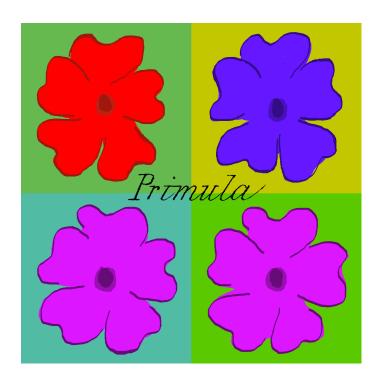
The *Primula* System: user's guide Version 3.0

Example: Generalized inference:
model-level explainer with MAP inference

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Introduction

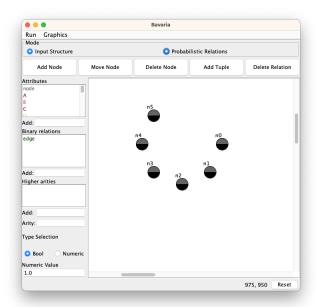
In the field of deep learning, explaining the behaviour of a trained model is becoming more and more required. As GNNs are increasingly used in many different fields, explaining techniques have received significant attention. In literature, there exist different approaches to explaining a GNN model, and most of the work that has been done is focused on instance-level explanation, where the goal is to explain the specific prediction. Not many works have been done on the model-level explanation, where the goal is to explain the model itself. We can define a model-level explainer as a method for constructing the *most probable explanation* (MPE) graph for a given class.

In this example, we will show how to use *Primula* to compute the MPE graph for a given class, demonstrating how *Primula* can be used as an out-of-the-box GNN explainer. The *.rbn file is a Relational Bayesian Network that is computationally equivalent to a Graph Neural Network, in particular, the architecture used is an ACR-GNN. This RBN contains the weights of a trained ACR-GNN model on a synthetic dataset. This dataset is composed of random graphs, where each node can have 7 different types [A, B, C, D, E, F, G]. Positive graphs have inside two specific motifs: one with a node A connected to two nodes B (B - A - B), and the other is one node C connected to two nodes D (C - D - C). We trained an ACR-GNN to classify the two classes obtaining high accuracy (0.9904), and we exported the trained model into a computationally equivalent RBN. Edges in the dataset are not directed, and in the RBN definition direction does not have any importance or meaning for the final results. Using this GNN-RBN combination, we can see with *Primula* which is the most probable *n-node* graph and compute also the the probability that this graph has on the model.

Primula settings

Load the model file rbn_acr.rbn and one of the data files \star .rdef from the folder (there are 3 files, for the 4/6/8-node graph).

Select in the *Primula* console Modules:Bavaria to open the graphical data editor. In *Bavaria* press the toggle Probabilistic Relations to view the attributes of nodes, there will be two colors: grey for the "node" attribute, while the black for the constraints. You will see something like this:



About the constraints: With RBNs we can impose some constraint for the graph generation during the MAP inference, those constraints in this case are useful to assign a high probability to having assigned only one attribute of the 7 different types for each node. In this case, it will be very hard to have graphs with multiple or zero types assigned.

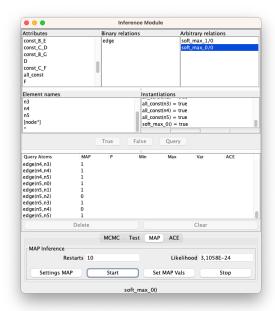
Setting Queries

Open the Modules:Inference Module and click the 'Query' button to activate the query mode.

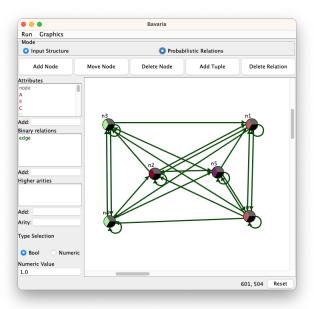
- Nodes: Select the blue attribute from the 'Attributes' list and click on the <code>[node*]</code> to select all the nodes. In the synthetic example, each node has 7 possible attributes [A, B, C, D, E, F, G]. In order to do this, click on one attribute (e.g. C) and click on the <code>[node*]</code> element in the Element names list. This assigns the selected Attributes to all nodes. Repeat this process for all 7 attributes (Note: the Query button can only be clicked on the first time).
- Edges: Assign all possible edge combinations to the nodes by selecting the edge attribute in the Binary relations list, and double-clicking again on the [node*] element (this required to be in the "query mode", click on the Query button to enter in this mode).
- Class: Set the class for which you want to compute the most probable graph.

 In the compiled RBN, all positive classes are assigned to the Arbitrary relation soft_max_0/0, negative to soft_max_1/0. Click the True button and then click on the soft_max_0/0 relation to assign it as the true value.

Computing MAP. Start the MAP computation by clicking the MAP button and then clicking the Settings MAP button. A new window will open, allowing you to set the number of restarts you want (-1 to stop manually or another value, e.g., 10). Click the Start button in the Inference Module and wait for the restarts to complete or manually stop the computation. When the computation finishes, press the 'Set MAP Vals' button to apply the computed values to the graph.



Visualizing the results. View the computed values from Bavaria. Save these results in a .rdef file by clicking on the *Primula* main interface's Save Data option under the Run menu. In Bavaria is it possible to see the color of the attributes to distinguish the different types of nodes. Otherwise, it is possible to see the computed values in the Inference Module. In the image below the two motifs for the positive class are being perfectly generated.



Extra: additional analysis

It is possible to compute the probability that this generated graph for the model directly on the *Primula* interface. The .rbn file represents the model and we can use the MCMC inference module to estimate the probability that the generated graph has on the GNN model with few decimals of error.

Open the saved .rdef file computed with the MAP inference with a text editor. This file is an XML-like file with all the attributes specified for the graph. In the ProbabilisticRelsCase> there are written all the assignments for the elements in the graph. Look for for the relation <d rel="soft_max_0" args="()" val="true"/> and delete that from the .rdef file. In this way, we do not assign the class to the graph and it will be possible to compute the true probability (otherwise it will be as 1.0 for the assignment).

Load the modified .rdef file computed with the MAP inference into *Primula* with the same .rbn of the computation before. Open the Inference Module and click on the MCMC button. Click on the Query button to query which class we want to select and click on the textttsoft_max_0/0 class in the Arbitrary relations (it is possible also to click on both the classes to have the probability of the other class). Click on the Start button and wait some seconds, the Sample Size will increase and in the Query Atoms, it will be possible to see the computed probability under the P column.

