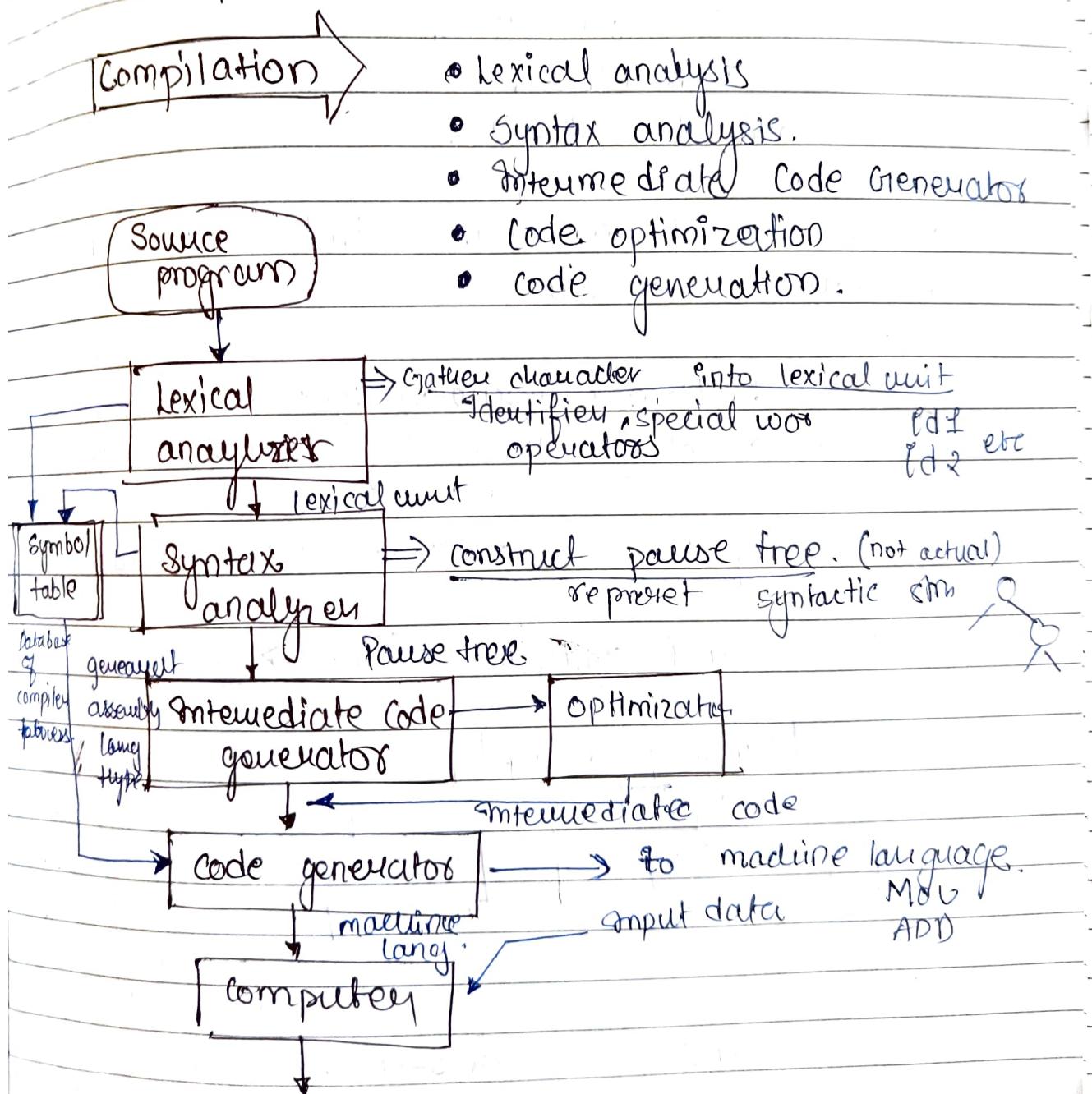


Implementation of programming lang

- compiler
- Pure Interpretation
- Hybrid Implementation System
- Preprocessors



Chapter - 3 : Describing Syntax and Semantics

- Define - Syntax and semantics
- Context-free grammars (Backus-Naur form)
- Parse Trees, Ambiguity, Operator precedence and Associativity, Extended Backus-Naur form
- Three formal method of describing semantics
 - operational, Axiomatic, Denotational

① Introduction:

Pbm: Diversity of the audience

- Initial Evaluators,
- Implementors,
- Production Users.

Syntax: form of expression, statnts & prog wth

Semantics: meaning.

② General problem of describing syntax:

Language \rightarrow set of strings of char from alpha

String of language \rightarrow Sentences / Statments

lowest level syntactic units \rightarrow , lexemes

language descript

Syntax Description

lexical specification

program

Strings of lexems

gives lexems
description

lexems - numeric literals

operators, spec

lexems

→ into groups

- name of var
 - methods
 - classes
- } → Identifier.

tokens

Identifier is token that have lexems or
instance eg sum
for var total

Token for + (plus-op) has only one
possible lexeme.

Ex. $\text{index} = 2 * \text{count} + 17;$ → semicolon,
 identifier int literal mult-op identifier plus-op
 equal-sign int literal

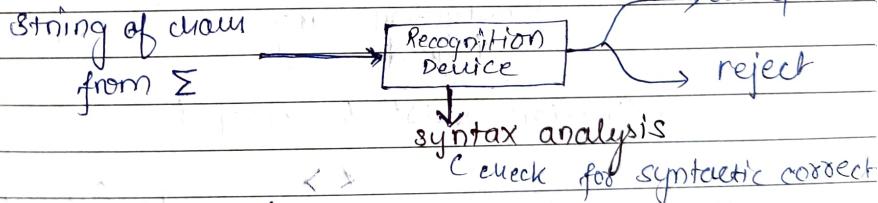
Black: lexems — e.g. index, =, *, count

Black: tokens — e.g. Identifier & equal-sign

(3) Language Recognizers

language → Recognition
language → Generation

Eg. lang L uses Σ of char.



(4) Language Generators

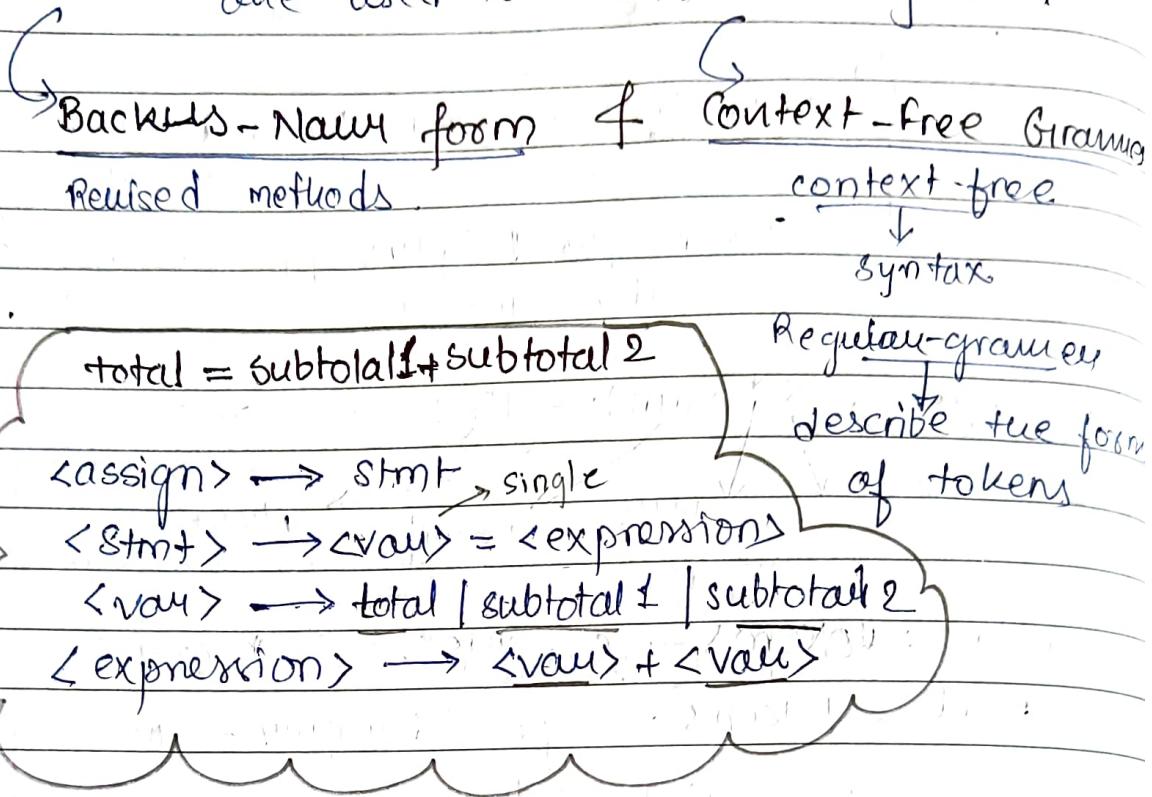
Device Generate sentences of lang [►] → sent

- Recognizer → Trial-and-error mode

- Generator → compare with structure of the generator

⑤ Formal methods of Describing Syntax

formal lang. generation mech \rightarrow Grammars,
are used to describe the syntax.



Fundamentals:

- metalang - used to describe another lang.
- BNF - use abstraction.
- java assignment statement
- rule / production } $\text{<assign>} \rightarrow \text{<val>} = \text{<expr>}$
- abstraction being defined. definition of RHS

definition must be useful.

can be expand

abstraction : non-terminal (ifstmt , expr)

lexemes and tokens of the rules : terminal

BNF or Grammars \rightarrow set of rules.

non-terminal \rightarrow can have more possible syntactic way.

$\text{<ifstmt>} \rightarrow \text{nn} | \text{nnn} | \text{nn}$

Describing Lists

Variable-length list using (1, 2, 3...)

BNF require alternate method

int a, b, c;

* uses recursion

a rule is recursive if LHS appears on RHS

<ident-list> → {identifier | identifier, id...}

Grammars and Derivations

Grammar — generative device of defining lang

sentence generation — derivation

<program> → begin <stmt-list> end

<stmt-list> → <stmt> | <stmt>; <stmt-list>

<stmt> → <var> = <expression>

<var> → A | B | C

<expression> → <var> + <var> | <var> * <var>
| <var>

<program> ⇒ begin <stmt-list> end

⇒ _____

⇒ begin A = B + C ; B = C end ←

<program> → start symbol

⇒, → derives

generated
sequence

leftmost derivation → leftmost non-terminal will

rightmost → Both left and right replaced
also exist

derivation → until no non-terminal left

Example:

A = B * (A + C)

<assign> → <id> = <exp>

<id> → A | B | C

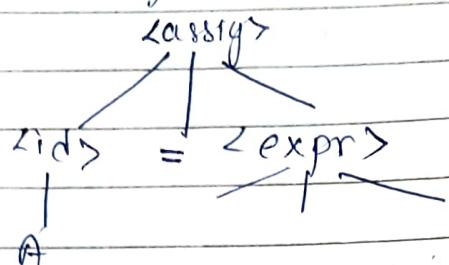
<exp> → <id> | , new line

<id> & <exp> | <id> * <exp> | <exp>

Pause Tree :

Describe hierarchical stru of sentences of the

every internal nodes — non-terminal
 every leaf nodes — terminal
 every sub-tree — one instance of an abstract



⑥ Ambiguity : Grammatic generate sentential form for which two or more distinct pause tree exists.

$\langle \text{Expr} \rangle \rightarrow \langle \text{Expr} \rangle \langle \text{Expr} \rangle \mid \langle \text{Expr} \rangle * \langle \text{Expr} \rangle$

⑦ Operator Precedence :

order of evaluation of operators

$x + y * z$

* More lower an operator in pause tree higher its precedence

Soln: add additional non-terminals and some new rules -

- $\langle \text{term} \rangle, \langle \text{factor} \rangle$

$A = B + C * D$

$\langle \text{assign} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$

$\langle \text{id} \rangle \rightarrow A \mid B \mid C$

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle$
 $\quad \quad \quad \mid \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle$
 $\langle \text{factor} \rangle \rightarrow \langle \text{expr} \rangle \mid \langle \text{id} \rangle$
 $\quad \quad \quad \mid \langle \text{factor} \rangle$

left most derivation

right most derivation

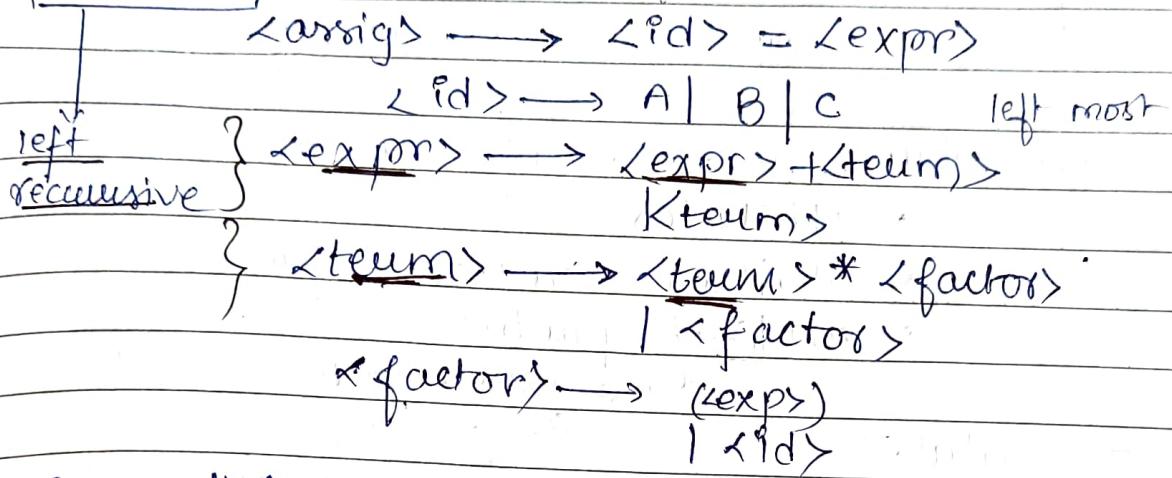
⑧ Associativity of operators

* two op with same precedence

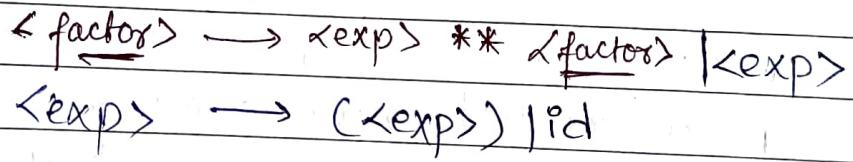
* generally associativity of addition in computer
is irrelevant

$$(A+B)+C = A+(B+C)$$

$$A \neq B+C+A,$$



** Exponentiation operator → right associative
— use right recursion



⑨ Extended BNF :

Increase readability & maintainability.
extension

- optional part of an RHS. | subscript opt
- indefinite repetition or leave it altogether
- Multiple-choice option. {, , } ↗ ↘
(* / / %) ↘ ↙
upper
(im)'

→ replace by :

new line

| : not needed

| replace by "one of "

yacc

⑩ Attribute Grammars:

* Extension of context-free grammar.

to describe type-compatibility

int a = "value";

useful for static semantics

some characteristic is difficult to des,

- Attribute grammar - context free grammar

- attributes

- Attribute computation function - how

- predicate function

↓ state static semantic

attribute
value

will

compute

- Attributes rule.

- Associated with grammar symbols

- Similar to variables

Features:

① associated with each grammar symbol

X is a set of attribute A(X)

E.val → F.val

Eval

↑
Fval

A(X) \rightarrow S(X) Syntactic attributes ↑
 \hookrightarrow I(X) Inherited attributes ↓ ↪

E.val = F.val

E.val

↓
Fval

② $x_0 \rightarrow x_1 x_n, S(x_0) = f(A(x_1), \dots, A(x_n))$

↓
semantic func

Same for I(x)

Chapter 4: Lexical and Syntax Analysis

Syntax analyzer - Application of grammars

Objective:

- Introduction to lexical analysis
- General parsing problem
- Recursive-descent implementation technique
→ top-down parsers
- Bottom-up parsing → LR parsing Algorithm

Introduction:

3 diff approaches to implement programming lang

- compilation : C++, C, C#
- pure interpretation : javascript
- Hybrid : Java, Perl

Most common syntax-description formalism
context free grammar / BNF

Syntax Analyzer Task : Lexical and syntax analysis

```

graph TD
    SA[Syntax Analyzer Task] --> Lex[Lexical]
    SA --> Synt[Syntax]
    Lex --> Small[small-scale  
(Name, literals)]
    Lex --> Large[large scale  
(Expression etc)]
  
```

lexical analyzers - pattern matching

- front end of syntax analyzer

collect char into lexemes & assign to tokens

<u>Token</u>	<u>Lexeme</u>
result = oldsum	result
IDENT	=
-value/100	oldsum
ASSIGN_OP	
IDENT.	

State transition Diagram

Directed Graph

node → state name

edges → labelled with input char. causes trans.

State diagrams used for lexical analyzer are representations of a class of mathematical machines called finite automata.

used to recognize members of a class of lang. called regular language

Lexical analyzer

finite automata

Tokens of a prog. lang.

Example: int a;

float b;

letter/digit

Name

Type

Tokens

Lexem

a

int

keyword

int

b

float

identifier

a

State

start

letter

id

Accept state

Digit

int

digit

addchar, getchar

return looksym (lexem)

return int-litvalue

token

construct symbol table

var-name	Type
a	float
b	int.

Parasing: Top-down, Bottom-up.

Terminal symbol → (a, b, c, ...) lowercase at start

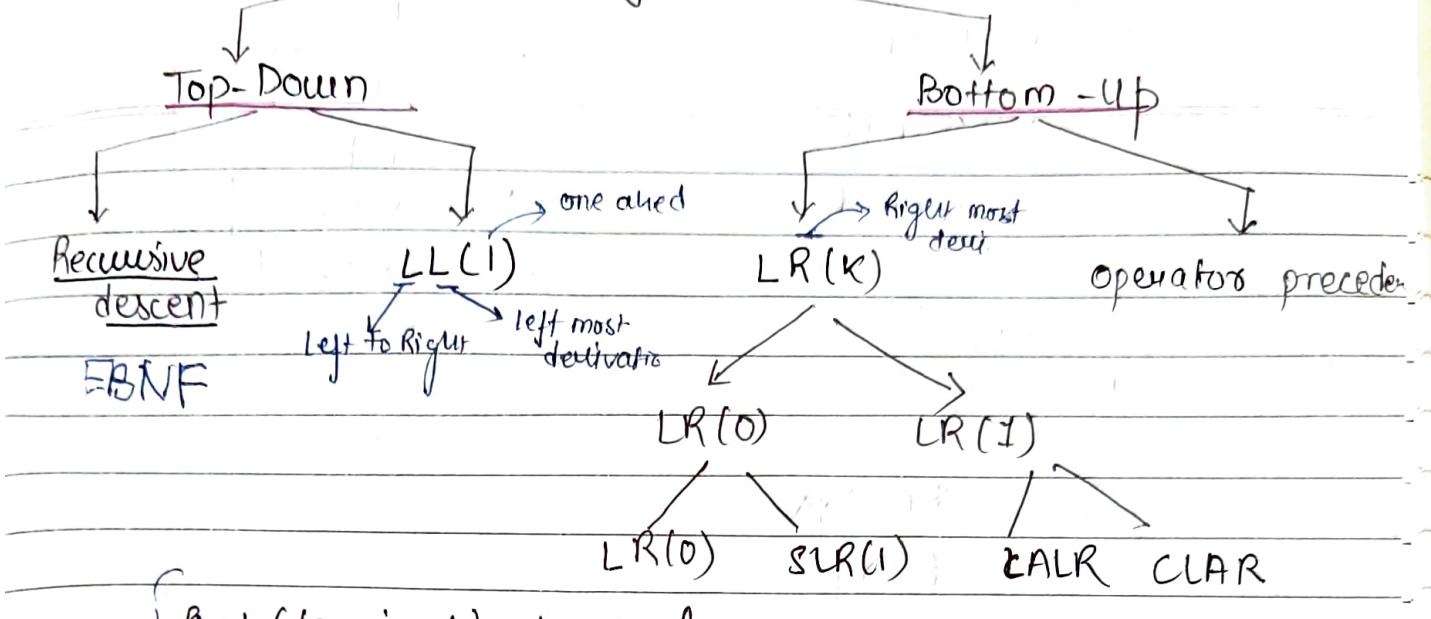
Non-terminal symbol → uppercase start (A, B, C, D, ...)

Terminal or non-terminal → uppercase end (W, X, Y, Z)

Strings of terminals → lowercase at end of alph (w)

Mixed strings → lowercase Greek letters.
(α, β, γ, δ)

Pausing



$\{ \text{first}(\text{terminal}) = \text{terminal}$

$\text{first}(\epsilon) = \epsilon$

left side

$\text{follow}(\text{start}) = \$ = \text{first}(A)$

right side

$\notin \rightarrow \text{will never come}$

$S \rightarrow \underline{\underline{ABC}}$

non terminal

① Recursive descent

EBNF, $\{ \} \rightarrow 0 \text{ or more times}$

$[] \rightarrow \text{once or not at all}$

$\langle \text{expr} \rangle \rightarrow \langle \text{term} \rangle \{ (+|-) \langle \text{term} \rangle \}$

$\langle \text{term} \rangle \rightarrow \langle \text{factor} \rangle \{ (*|/) \langle \text{factor} \rangle \}$

$\langle \text{factor} \rangle \rightarrow \text{id} | \text{int_constant} | \{ \langle \text{expr} \rangle \}$

② Lh Grammar class

$A \rightarrow A + B$ (left recursion).

Direct left recurs: \rightarrow non terminal

Rules $A \rightarrow A\alpha_1 \dots A\alpha_m | \beta_1 | \beta_2 \dots | \beta_n$

replace original A with

$A \rightarrow \beta_1 A' | \beta_2 A' \dots | \beta_n A'$

$A' \rightarrow \alpha_1 A' | \alpha_2 A' \dots | \alpha_m A' | \epsilon$

Erasure rule

example

$$\begin{array}{ll}
 E \rightarrow E + T | T & \Rightarrow \quad E \rightarrow TE' \\
 T \rightarrow T * F | F & \qquad\qquad E' \rightarrow +TE' | \epsilon \\
 F \rightarrow (E) | id & \qquad\qquad T \rightarrow FT' \\
 & \qquad\qquad T' \rightarrow *FT' | \epsilon \\
 & \qquad\qquad F \rightarrow (E) | id
 \end{array}$$

here $\left\{ \begin{array}{l} T \Rightarrow \beta \\ +T \Rightarrow \alpha \end{array} \right\}$
for E

for $T \rightarrow *F \Rightarrow \alpha$

$F \Rightarrow \beta$.

Indirect left recursion

$$A \rightarrow BA$$

$$B \rightarrow Ab$$

Problem for Top-bottom algo.

$$\text{FIRST}(\alpha) = \{ \alpha \mid \alpha \Rightarrow *ap \}$$

also, if $(\alpha \Rightarrow *e, e \text{ is in FIRST}(\alpha))$

$*$ → mean 0

or more derivation steps.

$$\text{eg. } A \rightarrow aB \mid bAb \mid Bb$$

$$B \rightarrow cB \mid d$$

$$\text{FIRST}(A) = \{ a^2b \}, \{ c, d \}.$$

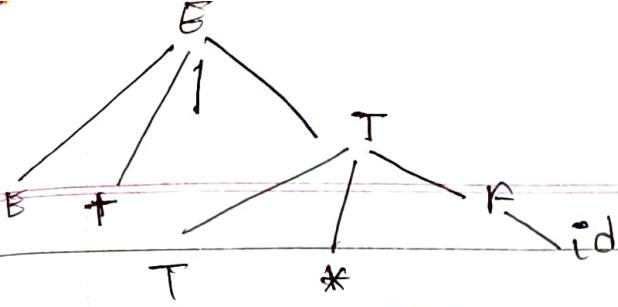
Bottom-Up Parsing

start expanding from right.

B is handle of right sentential form $r = \alpha_B u$
if only if $s \Rightarrow *_{rm} \alpha_A u \Rightarrow *_{rm} \alpha_B u$.

B is phrase if $s \Rightarrow *y = \alpha_1 A \alpha_2 \Rightarrow +x_1 B x_2$

B is simple phrase if $s \Rightarrow *y = \alpha_1 A \alpha_2 \Rightarrow x_1 B x_2$



- Phrase
- $E + T^* id$
 - $T^* id$
 - id
- simple phrase • id

Shift reduce pausing → Pause stack

$$\text{Grammar: } E \rightarrow E + E$$

$$E \rightarrow E * E$$

$$E \rightarrow (E)$$

$$E \rightarrow id$$

$$\text{String: } id * (id + id)$$

def out
RHS

stack

ip.string

Action

$id * (id + id) \$$ shift id

$* (id + id) \$$ $E \rightarrow id$

shift *

shift (

shift + id

$\$ id$

$\$ E$

$\$ E *$

$\$ E * ($

$* (id + id) \$$

$(id + id) \$$

$\$ id + id) \$$

action

→ shift: otherwise $x \notin \text{RHS}$ (ip to stack) $\$ E * (id + id) \$$ reduce

→ reduce: if $x \in \text{RHS}$ of grounder $\$ E * (E + E) \$$

→ accept of grounder $\$ E * (E + E) \$$

→ error (Stack to input) $\$ E * (E + E) \$$

↓
 $\$ E * (E + E) \$$

↓
 $\$ (E + E) \$$

↓
 $\$ (E) \$$

↓
 $\$ E * E$

↓
 $\$ E$

LR pausing

non recursive

LR(k)

shift reduce bottom up pausing

left to Right → look ahead symbols

Right most derivation

in reverse.

$S_0 | X_1 | S_1$

Action & goto

s : State symbol

$X \rightarrow$ Grammar symbol.

$((S_0 X_1 S_1 X_2 S_2, -), a_i a_{i+1} \dots a_n \$)$

Grammar: $S' \rightarrow S$.

$S \rightarrow AA - \textcircled{1} \gamma_1$

$A \rightarrow aA - \textcircled{2} \gamma_2$

$A \rightarrow b - \textcircled{3} \gamma_3$

Parsing the i/p string using tabel.

Steps	parsing stack	i/p	Action
1.	$\$ \underline{0}$	<u>aabb\$</u>	shift α_3
2.	$\$ 0 \underline{\alpha_3}$	<u>abb\$</u>	shift α_2
3.	$\$ 0 \alpha_3 \underline{\alpha_2}$	<u>bb\$</u>	shift by
4.	$\$ 0 \alpha_3 \alpha_2 \underline{b}$	<u>b\$</u>	reduce ($A \rightarrow b$)
5.	$\$ 0 \alpha_3 \underline{\alpha_2 A}$	<u>b\$</u>	reduce γ_2 ($A \rightarrow \gamma_2$)
6.	$\$ 0 \alpha_3 A$	<u>b\$</u>	reduce γ_1
7.	$\$ 0 A$	<u>b\$</u>	reduce γ_1
8.	$\$ \alpha_1 b$	<u>\$</u>	reduce γ_3 non term

States	Action (terminals)				Goto (variables)	
	a	b	\$		A	S
0	$\underline{\$ 0}$ 0	$\underline{S_3}$	S_4		2	1
1	$\underline{\$ 1}$ 1	1		accept		
2	$\underline{\$ 2}$				5	
3	$\underline{\$ 3}$ 2.	$\underline{S_3}$	S_4		6	
4	$\underline{\$ 4}$ 3	S_3	S_4			
5	$\underline{\$ 5}$ 4	γ_3	γ_{13}	γ_3		
6	$\underline{\$ 6}$ 5	γ_1	γ_1	γ_1		
7	$\underline{\$ 7}$	γ_2	γ_2	γ_2		

Regular Expression

↳ method we use to represent language (L)

↳ regular language
accept (FA)

like

$$L = \{\epsilon, a, aa, aaa, \dots\} \\ \text{or } L = a^*$$

let 'R' → Regular expression over alphabet Σ if R.

$$\left. \begin{array}{ll} R = \epsilon & L(R) = \{\epsilon\} \\ R = \emptyset & L(R) = \{\} \\ R = a & L(R) = \{a\} \end{array} \right\} \text{ primitive}$$

$R_1 \cup R_2$ = Regular. (union)

$$a \cup b = \{a, b\}$$

$R_1 \cdot R_2$ = Regular (concatenation)

$(RE)^*$ = Regular (* → closure)

$$a^* = \text{Reg } \{\epsilon, a, aa, \dots\}$$

$RE \Rightarrow (RE) \rightarrow \text{regular}$

we recursively.

Regular Expression of finite lang

lang

$$\Sigma(a, b)$$

no string : $\{\} \Rightarrow \emptyset$, length 0 : $\{\epsilon\} \Rightarrow \epsilon, \lambda$, length ≥ 1 : $\{a, b\}$

lengths : $\{aa, ab, ba, bb\}$

$(a+b)$

↑ union

$$(aa + ab + ba + bb)$$

$$(a+b)(a+b)$$

length 3

at most 1

$$0, 1 \Rightarrow \{\epsilon, a, b\} \Rightarrow (a+b+\epsilon)$$

$$(a+b)(a+b)(a+b)$$