Eine Woche, ein Beispiel
7.17 formalism

Here I collect some formalisms which enhance well-known theories.
Somehow it also explains the polularity of the abstraction in mathematics. We want to have a better understand, so we invent new languages and theories, which in turn causes more troubles for beginners. Hug those formalisms!

Axiomatic set Theory ⇝ Grothendieck Universe
Both let us be away from paradoxes. The latter is more convenient.

Category Theory ⇝ Infinite Category Theory
[adjoint fctor ⇔ preserve (co)limits] is some cases

(·/Braided/Symmetric) Monoidal Categories ⇝ Categorification
Extract combinatorical informations from categories

Examples ⇝ Classification
Specify and generalization.

See https://github.com/ramified/personal_tex_collection/blob/main/%E8%9B%99%E9%B8%A39-7/latest%20version.pdf

Parameter space ⇝ Moduli space
Structures on parameter spaces are important.

See https://github.com/ramified/moduli_in_algebraic_geometry

Topology ⇝ Grothendieck Topology
Get étale topology.

Topological space ⇝ Condensed Set
Get abelian category.

Scheme ⇝ Functor
Get more objects. e.g. Ind-Sch, stack, ...

Snake lemma ⇝ homological algebra, spectral sequence
Diagram chasing all the time!

(co)homdogy ⇝ derived category, six-fctor formalism.
Reduce important properties to categorical non-sense.

Finite field ⇝ ???
Should contain "field with one element".

Moreover, AR theory tells us the structure of indecomposable reps,
Bruhat-Tits theory tells us the structure of p-adic groups.