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Memo No. _____

Date ____/____/____

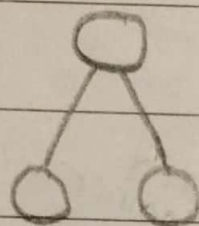
Boosting Algorithms:

→ We are adding sequential weak learner.

① Adaboost

Whenever we create a decision tree with just one depth.

This will lead to underfitting.



} Node with 2 leaves is called stump.

→ high bias [Training data \Rightarrow Accuracy \downarrow]
→ high/low variance [Test data \Rightarrow Accuracy \downarrow]

Aim bias to bias.
1) high variance \rightarrow Low variance
2) Low/high variance \rightarrow Low variance } we are using boosting for this.

Adaboost use stump.

Weak learner:

In Random Forest :- Majority Voting classifier [classification]
:- Average of O/p [Regression]



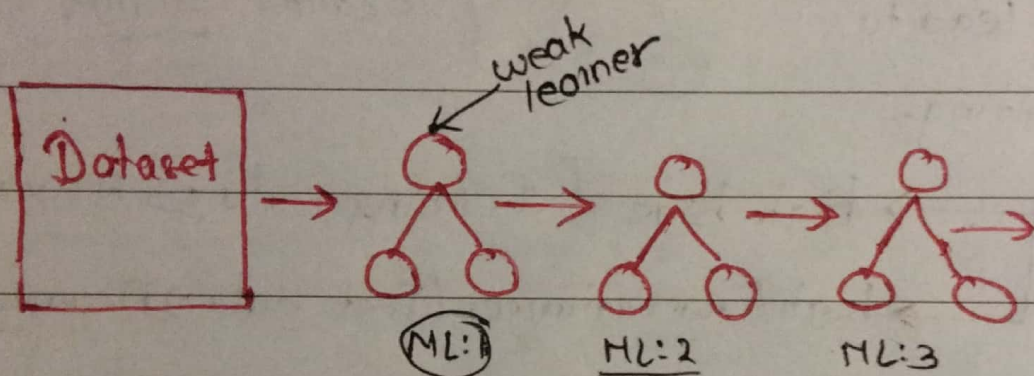
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Memo No. _____

Date / /

In Adaboost:

Dataset are passed to the stump which is weak learner. Since, one can't predict correctly, it push those incorrectly predicted dataset to another weak learner and it goes on.



Let us consider, we passed 100 datapoints to ML_1 . It predicted 80 datapoints correctly and 20 are wrongly predicted.

Now, these 20 points + other dataset are passed into ML_2 . Let's say 10 points predicted correctly, and rest wrongly predicted are passed into ML_3 and goes on.

$$\therefore f = d_1(H_1) + d_2(H_2) + d_3(H_3) + \dots + d_n(H_n)$$



Mo Tu We Th Fr Sa Su

Memo No. _____

Date / /

α is weight of model:

1) High value of $\alpha \Rightarrow$ depicts high responsibility of model

2) -ve value \Rightarrow depict model is not responsible

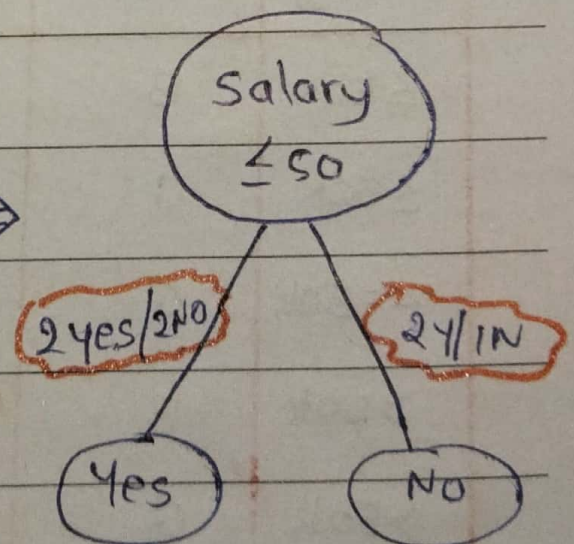
$H_1, H_2, \dots, H_n \rightarrow$ weak learners
 $\alpha_1, \alpha_2, \alpha_3, \dots, \alpha_n \rightarrow$ weight / score

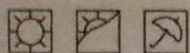
Example:

B - Bad
G - Good
N - Normal

Salary	Credit	Approval
$\leq 50K$	B	No
$\leq 50K$	G	Yes
$\leq 50K$	G	Yes
$> 50K$	B	No
$> 50K$	G	Yes
$\leq 50K$	N	No
$> 50K$	N	Yes

\Rightarrow

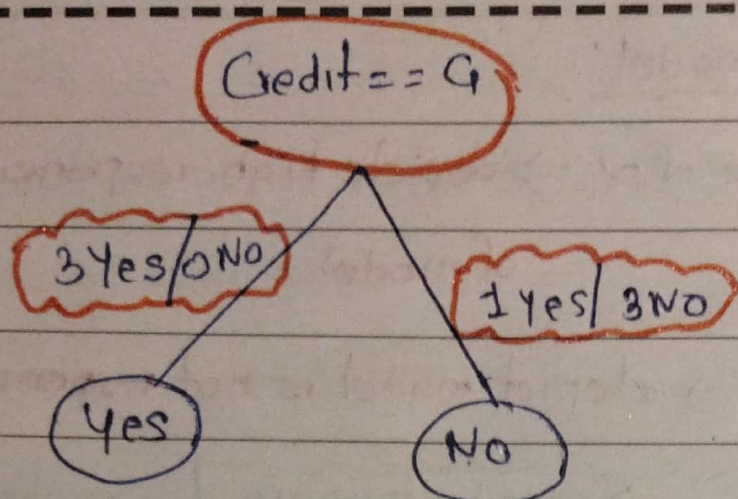




Memo No. _____

Date ____/____/____

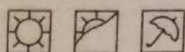
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Step 1: We create decision Tree Stamp by selecting the best one on the basis of **entropy** or **Gini**.

Step 2: Assigning weight

Salary	Credit	Approval	weight
$\leq 50k$	B	No	$\frac{1}{7}$
$\leq 50k$	G	yes	$\frac{1}{7}$
$\leq 80k$	G	yes	$\frac{1}{7}$
$> 50k$	B	No	$\frac{1}{7}$
$> 50k$	G	yes	$\frac{1}{7}$
$> 50k$	N	yes	$\frac{1}{7}$
$\leq 50k$	N	No	$\frac{1}{7}$

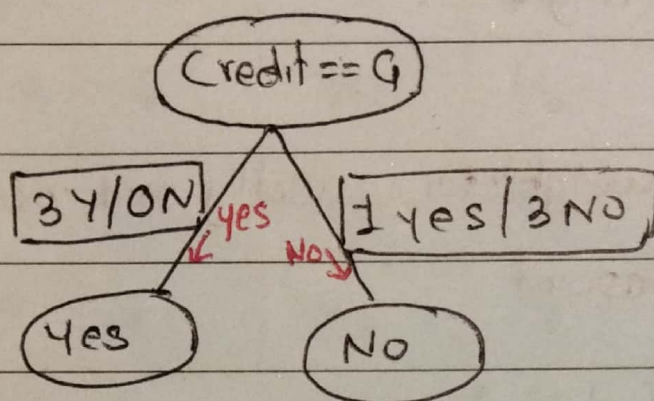


Mo	Tu	We	Th	Fr	Sa	Su
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Memo No. _____

Date / /

Here, split on the basis of credit == G was better since we had got a clean split on yes side.



Here, when we have credit == G, yes is final verdict. When we don't have credit == G, No is verdict, still we have 1 point which is wrongly predicted based on this. So, this weak learner model has error of $1/7$. $\therefore TE = 1/7$ (Addition of weight of wrong data point)

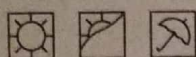
* We have to give the wrongly predicted data to another weak learner.

Step 3: Calculating performance of stump:

$$\text{performance score} = \frac{1}{2} \ln \left[\frac{1 - TE}{TE} \right]$$

$$= \frac{1}{2} \ln [6]$$

$$= 0.896 \rightarrow \text{Good performance}$$



Mo	Tu	We	Th	Fr	Sa	Su
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Memo No. _____

Date / /

$$f = \alpha_1(m_1) + \alpha_2(m_2) + \alpha_3(m_3) + \dots + \alpha_n(m_n)$$

$$\alpha_1 = 0.896$$

$$\therefore f = 0.896(m_1) + \dots$$

Step 4: Update the weight for correctly and incorrectly predicted datapoint

for correctly classified point:

$$= \text{weight} * e^{-\text{Performance}}$$

$$= \frac{1}{7} * e^{-(0.896)} = 0.058$$

for incorrectly classified point

$$= \text{weight} * e^{\text{Performance}}$$

$$= \frac{1}{7} * e^{0.896} = 0.349$$

Here, all the datapoints, which were correctly predicted, those weight has decreased and incorrectly predicted datapoint's weight has been increased.



Memo No. _____

Mo Tu We Th Fr Sa Su

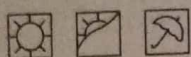
Date / /

Salary	Credit	Approval	Weight	Updated W.	
$< 50K$	B	No	$\frac{1}{7}$	0.058	
$< 50K$	G	Yes	$\frac{1}{7}$	0.058	
$< 50K$	G	Yes	$\frac{1}{7}$	0.058	
$> 50K$	B	No	$\frac{1}{7}$	0.058	
$> 50K$	G	Yes	$\frac{1}{7}$	0.058	
$> 50K$	N	Yes	$\frac{1}{7}$	0.349	wrongly predicted Hence weight increased
$< 50K$	N	No	$\frac{1}{7}$	0.058	

Step 5: Normalize weight and assign bins

- After this step, we have push wrongly predicted data-points to another model. Hence, it is very important step. We have make the total summation of the updated weight to 1. If we add the updated weight we will get 0.697.

$$\text{Normalized weight} = \frac{\text{updated weight}}{\text{sum of updated weight}}$$



Mo Tu We Th Fr Sa Su

$$\frac{0.058}{0.697} = 0.08$$

Memo No. _____

Date / /

Salary	Credit	Approval	Update weight	Normalize weight	Bin Assign.
$\leq 50K$	B	No	0.058	0.08	0-0.08
$\leq 50K$	G	Yes	0.058	0.08	0.08-0.16
$\leq 50K$	G	Yes	0.058	0.08	0.16-0.24
$> 50K$	B	No	0.058	0.08	0.24-0.32
$> 50K$	G	Yes	0.058	0.08	0.32-0.4
$> 50K$	N	Yes	0.349	0.50	0.4-0.90
$\leq 50K$	N	No	0.058	0.08	0.90-1
			0.697	$\sum 1$	

Since, the bin for the incorrectly predicted is high, so, the next model, the chances of data being selected from data that is wrongly predicted and it continue in a some steps in another model.

Final Prediction:

Suppose, we are using 4 decision tree for

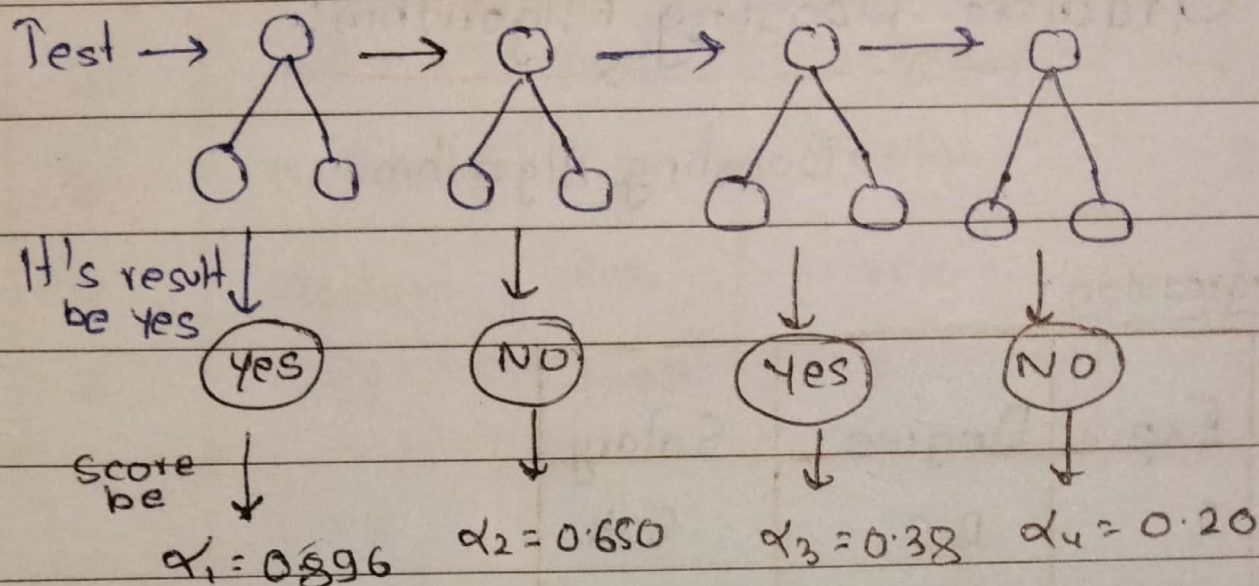


Mo	Tu	We	Th	Fr	Sa	Su
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Memo No. _____

Date / /

the same problem. So,



$$f = \alpha_1(M_1) + \alpha_2(M_2) + \alpha_3(M_3) + \alpha_4(H_4)$$

$$= 0.896(\text{yes}) + 0.650(\text{No}) + 0.38(\text{yes}) + 0.20(\text{No})$$

$$= \boxed{1.2(\text{Yes}) + 0.85(\text{No})}$$

Since, the weight of yes is more, so, the final classification is "Yes".