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Unsupervised Machine Learning

Unsupervised Machine learning → unlabeled data

Goal: To discover patterns or relationships with the data, such as grouping similar instances together into clusters or finding low dimensional representations.

Example: Clustering, Dimensionality Reduction, Anomaly detection

Clustering:

- Making group of similar data points
- It is used to uncover the underlying structure of the data and is often used in fields such as pattern recognition, image analysis and market research.



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Application:

a) For customer segmentation:

→ You can cluster your customer based on their purchase.

↓
useful for recommender system

b) For data analysis:

→ Perform analysis on each cluster.

c) Anomaly Detection

→ Any instance which has a low affinity to all cluster is likely to be anomaly detection

d) Dimensionality Reduction

e) for search engine

f) To segment an image



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Approaches for Clustering

a) Agglomerative:-

First considers all points as individual clusters and then finds out the similarity betⁿ two points, puts them into a cluster.



Then, It goes on finding similar points & clusters until there is only one cluster left i.e 'all points belong to big cluster' → bottom up approach

b) Divisive

- It is opposite of Agglomerative approach
first consider all points as a cluster

↓ in subsequent steps

Find out the points/cluster which are least similar to each other.



bigger cluster
↓
into smaller one

Continue till

cluster as
many as
datapoints



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K-Means Clustering

• Unsupervised Clustering algorithm

• Proposed by Stuart Lloyd at 'Bell labs'

K mean is a clustering approach in which the data is grouped into K distinct non overlapping clusters based on their distances from the K -centres.

Theory:

1) let $C_1, C_2, C_3 \dots C_K$ be the K clusters

2) Then, we can write,

$$C_1 \cup C_2 \cup \dots \cup C_K = \text{each data points}$$

3) Also,

$$C_K \cap C_{K'} = \phi \text{ for all } K \neq K'$$

This means, clusters are non overlapping.

3) The idea behind the K-Means clustering approach is that within cluster



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variation among the point should be minimum. The with-in-cluster variance is denoted by $W(C_k)$. Hence, according to the statement above, we need to minimize this variance for all the clusters.

Mathematically,

$$\text{minimize } c_1, \dots, c_k \left\{ \sum_{k=1}^K W(C_k) \right\}$$

5> The next step is to define the criterion for measuring the within cluster variance.

Generally, the criterion is Euclidean Distances between the datapoints.

$$W(C_k) = \frac{1}{|C_k|} \sum_{i, i' \in C_k} \sum_{j=1}^P (x_{ij} - x_{i'j})^2$$

→ It calculates the mean of variance in each cluster.



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So, ultimately, our goal is to minimize :-

$$\text{minimize}_{c_1, \dots, c_K} \left\{ \sum_{K=1}^K \frac{1}{|C_K|} \sum_{i, i' \in C_K} \sum_{j=1}^P (x_{ij} - x_{i'j})^2 \right\}$$

Algorithm:

1. Randomly assign K centres.
2. Calculate the distance of all the points from all the K centres and allocates the points to cluster based on the shortest distance. The model's inertia is the mean squared distance betⁿ each instance & it's closest centroid. The goal is to have low inertia.
3. Once all points are assigned to cluster, recompute the centroids.



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4. Repeat the steps 2 and 3 until the location of centroids stop changing and the cluster allocation of the points become constant.

Elbow Method:

- An optimum value of K is obtained using the elbow method.
- This method is based on the relationship between the within cluster sum of squared (WCSS or Inertia) and the number of clusters.
- It is observed that first with an increase in the number of clusters WCSS decreases steeply and then after a certain number of clusters, the drop in WCSS is not that prominent.
- The point after which the graph beⁿ



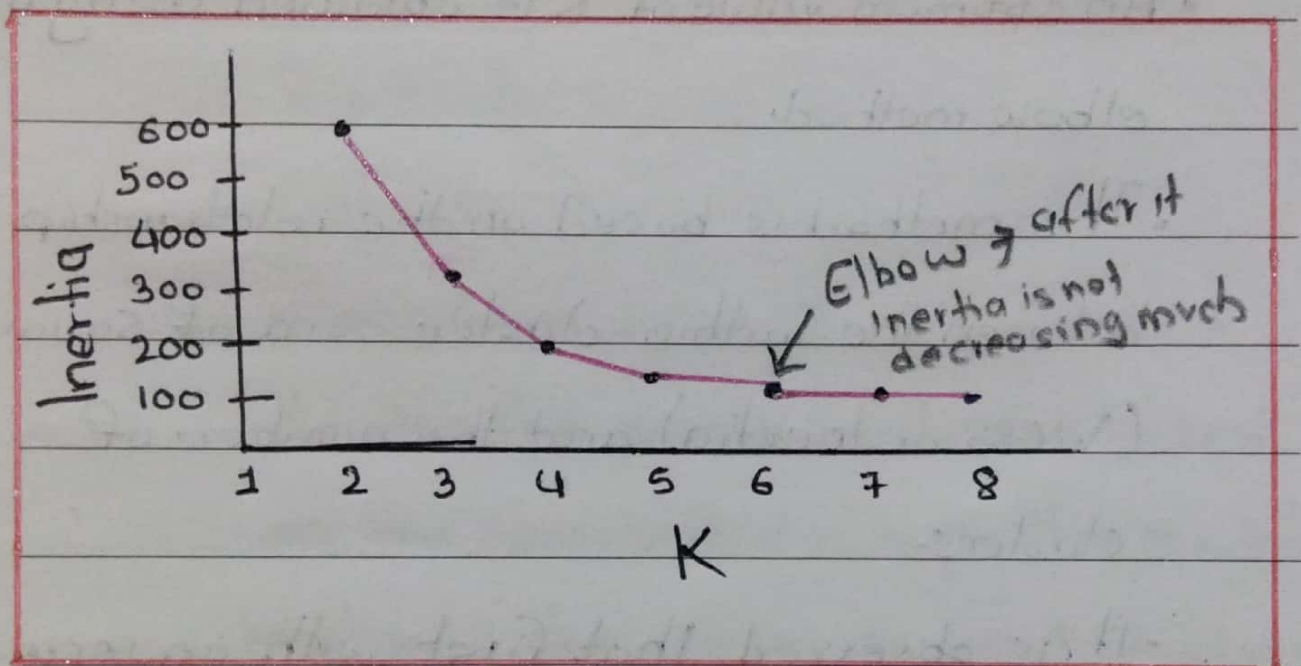
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WCSS and the number of clusters become comparatively become smoother is termed as the elbow.

- The number of cluster at the elbow point is optimum.



Challenges in K-Means:

- ① K-means do not behave well when cluster have varying shape, size, different densities or non spherical shape



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② Need to specify the number of cluster before hand.

Improvement:

K-Means ++

• Modified version of K-Means

Steps:

- 1> Choose the first centroid randomly
- 2> For each datapoint, calculate the distance from the selected centroid.
- 3> Assign the probability to each data point proportional to the square of its distance from the selected centroid.
- 4> Choose the next centroid randomly, with a probability that the selecting points are farther away from the existing centroid.
- 5> Repeat 2-4, until all K centroids have been selected.



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7) Assign data point to the closest centroid.

8) Recalculate the centroids as the mean of the data points in each cluster

9) Repeat 7-8 until centroid no longer move or maximum number of iteration is reached.

10) The final K-cluster, along with their centroids form the O/p.

Minibatch-Kmeans

Instead of using full dataset at each iteration, the algorithm is cable of using minibatches moving centroid just slightly at each iteration.

- This speedup the algorithm by 3-4 times

```
from sklearn.cluster import MiniBatchKMeans  
minibatch_kmeans = MiniBatchKMeans(n_clusters=5)  
minibatch_kmeans.fit(x)
```