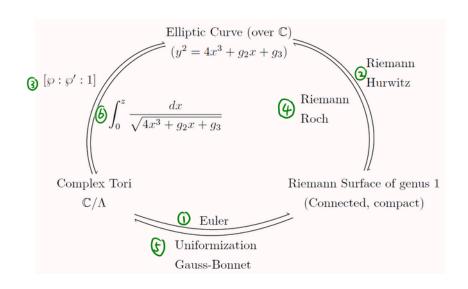
Modular form 1. origin of definition of modular form

- 1. EC
- 2 moduli space (from cplx points of view)
- 3. modular form

https://www.mathi.uni-heidelberg.de/~otmar/diplom/williams.pdf

1.EC



- Ex. 1. Discuss O. Discuss addition structure and their compatabilities.
 - 2. Some computations of 8,8'
 - 3. Describe rational fct field on EC.

2 moduli space (from cplx points of view)

Origin of H/SL2(Z)

Lemma. C/A = C/A' ⇔ A' = Zo A ∃ Zo ∈ C* Proof. [WWL, 命题 3.8·3, 练习 3.8·4]

Reduced to: Classify lattices (up to oplx scalar)

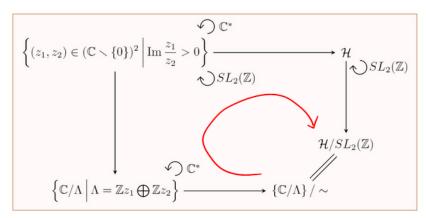


图 2.1 构造模空间/模形式的过程

Description of
$$H/SL_2(Z)$$

Ex. 1. Special items of $SL_2(Z)$ $T = (01)$ $S = (-10)$

2. (difficult) $\{X, SL_2(Z) = \langle T, S \rangle \in [Z_0, Prop 1] [JP, Prp, Th_m]_2\}$

= $\langle T, S | S^2, (ST)^3 \rangle$

3. Describe glue, elliptic pts and cusp pt, volume

the corresponding lattices

i: $E_{Z(i)}: y^2 = x^3 + x$ $\phi(x,y) = (-x,iy)$
 $f: E_{Z(p)}: y^2 = 4x^3 - 1$ $\phi(x,y) = (px,-y)$

https://math.stackexchange.com/questions/2051526/eisenstein-series-for-hexagonal-lattice/rq=1

http://www.fen.bilkent.edu.tr/~franz/publ/wald.pdf

https://math.stackexchange.com/questions/4043509/how-can-1-calculate-the-eisenstein-series-of-a-complex-lattice

https://mathematica.stackexchange.com/questions/89430/eisenstein-series-in-mathematica

1.1.2. (a) Show that $\operatorname{Im}(\gamma(\tau)) = \operatorname{Im}(\tau)/|c\tau + d|^2$ for all $\gamma = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \in \operatorname{SL}_2(\mathbf{Z})$. (b) Show that $(\gamma\gamma')(\tau) = \gamma(\gamma'(\tau))$ for all $\gamma, \gamma' \in \operatorname{SL}_2(\mathbf{Z})$ and $\tau \in \mathcal{H}$.

(c) Show that $d\gamma(\tau)/d\tau = 1/(c\tau + d)^2$ for $\gamma = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \in SL_2(\mathbf{Z})$.

Ex. 1 View modular form as fcts on the space of lattices 2. Eisenstein fct. Space $G_{k(\tau)} := \sum_{G_{k(\tau)}} \frac{1}{e^{k}} = \frac{1}{2} \sum_{(mn) \in \mathbb{Z}} \frac{1}{(m\tau + n)^{k}}$ We use We use $G_k(\Delta) := \sum_{z_0 \in \Lambda} \frac{1}{z_0^k}$ instead

(In $[Z_{\alpha}]$ G_{β} $G_$

—— Next time

为方便起晃, 取 $E_k:=G_k/(2\zeta(k))$ 使得 Fourier 常数项化为 1. 可以证明, $M_*(SL_2(\mathbb{Z}))\cong \mathbb{C}[E_4,E_6]$, 且 E_4,E_6 代数无关.

3.
$$\triangle$$
 and j
4. $M_*(SL_*(Z)) = \mathbb{C}[E_*, E_6]$

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