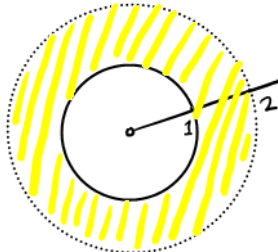


4.1. the complex torus of form $\mathbb{C}^x / \mathbb{Z}\gamma$

$$\gamma \in \text{Aut}(\mathbb{C}^*) \quad \gamma(z) = az \quad a \in \mathbb{C}^* \quad |a| > 1$$

1. fundamental set:



\Rightarrow only need 2 local chart

$$\mathbb{C}^* = \mathbb{C} / \mathbb{Z} \Rightarrow \mathbb{C}^* / \mathbb{Z}_Y = \mathbb{C} / (\mathbb{Z} \oplus \frac{1}{2\pi i} \ln 2 \mathbb{Z})$$

3. line bundle on \mathcal{C}

$$b \in \mathbb{C}^* \quad \mathcal{L}_b = \mathbb{C}^* \times \mathbb{C} / (z, \zeta) \sim (\zeta z, b\zeta) \quad \Rightarrow \quad \textcircled{1} \quad \mathcal{L}_b \in \text{Pic}_0(C); \quad (\mathcal{L}_b \sim \mathcal{L}_1 \cong \mathcal{O}_C) \quad \text{cont. deformation}$$

$$\downarrow$$

$$\mathcal{C} = \mathbb{C}^* / z \sim \zeta z$$

$$\textcircled{2} \quad \text{Pic}_0(C) \cong C = \mathbb{C}^* / \mathbb{Z}\gamma \quad \text{(naive, base pt } 1 \in \mathbb{C}^* / \mathbb{Z}\gamma)$$

$$\mathcal{L}_b \longmapsto b$$

Reduced to: find a section s on \mathcal{L}_b st $\text{div } s = [b] - [1]$

Reduced to: find a meromorphic functions g on \mathbb{C}^* s.t

① $g(2z) = bg(z)$ $b \in \mathbb{C}^*$, $b \neq 2^k$; e.g. $b=3$

② g has simple poles on 2^n , and simple zeros on $2^n b$ $n \in \mathbb{Z}$

$$g(z) = \frac{\theta [1'_{-2c}](w(z), \tau)}{\theta \begin{bmatrix} 1 \\ 1 \end{bmatrix} (w(z), \tau)}$$
 is the required one.

is the required one.

Blue — example

Orange — more than this example

Red — important results

Purple — I don't know the answer/proof

Green — sketch of proof: in a minimal way

Grey — some supplementary explanation. Unimportant assumptions.

Hell grey — explanation on well-known notations.

Brown — small title in subsections.

My symbol collection set

		Mathbb	Mathrsf/Mathcal	Greek	
A abelian variety	a	A adèles	A apartment		α
B	b	B	B building		β
C	c	C cplx number	C category	Γ gp graph	γ
D	d	D	D Poincare disk	Δ diag embedding	δ
E elliptic curve	e	E	E		ε
F field	f	F finite field	F sheaf		ζ
G group	g	G gp scheme	G Lie alg		η
H	h	H	H upper half plane	⊕ Hecke alg	θ
I ideal	i	I	I ideal of sheaf		ι injection
J	j	J	J		κ
K cos/base field	k ← k	K	K	Λ lattice	λ
L	l	L	L		μ
M module	m	M	M moduli space		ν
N	n	N natural number	N		ξ root of unity (ξ/ω)
O	o	O	O structure sheaf	Π multi	ζ constant
P	p	P proj space	P Weierstrass		π uniformizer
Q	q	Q rational number	Q	Σ sum	ρ ← ρ projection
R ring	r	R real number	R		σ
S base scheme	s	S	S	Φ	τ
T tangent space	t	T torus	T		φ
U ← U	u	U	-	Ψ	χ character
V v.s.	v	V	∇	Ω	ψ
W witt vector	w	W	-		ω ω ≈ ωω
X	x	X	X		
Y = Y	y	Y	Y	hebrew	Russian
Z center	z	Z integer	Z	N cardinal	Ш sha gp

Green: number / basic stuffs in senior high school

Orange: scheme - related

Darkyellow: advanced algebra

Don't use them simultaneously! (usually)

Don't mix: $w/\omega, \xi/\zeta, k/\kappa/\mathcal{K}/K$

$1/l/v, x/\chi/\mathcal{X}$,

$\varphi/\psi, e/c, \gamma/\nu$

$\omega\omega$ `\varpi\boldsymbol{\omega}` (need amsbsy package)

Japanese mathematicians and their Chinese translations.

	Matsumoto	松本	Hideya Matsumoto	松本英野		
1860	Sawayama	沢山	Yuzaburo Sawayama	沢山勇三郎		
1875.4			Teiji Takagi	高木贞治	高木	貞治
1901.4	Oka	岡	Kiyoshi Oka	岡 洁	岡	潔
1902.8	Akizuki	秋月	Yasuo Akizuki	秋月康夫	秋月	康夫
1908.12	Tannakian	淡中の	Taduo Tannaka	淡中忠郎		
1912.7	Nakayama	中山	Tadashi Nakayama	中山正		
1915.3	Kodaira	小平	Kunihiko Kodaira	小平邦彦		
1917.11	Iwasawa	岩泽	Kenkichi Iwasawa	岩泽健吉	岩泽	健吉
1924.1	Igusa	井草	Jun-Ichi Igusa	井草准一	井草	準一
1924.2	Tomita	富田	Minoru Tomita	富田稔	富田	稔
1925.11	Tamagawa	玉河	Tsuneo Tamagawa	玉河恒夫		
1926	Iwahori	岩堀	Nagayoshi Iwahori	岩堀长庆	岩堀	長慶
1927.11	Taniyama	谷山	Yutaka Taniyama	谷山丰	谷山	豊
1927.12	Satake	佐武	Ichirō Satake	佐武一郎		
1928			Hiroshi Toda	戸田宏	戸田	宏
1928.4	Sato	佐藤	Mikio Sato	佐藤千夫	佐藤	千夫
1930.2	Shimura	志村	Gorō Shimura	志村五郎		
1930.3	Yoneda	米田	Nobuo Yoneda	米田信夫		
1930	Matsumura	松村	Hideyuki Matsumura	松村英之		
1931.4	Hironaka	广中	Heisuke Hironaka	广中平祐	广中	平祐
1933.7	Takesaki	竹崎	Masamichi Takesaki	竹崎正道	竹崎	正道
1944.3			Toshitsune Miyake	三宅敏恒		
1947.1			Masaki Kashiwara	柏原正树	柏原	正樹
1951.2	Mori	森	Shigefumi Mori	森重文		
1952.1			Kazuya Kato	加藤和也		
1953.12.8	Mukai	向井	Shigeru Mukai	向井茂		
1959.3	Fukaya	深谷	Kenji Fukaya	深谷贤治		
1961.9	Saito	斎藤	Takeshi Saito	斎藤毅	斎藤	毅
1962.11	Nakajima	中岛	Hiraku Nakajima	中岛启	中岛	啓
1969.3			Shinichi Mochizuki	望月新一		

Confusion list:

1. Ring has unit. Don't consider 0-Ring.
2. Read the diagram from top to bottom.
3. countable = finite + inf countable (at most countable)
4. g fix set A : $\forall a \in A, ga = a$ (use "stabilized" instead)
5. \subset only mean a subset, or an injective map
(incompatible structures are allowed, e.g. $L^\infty([0,1]) \subset L'([0,1])$)
6. definition of norm/seminorms
7. $HK \neq H \times K$ $HK = \{g \in G \mid g = hk \text{ for some } h \in H, k \in K\}$