

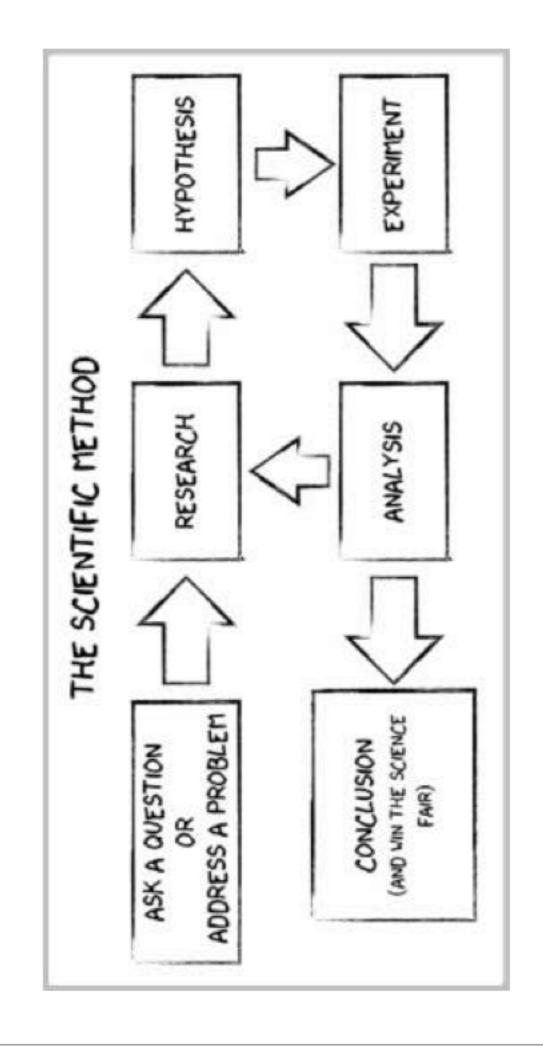


Bayesian Inference **Using Probabilistic** Programming for

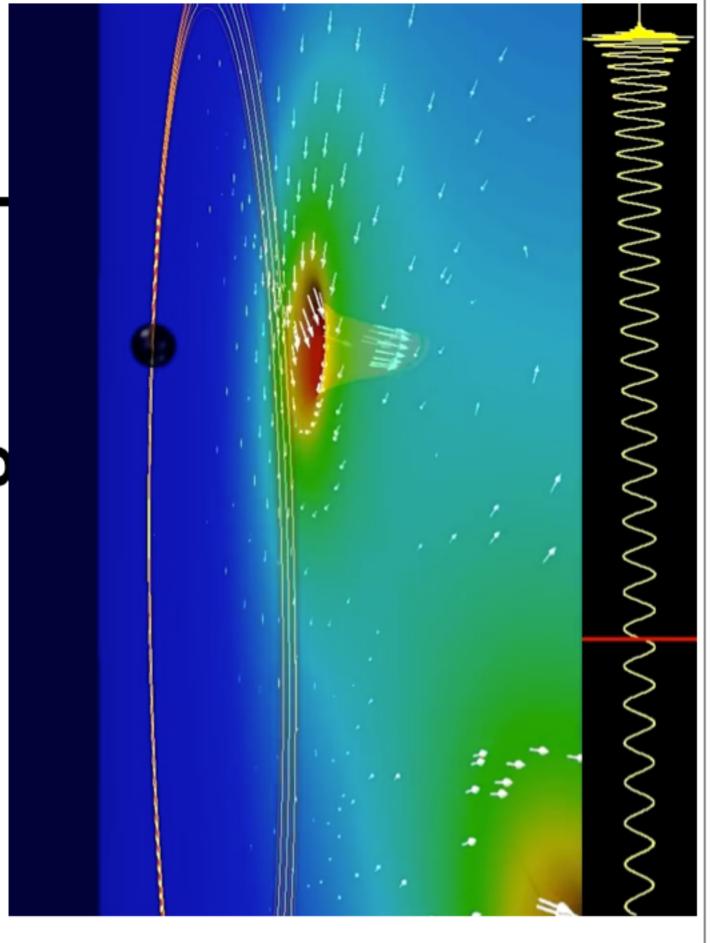
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The Scientific Process



Motivating example

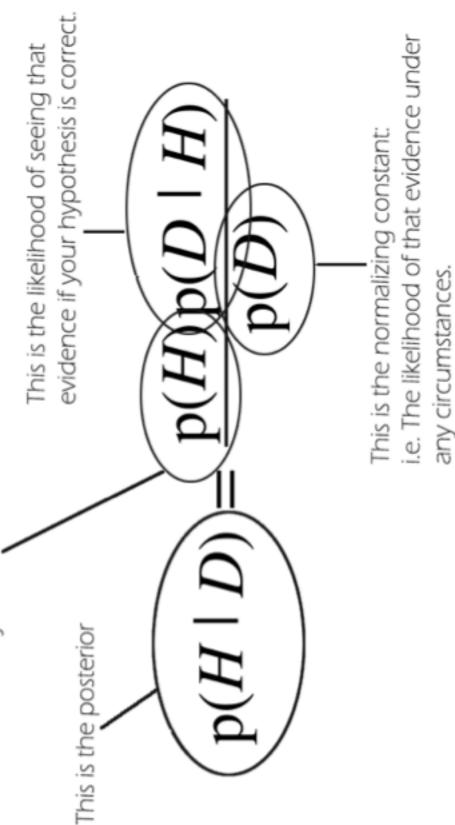


Parameter estimation Bayesian Inference/

- We need to extract/infer the most information possible from the data
- e.g Learn source parameters for gravitational waves
- Also want to make predictions about the future
- Need to do this in a statistically sound way with a measure of certainty

Bayes Theorem

This is the prior: i.e. what you believed before you saw the evidence.



The Problem

In General not possible to calculate an analytic solution

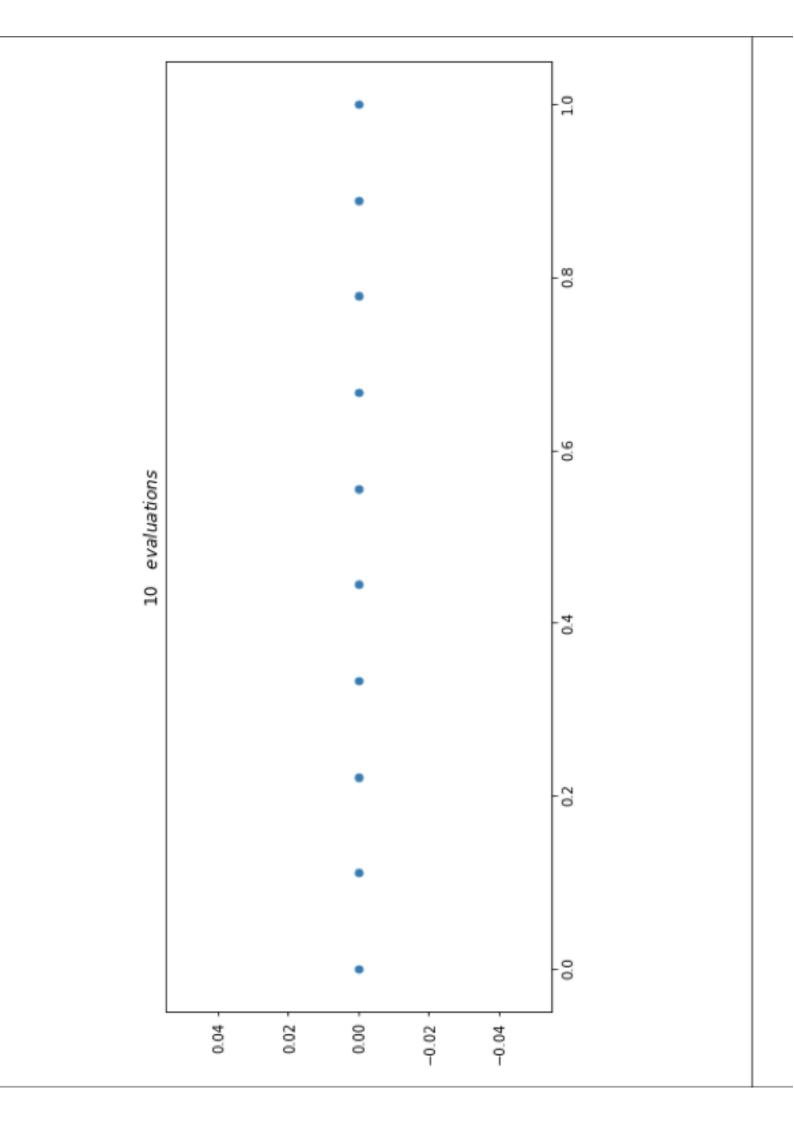
The evidence term is usually intractable

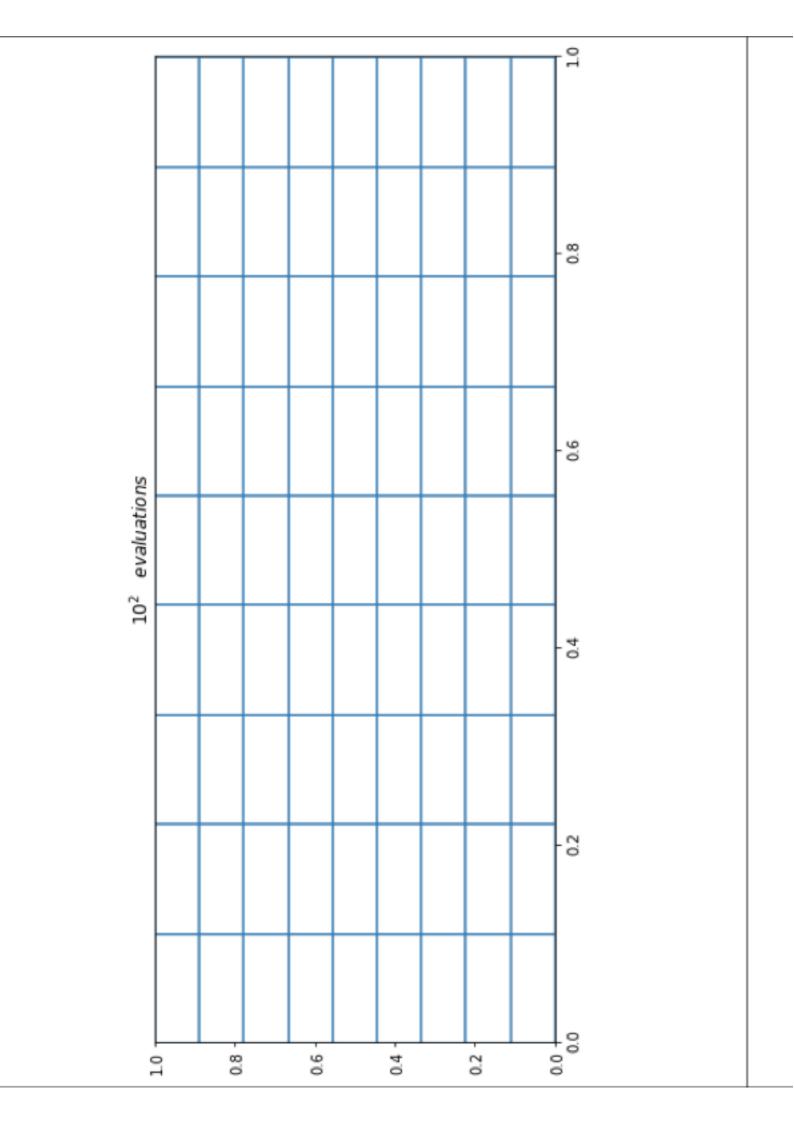
$$p(D) = \int p(D \mid H)p(H)dH \approx \sum_{i}^{n} p(D \mid H_{i})p(H_{i})$$

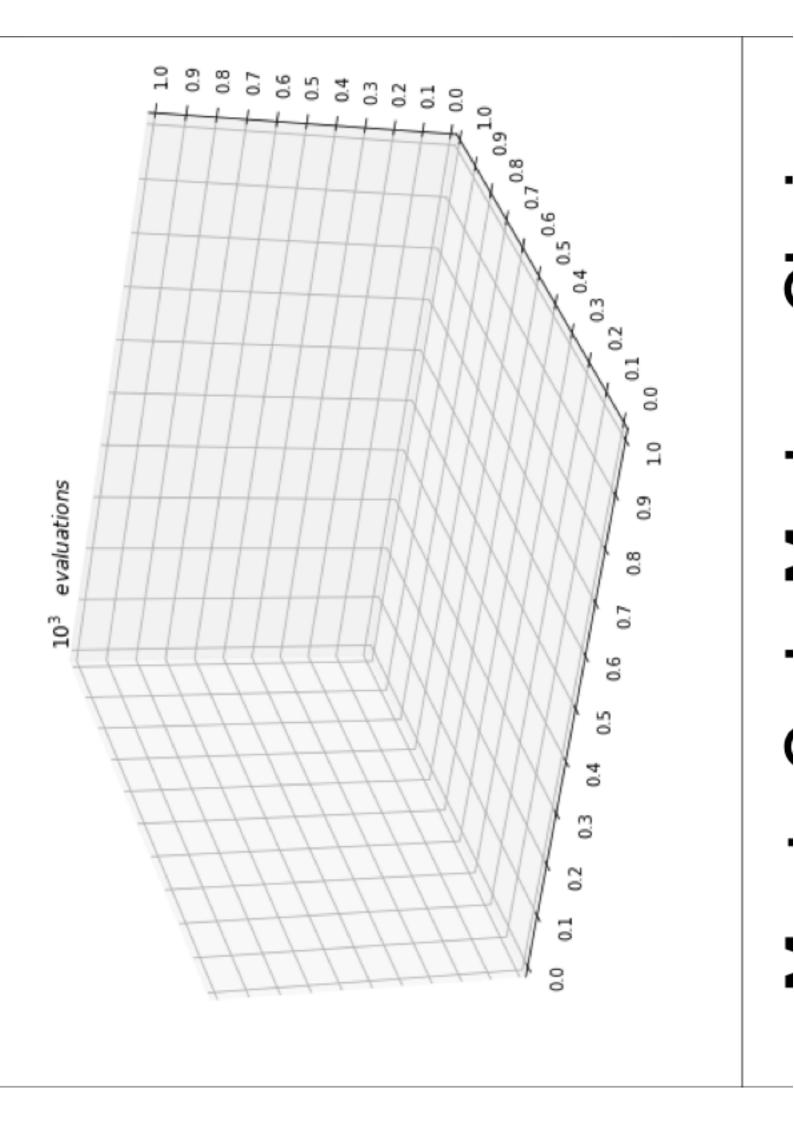
Need to resort to approximations

Sampling based solutions

- We can sample the parameter space and find the set of parameters that fits the data best
- If we take infinite samples across the parameter space we are guaranteed to find the true solution
- Taking infinite samples is clearly not possible
- Curse of dimensionality is a huge problem here



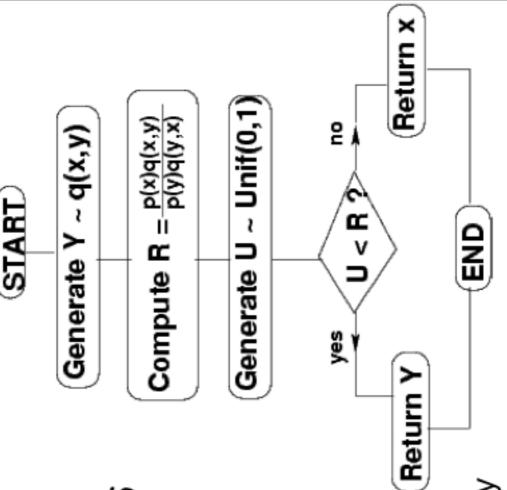


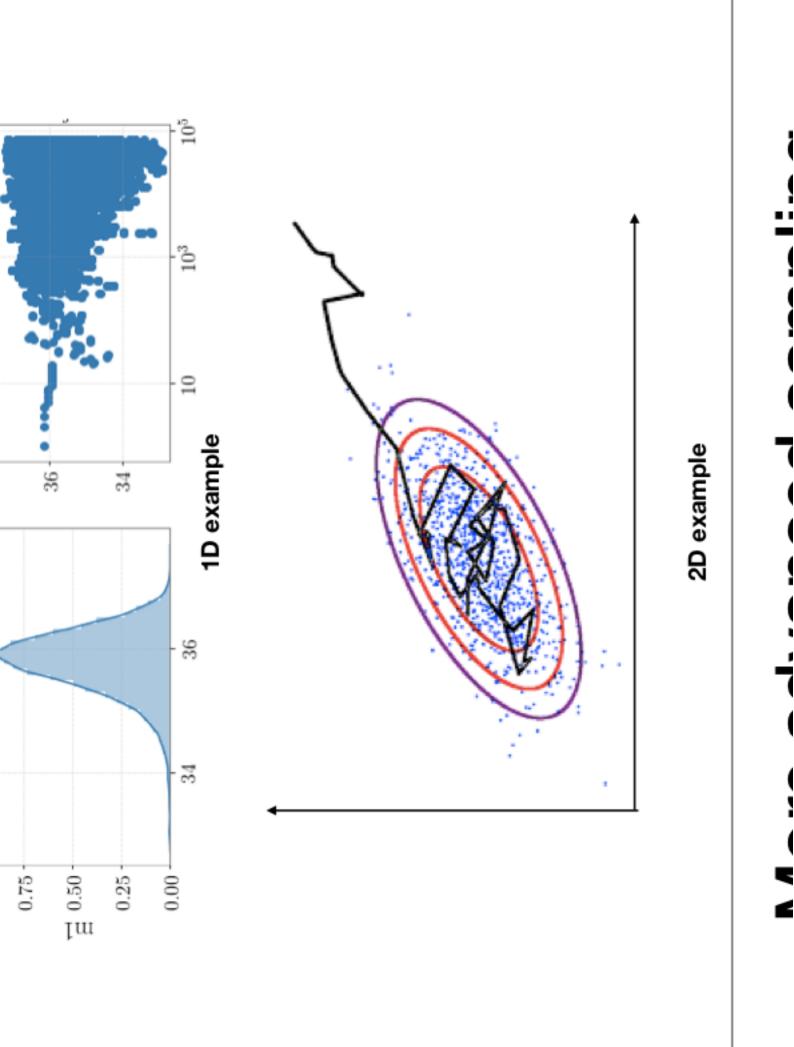


Monte Carlo Markow Chain

(MCMC)

- Current position is x
- Propose a new position y = x + δ
- Move if Metropolis Hastings condition satisfied
- "Walks" around the parameter space to approximate posterior
- Moves are stochastic but walk tends to region of high probability





More advanced sampling approaches

- Gibbs Sampling
- Nested sampling
- Hamiltonian Monte Carlo sampling
- NUTS Sampler
- Higher order (Riemannian Geometry) Based Sampling

Pros/cons with Sampling

- Guarantee asymptotically correct solutions
- Can be applied in principle to any model
- Can be very slow to explore large high dimensional data sets
- Can struggle with highly correlated or multi-modal parameter spaces
- Can be difficult to code up more advanced algorithms

Variational Inference

- minimise KL-divergence between them Propose some simple $q(z) \sim p(z|x)$ then
- KL Divergence is a measure of similarity between distributions

- Not a distance metric
- KL divergence tells you how much information you lose by approximating one distribution with another
- $KL(q(z)||p(z|x)) = \int q(z)log(\frac{q(z)}{p(z|x)})dx$
- Can then use standard optimisation (similar to neural networks) techniques to minimise this

Pros\cons with VI

- Much Faster than sampling
- Scale to high dimensional datasets
- No guarantee of convergence to global optimum
- Also in general difficult to code up

Probabilistic Programming











- STAN, Pyro, Tensorfow Probability, PyMC, Bilby ...
- Attempts to make the computer science/statistics of doing science easy
- bayesian inference without coding difficult algorithms User friendly API which allows scientists to perform
- Similar to Tensorflow, Pytorch for neural networks

Thanks for listening Any questions?