Eine Woche, ein Beispiel 3.27 model theory

Ref: https://philippschlicht.github.io/teaching/files/Lecture.pdf I heard something from Yilong Zhang, and want to jot down some key points so that I won't be confused next time.

Modern Algebra (H)

Preliminaries

Logic. set & map, operations on Set.
 Axiomatic set theory (ZFC)

(Automatic set theory (ZFC)
(Cartesian product)

- Russell's paradox

- type of proof : constructive, algorithm,...

Ex. graph

Classify topologies of [1, ..., n]

First adjunction: $Map(A \times B, C) \cong Map(A, Map(B, C))$

· From IN to C (the basic of examples, though logically it's not here)

- Peano axioms. Axiom of induction

- alg structure, order and typology

- Completeness axiom

· Cardinal the only property of set.

- naive definition

https://math.stackexchange.com/questions/1712964/attempt-at-proving-the-class-of-all-cardinals-is-a-proper-class

	alg	total order	topo
IN	(+,x)	V	discrete
7	(+,-,×)	✓	discrete
Q	(+, - , ×, ÷)	✓	dense but not complete
	(+,-, ×,÷)	✓	complete
C	(+, -, ×,÷)	 	complete

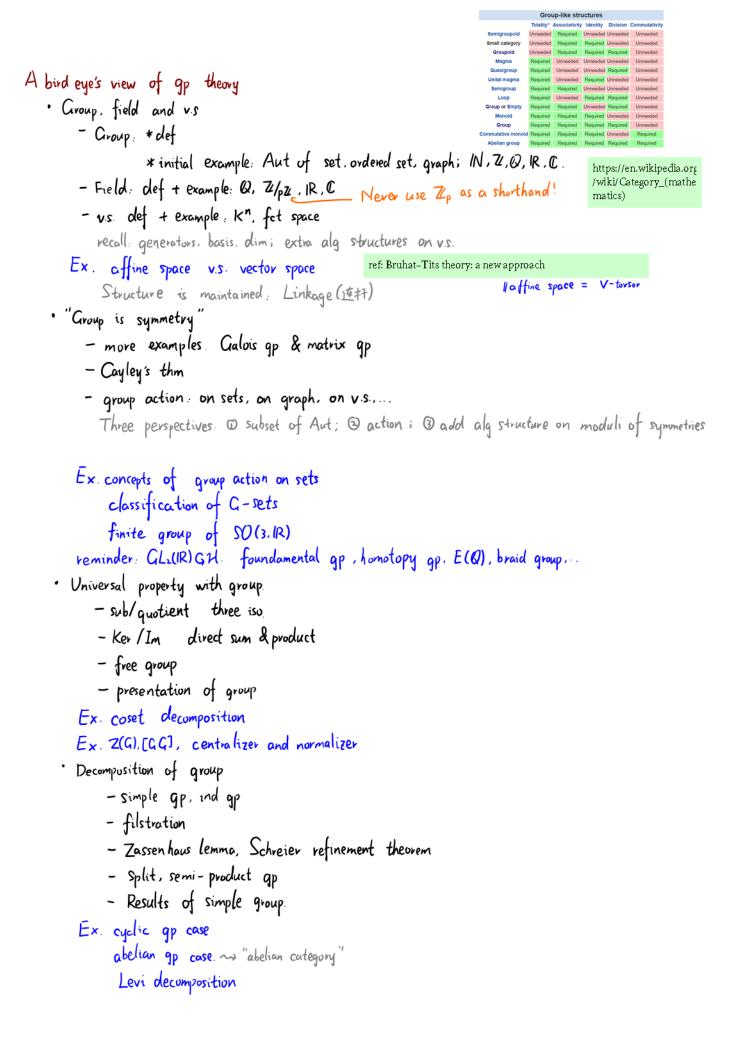
- operations on cardinal
- examples
- The continuum hypothesis
- large cardinal axiom
- · Order structure
 - def, operations and properties (partial/total/well order)
 - ordinal, relationship with cardinal.

Ex. "well-order" on class of cardinals.

Classify subpartial ordered set of Psubsets of P1, , ng 1, up to iso. ns the Monoid R, surreals

poset = partial order set

Coset = 陪集



Down-to-earth analysis.

· f.g. abelian gp + apps.

Ex. lattice & Crystallographic point gp sublattice count dual lattice $\Lambda^* = f f : \mathbb{R}^n \to \mathbb{R}$ linear $\{f, \times\} \in \mathbb{Z} \quad \forall \times \in \Lambda$ lattice in Euclidean space

- Combinatorics related to q-polynomial \leftarrow can be quite tricky. Ex. finite field with one element
- · Gact on G
- · Sylow thm
- · app: classifications of gp of small order. research on specific gp.

Never use the meaning in Model theory!

Ring & module

R(x) R((x)) R[[x]] R << x>

· Basic def. e.g. R[x] . R[[x]], R[x], R(x)

https://math.stackexchange.com/questions/765787/ring-of-convergent-power-series-in-r-and-c-is-a-local-ring

· Category , k-algs

Ex. groupoid

· Basic def of modules, abelian category

E.x. R-algs.

tensor product, change of basis three rep theory

- · AG translation, examples.
- · Concepts under AG translation
- · ED ⇒ PID ⇒ UFD ⇒ domain

Ex. Elementary divisor thm $R: PID. \qquad M_2(R) - \{0\} = \coprod_{a \mid b \in R} GL_2(R) \binom{a}{b} GL_2(R)$

· classification of f.g. module over PID.

Field and Calois theory (See [GT/M167])

Can focus more on IFp, Qp, IFp((t)), and geometrical point of view. (Reminder) other structures norm, metric & topo; measure; sheaf.