Eine Woche, ein Beispiel 3.27 model theory

Ref: https://philippschlicht.github.io/teaching/files/Lecture.pdf I heard something from Yilong Zhang, and want to jot down some key points so that I won't be confused next time.

Modern Algebra (H)

Preliminaries

Logic. set & map, operations on Set.
 Axiomatic set theory (ZFC)
 (Cartesian product

- Russell's paradox

- type of proof : constructive, algorithm,...

Ex. graph

Classify topologies of [1, ..., n]

First adjunction: $Map(A \times B, C) \cong Map(A, Map(B, C))$

· From IN to C (the basic of examples, though logically it's not here)

- Peano axioms. Axiom of induction

- alg structure, order and typology

- Completeness axiom

· Cardinal the only property of set.

- naive definition

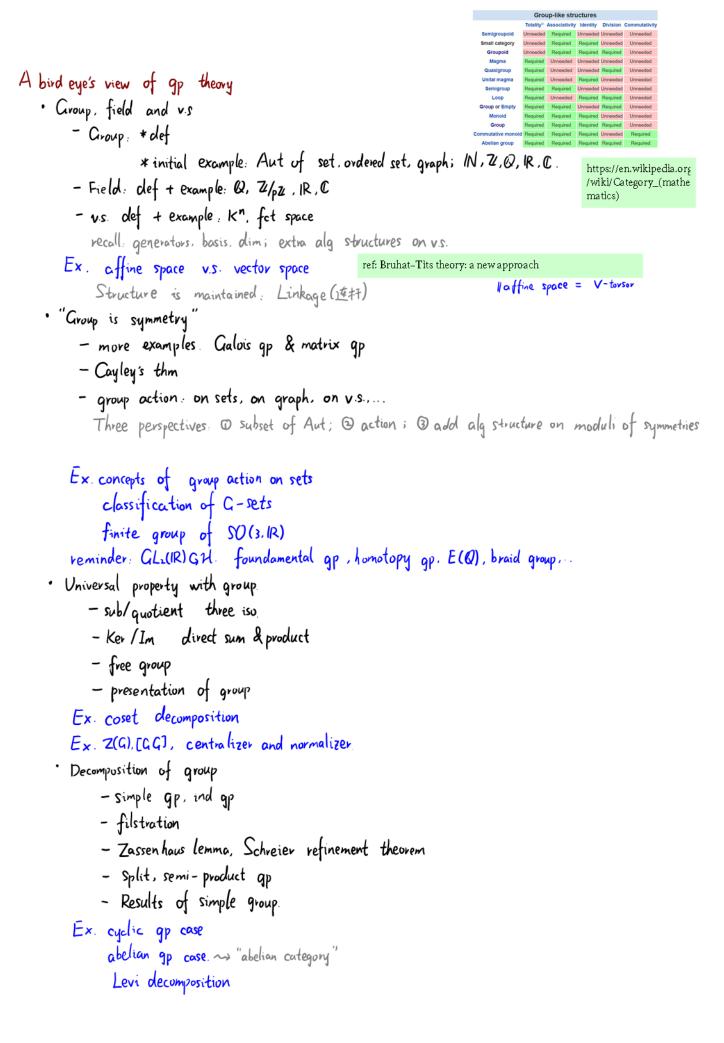
https://math.stackexchange.com/questions/1712964/attempt-at-proving-the-class-of-all-cardinals-is-a-proper-class

	alg	total order	topo
IN	(+,x)		discrete
7	(+,-,×)	✓	discrete
Q	(+, - , ×, ÷)	✓	discrete dense but not complete
IR	(+,-, ×,÷)	✓	complete
C	(+, -, ×,÷)	X	complete

- operations on cardinal
- examples
- The continuum hypothesis
- large cardinal axiom
- · Order structure
 - def, operations and properties (partial/total/well order)
 - ordinal, relationship with cardinal.

Ex. "well-order" on class of cardinals.

Classify subpartial ordered set of Psubsets of P1, , mil, up to iso. the Monoid R, surreals



Down-to-earth analysis.

- · f.g. abelian gp + apps.

 Ex. lattice & Crystallographic point gp

 Sublattice count
- Combinatorics related to q-polynomial
 ← can be quite tricky.
 Ex. finite field with one element
- · Gact on G
- · Sylow thm
- · app: classifications of gp of small order research on specific gp.

Ring & module

R(x) R((x)) R[{x}] R(cx)

· Basic def. e.g. R[x], R[x], R[x], R(x)

· Category , k-algs

Ex. groupoid

· Basic def of modules, abelian category E.x. R-algs.

tensor product, change of basis three rep theory

- · AG translation, examples.
- · Concepts under AG translation
- · ED > PID > UFD > domain
- · classification of f.g. module over PID.

Field and Calois theory (See [GT/M167])

Can focus more on IFp, Qp, IFp((t)), and geometrical point of view. (Reminder) other structures norm, metric & topo; measure; sheaf.

https://math.stackexchange.com/questions/765787/ring-of-convergent-power-series-in-r-and-c-is-a-local-ring