Eine Woche, ein Beispiel 3.27 model theory

Ref: https://philippschlicht.github.io/teaching/files/Lecture.pdf I heard something from Yilong Zhang, and want to jot down some key points so that I won't be confused next time.

Modern Algebra (H)

Preliminaries

Logic set & map, operations on Set.
 - Axiomatic set theory (ZFC)
 \(\text{OU-c}, \text{ sub/quotient}, \text{ two ways of disjoint union} \)
 Cartesian product

- Russell's paradox

- type of proof : constructive, algorithm,...

Ex. graph

· From IN to C (the basic of examples, though logically it's not here)

- Peano axioms. Axiom of induction

- alg structure, order and topology

- Completeness axiom

· Cardinal: the only property of set.

- naive definition

https://math.stackexchange.com/questions/1712964/attempt-at-proving-the-class-of-all-cardinals-is-a-proper-class

	alg	total order	topo
IN	(+,x)	✓	discrete
7	(+,-,×)	✓	discrete
Q	(+, - , ×, ÷)	✓	dense but not complete
	(+,-, ×,÷)	✓	complete
C	(+, -, ×,÷)	X	complete

- operations on cardinal
- examples
- The continuum hypothesis
- large cardinal axiom
- · Order structure
 - def, operations and properties (partial/total/well order)
 - ordinal, relationship with cardinal.

Ex. "well-order" on class of cardinals.

Classify subpartial set of Psubsets of P1, , my Lup to iso.

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A bird eye's view of gp theory
   · Group, field and vs
        - Group: * def
                  *initial example: Aut of set, ordered set, graph; IN, Z, Q, IR, C.
        - Field: def + example: Q, Z/pz, IR, C
        - v.s. def + example: Kn, fet space
          recall: generators, basis, dim; extra alg structures on v.s.

    "Group is symmetry"

         - more examples. Galois ap & matrix ap
         - Cayley's thm
        - group action. on sets, on graph, on v.s.,...
       Ex. concepts of group action on sets
            finite group of SO(3,1R)
       reminder: GLz(IR) GH. foundamental gp, homotopy gp. E(Q), braid group,...
    · Universal property with group
          - sub/quotient three iso
          - Ker/Im direct sum & product
          - free group
          - presentation of group
       Ex. coset decomposition
       Ex. Z(G), [GG], centralizer and normalizer
     * Decomposition of group
           - simple ap, ind ap
           - filstration
            - Zassenhaus lemma, Schreier refinement theorem
            - Split, semi-product ap
            - Results of simple group.
       Ex. cyclic ap case
             abelian gp case. ~ "abelian category"
             Levi decomposition
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Down-to-earth analysis.

- f.g. abelian gp + apps.
 Ex. lattice & Crystallographic point gp
- · Gact on G
- · Sylow thm
- · app: classifications of gp of small order research on specific gp.

Ring & module

- · Basic def. e.g. R[x], R[x], R[x], R(x)
- · Category , k-algs
- · Basic def of modules, abelian category

 E.x. R-algs.

 tensor product, change of basis

 three rep theory
- · AC translation, examples
- · Concepts under AG translation
- · ED > PID > UFD > domain
- · classification of f.g. module over PID.

https://math.stackexchange.com/questions/765787/ring-of-convergent-power-series-in-r-and-c-is-a-local-ring

Field and Galois theory (See [GT/M167])

Can focus more on IFp, Qp, IFp((t)), and geometrical point of view. (Reminder) other structures norm, metric & topo; measure; sheaf.