Paging and Virtual Memory Translation

ECE 469, Jan 18

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Virtual Memory



- Three goals
 - Transparency: does not need to know system's internal state
 - Program A is loaded at 0x8048000. Can Program B be loaded at 0x8048000?
 - Efficiency: do not waste memory; manage memory fragmentation
 - Can Program B (288KB) be loaded if 288 KB of memory is free, regardless of its allocation?
 - Protection: isolate program's execution environment
 - Can we prevent an overflow from Program A from overwriting Program B's data?

Multi-programming Environment

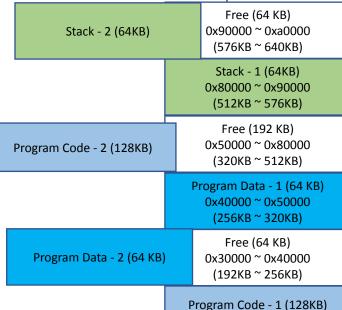
0x10000 ~ 0x30000

(64KB ~ 192KB)

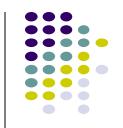
OS 0x00000 ~ 0x10000 (0 ~ 64KB)

- Run two programs
- System's memory usage determines allocation
- Program need to be aware of the environment
 - Where does system loads my code?
 - You can't determine... system does...

No Transparency...







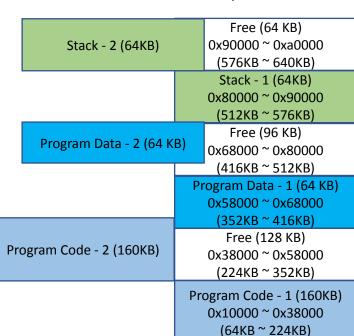
OS

0x00000 ~ 0x10000 (0 ~ 64KB)

- Run two programs
 - Program size: 64KB + 64KB + 160K = 288KB

Free mem: 64 + 96 + 128 = 288KB

- Cannot run Program 2
 - Can't fit...



Not efficient.. Suffers memory fragmentation problem..



Run two programs

What if Program-2's stack underflows?

• What if Program-2's data overflows?

- Without virtual memory
 - Programs can affect to the other's execution

No isolation. Security problem.

Stack - 2 (64KB)

Stack (64KB) 0x80000 ~ 0x90000 (512KB ~ 576KB)

Program Code - 2 (128KB)

Program Data (64 KB) 0x40000 ~ 0x50000 (256KB ~ 320KB)

Program Data - 2 (64 KB)

Program Code (128KB) 0x10000 ~ 0x30000 (64KB ~ 192KB)

OS 0x000000 ~ 0x10000 (0 ~ 64KB)

Paging!

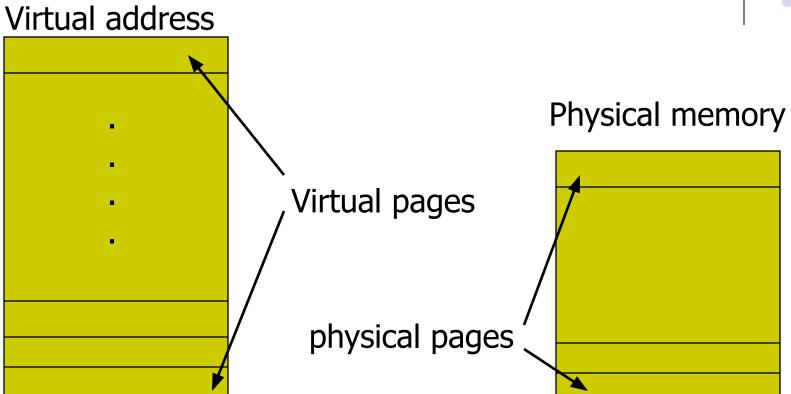


- Idea: Make all chunks of memory the same size, called pages
 - Both virtual and physical memory divided into same size chunks.

 For each process, a page table defines the base address of each of that process' pages along with existence and read/write bits

Paging!





Page Table: matters of size



- Table of entries:
 - Virtual memory page to physical memory page.
 - Number of entries proportional to the size of page.
 - Each entry is of the size of a pointer = 4 bytes
- Page table size for 32-bit address space:
 - With page size $4KB = (2^32)/(2^12) = (2^20)$ entries = $(2^20)^4$ bytes = 4 MB.
 - With page size $8KB = (2^32)/(2^13) = (2^19)$ entries = $(2^19)^4$ bytes = 2MB.
 - With page size $8MB = (2^32)/(2^23) = (2^9)$ entries = $(2^9)^4$ bytes = 2KB.

Page size / fragmentation



- If a page size is too small, it requires a big page table
 - 1B, 4GB
 - 4KB, 4MB
 - 4MB, 4KB
 - 1G, 16B
- If a page size is too big, unused memory in a page will be wasted
 - 1B 1B (no waste)
 - 4KB − 1B
 - 4MB − 1B
 - 1G 1B

Design consideration:

Memory fragmentation matters!

Paging



- A method of implementing virtual memory common page size: 4KB
- Split memory into multiple 4,096 byte blocks (12-bit offset)
 - Page start address: Last 3 digits of page address are ZEROs (in hexadecimal)
 - E.g., 0x0, 0x1**000**, 0x2**000**, ..., 0x8048**000**, 0x804a**000**, ..., 0x7fffe**000**, etc.
- Having an indirect map between virtual page and physical page
 - Set an arbitrary virtual address for a page, e.g., 0x81815000
 - Set a physical address to that page as a map, e.g., 0x32000
 - 0x81815000 ~ 0x81815fff will be translated into
 - 0x32000 ~ 0x32fff

Virtual Memory - Paging

Having an indirect table that maps virt-addr to phys-addr



Physical Memory

Program code 0x804a000

Stack 0xbffdf000

Program code 0x8049000

Program code 0x8048000

Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x14000
0xbffdf000	0x12000

Program code 0x14000

Stack 0x12000

Program code 0x11000

Program code 0x10000

Virtual Memory - Paging

Having an indirect table that maps virt-addr to phys-addr

Stack-2	Stack
0xbffdf000	0xbffdf000
Program code-2	Program code
0x804a000	0x804a000
Program code-2	Program code
0x8049000	0x8049000
Program code-2	Program code
0x8048000	0x8048000

Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x14000
0xbffdf000	0x12000

Virtual-2	Physical-2
0x8048000	0x13000
0x8049000	0x15000
0x804a000	0x16000
0xbffdf000	0x17000



Physical Memory

Stack-2 0x17000

Program code-2 0x16000

Program code-2 0x15000

Program code 0x14000

Program code-2 0x13000

> Stack 0x12000

Program code 0x11000

Program code 0x10000

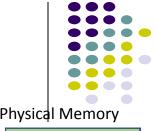
Transparency: does not need to know system's internal state Program A is loaded at 0x8048000. Can Program B be loaded at 0x8048000?

Having an indirect table that maps virt-addr to phys-addr

Stack-2	Stack
0xbffdf000	0xbffdf000
Program code-2	Program code
0x804a000	0x804a000
Program code-2	Program code
0x8049000	0x8049000
Program code-2	Program code
0x8048000	0x8048000

Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x14000
0xbffdf000	0x12000

Virtual-2	Physical-2
0x8048000	0x13000
0x8049000	0x15000
0x804a000	0x16000
0xbffdf000	0x17000



Physical Memory

0x17000 Program code-2 0x16000

Stack-2

0x15000 Program code

0x14000

Program code-2

Program code-2 0x13000

Stack

0x12000 Program code 0x11000

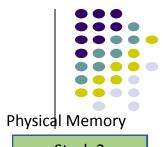
Program code 0x10000

Efficiency: do not waste memory Can Program B (288KB) be loaded if only 288 KB of memory is free, regardless of its allocation?

Having an indirect table that maps virt-addr to phys-addr

0xbffdf000
Program code 0x804a000
Program code 0x8049000
Program code 0x8048000

Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x14000
0xbffdf000	0x12000
Virtual-2	Physical-2
Virtual-2 0x8048000	Physical-2 0x13000
	· ·
0x8048000	0x13000
0x8048000 0x8049000	0x13000 0x15000



Stack-2

0x17000

Program code-2 0x16000 Program code-2 0x15000

Program code 0x14000

Program code-2 0x13000

Stack 0x12000 Program code 0x11000 Program code

0x10000

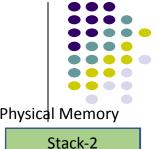
Protection: isolate program's execution environment Can we prevent an overflow from Program A from overwriting Program B's data?

Having an indirect table that maps virt-addr to phys-addr

Stack-2	Stack
0xbffdf000	0xbffdf000
Program code-2	Program code
0x804a000	0x804a000
Program code-2	Program code
0x8049000	0x8049000
Program code-2	Program code
0x8048000	0x8048000

Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x14000
0xbffdf000	0x12000
Virtual-2	Physical-2

Virtual-2	Physical-2
0x8048000	0x13000
0x8049000	0x15000
0x804a000	0x16000
0xbffdf000	0x17000



Physical Memory

0x17000 Program code-2 0x16000

0x15000 Program code 0x14000

Program code-2

Program code-2 0x13000

Stack 0x12000 Program code 0x11000

Program code 0x10000

Page Table



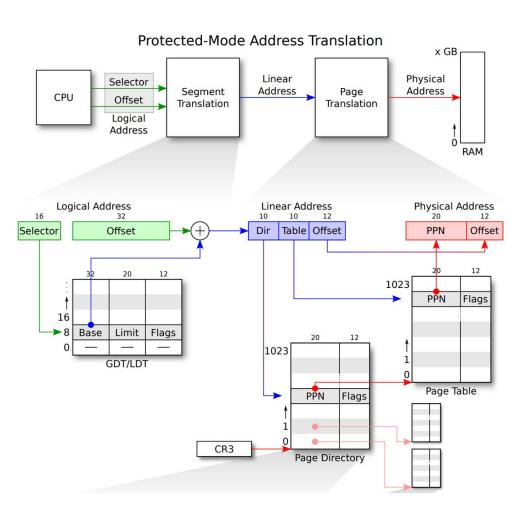
- We access page table by virtual address
- Page size: 4 KB (12bits)
- Page number: 20 bits
- What is the page number and offset of
 - 0x8048000
 - 0xb7ff3100



Balancing Page Size v/s Page Table Size



- Page size: 4 KB (12 bits)
 - Page Table size: (2^20)*4 bytes = 4MB (of contiguous physical memory).
- If a program needs 1KB of memory, it still needs 4MB for its page table??!!!
- How do we balance this?
 - Add another level of indirection: Page directories and Page Tables.

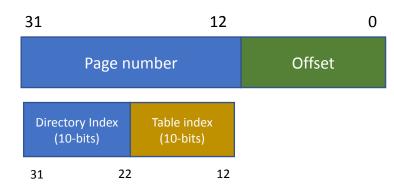




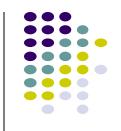
Page Directory / Table

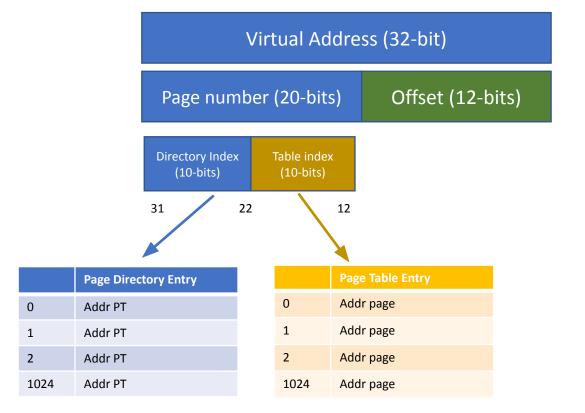


- In x86 (32-bit), CPU uses 2-level page table
- 10-bit directory index
- 10-bit page table index
- 12-bit offset

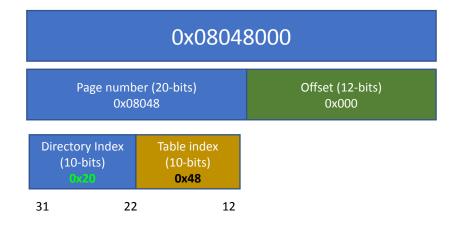


Address Translation







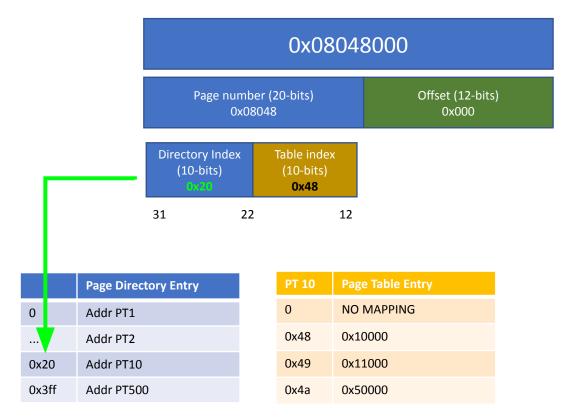


Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x50000

	Page Directory Entry
0	Addr PT1
	Addr PT2
0x20	Addr PT10
0x3ff	Addr PT500

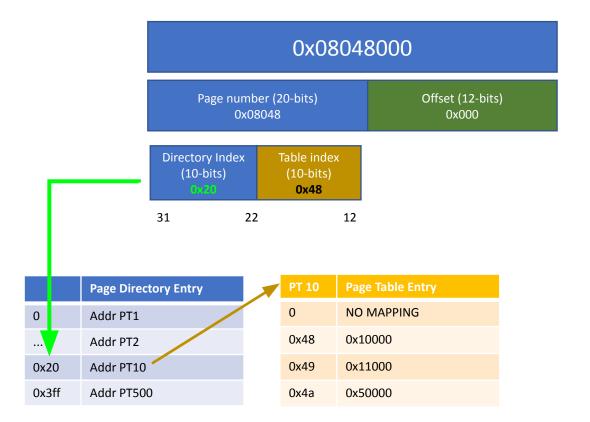
PT 10	Page Table Entry
0	NO MAPPING
0x48	0x10000
0x49	0x11000
0x4a	0x50000





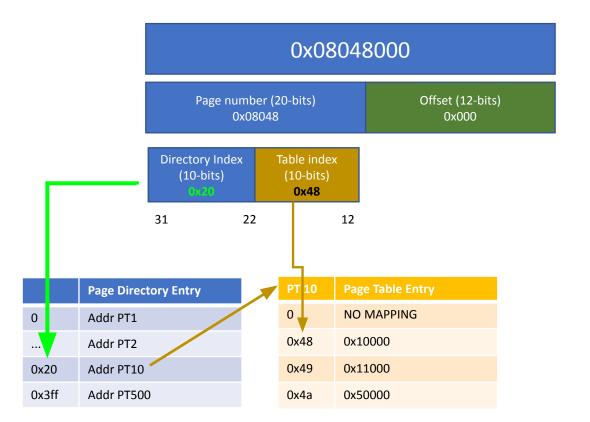
Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x50000





Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x50000



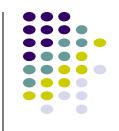


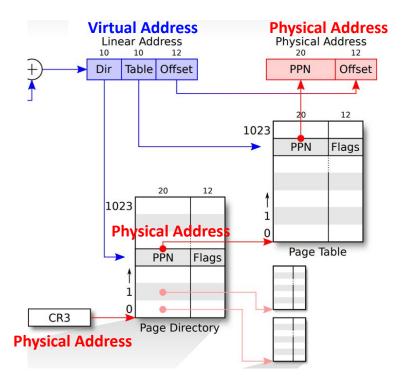
Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x50000





Addresses in use!



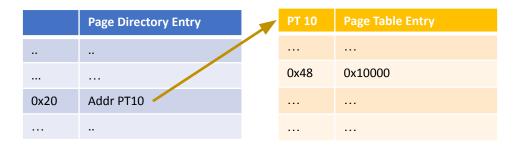


Page Directory and Page Table sizes

- Program wants to 1 KB of memory (0x8048000 -> 0x10000):
 - Traditional page table:
 - Page Table: (2^20)*4 bytes = 4 MB.
 - 1 page : 4 KB.
 - Overhead: 4 MB + 3 KB

Virtual	Physical
0x8048000	0x10000

- Page directories:
 - Page directory = (2^10) * 4 bytes = 4KB.
 - 1 Page table chunk = (2^10) * 4 bytes = 4KB.
 - 1 page : 4KB.
 - Overhead: 4 KB + 4 KB + 3 KB



4KB 4KB

Notable features of x86 paging!

- We only ever want 4KB of contiguous memory:
 - Page directory: 4KB.
 - Page table chunk or Second level page table: 4KB.
 - Page size: 4KB.
- All metadata is of size 4KB!!

Page Table Entry



- Address translation is from virtual page to physical page
 - E.g., 0x8048000 -> 0x11000
- We do not need to translate lower 12 bits
 - E.g., 0x8048001 -> 0x8048000 + 0x001 -> 0x11000 + 0x001

- So page table entry only uses higher 20 bits to store physical page address
 - Lower 12 bits are remaining as the same
 - We do not translate the lower 12 bits!



- Virtual address 0x8048338
 - Virtual page number: 0x8048
 - Offset: 0x338
 - Physical page number: 0x10
 - Physical address: 0x10(000) + 0x338 = 0x10338
- Virtual address 0x443325af
 - Virtual page number: 0x44332
 - Offset: 0x5af
 - Physical page number: 0x33885
 - Physical address: 0x33885000 + 0x5af = 0x338855af

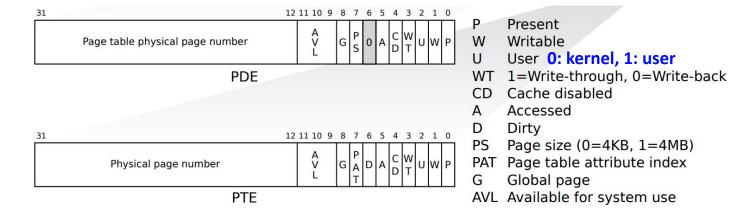
Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x14000
0xbffdf000	0x12000
0x44332000	0x33885000

Virtual	Physical
0x8048	0x10
0x8049	0x11
0x804a	0x14
0xbffdf	0x12
0x44332	0x33885

4 I

PDE, PTE



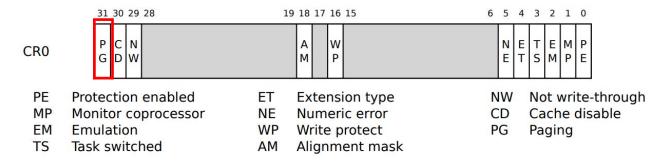


	Page Directory Entry
0	Addr PT1
	Addr PT2
0x20	Addr PT10
0x3ff	Addr PT500

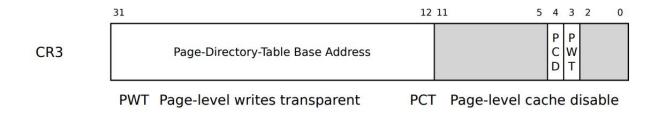
PT 10	Page Table Entry
0	NO MAPPING
0x48	0x10000
0x49	0x11000
0x4a	0x50000

Paging in X86

Can be enabled by CRO



Page table address (physical) need to be stored in CR3



Paging in X86



In JOS (kern/entry.S)

```
# Load the physical address of entry_pgdir into cr3. entry_pgdir
# is defined in entrypgdir.c.
movl $(RELOC(entry_pgdir)), %eax
movl %eax, %cr3 Set cr3 to point the address of page directory
# Turn on paging.
movl %cr0, %eax
orl $(CR0_PE|CR0_PG|CR0_WP), %eax Turn on CR0_PG!
movl %eax, %cr0
```

After CRO_PG is set -> Paging is in effect!

Accessing physical address



- After CRO_PG is up (paging is turned on)
 - All normal address access regarded as virtual address
 - Special addresses. E.g., CR3 will be considered as physical address

- What if we would like to access the physical address 0x100010?
 - Our kernel is at physical address 0x100000 ~ 0x110000

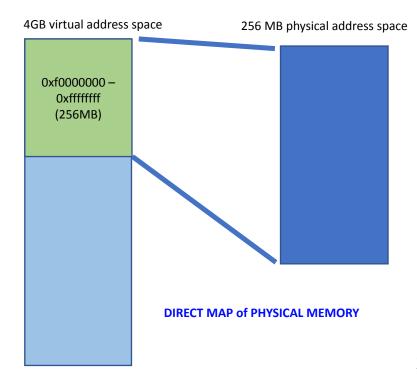
What's the virtual addresses of that area?

Accessing physical address



- In JOS, we will map 0xf0000000
 ~ 0xffffffff to
 - Physical address
 - 0x00000000 ~ 0x0fffffff
 - 256 MB Region

- 0xf0100010 -> 0x00100010
- $0xf1333358 \rightarrow 0x01333358$



Setting up page directory in JOS



In JOS (kern/entrypgdir.c)

```
Entry_pgdir only contains two entries;
0 ~ 0x400000 to 0 ~ 0x400000 (not writable)
0xf0000000 ~ 0xf0400000 to 0 ~ 0x400000 (writable)
```

Page table in JOS

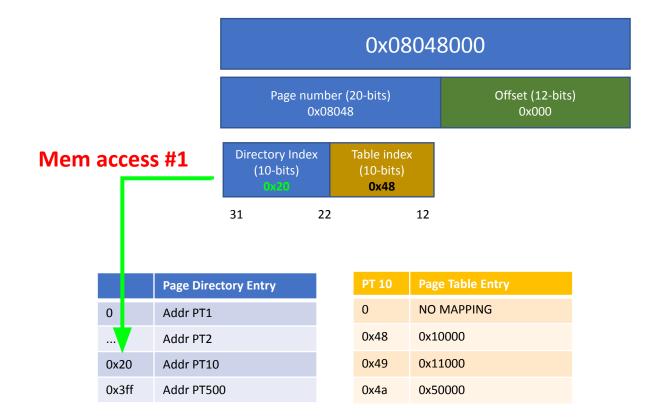
In JOS (kern/entrypgdir.c)

```
Oxf0001000 will consult entry_pgtable[1] -> 0x001000 | PTE_P | PTE_W
```

Phyaddr: 0x1000

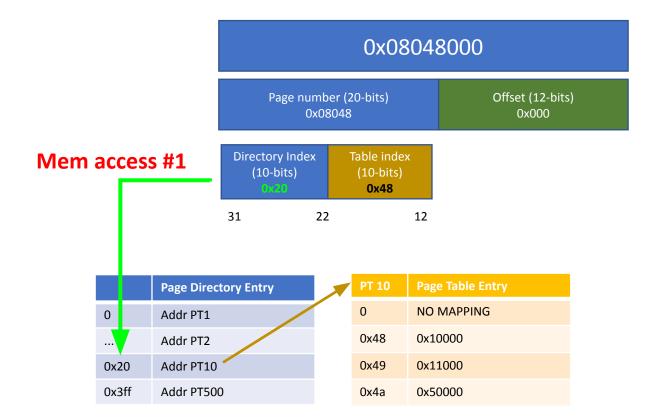
```
attribute (( aligned (PGSIZE)))
pte t entry pgtable[NPTENTRIES] =
    0x000000
                PTE P
                        PTE W,
    0x001000
                PTE P
                        PTE W,
                PTE P
                        PTE W.
    0x002000
    0x003000
                PTE_P
                        PTE W,
    0x004000
                        PTE W.
                PTE P
    0x005000
                        PTE_W,
                PTE P
    0x006000
                PTE P
                        PTE W.
    0x007000
                PTE P
                        PTE W.
    0x008000
                PTE P
                        PTE_W,
    0x009000
                        PTE W.
                PTE P
                PTE P
    0x00a000
                        PTE W.
    0x00b000
                PTE P
                        PTE W,
    0x00c000
                PTE P
                        PTE W.
    0x00d000
                        PTE W.
                PTE P
                        PTE W.
    0x00e000
                PTE P
    0x00f000
                PTE P
                        PTE W.
    0x010000
                PTE P
                        PTE W.
    0x011000
                PTE P
                        PTE W.
```





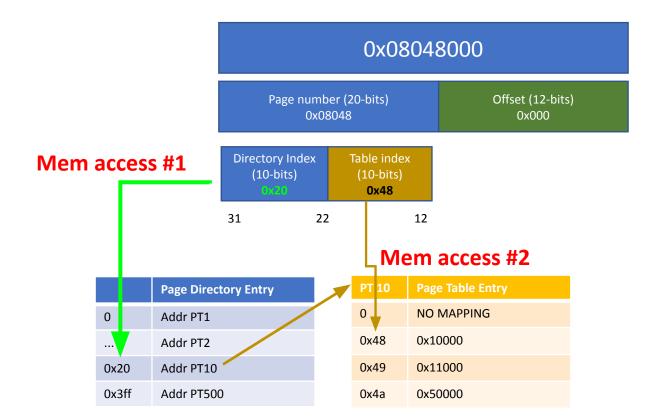
Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x50000





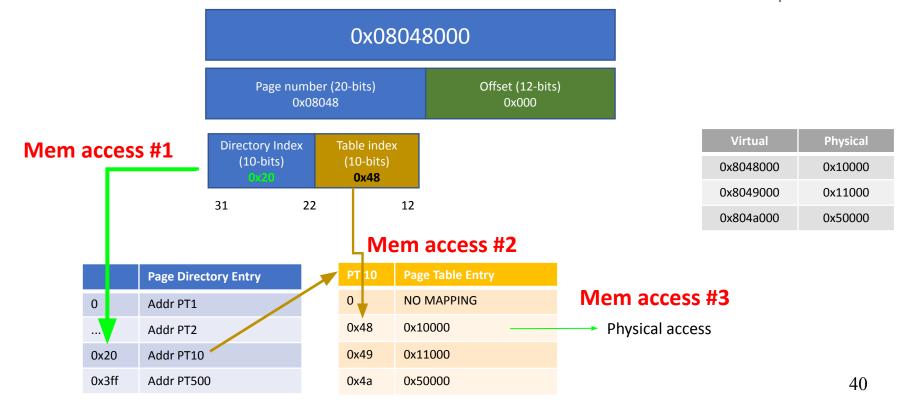
Virtual	Physical
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0x804a000	0x50000



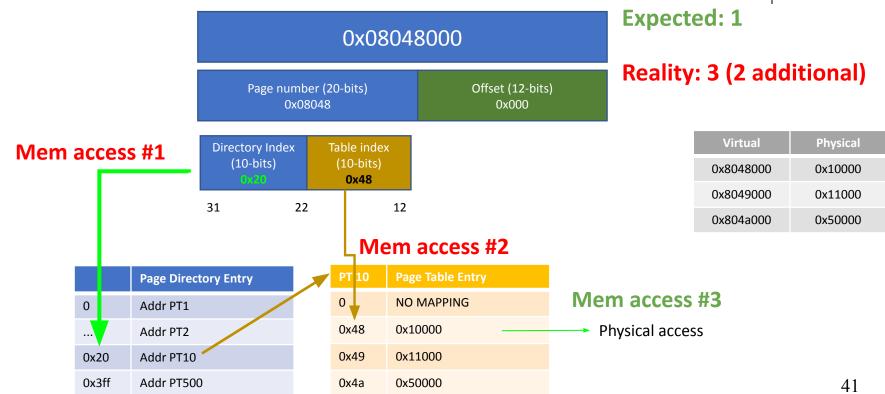


Virtual	Physical
0x8048000	0x10000
0x8049000	0x11000
0x804a000	0x50000









Access overhead!



- Access example
 - movl 0x12345678, %eax
- 3 memory access per each memory access SLOW!
 - 2 additional accesses due to page table lookup
 - mov instruction takes 1 cycle
 - memory access takes ~200 cycles…
 - 200 (access the address) + 1 (mov) + 200 * 2 (page table...) = 601 cycles.

How can we fix this?



Hint: What do we do for regular memory?

Caching!

- Cache the frequently used page table entries:
 - Exploit locality
 - Translation Lookaside Buffer (TLB)
 - Cache for translation entries.

Translation Lookaside Buffer (TLB)



Stores VA-PA mappings and caches them!

VPN (Virt Page Number)	PPN (Phy Page Number)	Valid
0x12345	0x0	1
0x12346	0x5	1
0x12347	0xff	1
0x12348	0xfff	1

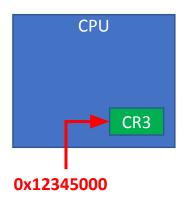
0x12345678 -> 0x678

0x12346678 -> 0x5678

0x12347678 -> 0xff678

0x12348678 -> 0xfff678

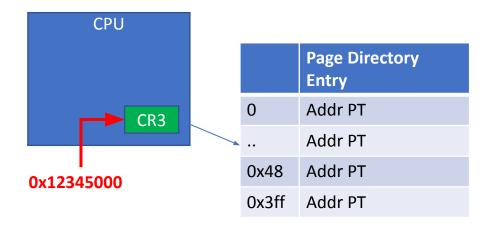




	Page Directory Entry
0	Addr PT
	Addr PT
0x48	Addr PT
0x3ff	Addr PT

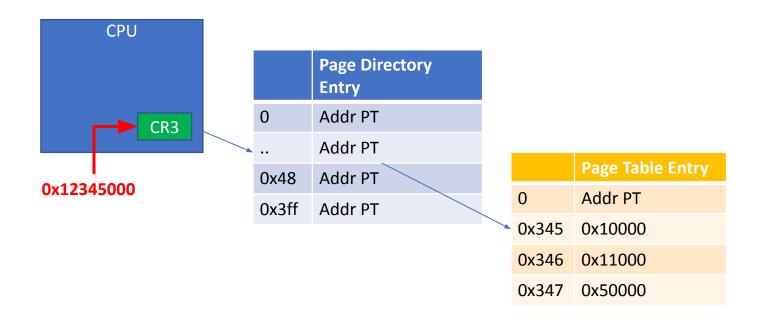
	Page Table Entry
0	Addr PT
0x345	0x10000
0x346	0x11000
0x347	0x50000



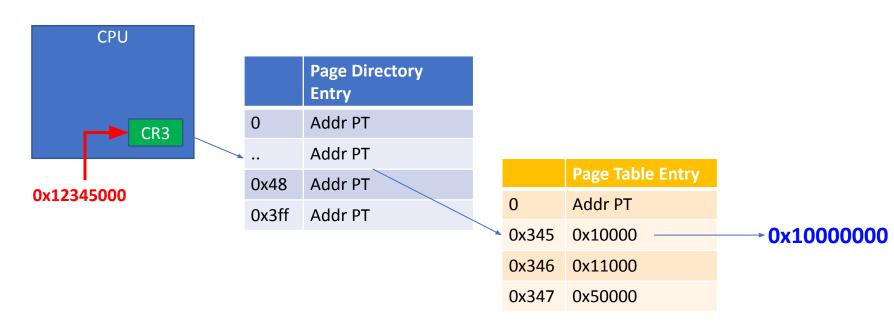


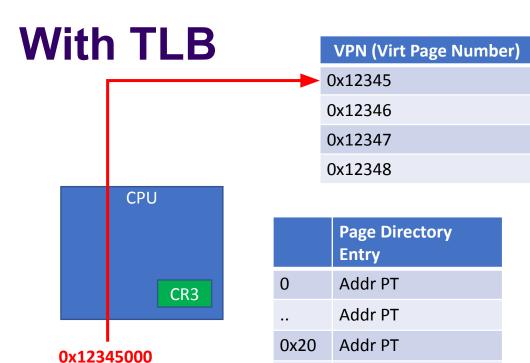
	Page Table Entry
0	Addr PT
0x345	0x10000
0x346	0x11000
0x347	0x50000











0x3ff

Addr PT

	Page Table Entry
0	Addr PT
0x48	0x10000
0x49	0x11000
0x4a	0x50000

PPN (Phy Page Number)

0x10000

0x5

0xff

0xfff

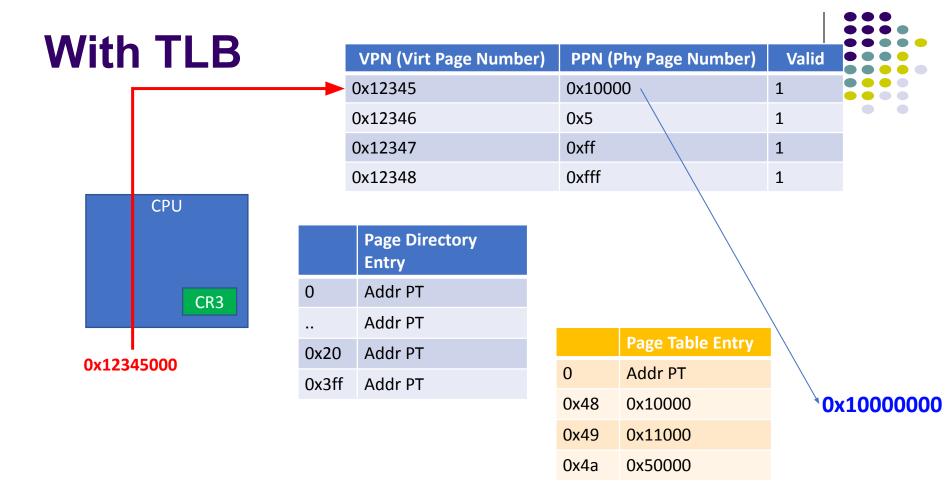
Valid

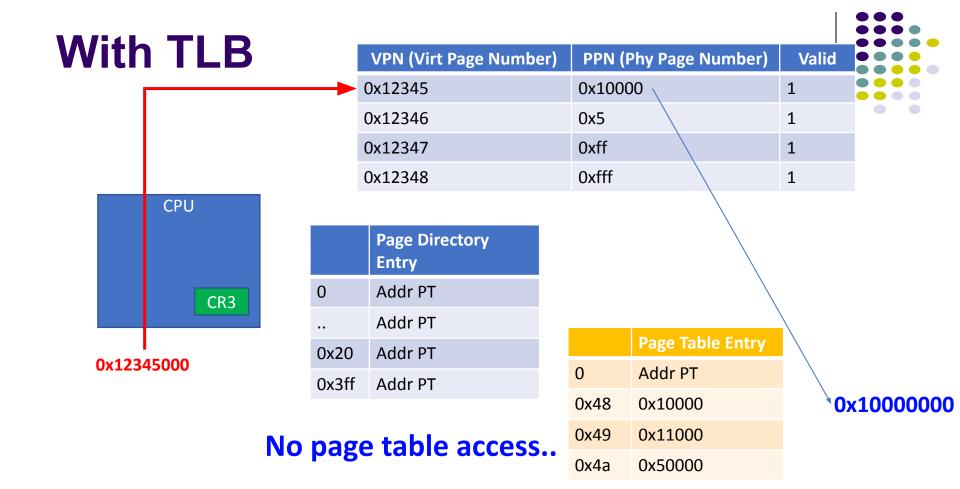
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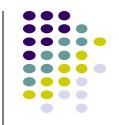
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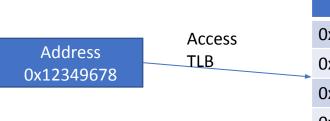
1

50



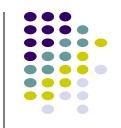


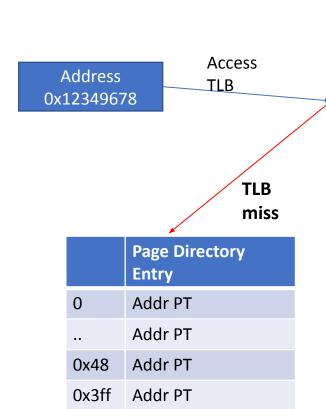




VPN	PPN	Valid
0x12345	0x0	1
0x12346	0x5	1
0x12347	0xff	1
0x12348	0xfff	1
0	0	0

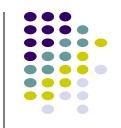
TLB

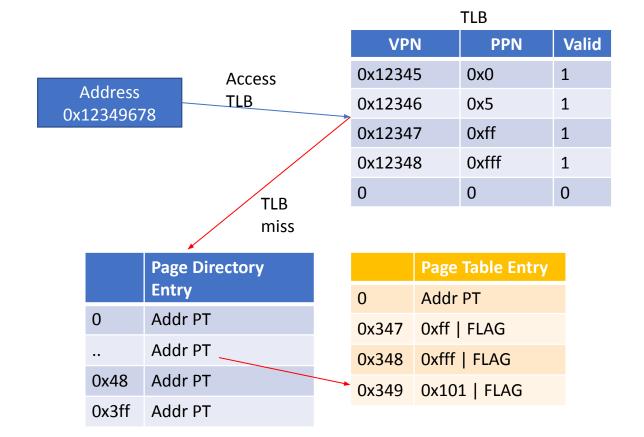


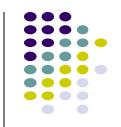


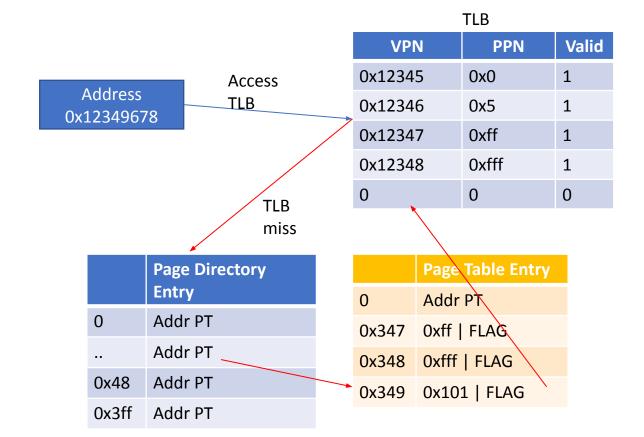
VPN	PPN	Valid
0x12345	0x0	1
0x12346	0x5	1
0x12347	0xff	1
0x12348	0xfff	1
0	0	0

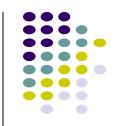
TI D

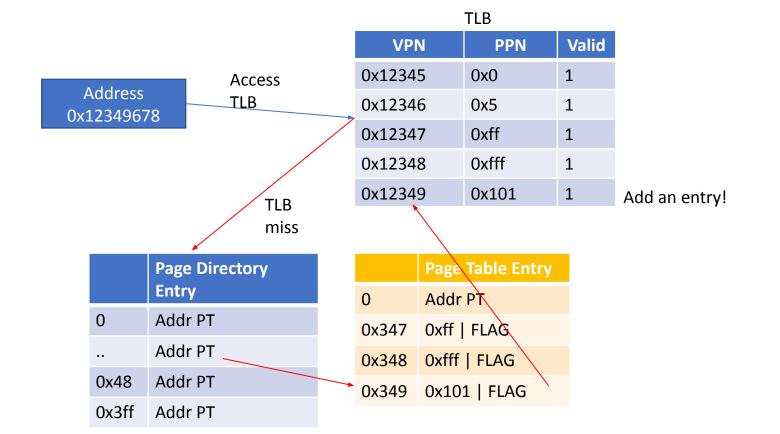






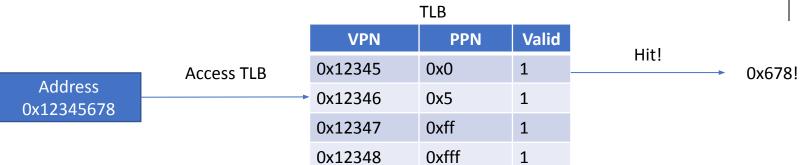






TLB hit





TLB Performance



- Core i7-6700K (Skylake, 4.00 GHz)
 - Data TLB L1: 64 items. 4-way. Miss penalty = 9 cycles. Parallel miss: 1 cycle per access
 - Data TLB L2 (STLB): 1536 items. 12-way. Miss penalty = 17 ? cycles. Parallel miss: 14 cycles per access
 - PDE cache = ? items. Miss penalty = ? cycles.

Size	Latency	Increase	Description
32 K	4		

• TLB hit requires 4 cycles, 1ns!

TLB Performance



TLB hit requires 4 cycles, 1ns!

- Page table walk requires 2 memory access for translation
 - Uncached: 9 cycles + (42 cycles + 51ns) * 2
 - [TLB miss] [RAM latency]

- Cached: 9 + 4 * 2 = 17 cycles if all blocks cached in L1 (4 ns, 4 times slower!)
 - Data TLB L1: 64 items. 4-way. Miss penalty = 9 cycles. Parallel miss: 1 cycle per access
 - Data TLB L2 (STLB): 1536 items. 12-way. Miss penalty = 17 ? cycles. Parallel miss: 14 cycles per access
 - PDE cache = ? items. Miss penalty = ? cycles.
 - L1 Data Cache Latency = 4 cycles for simple access via pointer
 - L1 Data Cache Latency = 5 cycles for access with complex address calculation (size_t n, *p; n = p[n]).
 - L2 Cache Latency = 12 cycles
 - L3 Cache Latency = 42 cycles (core 0) (i7-6700 Skylake 4.0 GHz)
 - L3 Cache Latency = 38 cycles (j7-7700K 4 GHz, Kaby Lake)
 - RAM Latency = 42 cycles + 51 ns (i7-6700 Skylake)

Limited TLB Size



- Core i7-6700K (Skylake, 4.00 GHz)
 - Data TLB L1: 64 items. 4-way. Miss penalty = 9 cycles. Parallel miss: 1 cycle per access
 - Data TLB L2 (STLB): 1536 items. 12-way. Miss penalty = 17 ? cycles. Parallel miss: 14 cycles per access
 - PDE cache = ? items. Miss penalty = ? cycles.
- 64 items for L1 d-TLB, 1536 items for L2 d-TLB
- CPU need to schedule this cache
 - Based on Temporal/Spatial locality...

TLB Replacement Policy



- Smart: LRU (Least Recently Used)
 - Mark when the block was accessed (update timestamp upon access)
 - When an eviction is required, evict the one with the oldest timestamp
- Random
 - Do not do anything when accessed
 - When an eviction is required, evict an entry randomly...
 - Sometimes, this works better than LRU...
- We will learn more about such scheduling later
 - When we learn about process scheduling...

TLB Synchronization



- CPU uses the TLB for caching Page Table Entries
- What will happen if content in TLB mismatches to the PTE in the page table?
 - Access wrong physical memory...
 - Does not honor the correct privilege in PTE (if we updated PTE after caching)
 - Running a new process with new CR3
 - Use old process's mapping, wrong access

TLB and Page Table Update



Address 0x12349678

I	l	_	В

VPN	PPN	Valid
0x12345	0x0	1
0x12346	0x5	1
0x12347	0xff	1
0x12348	0xfff	1
0x12349	0x101	1

	Page Directory Entry
0	Addr PT
	Addr PT
0x48	Addr PT
0x3ff	Addr PT

	Page Table Entry
0	Addr PT
0x347	0xff FLAG
0x348	0xfff FLAG
0x349	0x101 FLAG

TLB and Page Table Update



Address 0x12349678

TLB

VPN	PPN	Valid
0x12345	0x0	1
0x12346	0x5	1
0x12347	0xff	1
0x12348	0xfff	1
0x12349	0x101	1

	Page Directory Entry
0	Addr PT
	Addr PT
0x48	Addr PT
0x3ff	Addr PT

	Page Table Entry
0	Addr PT
0x347	0xff FLAG
0x348	0xfff FLAG
0x349	0x102 FLAG

Update

TLB and Page Table Update



Address 0x12349678

TLB

VPN	PPN	Valid
0x12345	0x0	1
0x12346	0x5	1
0x12347	0xff	1
0x12348	0xfff	1
0x12349	0x101	0

We need to invalidate this entry

	Page Directory Entry
0	Addr PT
••	Addr PT
0x48	Addr PT
0x3ff	Addr PT

	Page Table Entry
0	Addr PT
0x347	0xff FLAG
0x348	0xfff FLAG
0x349	0x102 FLAG

Update



Address 0x12349678

CR3

VPN	PPN	Valid
0x12345	0x0	1
0x12346	0x5	1
0x12347	0xff	1
0x12348	0xfff	1
0x12349	0x101	1

TLB

	Page Directory Entry
0	Addr PT
	Addr PT
0x48	Addr PT
0x3ff	Addr PT

	Page Table Entry
0	Addr PT
0x347	0xff FLAG
0x348	0xfff FLAG
0x349	0x101 FLAG



Address

CR3

VPN	PPN	Valid
0x12345	0x0	1
0x12346	0x5	1
0x12347	0xff	1
0x12348	Oxfff	1

0x101

TLB

	Page Directory Entry
0	Addr PT
••	Addr PT
0x48	Addr PT
0x3ff	Addr PT

	Page Table Entry		
0	Addr PT		
0x347	0xff FLAG		
0x348	0xfff FLAG		
0x349	0x101 FLAG		

0x12349

TLB

Valid **PPN VPN** 0x12345 0x0 1 0x5 0x12346 0x12347 0xff 1 0xfff 0x12348 0x12349 0x101 1

Address x12359888

CR3

	Page Directory Entry
0	Addr PT
	Addr PT
0x48	Addr PT
0x3ff	Addr PT

	Page Table Entry		
0	Addr PT		
0x347	0xff FLAG		
0x348	0xfff FLAG		
0x349	0x101 FLAG		

	Page Directory Entry	
0	Addr PT	
	Addr PT	
0x48	Addr PT	
0x3ff	Addr PT	

	Page Table Entry
0	Addr PT
0x347	0x20 FLAG
0x348	0x30 FLAG
0x349	0x50 FLAG
	ロソ



TLB

Valid **PPN VPN** 0x12345 0x0 0 0x12346 0x5 0x12347 0xff 0 0xfff 0x12348 0 0x12349 0x101 0

We need to invalidate all previous entries..

	Page Directory Entry
0	Addr PT
	Addr PT
0x48	Addr PT
0x3ff	Addr PT

Address

CR3

	Page Table Entry		
0	Addr PT		
0x347	0xff FLAG		
0x348	Oxfff FLAG		
0x349	0x101 FLAG		

	Page Directory Entry	
0	Addr PT	
••	Addr PT	
0x48	Addr PT	
0x3ff	Addr PT	

	Page Table Entry
0	Addr PT
0x347	0x20 FLAG
0x348	0x30 FLAG
0x349	0x50 FLAG
	/11

/U

Updating Page Table



- When updating a Page Table Entry
 - We must invalidate TLB for that entry
 - invlpg

INVLPG — Invalidate TLB Entries

Op/En	64-Bit Mode	Compat/Leg Mode	Description
M	Valid	Valid	Invalidate TLB entries for page containing m .

Updating Page Table



In JOS (kern/pmap.c & inc/x86.h)

```
Invalidate a TLB entry, but only if the page tables being
   edited are the ones currently in use by the processor.
void
tlb_invalidate(pde_t *pgdir, void *va)
    // Flush the entry only if we're modifying the current address space.
    // For now, there is only one address space, so always invalidate.
    invlpq(va);
static inline void
invlpg(void *addr)
   asm volatile("invlpg (%0)" : : "r" (addr) : "memory");
```

Manipulating Page Tables in JOS



- PGNUM(x)
 - Get the page number (x >> 12) of the address x
- PDX(x)
 - Get the page directory index (top 10 bits) of the address x
- PTX(x)
 - Get the page table index (mid 10 bits) of the address x
- PGOFF(x)
 - Get the page offset (lower 12 bits) of the address x

Manipulating Page Tables in JOS



- PTE_ADDR(pte)
 - Get the physical address that a pte points
 - PTE_ADDR(pte) + PGOFF(x)
 - The physical address pointed by the PTE, translated by a virtual address x
- Translate a virtual address va to physical address pa
- pte = CR3[PDX(va)][PTX(va)]
 - pte_t **cr3 = lcr3(); # or, kern_pgdir
 - pte t *pt = cr3[PDX(va)]
 - pte_t pte = pt[PTX(va)]
- physaddr_t pa = PTE_ADDR(pte) + PGOFF(va);