## Eine Woche, ein Beispiel 12.26 Average Resistance z(17)

Goal: compute parameters in https://arxiv.org/pdf/0901.3945.pdf [Cin] and think of their physical meaning (I need your help!)

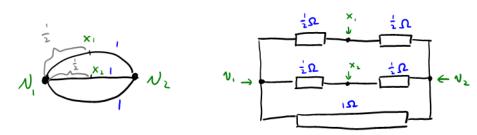
If possible, find a way to explain the Cinkir's bound [Cin, Thm 5.21].

We begin with an undirected weighted connected graph 17. (weight is always positive, and can be thought as the length; I have at lease 1 edge)

	1 v, e, v,	v ∕ e	N ( e, 1)
Vertices V= V(17)	{υ., υ≥}	FW]	ξυ, ν2}
Edges E=E(17)	se.z	<b>ે</b> ૧૧	fe., e., e, ]
total length (=((1°)	1	L	3
•			

You can think a graph  $\Gamma$  as some electrical wives with given length and constant resistivity  $1\Omega/m$ . Then we can compute the resistance between two points  $p,q\in\Gamma$ , and denote it by r(p,q).  $\Gamma$  can be points on edges

## E.g. In Fig 1, $r(v_1, v_2) = \frac{1}{3}\Omega$ , $r(x_1, x_2) = \frac{1}{2}\Omega$



Thm. There exists a unique real signal Borel measure  $\mu$ can on  $\Gamma$ , satisfying:

(i)  $\mu(\Gamma) = 1$ ,  $\mu$ 

is independent of the variant  $\times$ . We denote  $\tau = \tau(\Gamma) = \frac{1}{2} \int_{\Gamma} r(x,y) d\mu_{con}(y)$ , and call it the average resistance.

E.g.		1 N, E, N,	v € e	N, e, , , N,
	Mcan	= Ev. + = Ev2	<sup>1</sup> ℓ d×	-28v,-28v2 + 3 dx
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Ex. Verify the value of  $z(\Gamma)$  in the tables. (assuming that  $\mu$  can is already known). Q: Do we have any physical explanation for  $z(\Gamma)$ ?

Actually we can write down Mcan explicitly. For doing so we have to introduce some new concepts.