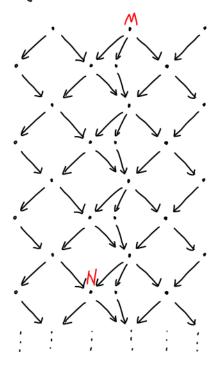
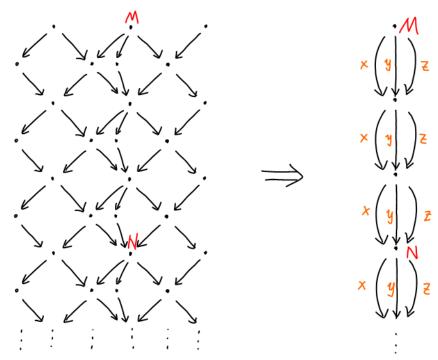
Eine Woche, ein Beispiel 6.11 more combinatorics in AR-quiver

- 1. dimension of Hom/path
- 2. database for sectional map
- 1. dimension of Hom/path
 Suppose that you have some arrows: (type E7)



- Q: 1. How many paths do we have from M to N?
 - 2. After identifying paths by AR-sequence, how many paths do we have from M to N?
- A: (partial) By induction process. Ex: find a basis for Hom(M,N).

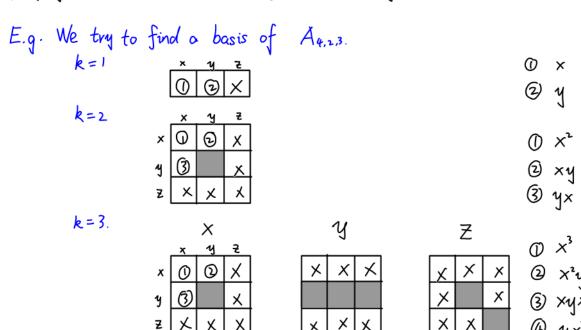
Special cases:

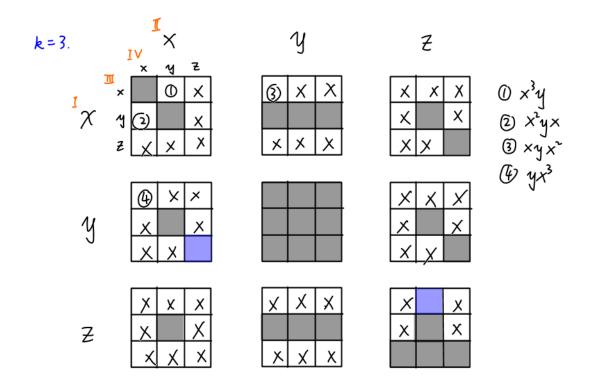


dim & Hom (M, N) = dim (C [x,y, Z]/(x4,y2, Z3, x+y+Z)) deg 4

"Cor" The Z-graded alg
$$A_{a,b,c}:=Cf\times,y,zf/(x^{a},y^{b},z^{c},x+y+z) \qquad a,b,c\in |N_{\geq 1}|$$
 is f.d. iff $\frac{1}{a}+\frac{1}{b}+\frac{1}{c}>1$.

We can find a (degree k) monomial basis of Aa,b,c by playing the "Tic-tac-toe" game on fx,y,z30k.

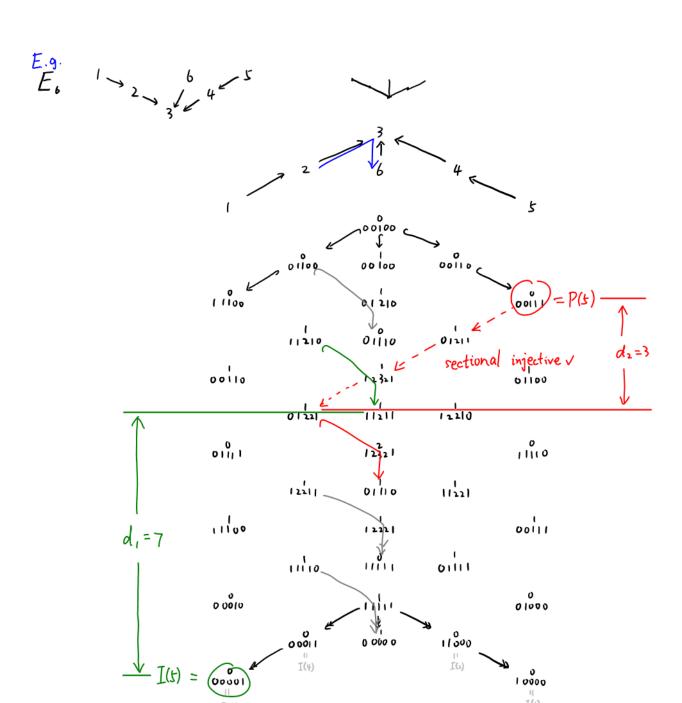




2. database for sectional map

We want to compute kernel & cokernel of some map, which turns out to be rather complicated (even though doable, and some techniques can speed up the computation).

We collect informations into tables, just like how people create character tables.



Consider the sectional map from 2 to 6.

index of kernel or cokernel; e.g.
$$P(s)$$

$$\begin{array}{c|cccc}
 & b \\
\hline
2 & X \\
\hline
Sec surj? \\
\hline
d_1 & 6 \\
\hline
2 & 7
\end{array}$$
Sec inj?
$$\begin{array}{c|cccc}
 & d_2 & 6 \\
\hline
2 & 7
\end{array}$$

E₆ case

	1	2	3	4	5	6
1	_	7	4	6	Ь	1
2	1	١	5	1	6	5
3	2	1	-	7	4	6
4	Ь	5	1	ı	ኔ	1
5	1	6	2	1	-	5
6	5	1	6	5	1	-

	1	2	3	4	ځ	6
1	-	~	✓	✓	>	✓
2	Χ	1	<	×	X	×
3	Χ	Х	1	×	×	Х
4	X	X	√	١	Х	Х
5	>	\	V	√	-	√
6	X	>	✓	✓	Χ	-

Sec surj ?

dı	1	2	3	4	5	6
1	~	1	1	2	4	3
2	10	1	2	ځ	7	7
3	9	9	-	9	9	10
4	7	5	2	1	10	7
5	4	2	1	1	-	3
6	6	3	1	3	6	_

 $d_1 + d_2 + length = 12$

	1	2	3	4	5	6
1	-	×	×	×	>	X
2	/	1	X	Х	>	/
3	\	✓	-	✓	✓	/
4	✓	×	Х	١	✓	✓
5	\	X	Х	×	1	X
6	/	X	Х	×	√	_

sec mono?

dz	1	2	3	4	کا	6
1	-	10	9	7	4	6
2	1	ı	9	ځ	2	3
3	1	2	-	2	1	1
4	2	7	9	1	1	3
5	4	7	9	10	1	6
6	3	7	10	7	3	-

Rnk. The information inside is well-regulated, while it is a mess outside is.

	1	2	3	4	5	6	7
1	J	1	2	3	7	1	6
2	1	١	1	2	6	6	1
3	2	1	1	1	1	7	6
4	3	٨	1	1	6	5	7
5	7	6	1	6	J	Ь	1
6	1	6	7	5	6	1	1
7	6	1	6	7	1	1	_

	1	2	3	4	5	6	7
1	_	>	>	✓	~	>	>
2	人	1	>		*	×	×
3	X	X	1	✓	×	×	×
4	X	X	X)	X	×	X
5	X	×	×	\	ı	Х	×
6	X	/	V	/	✓	1	/
7	X	×	/	✓	/	×	_

Sec surj?

d,	1	2	3	4	5	6	7
1	_	1	1	1	2	4	3
2	16	1	Ŋ	2	5	10	8
3	15	15	1	3	10	13	13
4	14	14	14	1	15	15	16
5	12	10	6	2	J	<i>[</i> 6	12
6	8	4	2	1	1	_	4
7	11	7	3	1	4	()	-

$$d_1+d_2+length=18$$

	1	2	3	4	5	6	7
1	_	×	X	X	X	X	×
2	✓	1	×	X	×	<	X
3	V	>	1	×	×	<	\checkmark
4	/	>	>	l	>	✓	✓
5	✓	X	×	×	l	✓	✓
6	/	×	Х	X	×	_	×
7	\checkmark	X	Х	Х	×	✓	_

sec inj?

dz	1	2	3	4	5	6	7
1	J	16	15	14	12	8	1
2	1	l	4	14	10	4	7
3	1	2	1	14	6	ک	3
4	1	2	3)	2	1	1
5	2	7	lo	15	1	1	4
6	5	lο	13	15	16	-	4
7		8					_

 E_8 case

	1	2	3	4	5	6	7	8
1	-	1	2	3	4	8	1	7
2	1	J	1	2	3	7	1	1
3	2	1	-	1	2	1	7	1
4	3	2	1	-	1	1	8	7
5	4	3	2	1	1	7	6	8
6	8	7	1	1	7	I	7	1
7	1	1	7	8	6	7	-	1
8	7	1	1	7	8	1	1	_

	1	2	3	4	5	6	7	8
1	-	>	✓	✓	/	✓	>	✓
2	X	J	>	>	>	X	X	X
3	X	χ	1	\	>	Х	X	X
4	×	X	X	1	\	Х	×	×
5	Χ	×	Х	Х)	X	Х	×
6	X	X	×	X	\checkmark	I	X	X
7	X	×	/	\	✓	\	_	\checkmark
8	X	X	×	\	\checkmark	✓	×	_

Sec Surj?

d,	1	2	3	4	5	6	7	8
1	-	1	1	1	1	2	6	3
2	28	J	2	2	2	5	/6	9
3	27	27	1	3	3	1/	22	19
4	26	26	26	1	4	21	25	ىكد
5	٤ţ	삸		25	l	27	27	28
6	23	21	16	7	2	I	28	23
7	18	9	4	2	1	1	_	5
8	22	17	8	3	1	5	22	_

	1	2	3	4	5	6	7	8
1	-	Х	X	X	Х	人	X	X
2	\checkmark	J	X	×	×	X	×	X
3	✓	>	1	X	Х	×	>	Χ
4		\						
5	$\sqrt{}$		J	/)	✓	✓	✓
		X						
		×						
8	/	×	×	Х	Χ	X	~	-

sec inj?

dr	1	2	3	4	5	6	7	8
1	-	28	27	26	25	23	18	22
2	1	J	27	26	25	21	9	17
3	1	2	1	26	25	16	4	8
4	1	2	3	1	25	7	2	3
5	1	2	3	4	l	2	1	1
6	2	5	11	2	27	1	1	5
7	6	16	22	ځ2	27	28	-	22
8	3					23		