

# SO with BI study

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# SO simulation considerations

- Recovering of the **SO forecast**: it's just a proxy.
    - If we consider the polarization white noise level and add a  $\sqrt{2}$  in the likelihood noise covariance matrix, we find  $\sigma(r)$  close to forecast
    - However, it's just a proxy. Not even sure we are comparing apples-to-apples since we discard 1/f noise, hit map, FG marginalization, ...
  - We find that we get some **NANs in the DIs** computation. They significantly reduce when doing compsep full sky or using `nside_fit_parameters = 4`. It's some sky coverage related effects, but we don't know precisely why it happens and how to solve it
  - About the **Ultra Wide-Band** proposal: Mathias was considering a single UWB from 90 GHz to 250 GHz. However, this means almost 100% bandwidth and from the hardware point of view I think it's too much for feedhorns. If we write this proposal down in a paper, I think that any referee with a bit of familiarity with hardware stuff might argue that's unfeasible.  
In this regard, we might think of doing BI with **back-to-back Lenslets**: wouldn't bet on this and for sure it requires a more in-depth thought, but if feedhorns can't make it to 100% bandwidth, maybe lenslets can.
- These are my two cents.

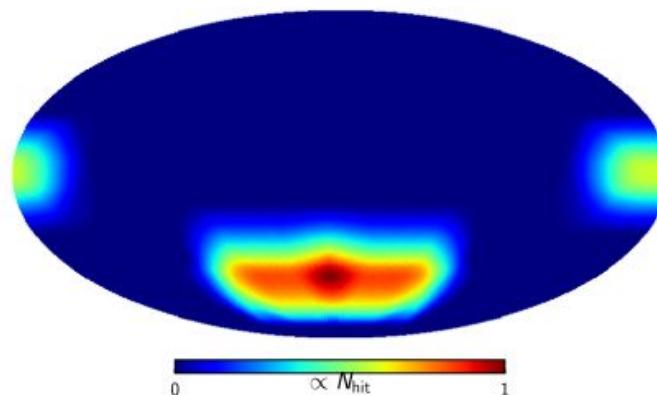
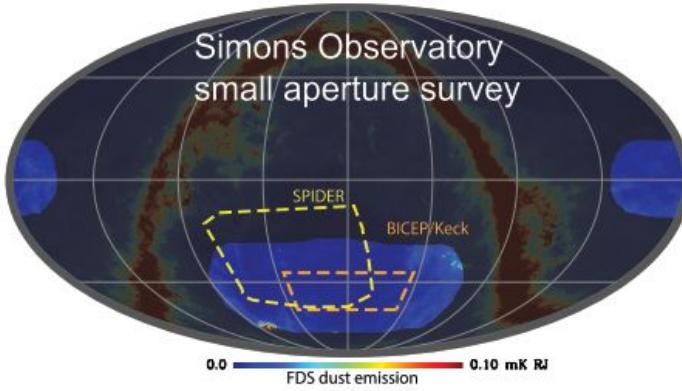
# SO SAT baseline

**Table 1**  
Properties of the planned SO surveys<sup>a</sup>.

<https://arxiv.org/abs/1808.07445>

Freq. [GHz]	SATs ( $f_{\text{sky}} = 0.1$ )			LAT ( $f_{\text{sky}} = 0.4$ )		
	FWHM (')	Noise (baseline) [ $\mu\text{K}\text{-arcmin}$ ]	Noise (goal) [ $\mu\text{K}\text{-arcmin}$ ]	FWHM (')	Noise (baseline) [ $\mu\text{K}\text{-arcmin}$ ]	Noise (goal) [ $\mu\text{K}\text{-arcmin}$ ]
27	91	35	25	7.4	71	52
39	63	21	17	5.1	36	27
93	30	2.6	1.9	2.2	8.0	5.8
145	17	3.3	2.1	1.4	10	6.3
225	11	6.3	4.2	1.0	22	15
280	9	16	10	0.9	54	37

<sup>a</sup> The detector passbands are being optimized (see [Simons Observatory Collaboration in prep.](#)) and are subject to variations in fabrication. For these reasons we expect the SO band centers to differ slightly from the frequencies presented here. ‘Noise’ columns give anticipated white noise levels for temperature, with polarization noise  $\sqrt{2}$  higher as both  $Q$  and  $U$  Stokes parameters are measured. Noise levels are quoted as appropriate for a homogeneous hits map.



<https://arxiv.org/pdf/2302.04276.pdf>

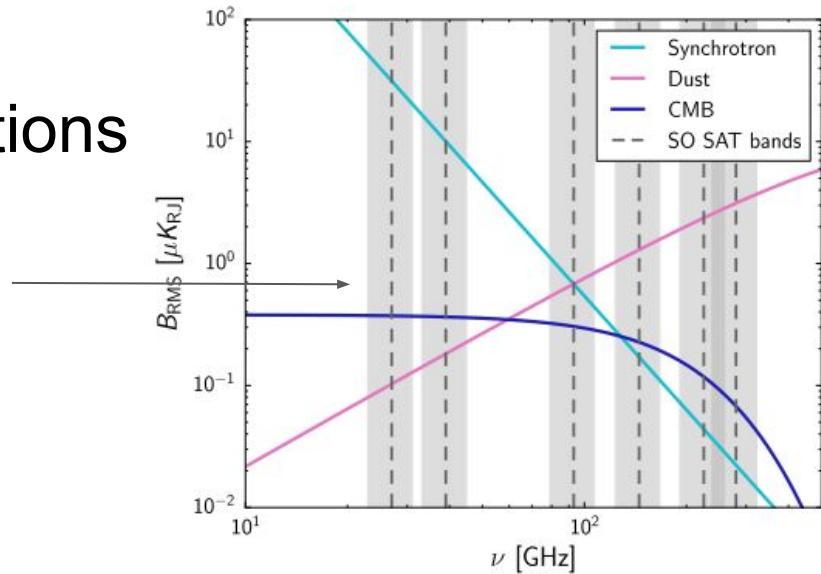
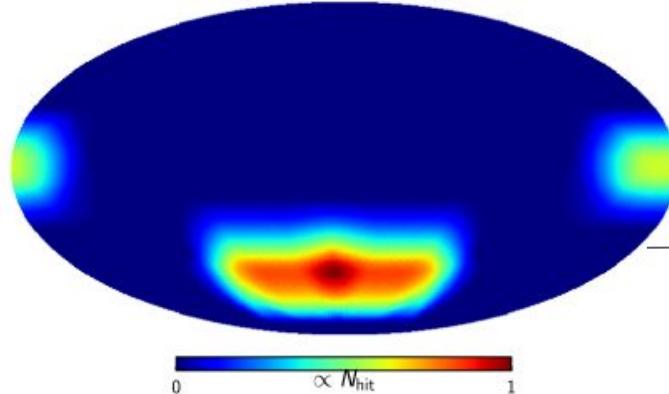


# Required modifications and additions

Bandwidth taken from digitalized version of this plot, taken from <https://arxiv.org/abs/1808.07445>



Sky patch taken from  
<https://github.com/simonsobs/BBPower/tree/main>



**Figure 4.** Frequency dependence, in RJ brightness temperature, of the synchrotron and thermal dust emission at degree scales within the proposed footprint for the SATs, compared to the CMB lensing  $B$ -mode signal. The turnover of the modified blackbody law for the dust lies above this frequency range.

- From Nside=64 to Nside=256
- From Equatorial (celestial) to Galactic

# Noise properties: add 1/f noise in sph. arm. space + 2map

These noise levels are expected to be appropriate for small angular scales, but large angular scales are contaminated by 1/ $f$  noise at low frequencies in the detector time stream, which arises primarily from the atmosphere and electronic noise. We model the overall expected SO noise spectrum in each telescope and band to have the form

$$N_\ell = N_{\text{red}} \left( \frac{\ell}{\ell_{\text{knee}}} \right)^{\alpha_{\text{knee}}} + N_{\text{white}}, \quad (1)$$

where  $N_{\text{white}}$  is the white noise component and  $N_{\text{red}}$ ,  $\ell_{\text{knee}}$ , and  $\alpha_{\text{knee}}$  describe the contribution from 1/ $f$  noise. We adopt values for these parameters using data from previous and on-going ground-based CMB experiments. We do not model the 1/ $f$  noise for the SATs in temperature: we do not anticipate using the SAT temperature measurements for scientific analysis, as the CMB signal is already well measured by *WMAP* and *Planck* on these scales.

*SAT polarization:* In this case we normalize the model such that  $N_{\text{red}} = N_{\text{white}}$ . At a reference frequency of

**Table 2**  
Band-dependent parameters for the large-angular-scale noise model described in Eq. 1. Parameters that do not vary with frequency are in the text.

Freq. [GHz]	SAT Polarization			LAT Temperature
	$\ell_{\text{knee}}^{\text{a}}$	$\ell_{\text{knee}}^{\text{b}}$	$\alpha_{\text{knee}}$	$N_{\text{red}} [\mu\text{K}^2\text{s}]$
27	30	15	-2.4	100
39	30	15	-2.4	39
93	50	25	-2.5	230
145	50	25	-3.0	1,500
225	70	35	-3.0	17,000
280	100	40	-3.0	31,000

<sup>a</sup> Pessimistic case. <sup>b</sup> Optimistic case.

# SO SAT Forecast

**Table 4**

Forecasts for  $r = 0$  model using six different cleaning methods, for fiducial foreground model<sup>a</sup>

Method	SO Baseline		SO Goal		
	pess-1/f	opt-1/f	pess-1/f	opt-1/f	
$A_{\text{lens}} = 1$	$C_\ell$ -Fisher	$\sigma = 2.4$	$\sigma = 1.9$	$\sigma = 1.7$	$\sigma = 1.5$
	$C_\ell$ -MCMC	$1.9 \pm 2.6$	$2.3 \pm 2.3$	$2.2 \pm 2.1$	$2.4 \pm 2.1$
	xForecast	$1.3 \pm 2.7$	$1.6 \pm 2.1$	$1.4 \pm 1.9$	$1.6 \pm 1.6$
	xForecast <sup>b</sup>	$0.0 \pm 4.0$	$0.0 \pm 3.5$	$0.0 \pm 3.3$	$0.2 \pm 2.8$
	BFoRe <sup>b</sup>	$-0.5 \pm 5.8$	$-0.5 \pm 3.6$	$-0.6 \pm 4.3$	$-0.5 \pm 3.4$
	ILC <sup>b</sup>	$-0.4 \pm 3.9$	$-0.3 \pm 3.1$	$-0.2 \pm 3.9$	$-0.3 \pm 3.0$
$A_{\text{lens}} = 0.5$	$C_\ell$ -Fisher	$\sigma = 1.8$	$\sigma = 1.4$	$\sigma = 1.2$	$\sigma = 0.9$
	$C_\ell$ -MCMC	$1.7 \pm 2.1$	$2.2 \pm 2.0$	$2.0 \pm 1.7$	$2.2 \pm 1.7$
	xForecast	$1.3 \pm 2.1$	$1.6 \pm 1.5$	$1.3 \pm 1.3$	$1.5 \pm 1.0$
	xForecast <sup>b</sup>	$0.1 \pm 3.2$	$0.1 \pm 2.6$	$0.0 \pm 2.5$	$0.3 \pm 1.8$
	BFoRe <sup>b</sup>	$-0.2 \pm 5.0$	$-0.4 \pm 2.6$	$-0.6 \pm 3.2$	$-0.5 \pm 2.0$
	ILC <sup>b</sup>	$-0.3 \pm 3.0$	$-0.3 \pm 2.4$	$-0.1 \pm 2.8$	$-0.2 \pm 2.3$

<sup>a</sup> Table gives  $(r \pm \sigma(r)) \times 10^3$  for different analysis pipelines (different rows), and different noise configurations (different columns, see Sec. 2.2 for details.). The results for the fiducial lensing and noise combination are highlighted in boldface.

<sup>b</sup> In these cases a foreground residual is additionally marginalized over after map-based cleaning.

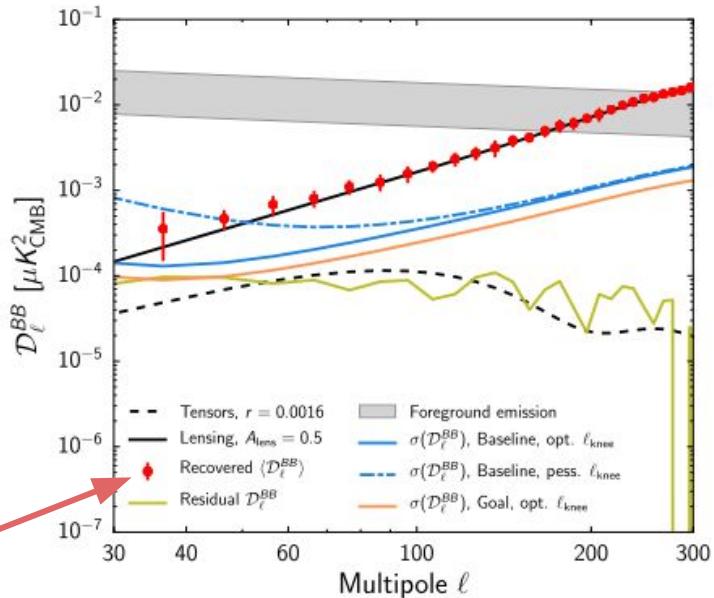
**Table 5**

Forecasts exploring departures from the fiducial case<sup>a</sup>

Method	Fiducial	$r = 0.01$	2-dust +AME	High-res $\beta_s$
$C_\ell$ -Fisher	$\sigma = 1.4$	$\sigma = 1.8$	$\sigma = 1.4$	$\sigma = 1.4$
$C_\ell$ -MCMC	$2.2 \pm 2.0$	$2.2 \pm 2.3$	$1.5 \pm 1.9$	$5.3 \pm 2.0$
xForecast <sup>b</sup>	$0.1 \pm 2.6$	$9.9 \pm 3.3$	$0.5 \pm 3.1$	$0.0 \pm 2.7$
BFoRe <sup>b</sup>	$-0.4 \pm 2.6$	$9.5 \pm 3.2$	$-0.3 \pm 2.4$	$-0.4 \pm 2.7$
ILC <sup>b</sup>	$-0.3 \pm 2.4$	$9.7 \pm 2.8$	$-0.3 \pm 2.5$	$-0.5 \pm 3.5$

<sup>a</sup> Table gives  $(r \pm \sigma(r)) \times 10^3$  for different analysis pipelines (different rows), and different departures from the fiducial case (an  $r = 0.01$  model and two alternative foreground models).

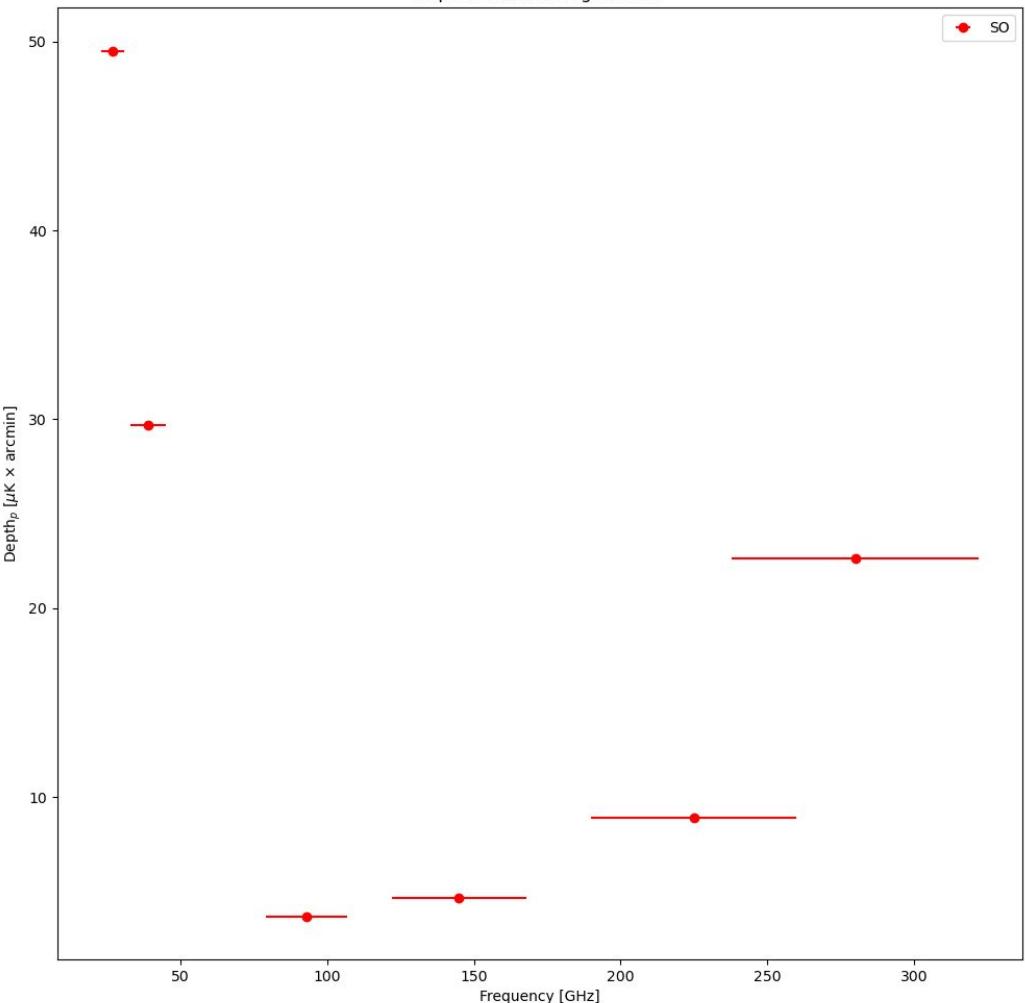
<sup>b</sup> Marginalized over foreground residual after cleaning.



**Figure 11.** Mean  $B$ -mode power spectrum,  $D_\ell^{BB}$ , estimated from simulations using map-level component separation (red) with errors from 100 realizations. The input spectrum (black solid) has  $r = 0$  and assumes 50% delensing. The power of the total foreground emission is shown shaded (between 93 GHz, lower, and 145 GHz, upper). Power spectrum uncertainties for  $\Delta\ell = 10$  bandpowers are shown (blue, orange) for different SO noise configurations. The contribution of foreground residuals to the recovered  $D_\ell^{BB}$  (yellow) biases the red circles above the input and is comparable to a signal with tensor-to-scalar ratio  $r = 0.0016$  (dashed). This bias can be suppressed by marginalizing over the foreground residuals in the likelihood.

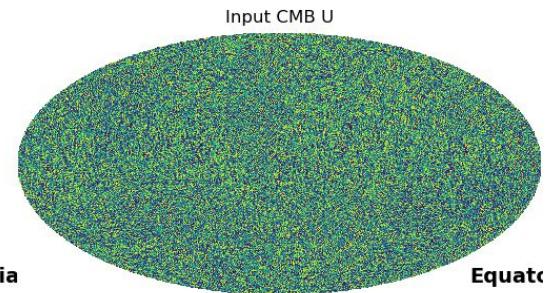
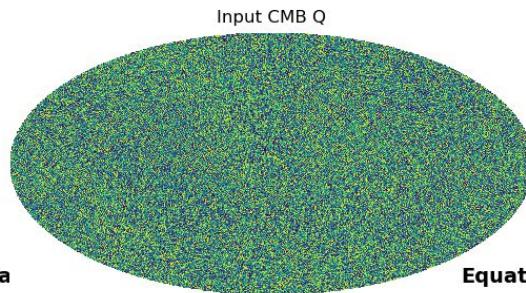
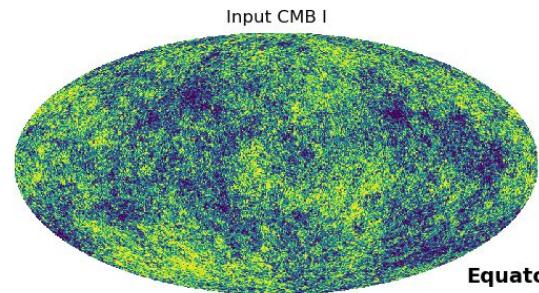
# Define instrumental setup

Experimental configurations

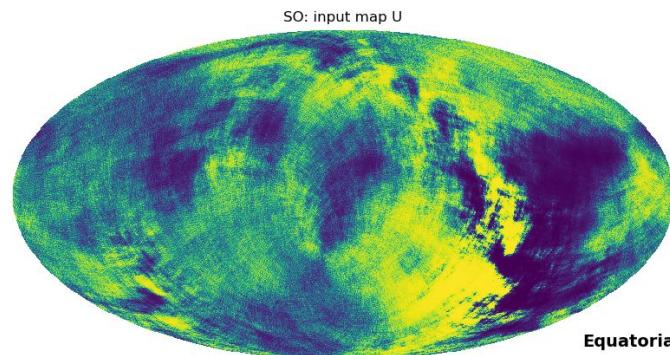
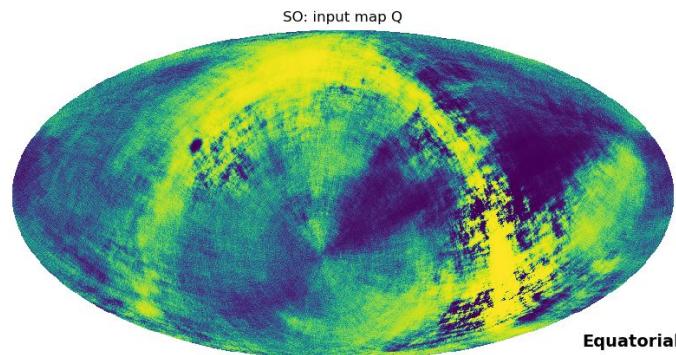


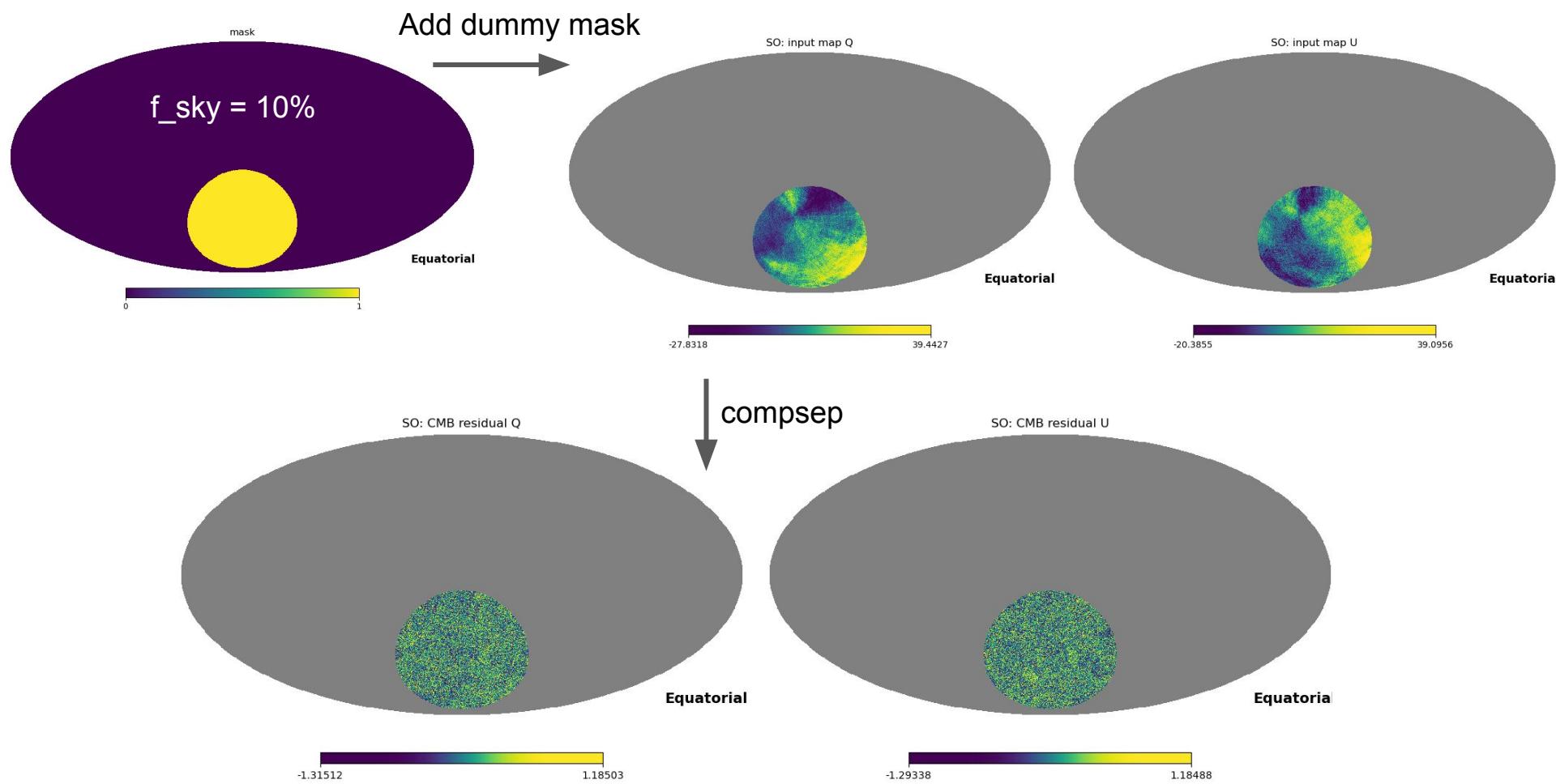
Dummy test on a circular sky patch  
with just white noise

# Test the code on a circular patch

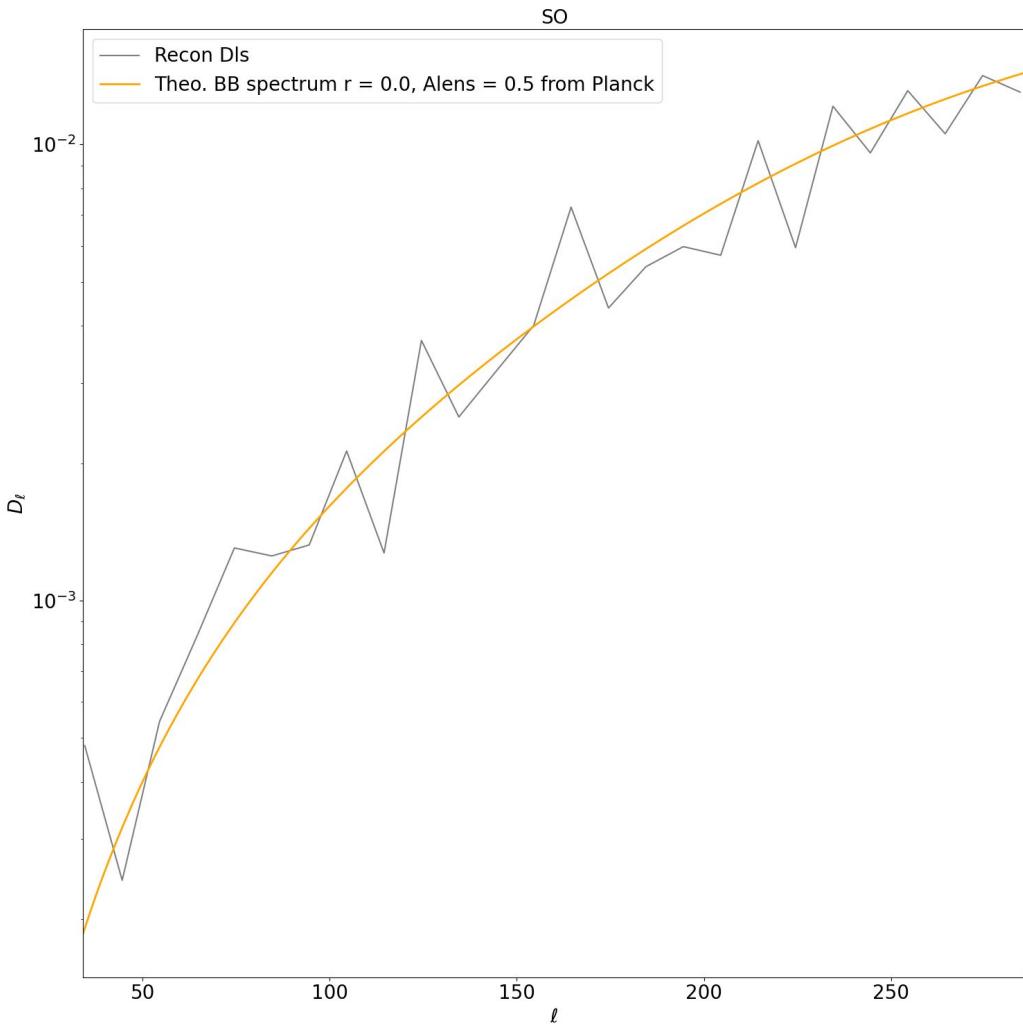
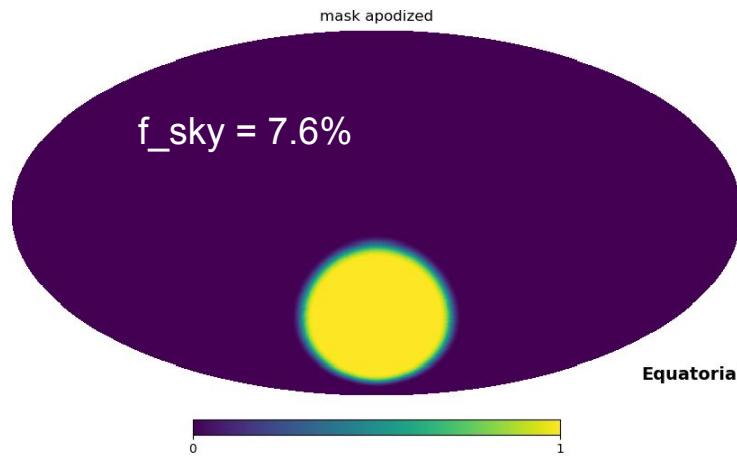


↓  
+ noise + FG →

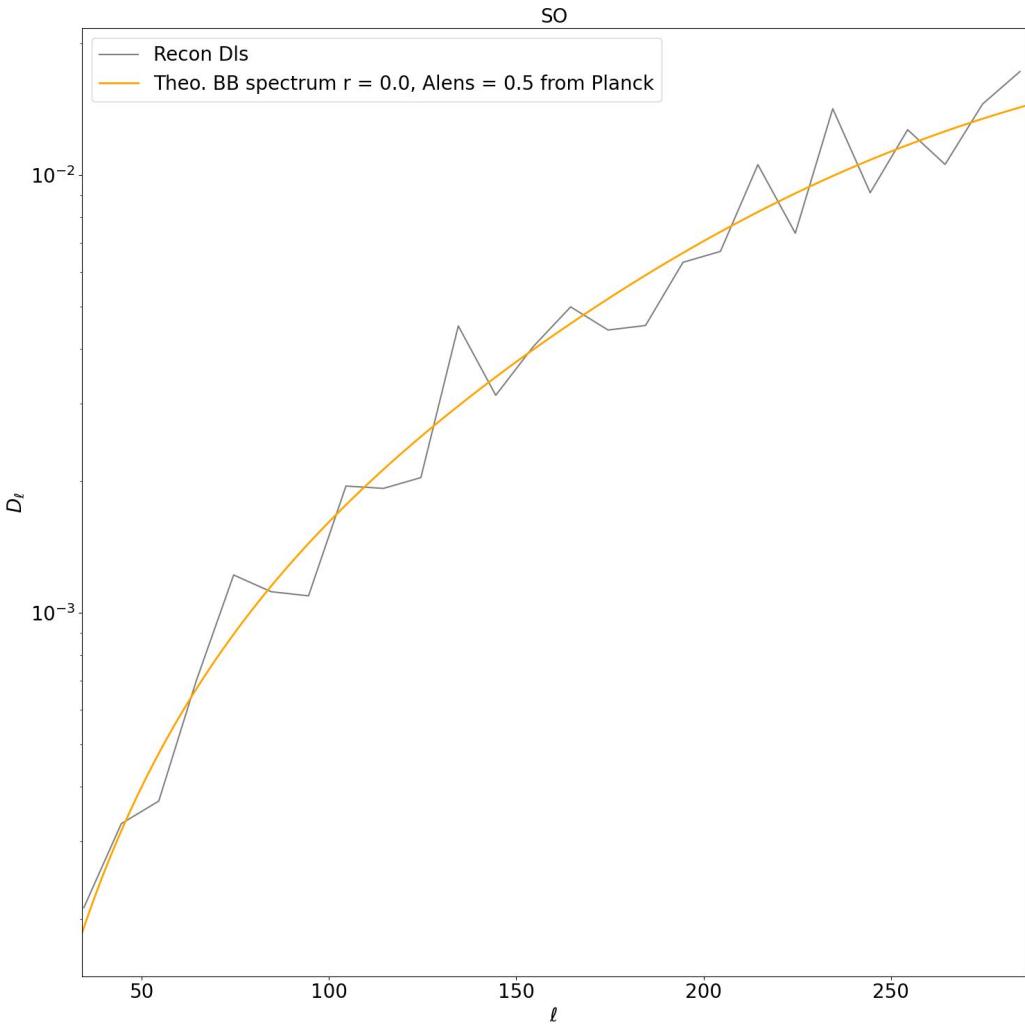




# From map to Dls

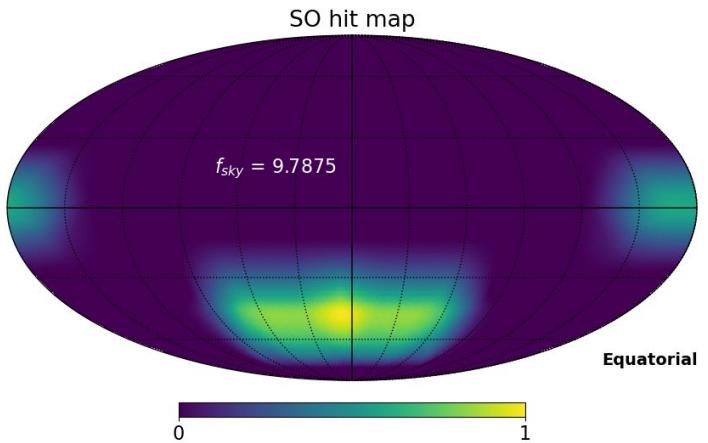


Same result, but from  
different realization: seems ok



Test with the official sky patch  
but just white noise

# Define coverage

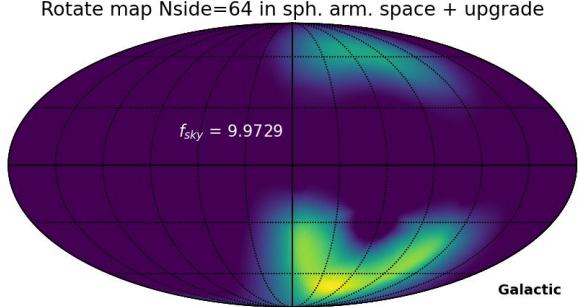


From Nside=64  
to Nside=256

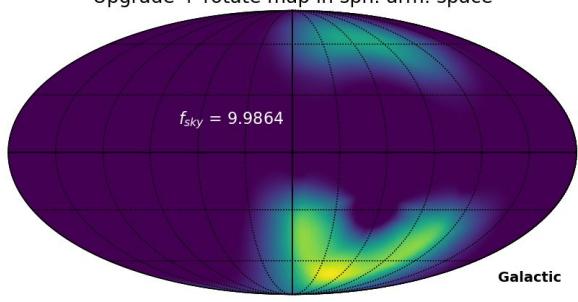
From Equatorial  
(celestial) to  
Galactic

Loris docet: this has less contamination

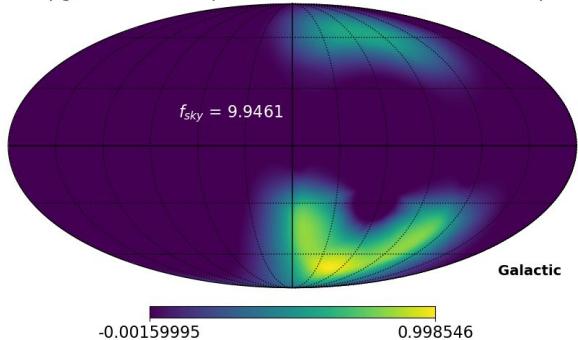
method 1



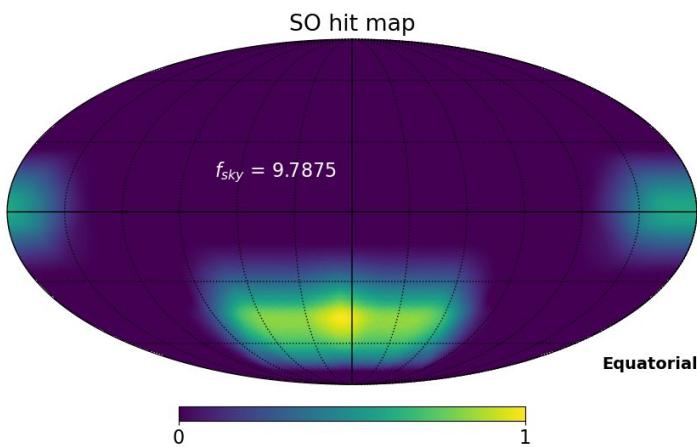
method 2



method 3

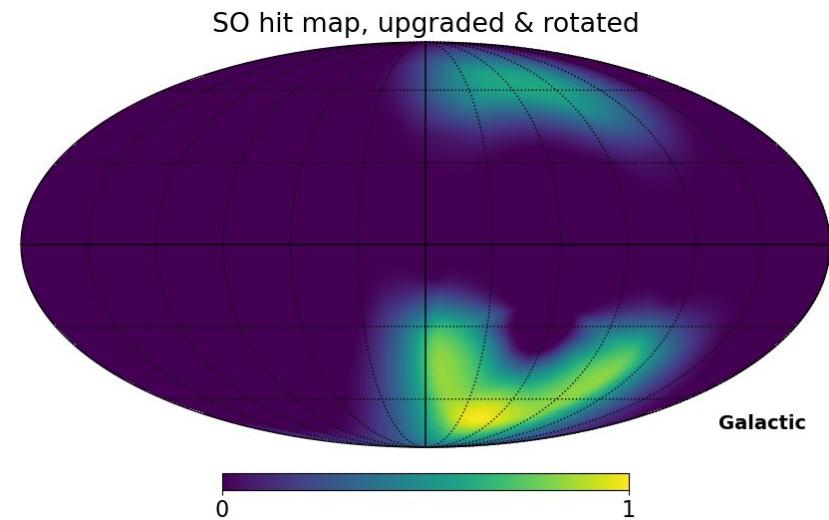


# Define coverage



From Nside=64  
to Nside=256

From Equatorial  
(celestial) to  
Galactic

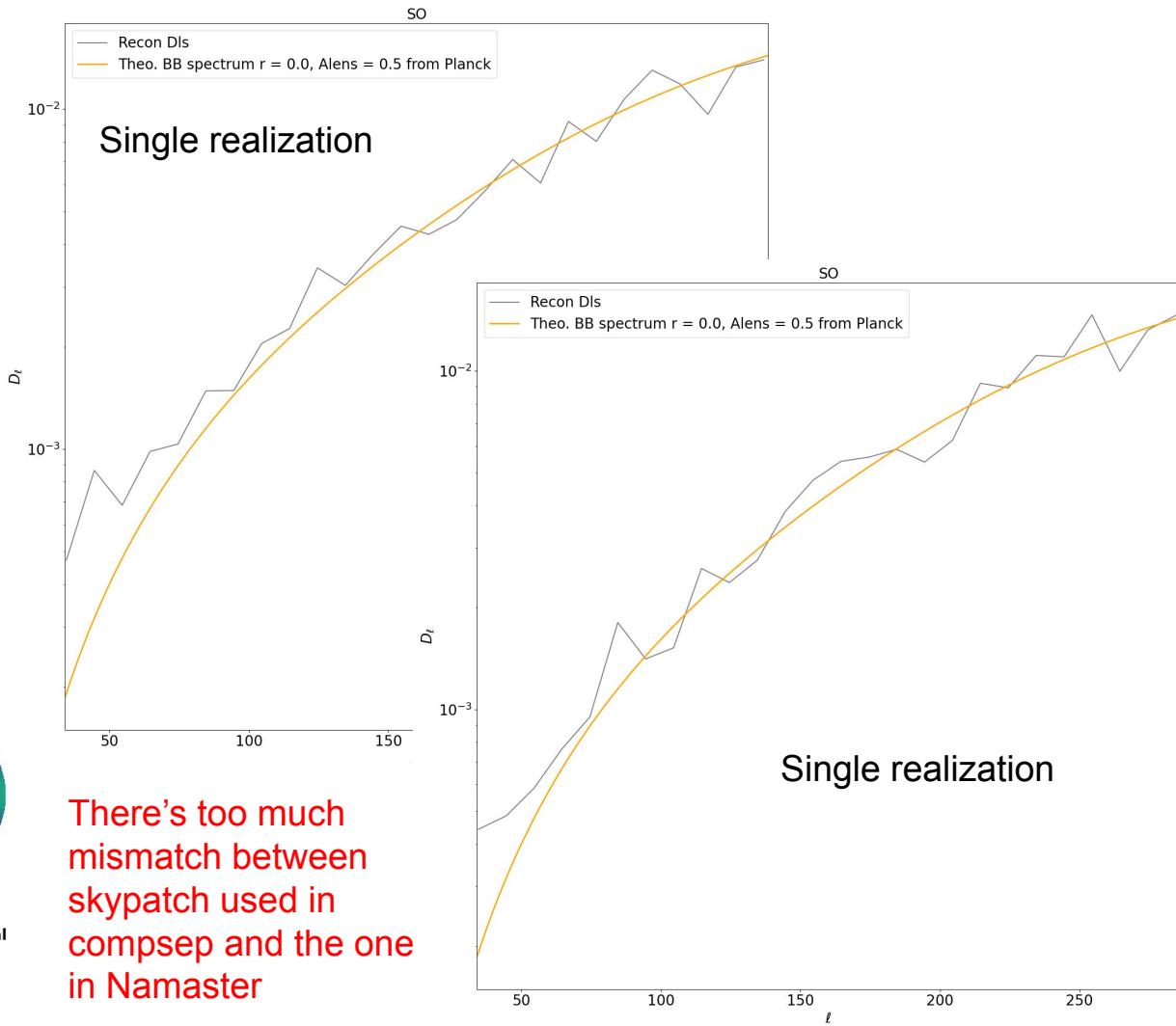
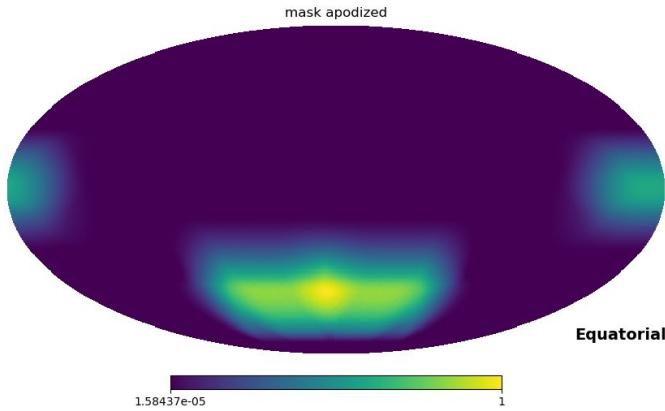


Obtained with method 3  
and then normalized

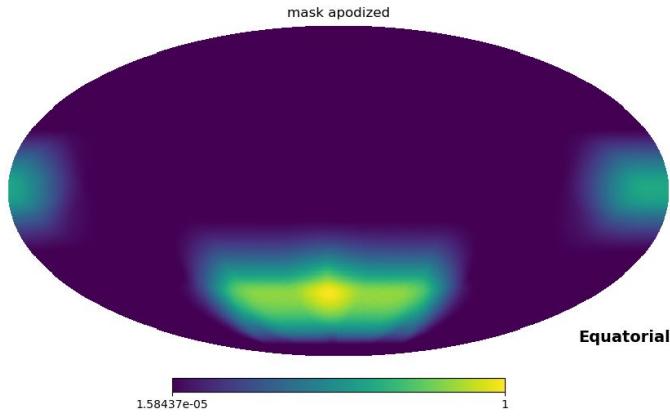
# Test 1

Sky patch for compsep defined by taking pixels with coverage > 0.05

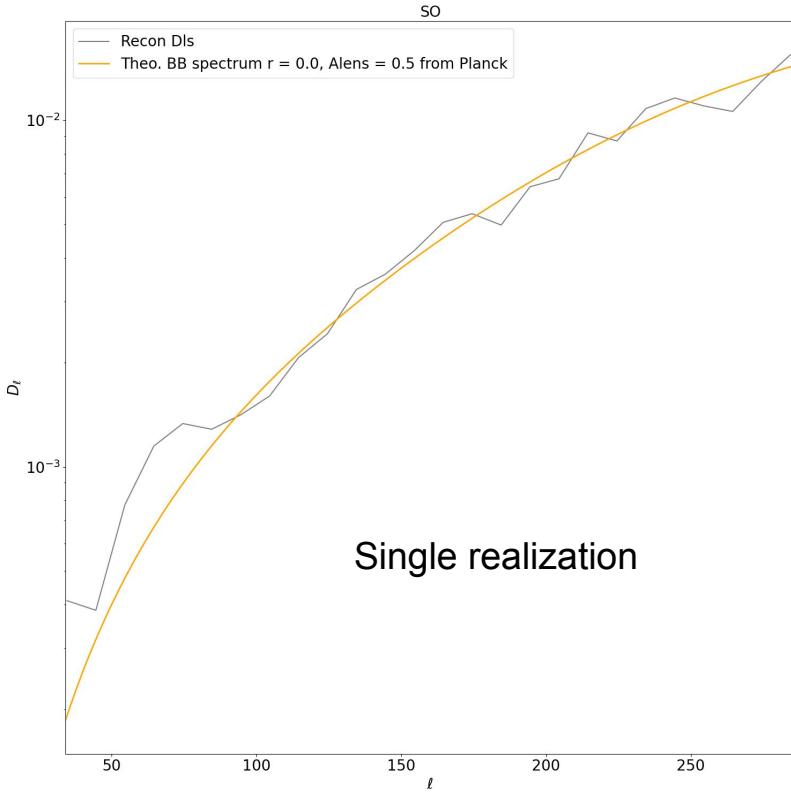
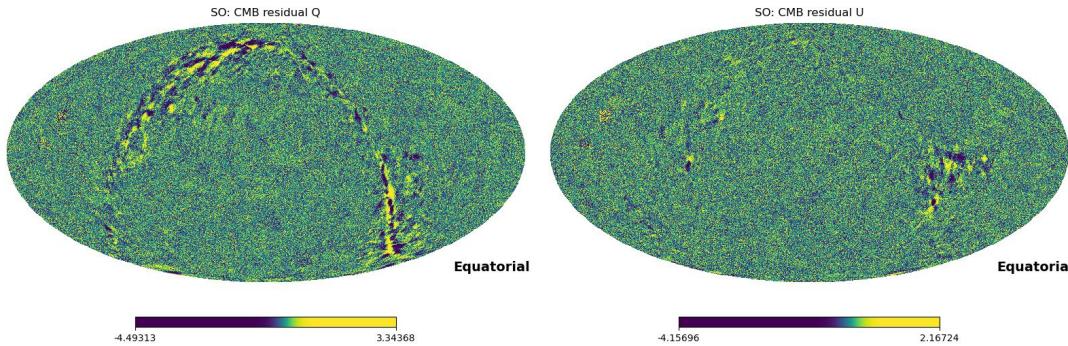
Then I pass to Namaster the hit map itself with `apo_size=1` (so that it doesn't modify the hit map significantly. If I use `apo_size=0` I get all NaNs and I don't know why)



# Test 2

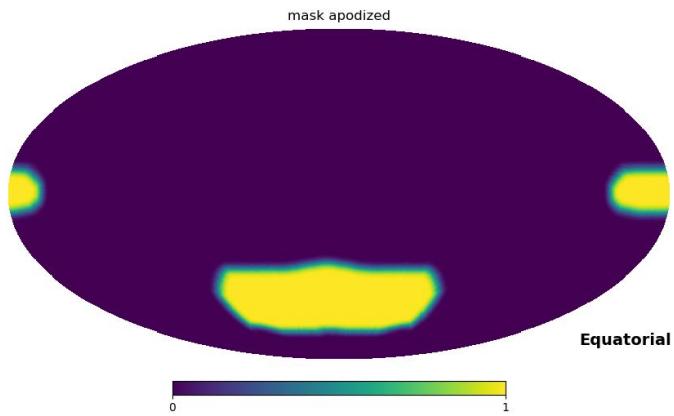


compsep almost full sky (pixel seen if cov > 0)  
+ mask in Namaster is the official SO hit mask with  
additional 1 deg apo to make Namaster work



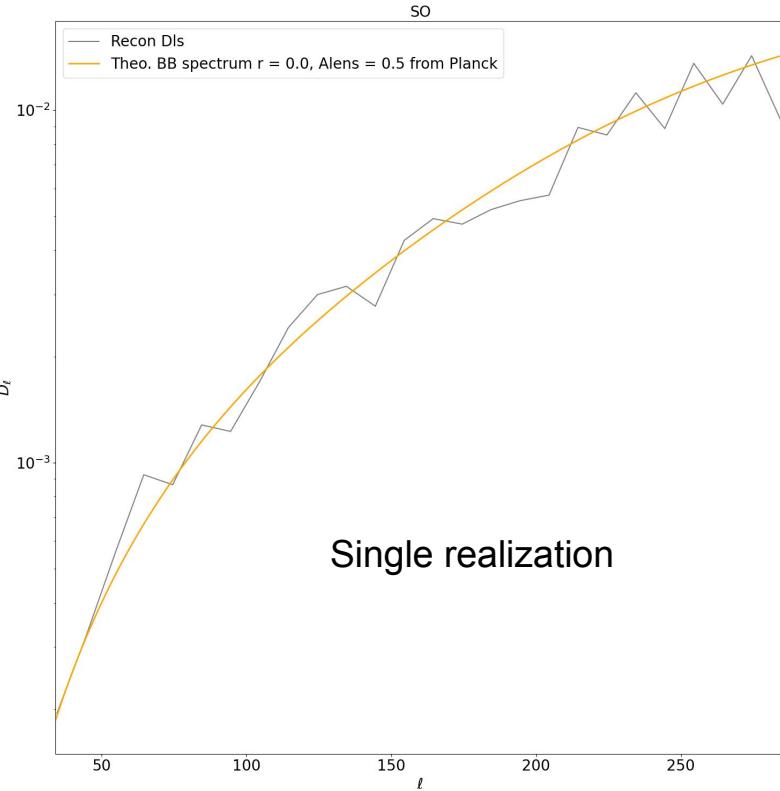
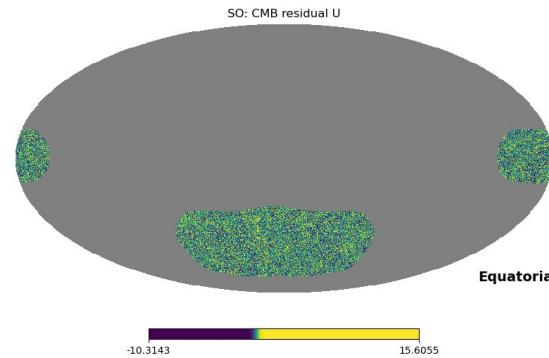
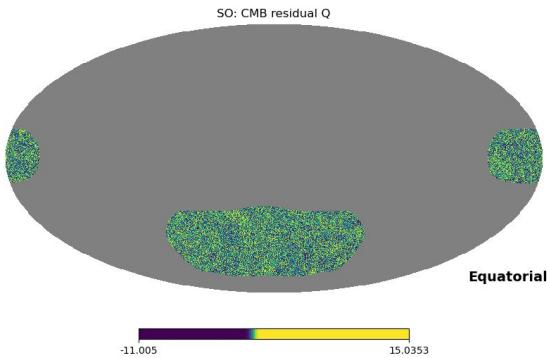
This method is self-consistent but the compsep is almost full sky. But FGB doesn't take hit maps, just zeros or hp.UNSEEN

# Test 3



Def pixel as seen if coverage > 0.3

Pass this coverage to Namaster + apo = 10 deg

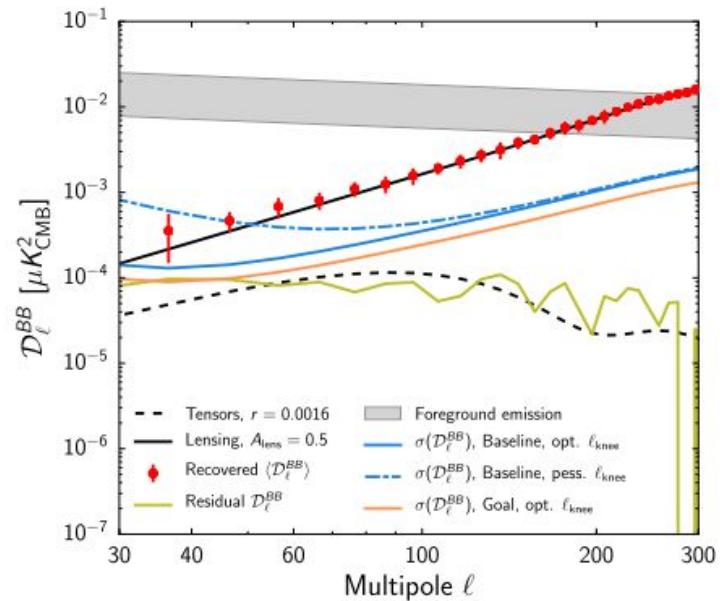
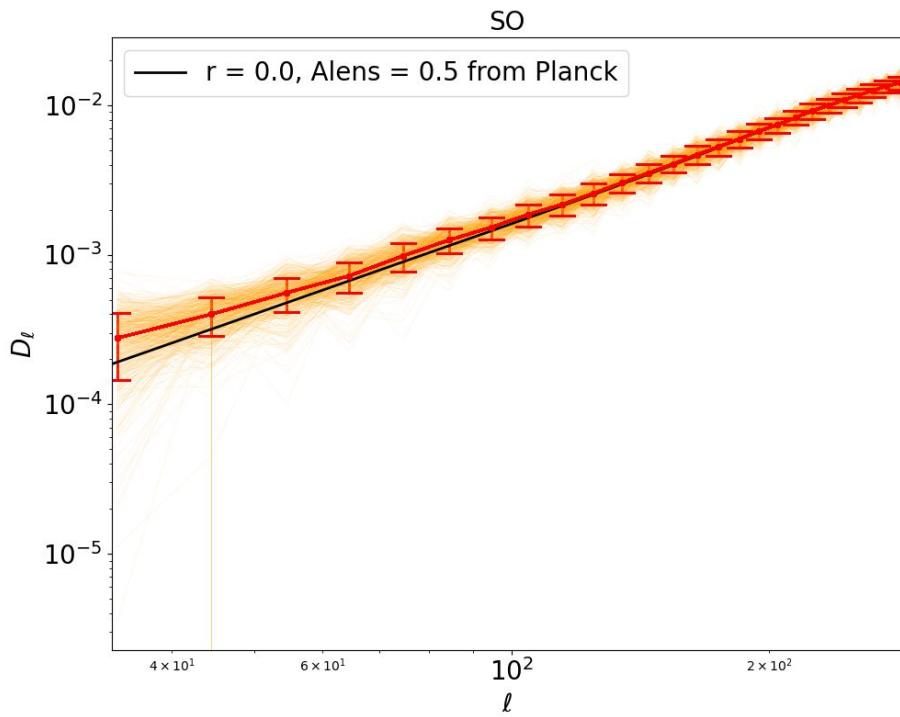


Single realization

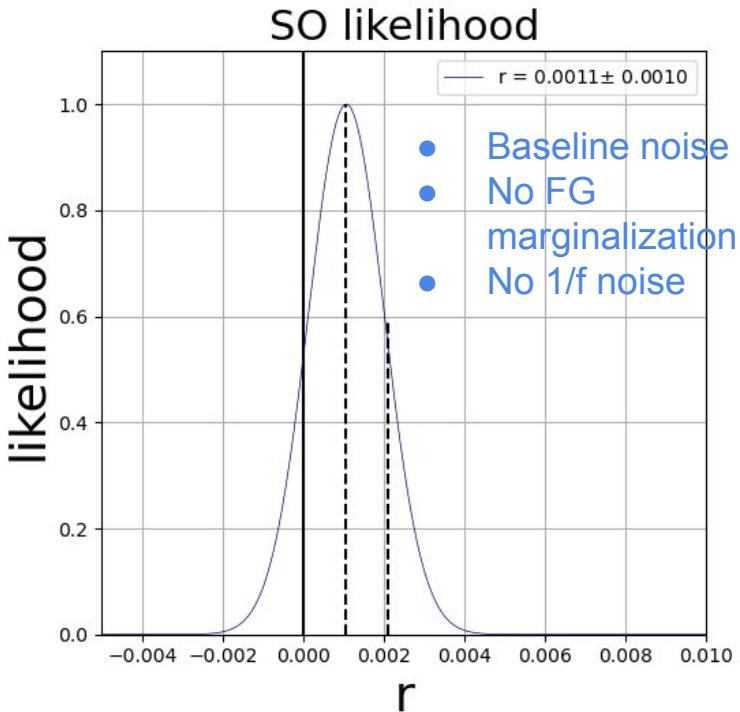
This method is also self-consistent but the sky patch deviates from the official one

# Test 2 with full pipeline (500 reals)

compsep almost full sky (pixel seen if cov > 0)  
+ mask in Namaster is the official SO hit mask with  
additional 1 deg apo to make Namaster work



# Test 2 with full pipeline (500 reals)



**Table 4**  
Forecasts for  $r = 0$  model using six different cleaning methods, for fiducial foreground model<sup>a</sup>

	Method	SO Baseline		SO Goal	
		pess-1/f	opt-1/f	pess-1/f	opt-1/f
$A_{\text{lens}} = 1$	$C_\ell$ -Fisher	$\sigma = 2.4$	$\sigma = 1.9$	$\sigma = 1.7$	$\sigma = 1.5$
	$C_\ell$ -MCMC	$1.9 \pm 2.6$	$2.3 \pm 2.3$	$2.2 \pm 2.1$	$2.4 \pm 2.1$
	xForecast	$1.3 \pm 2.7$	$1.6 \pm 2.1$	$1.4 \pm 1.9$	$1.6 \pm 1.6$
	xForecast <sup>b</sup>	$0.0 \pm 4.0$	$0.0 \pm 3.5$	$0.0 \pm 3.3$	$0.2 \pm 2.8$
	BFoRe <sup>b</sup>	$-0.5 \pm 5.8$	$-0.5 \pm 3.6$	$-0.6 \pm 4.3$	$-0.5 \pm 3.4$
	ILC <sup>b</sup>	$-0.4 \pm 3.9$	$-0.3 \pm 3.1$	$-0.2 \pm 3.9$	$-0.3 \pm 3.0$
$A_{\text{lens}} = 0.5$	$C_\ell$ -Fisher	$\sigma = 1.8$	<b><math>\sigma = 1.4</math></b>	$\sigma = 1.2$	$\sigma = 0.9$
	$C_\ell$ -MCMC	$1.7 \pm 2.1$	<b><math>2.2 \pm 2.0</math></b>	$2.0 \pm 1.7$	$2.2 \pm 1.7$
	xForecast	<b><math>1.3 \pm 2.1</math></b>	<b><math>1.6 \pm 1.5</math></b>	$1.3 \pm 1.3$	$1.5 \pm 1.0$
	xForecast <sup>b</sup>	$0.1 \pm 3.2$	<b><math>0.1 \pm 2.6</math></b>	$0.0 \pm 2.5$	$0.3 \pm 1.8$
	BFoRe <sup>b</sup>	$-0.2 \pm 5.0$	<b><math>-0.4 \pm 2.6</math></b>	$-0.6 \pm 3.2$	$-0.5 \pm 2.0$
	ILC <sup>b</sup>	$-0.3 \pm 3.0$	<b><math>-0.3 \pm 2.4</math></b>	$-0.1 \pm 2.8$	$-0.2 \pm 2.3$

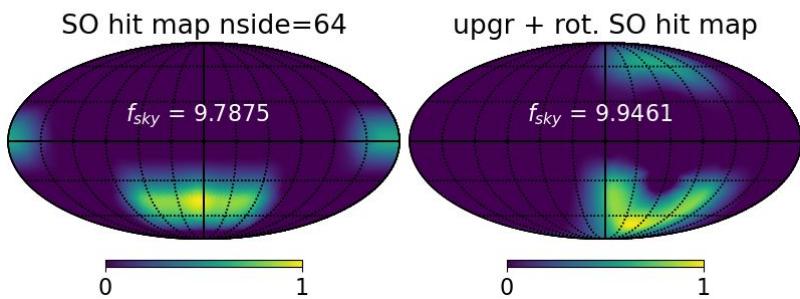
- Baseline noise
- No FG marginalization
- opt-1/f noise

<sup>a</sup> Table gives  $(r \pm \sigma(r)) \times 10^3$  for different analysis pipelines (different rows), and different noise configurations (different columns, see Sec. 2.2 for details.). The results for the fiducial lensing and noise combination are highlighted in boldface.

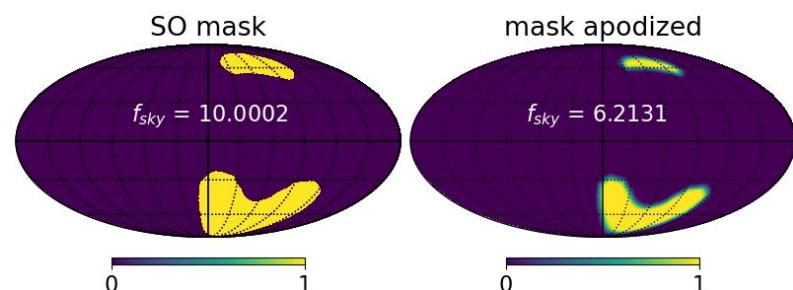
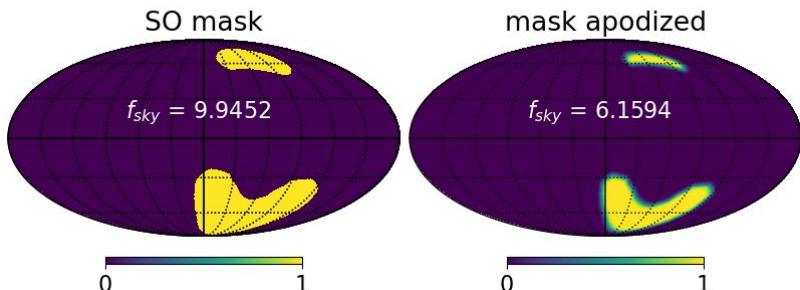
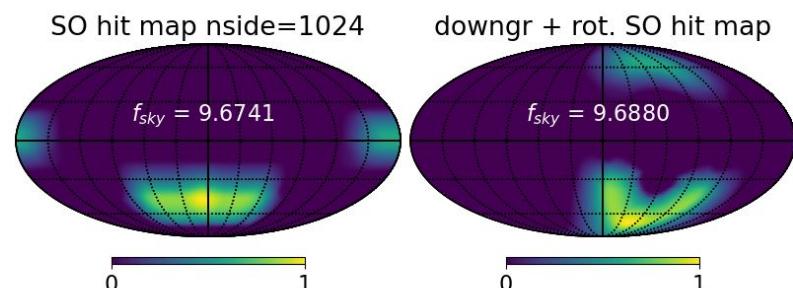
<sup>b</sup> In these cases a foreground residual is additionally marginalized over after map-based cleaning.

On the discrepancy between my and  
Mathias' results

Coverage map from SO hit map nside=64



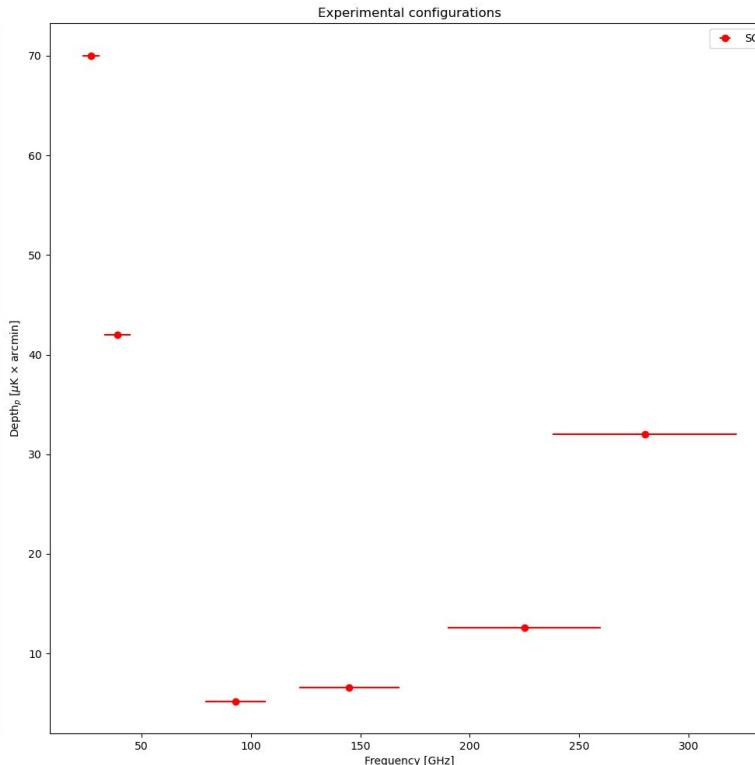
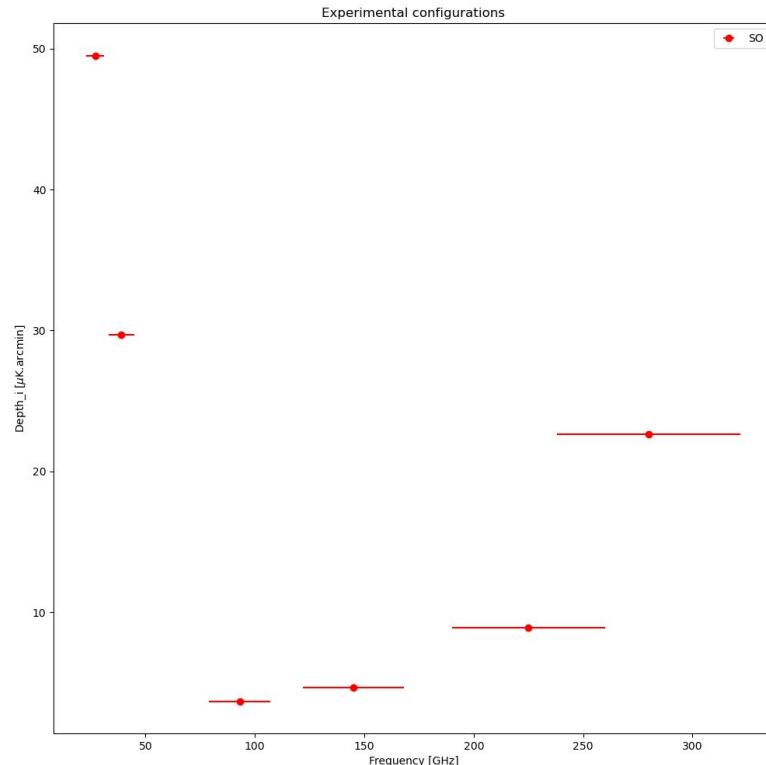
Coverage map from SO hit map nside=1024



no major difference

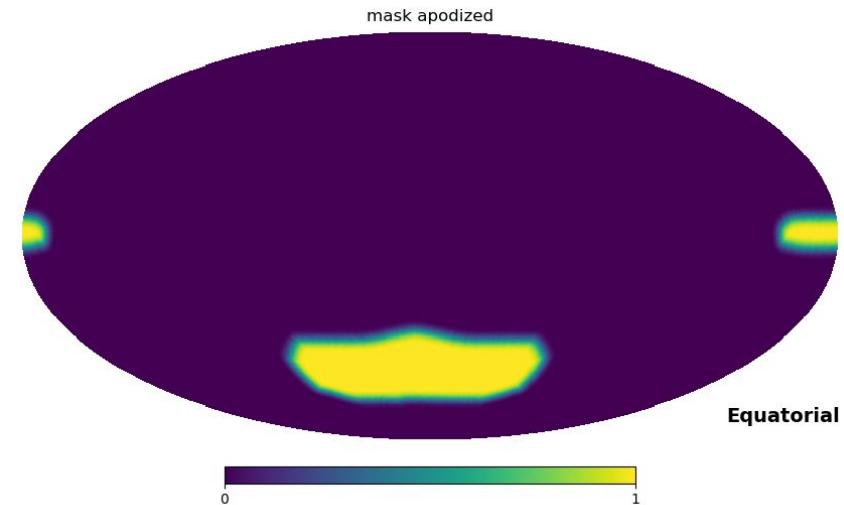
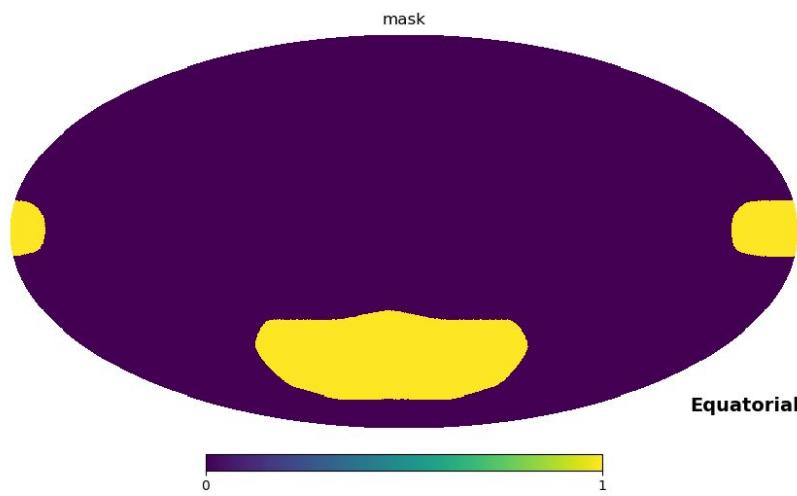
# Test single realization using:

- pol wh noise\*sqrt(2) for cross-spectra
- binary coverage from hit map at nside=1024



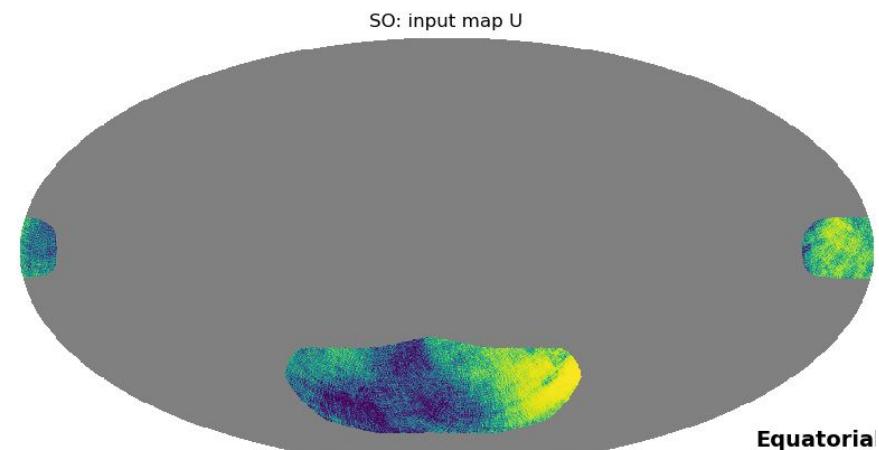
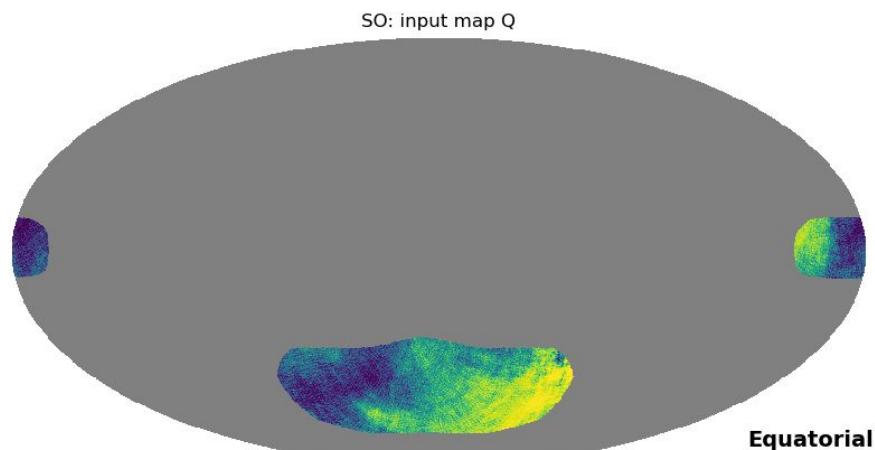
Test single realization using:

- pol wh noise\*sqrt(2) for cross-spectra
- binary coverage from hit map at nside=1024



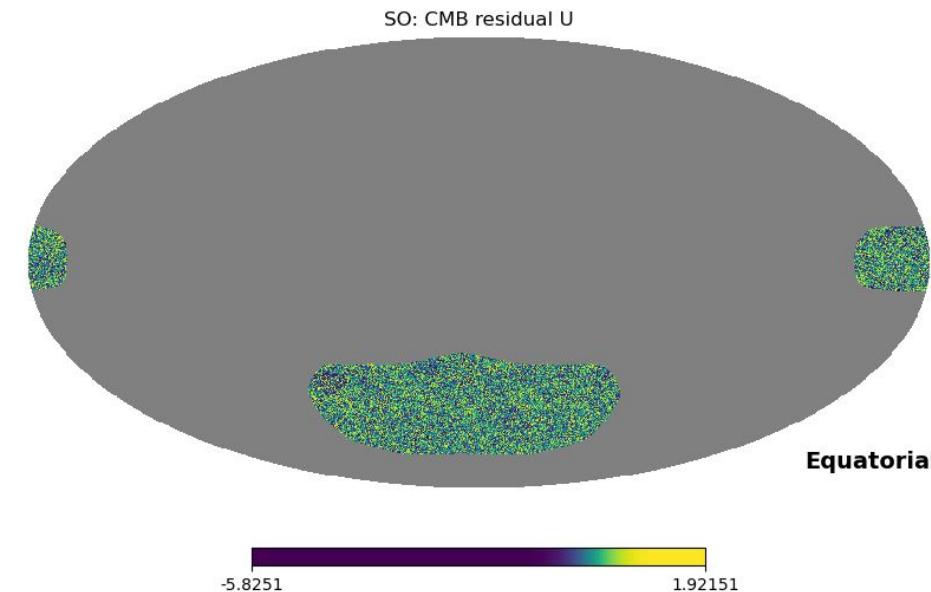
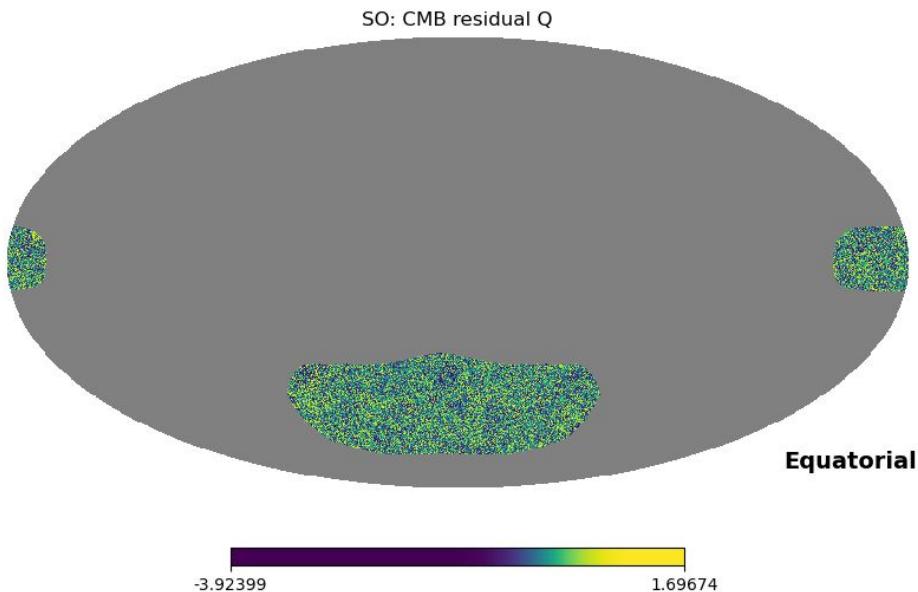
Test single realization using:

- pol wh noise\*sqrt(2) for cross-spectra
- binary coverage from hit map at nside=1024



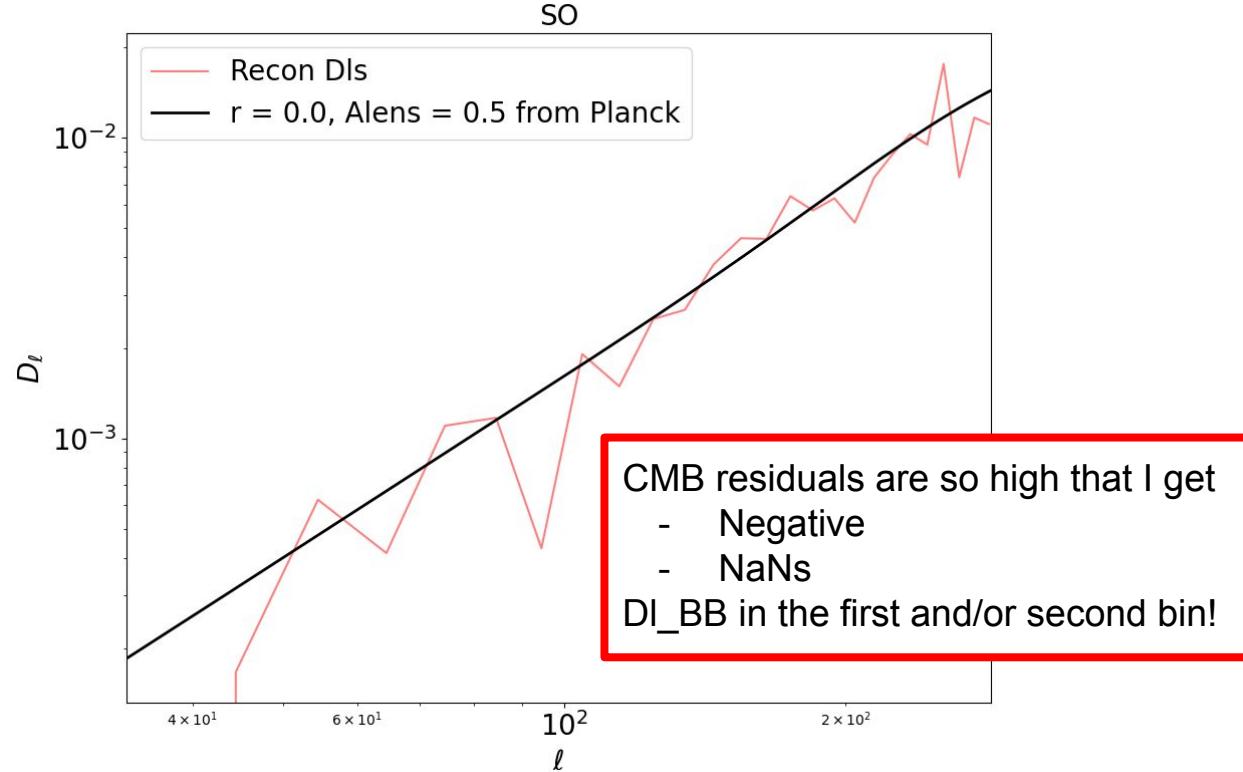
Test single realization using:

- pol wh noise\*sqrt(2) for cross-spectra
- binary coverage from hit map at nside=1024



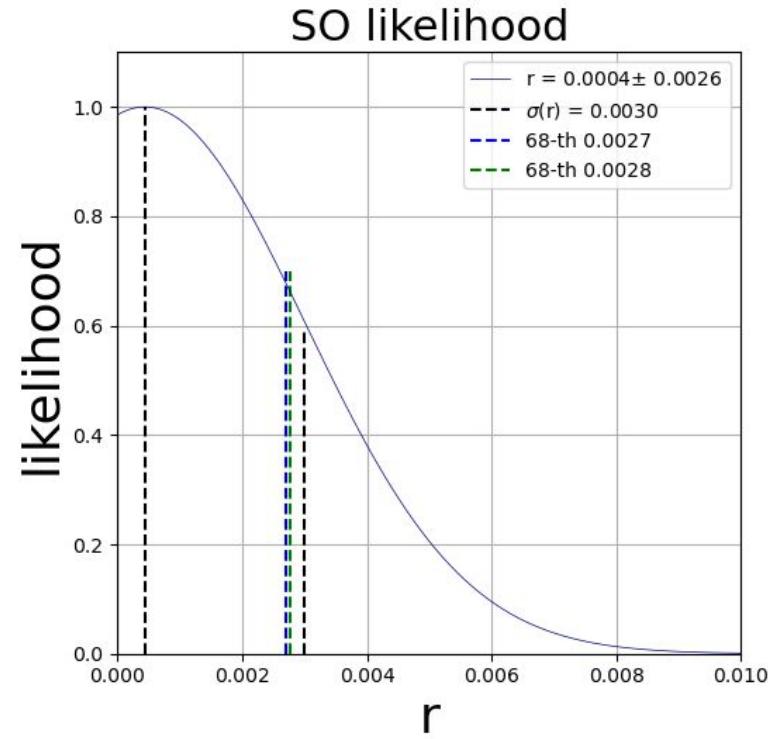
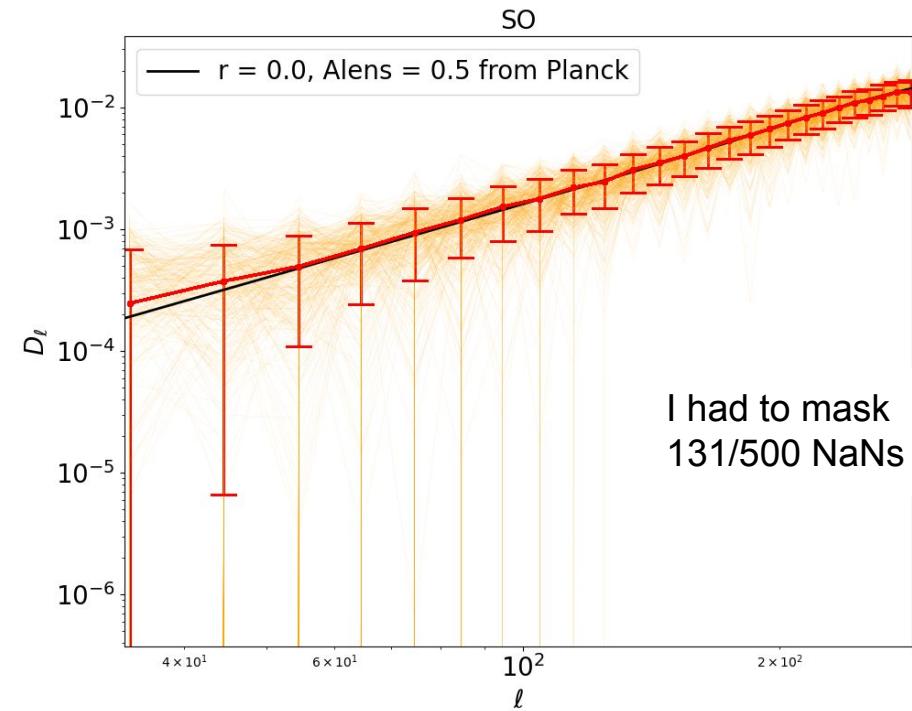
## Test single realization using:

- pol wh noise\*sqrt(2) for cross-spectra
- binary coverage from hit map at nside=1024



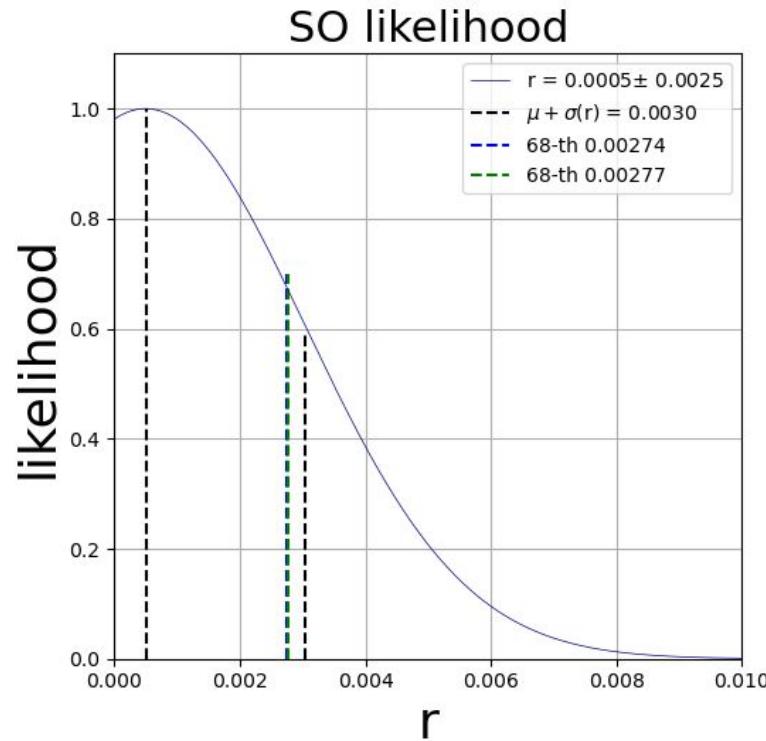
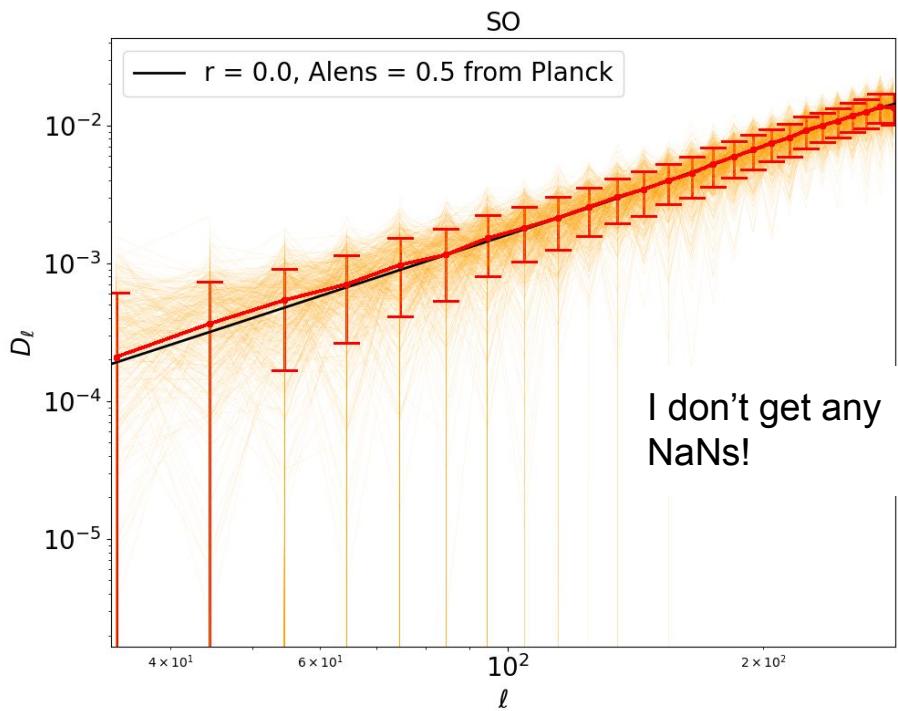
# Full pipeline using:

- pol wh noise\*sqrt(2) for cross-spectra
- binary coverage from hit map at nside=1024

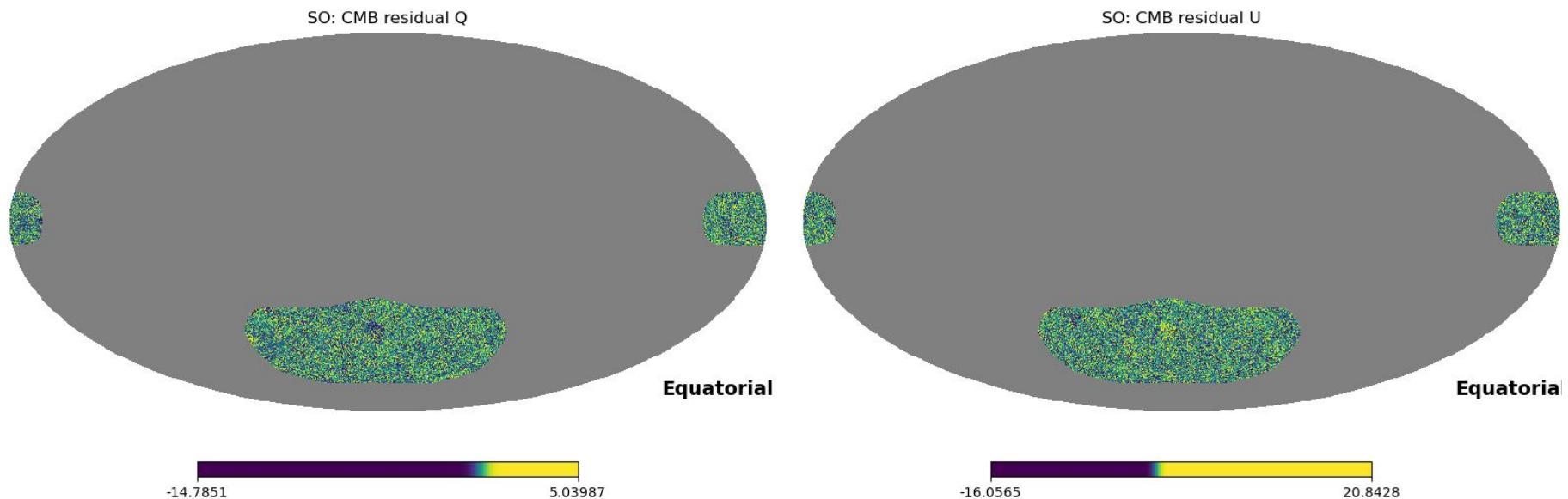


# Full pipeline **FULL-SKY** using:

- pol wh noise\*sqrt(2) for cross-spectra
- binary coverage from hit map at nside=1024

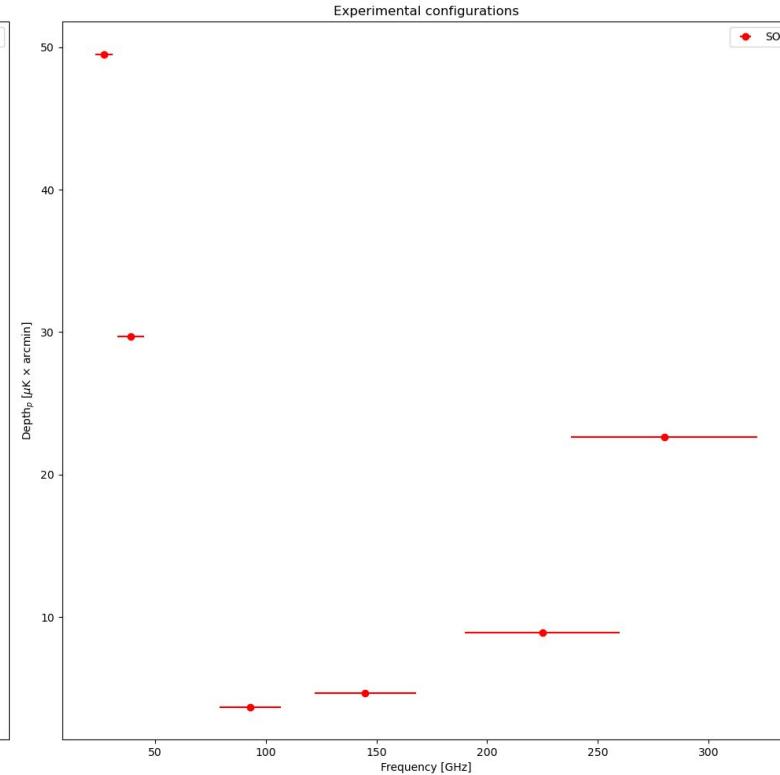
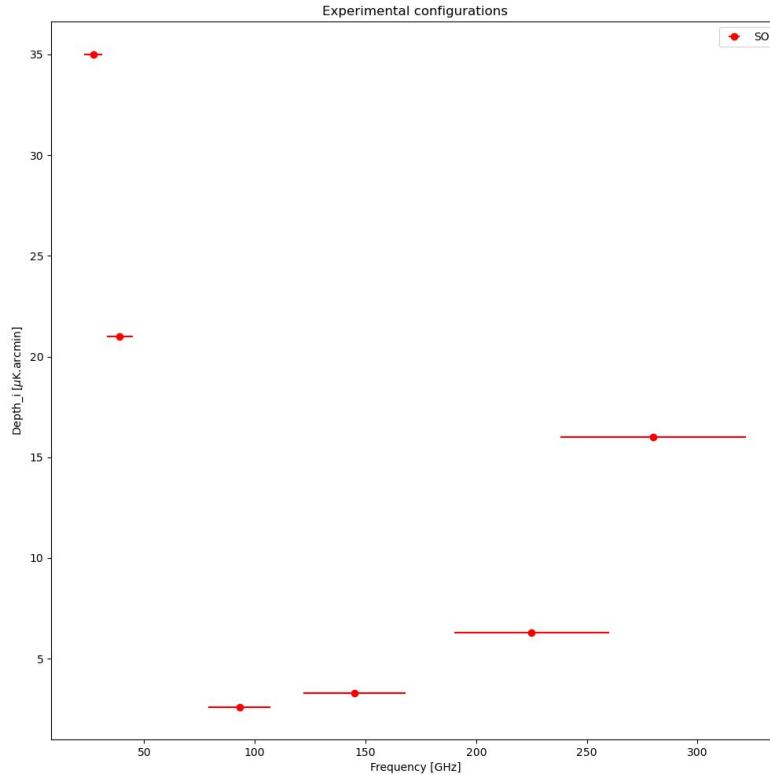


# Example of reconstructed CMB map that leads to NaN



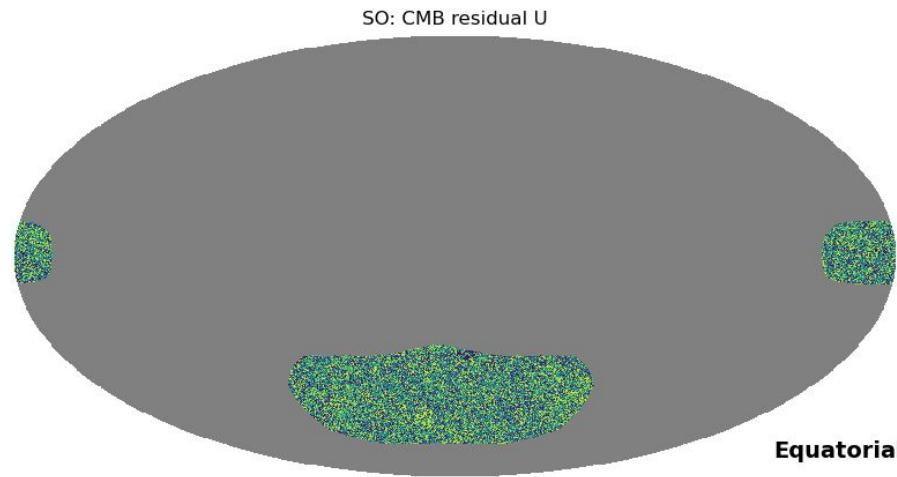
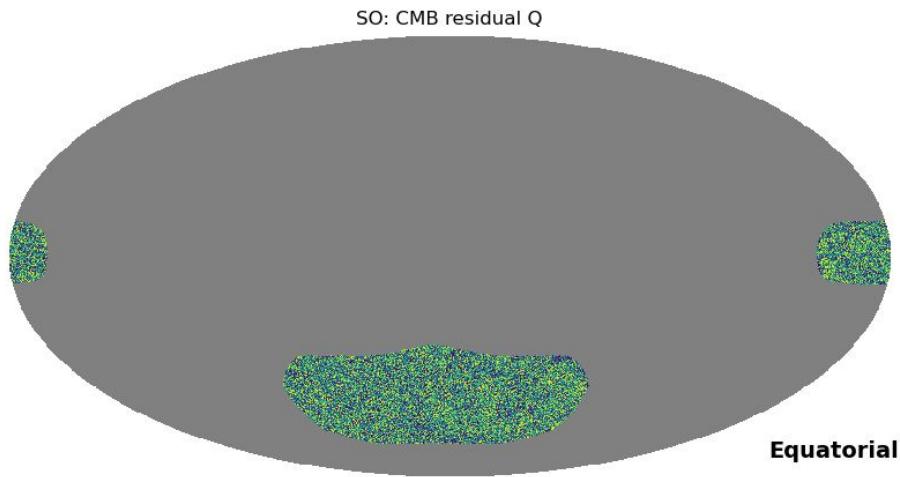
# Test single realization using:

- pol wh noise
- binary coverage from hit map at nside=1024



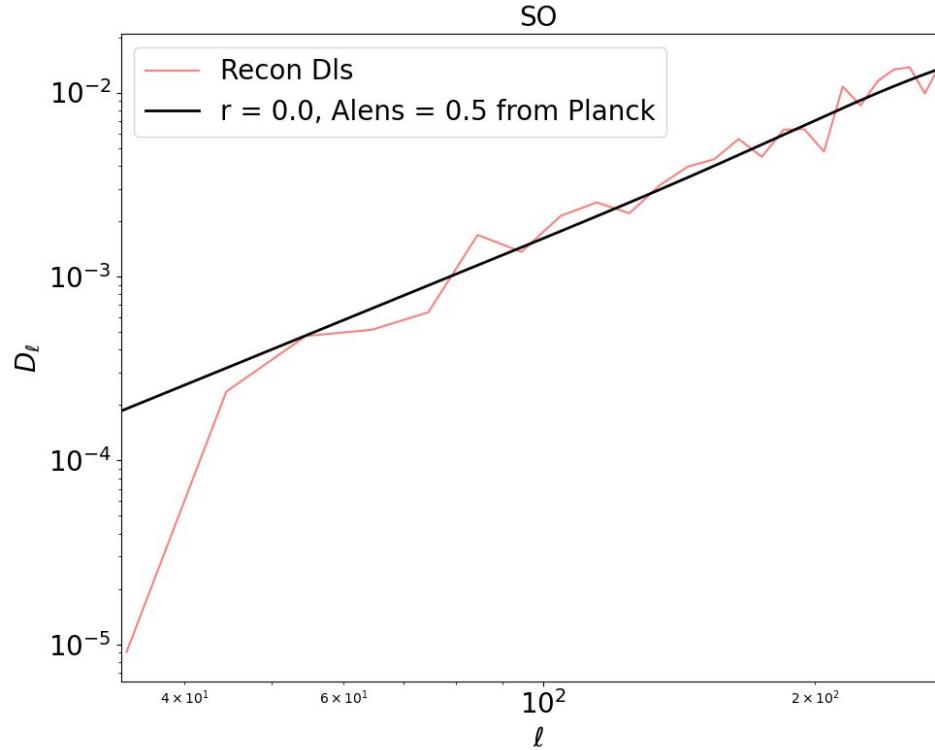
Test single realization using:

- pol wh noise
- binary coverage from hit map at nside=1024



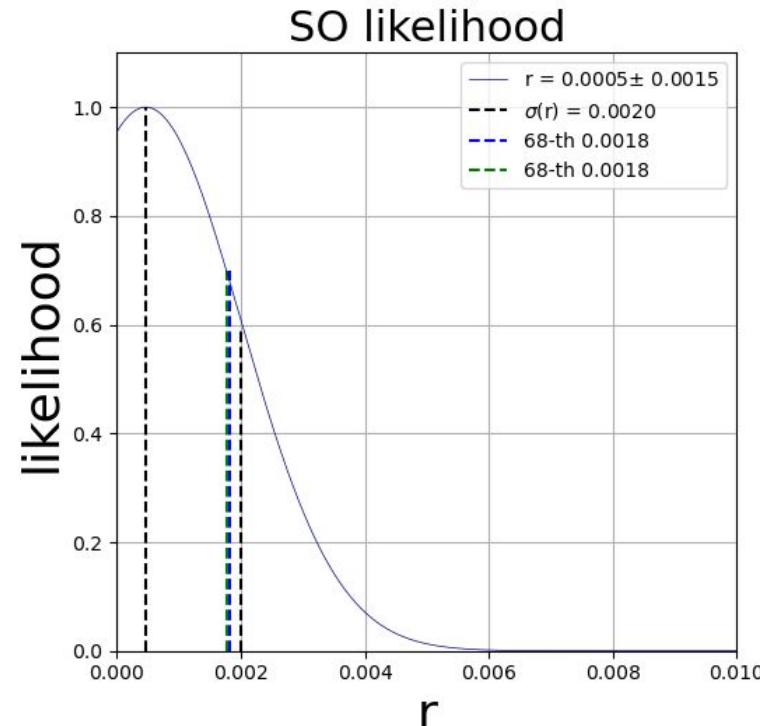
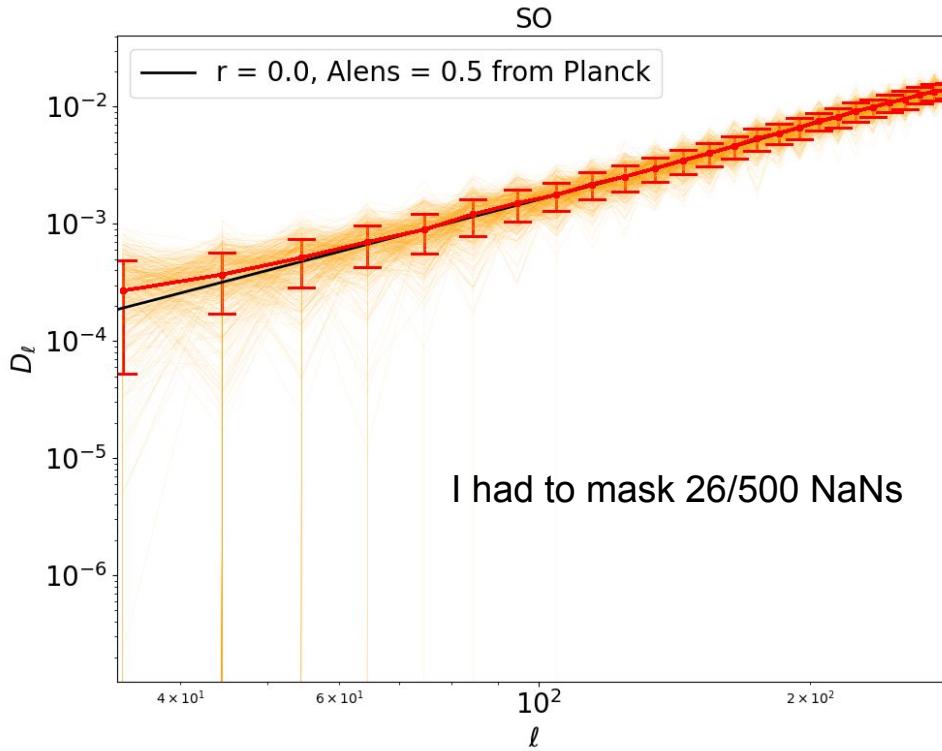
Test single realization using:

- pol wh noise
- binary coverage from hit map at nside=1024



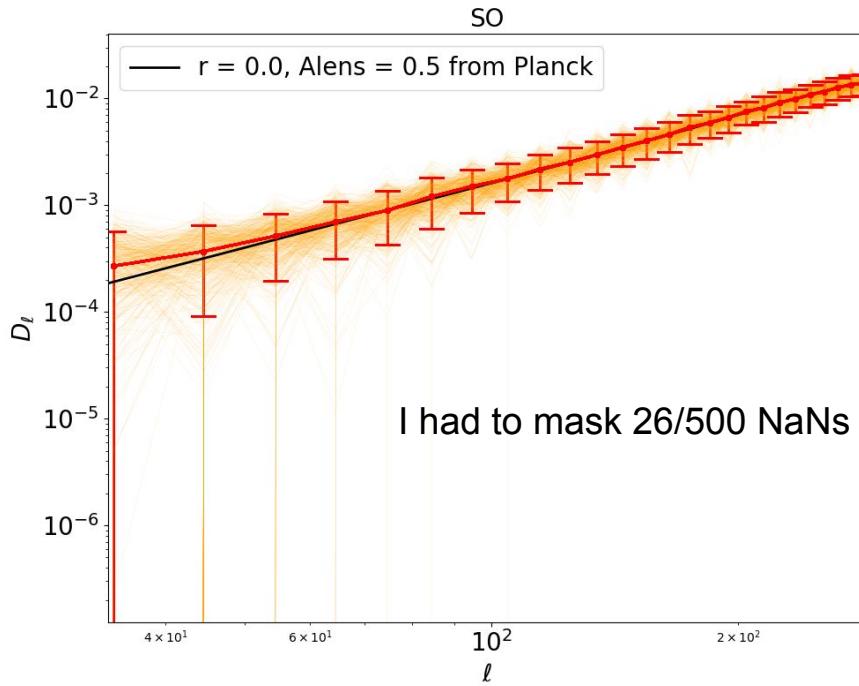
# Test full pipeline using:

- pol wh noise
- binary coverage from hit map at nside=1024



# Test full pipeline using:

- pol wh noise
- binary coverage from hit map at nside=1024
- add  $\sqrt{2}$  in the noise cov matrix N



This is the only way I could recover something close to Mathias'

