Eine Woche, ein Beispiel
6.30 starting functions.

This is a follow-up of [2021.08.15], [2022.02.20] and [2021.05.07]. The combinatorics of starting functions is more intricate than I thought. Therefore, I collect these findings here, and wish somebody can give a rigorous proof for these phenomenons (e.p. the numbers of 1's).

1. folding & starting fcts

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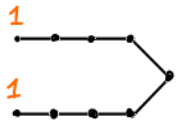
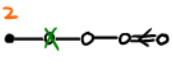
•: minuscule rep
×: quasi-minuscule rep
×: adjoint rep

E.g. C_5

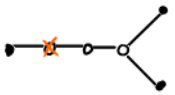


A_9

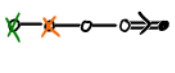
(unfold)



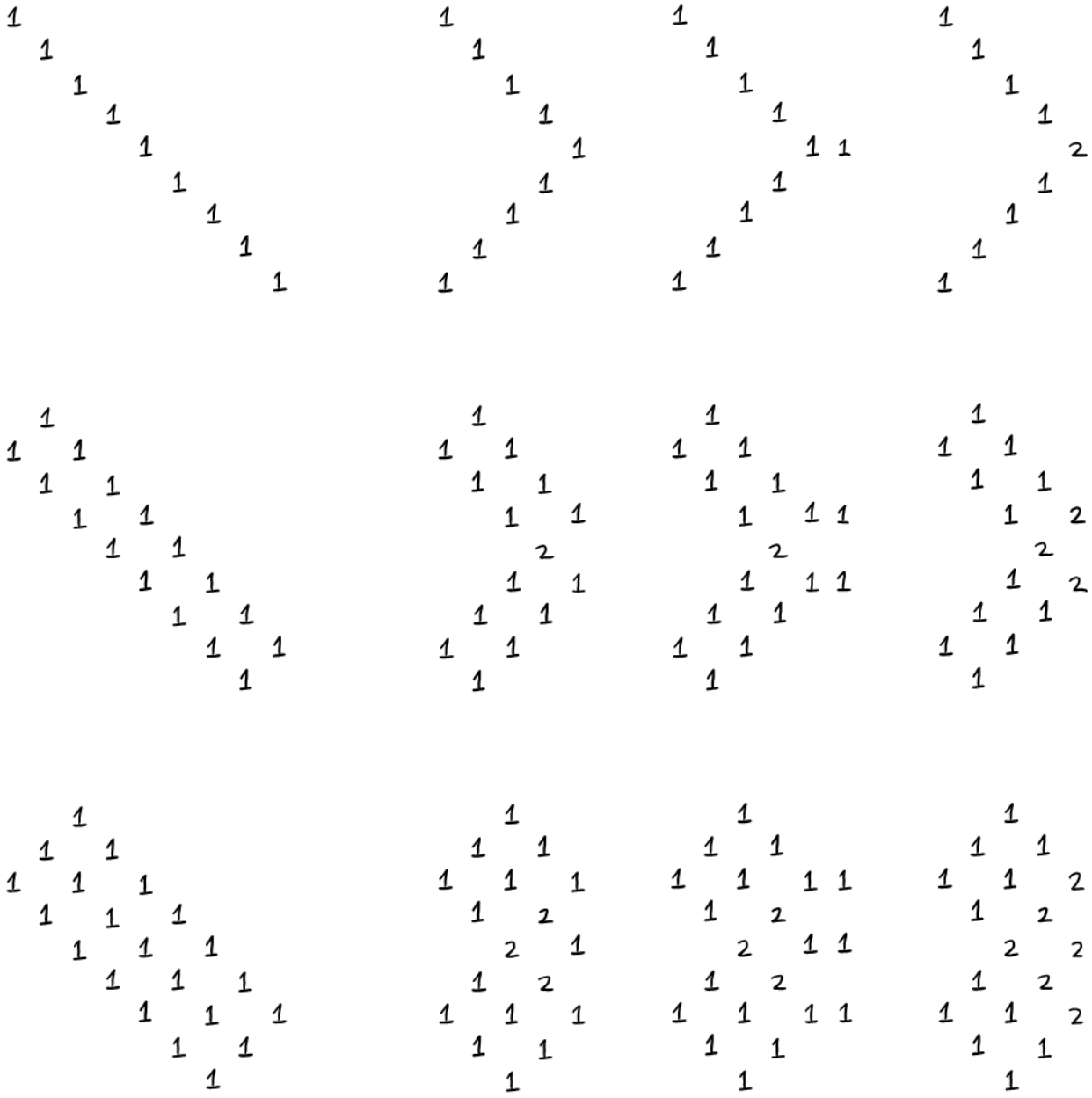
C_5

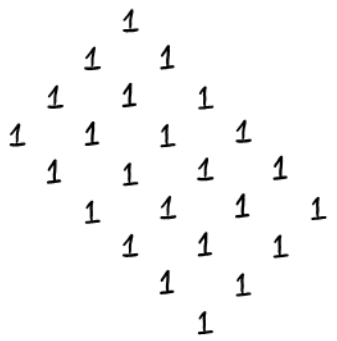


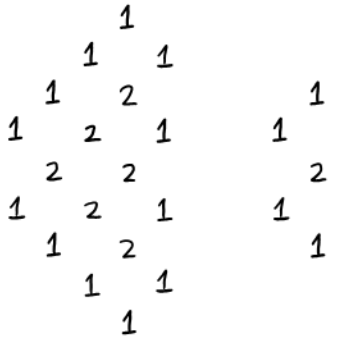
D_6

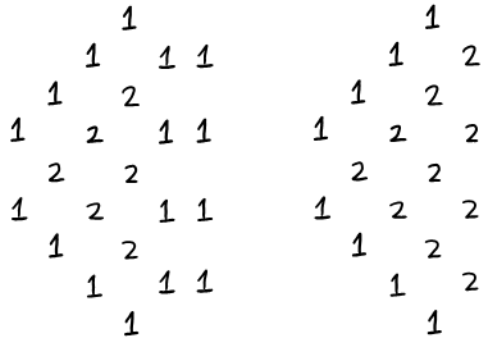


B_5

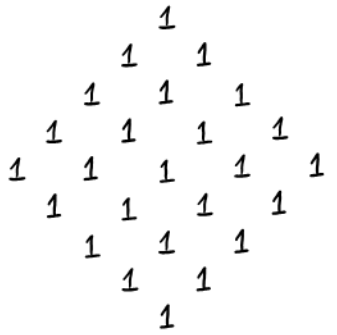


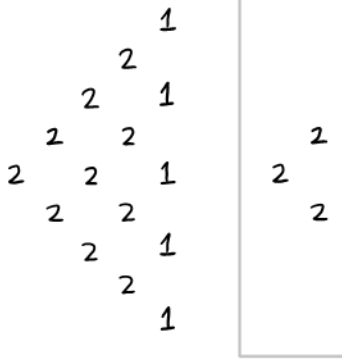


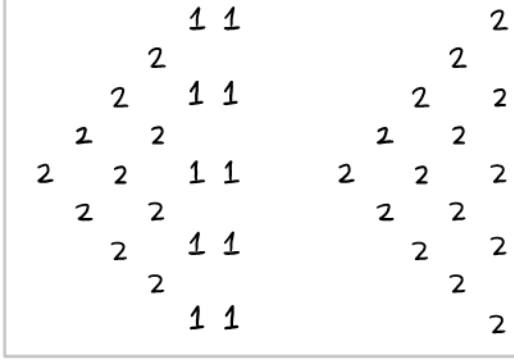




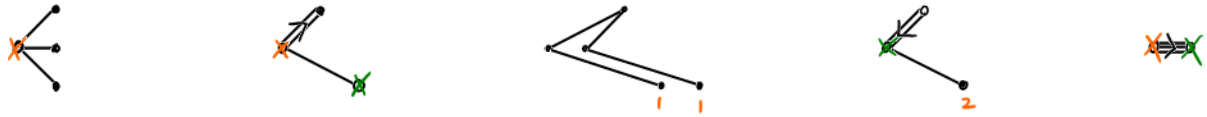
non-reduced





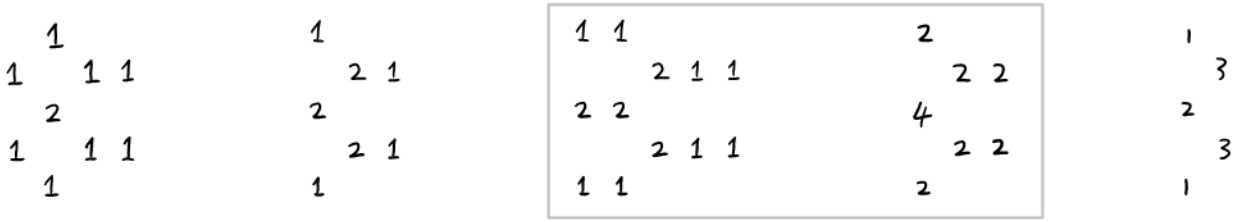


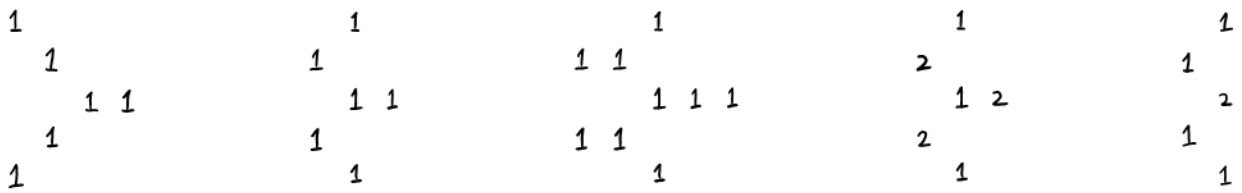
E.g. B_3



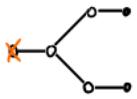
D_4 B_3 A_1 C_3 G_2

(unfold)



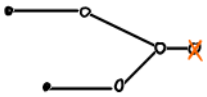


E.g. F_4



E_6

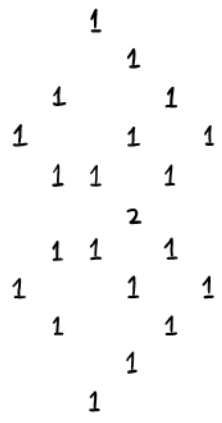
F_4

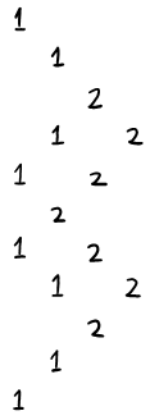


E_6

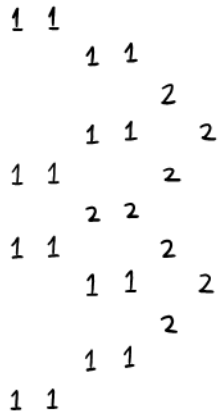
F_4

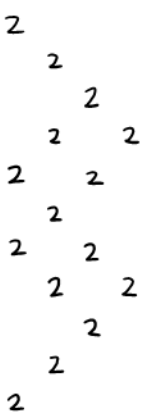
(unfold)

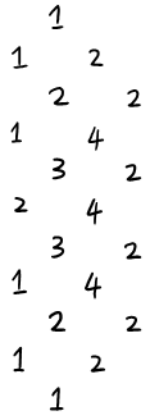


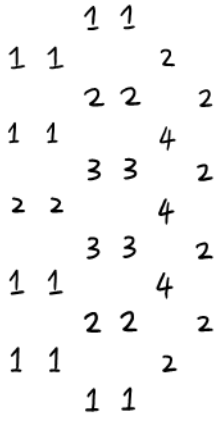


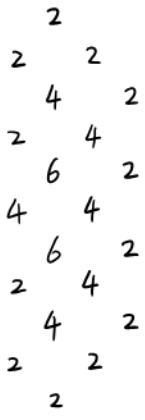
non-reduced

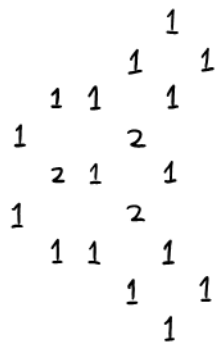


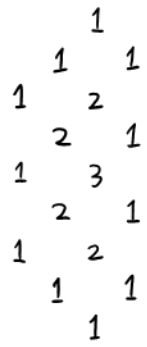


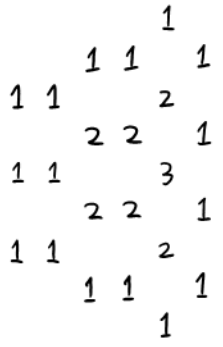


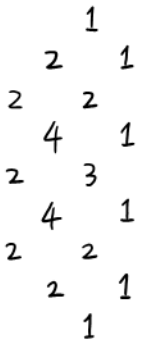


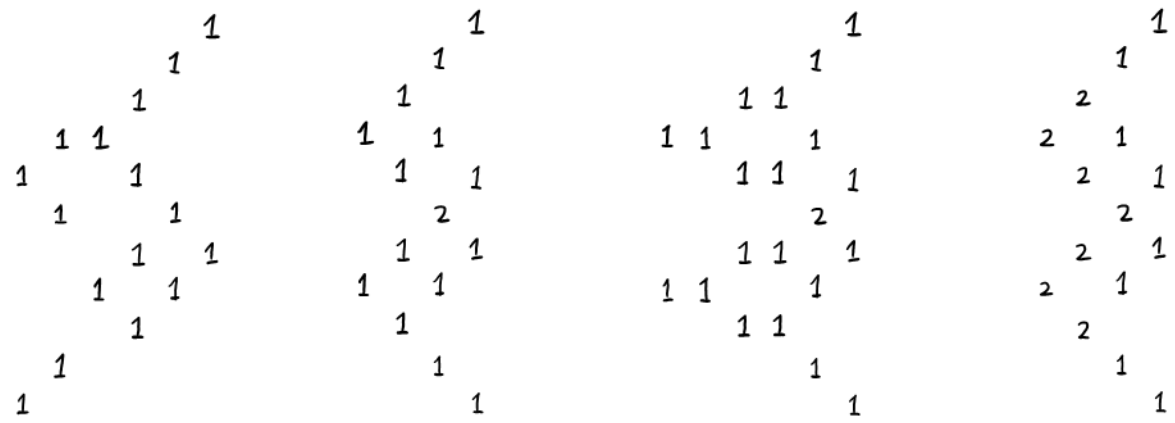












Rmk. Adjoint rep is compatible with normal folding. while
quasi-minuscule rep } are compatible with reversed folding
minuscule rep

E.p. simply-laced $\Leftrightarrow$ (quasi-minuscule = adjoint)

For minuscule rep, 

https://mathoverflow.net/questions/111469/dual-versions-of-folding-symmetric-ade-dynkin-diagrams