

The following exercise tells you how to compute the Essential matrix using the 8 point method.

$$E = q2.transpose * [tx] * q1$$

1. Generate 3d 50 points using uniform distribution

`np.random.uniform()`

In the range 0 to 1

The matrix can be 3 X 50. = Q

Solution:

```
p = np.random.uniform(0,1, (50,3))
```

2. Add [ 1 4 3] to all the points -> 1 to x, 4 to y and 3 to z.

```
p = p + b = np.repeat([[1,4,3]],50,axis=0)
```

This will give p => 50 X 3

-- You need to put the homogenous component "1" at the end of each 3d vector.

Final matrix will be of size 4X 50 or 50 X 4.

```
o1 = np.ones(50,1)
```

```
p = np.hstack((p,o1))
```

3. Project the points into two cameras using the two projection matrices.

$P1 = [ I \ 0 ]$

```
P1 = [ [1 0 0 0], [0 1 0 0], [0 0 1 0]] -> first camera
```

```
q = np.dot(P1, Q.T)
```

```
q = q.T
```

```
u1 = q[:,0]/q[:,2]
```

```
v1 = q[:,1]/q[:,2]
```

For each point,

$q = P1 * Q$

The output is in homogenous coordinates, divide by the last component to get [u1, v1, 1]

Generate a rotation and translation

$R = [ 0.8660 \ 0.2500 \ 0.4330$

$0 \ 0.8660 \ -0.5000$

-0.5000 0.4330 0.7500]

T = [-0.4 0.3 0.6]

q = P2 \* Q

```
q = np.dot(P2, Q.T)
q = q.T
```

```
u2 = q[:,0]/q[:,2]
v2 = q[:,1]/q[:,2]
```

P2 = [[ R t]] -> **second camera**

q2 = P2 \* Q

The output is in homogenous coordinates, divide by the last component of each point to get [u2, v2, 1]

4. Use corresponding points in the image to generate 8 point equations

A = [u2 \* u1, u2 \* v1, u2, v2 \* u1, v2 \* v1, v2, u1, v1, 1]

5. Formulate two equations:

Solve  $Ax = 0$

```
u, s, vh = np.linalg.svd(A, full_matrices=True)
```

F = vh[

$Ax = 0$  and

$Ax = b$

6. Solve using svd and pseudoinverse

7. What are the values?

8. Use python-opencv to decompose the essential matrix:

R1, R2, T = cv2.decomposeEssentialMat(E)

