. R_0 was calculate for

each city based on the MLE parameters (SI text). We define the null interval as the window of time
that ends at the start of the vaccination campaign (year 49) and starts at a time that results in an
interval equal in length the test interval (Fig. S3). EWS were then calculated for each interval.

52 Early warning signals

values.

We considered nine candidate early warning signals (Table 2). We used the 153 spaero::get_stats() function (21) in R (17) to calculate EWS according to the formulas in 154 Table 2. All EWS except the coefficient of variation are expected to increase as $R_E(t)$ approaches 1 155 from below (3, 10, 12). Less is known about the behavior of EWS as $R_E(t)$ approaches 1 from 156 above. But, theory does tell us that, for SIR models, the mean should decrease, autocorrelation 157 should increase, and the variance should decrease (3). For each simulation of re-emergence and elimination, we calculated EWS for the time series of 159 expected cases in the null and test intervals. This yields a distribution of EWS over the 500 null and 160 test intervals. We assessed the performance of each EWS using the Area Under the Curve (AUC) 161 statistic. Specifically, we use AUC to calculate the amount of overlap between the distributions of 162 each EWS from the null and test intervals. Higher values of AUC indicate a greater degree of separation and thus better performance of a particular EWS in terms of classifying whether $R_E(t)$ is approaching a critical transition. We used the pROC: auc() function (22) in R to calculate AUC

Table 2. List of candidate early warning signals and their estimating equations. Note that b denotes the bandwidth. See (12) for details.

		Theoretical Correlation
EWS	Estimator	with $R_E(t)$
Mean	$\mu_t = \sum_{s=t-(b-1)\delta}^{t+(b-1)\delta} \frac{X_s}{2b-1}$	Positive
Variance	$\sigma_t^2 = \sum_{s=t-(b-1)\delta}^{t+(b-1)\delta} rac{(X_s - \mu_s)^2}{2b-1}$	Positive

		Theoretical Correlation
EWS	Estimator	with $R_E(t)$
Coefficient of	$CV_t = rac{\sigma_t}{\mu_t}$	Null
variation		
Index of dispersion	$ID_t = rac{\sigma_t^2}{\mu_t}$	Positive
Skewness	$S_t = \frac{1}{\sigma_t^3} \sum_{s=t-(b-1)\delta}^{t+(b-1)\delta} \frac{(X_s - \mu_s)^3}{2b-1}$	Positive
Kurtosis	$K_t = \frac{1}{\sigma_t^4} \sum_{s=t-(b-1)\delta}^{t+(b-1)\delta} \frac{(X_s - \mu_s)^4}{2b-1}$	Positive
Autocovariance	$ACov_t = \sum_{s=t-(b-1)\delta}^{t+(b-1)\delta} \frac{(X_s - \mu_s)(X_{s-\delta} - \mu_{s-\delta})}{2b-1}$	Positive
Autocorrelation	$AC_t = \frac{ACov_t}{\sigma_t \sigma_{t-\delta}}$	Positive
Decay time	$\overline{ au}_t = -\delta/\ln\left[\operatorname{AC}_t(\delta) ight]$	Positive

Results

The fitted models adequately reproduce observed dynamics (Fig. 1B), with in-sample R^2 s from one-step-ahead predictions ranging from 0.54 for Agadez to 0.89 for Maradi (Fig. 2A). Stochastic simulations of the models displayed dynamics typical of each city (Fig. S1), including the decline in seasonality amplitude as population size decreases (Fig. 2B) (15). Our model for Agadez performs poorly relative to the other cities.

Table 3. Maximum likelihood estimates for select epidemiological parameters.

City	Log likelihood (S.E.)	β	σ	Ψ	ρ	$S_{t=0}$
Agadez	-960.65 (0.11)	171.47	0.10	7.80	0.77	0.23
Maradi	-1746.56 (0.16)	483.09	0.06	24.88	0.33	0.10
Niamey	-1454.73 (0.15)	370.63	0.09	23.28	0.26	0.11
Zinder	-1415.52 (0.09)	180.09	0.08	10.47	0.36	0.22

In the approach to re-emergence, the EWS generally perform as expected, with Niamey being an exception (Fig. 3A). Skewness, kurtosis, and coefficient of variation performed poorly across all levels of susceptible depletion in all cities except Niamey. For Niamey, it appears these metrics

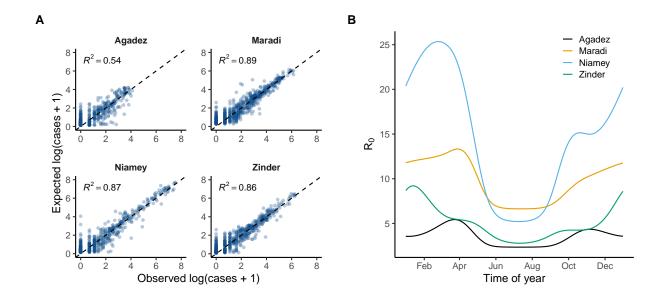


Fig. 2. Accuracy of the fitted SEIR models and estimated seasonality. (A) Comparison of in-sample model predictions and observations for each city. Expected cases are one-step-ahead predictions from the fitted models. The dashed line shows 1:1. Coefficients of determination (R^2) were calculated as the reduction in the sum-of-squared errors from model predictions relative to a null model of the mean number of cases (SI text). (B) The estimated seasonality of the basic reproductive ratio (R_0) for each city. R_0 was calculated as: $\frac{\eta \beta_1 \mu}{\nu(\eta + \nu)(\gamma + \nu)}$, where $1/\eta$ is the infectious period, $1/\gamma$ is the recovery period, β_t is the time-specific rate of transmission, μ is the birth rate, and ν is the death rate. Only β_t is estimated by our model. We set $1/\eta = 8$ days, $1/\gamma = 5$ days, $\mu = \nu = 0.05$ for calculating R_0 as shown in this figure.

perform well at the highest levels of susceptible depletion (i.e., low discounting factors). In fact, the
high AUC values for Niamey result from exceptionally poor performance: they are all higher in the
null interval rather than the test interval, contrary to theoretical expectations (Table 2). Thus, these
metrics are unreliable.

For the other cities, variance, mean, index of dispersion, decay time, autocovariance, and autocorrelation all perform equally well at predicting re-emergence (Fig. 3A). Their performance declines as the amount of susceptible depletion decreases. This is expected because more rapid returns to $R_E(t) = 1$ result in shorter null and test intervals, making estimates of EWS less precise. Likewise, as the total time to reach $R_E(t) = 1$ decreases, the null and test intervals start to behave more similarly. In part, this is because susceptible replenishment is linear in our model. Nonlinear increases in the susceptible pool would lead to different dynamics.

The EWS did not perform as well when anticipating elimination, relative to emergence (Fig. 3B).

Only three metrics are reliable: mean, autocovariance, and variance. All three metrics decreased as $R_E(t)$ approached the critical transition (Fig. S5). As in the case of anticipating elimination, AUC values decreased as the speed of the vaccine campaign increased. Again, this is due to shorter null and test intervals.

In all, the suite of EWS suggest that critical slowing down does occur in measles dynamics as a critical transition is approached.

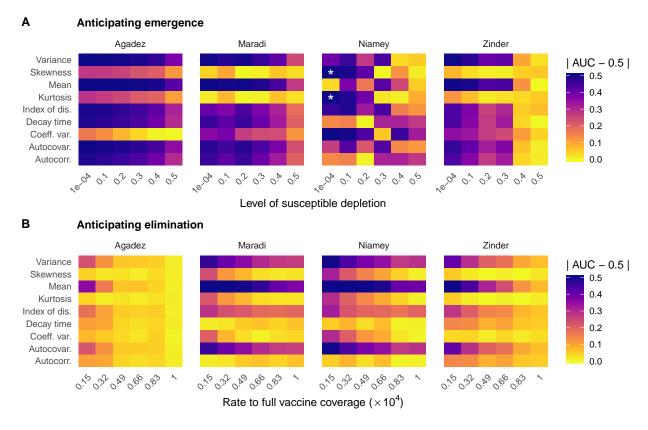


Fig. 3. Performance of early warning signals (EWS). EWS were calculated over two windows, one far from a critical transition and one near, for simulations of re-emergence (**A**) and elimination (**B**). EWS performance is quantified using the AUC metric, which we show here as a heatmap of AUC values minus 0.5. AUC values closer to 0.5 indicate higher ability to distinguish among time series near and far from a critical transition. The asterisks (*) in (A) for Niamey note EWS with high AUC but for the wrong reason: skewness and kurtosis *decrease* as $R_E(t)$ approaches 1 rather than increase. This occurs because of the negative binomial sampling in the measurement component of our SEIR model.

Discussion

- Using empirically-based disease transmission models, we found evidence of critical slowing down
- before critical transitions to re-emergence and elimination of measles. This evidence comes from
- the fact that several EWS accurately anticipate the critical transition.

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References

- 1. B. A. Han, J. M. Drake, *EMBO reports*, e201642534 (2016).
- 2. J. M. Drake, S. I. Hay, Tropical Medicine and Infectious Disease. 2, 20 (2017).
- 3. S. M. O'Regan, J. M. Drake, *Theoretical Ecology*. **6**, 333–357 (2013).
- 4. J. M. Heffernan, R. J. Smith, L. M. Wahl, *Journal of the Royal Society Interface*. **2**, 281–293 (2005).
- 5. M. Scheffer et al., Nature. **461**, 53–59 (2009).
- 6. M. Scheffer et al., Science. 338, 344–348 (2012).

- 7. E. H. van Nes, M. Scheffer, *The American Naturalist*. **169**, 738–747 (2007).
- 8. S. R. Carpenter, W. A. Brock, *Ecology Letters*. **9**, 311–318 (2006).
- 9. C. J. Dibble, E. B. O'Dea, A. W. Park, J. M. Drake, *Journal of the Royal Society Interface*. 13, 20160540 (2016).
- 10. S. M. O'Regan, J. W. Lillie, J. M. Drake, *Theoretical Ecology*. **9**, 269–286 (2016).
- 11. T. S. Brett, J. M. Drake, P. Rohani, Journal of the Royal Society Interface. 14, 20170115 (2017).
- 12. T. S. Brett et al., PLoS Computational Biology. 14, e1006204 (2018).
- 13. P. B. Miller, E. B. O'Dea, P. Rohani, J. M. Drake, *Theoretical Biology and Medical Modelling*. **14**, 17 (2017).
- 14. C. Bretó, E. L. Ionides, Stochastic Processes and their Applications. 121, 2571–2591 (2011).
- 15. M. J. Ferrari *et al.*, *Nature*. **451**, 679–684 (2008).
- 16. E. L. Ionides, D. Nguyen, Y. Atchadé, S. Stoev, A. A. King, *Proceedings of the National Academy of Sciences*. **112**, 719–724 (2015).
- 17. R Core Team, R: A language and environment for statistical computing (2017), (available at http://www.mendeley.com/research/r-language-environment-statistical-computing-96/{\%}5Cnpapers2://publication/uuid/A1207DAB-22D3-4A04-82FB-D4DD5AD57C28).
- 18. A. A. King, D. Nguyen, E. L. Ionides, *Journal Of Statistical Software*. **69**, 1–43 (2016).
- 19. A. A. King *et al.*, pomp: Statistical Inference for Partially Observed Markov Processes (R package, version 1.18) (2018).
- 20. M. Martinez-Bakker, A. A. King, P. Rohani, *PLoS Biology* (2015), doi:10.1371/journal.pbio.1002172.
- 21. E. B. O'Dea, spaero: Software for Project AERO (R package version 0.3.0) (2018).
- 22. X. Robin et al., BMC Bioinformatics. 12, 77 (2011).