Eine Woche, ein Beispiel 5.14. Examples in ANT.

Goal . Calculate examples in ANT, containing.

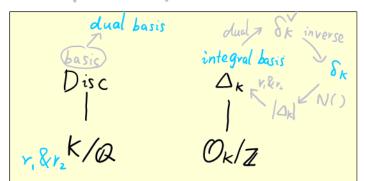
Q(Ta) Q(SN) d square-free Q[T]/(T3-2) Q(T5, i) Q(T23)[T]/(T3-T-1)

٠.,

1 K Ok Galois? If so, Gal (K/Q) subgroup & subfield

2) SKR Ak : See the picture

- $\mathfrak{G}$   $\mathcal{O}_{K}^{\times}$ ,  $\mathcal{C}l(K)$ .  $\pi_{\iota}(\mathcal{O}_{K})$
- @ Gal ext => Frob element of
- 6 local field KA places Mk



$$N_{k/\omega}(x)$$
  $N_{k/\omega}(I)$   $N_{L/k}(I)$ 

$$\downarrow S_{k/\omega} \qquad \downarrow S_{L/k} \qquad \downarrow N_{L/k}$$
 $\downarrow N_{k/\omega} \qquad \downarrow N_{L/k}$ 
 $\downarrow N_{L/k}$ 

```
K=Q(A)
                1) All quartic extension of Q have form Q(Ta) 1, 1 = ?
                2) Gal (Q(b)/Q) = 71/2/2
                3) Tr (A)=0 Tr (A+1)=1 N(A)=-d N(A+1)=1-d
                4) a basis (d,,d) = (1,12)
                    the dual basis. (di, di) = (=, 1/4)
            Recall how do we verify a basis (by Disc). the prop of Disc. "Verify"!

① Disc (2,, ..., 2n) = det (Tr k/Q (didj)) = [ (2 Zdi : (2 Zdi ) ) 2 det (oi(dj)) 2
                  @ Disc (1, 2, ..., 2 ) = (-1) = (-1) NKW (f(2)) If K = W[T]/(f) = Q(2)
                  5) \mathcal{O}_{Q(\overline{A})} = \int \mathbb{Z}\left[\frac{\overline{A}+1}{2}\right] d \equiv 1 \mod 4

\mathbb{Z}\left[\overline{A}\right] d \equiv 2,3 \mod 4

Define w_d = \int \frac{\overline{A}+1}{2} d \equiv 1 \mod 4
d \equiv 2,3 \mod 4

d \equiv 2,3 \mod 4
                       then OQ(A) = ZOZwa
                   6) D = \Delta \omega (a) = Disc (1, w_d) = \begin{cases} d \\ 4d \end{cases} d = 1 \mod 4
d = 2,3 \mod 4
                   7) Again use Lemma 1.3.7 / Prop 1.3.8 => 5)
            Recall how do we verify an integral basis (by Prop 1.3.8)
             e.p. when Disc (β1,..., βn) is square free, then {β1,... βn} is an integral basis.
                   8) \delta_{\omega(\sqrt{d})} = \delta(\sqrt{d}) d \equiv 1 \mod 4 d \equiv 2,3 \mod 4
                                     d = -1
ED
         \delta_{Q(i)} = (2) = (1+i)^{*}
          d = -2 \qquad \int_{2i}^{2i} |+f_{2i}| +f_{2i} |-f_{2i}| \leq 7 + f_{2i} +f_{2i} |3
\int_{\omega(f_{2i})} = (f_{2})^{3} \qquad |2| / | | | / | |
         d = -2
                                       2 3 5 7 11
                                      2 Bi 5 1+35i 1-35i 11 1+35i 1-35i
          d = -3
           δα(si) = (sa)
                                                            5 7 11 13
                                      d = 2
           \delta_{Q(\Sigma)} = (\Sigma)^3
                                        1+13 13 5 7 8+15 8-15 4+13 4-13
2 1 1 \ / \ /
           d = 3
                                         2
            \delta_{\mathcal{Q}(\overline{B})} = (1+\overline{B})^{2}(\overline{B})
```

The following calculation need the theory of frobenius element.

(P) Legendre Symbol

$$(\frac{-1}{P}) = (-1)^{\frac{p-1}{2}} = \begin{bmatrix} 1 & p \equiv 1 \mod 4 \\ -1 & p \equiv 3 \mod 4 \end{bmatrix}$$
 $(\frac{-2}{P}) = (-1)^{\frac{p^2-1}{8}} = \begin{bmatrix} 1 & p \equiv 1, 7 \mod 8 \\ -1 & p \equiv 3, 5 \mod 8 \end{bmatrix}$ 

10) Quadratic reciprocity law  $(p, q)$  and prime,  $p \neq q$ 

$$\left(\frac{P}{9}\right) = \left(\frac{9^*}{P}\right)$$
 i.e.  $\left(\frac{P}{9}\right)\left(\frac{9}{P}\right) = (-1)^{\frac{P-1}{2}\frac{9-1}{2}}$ 

## 11) Remification

$$P=2$$
  $D \not\equiv 1 \mod 4$  ramified  
 $D \equiv 1 \mod 8$  split  
 $D \equiv 5 \mod 8$  inert  
 $P \pmod p \mid D$  ramified  
 $\binom{D}{P} = 1$  split  
 $\binom{D}{P} = -1$  inert

$$\mathcal{O}_{\mathcal{Q}(\overline{h})}^{\times} \quad o(>\circ) \qquad N(\varepsilon_{\circ}) \\
\mathcal{F}_{2} = [1, \overline{2}] \quad 1+\overline{f_{2}} \quad - \qquad \overline{f_{7}} = [4, \overline{8}] \quad 4+\overline{f_{7}} \quad - \\
\mathcal{F}_{3} = [1, \overline{1}, \overline{2}] \quad 2+\overline{f_{3}} \quad + \qquad \overline{f_{9}} = [4, \overline{x_{1}}, \overline{1, x_{2}}, \overline{1, x_{3}}] \quad f_{9} + f_{9} = [4, \overline{x_{1}}, \overline{1, x_{2}}, \overline{1, x_{3}}] \quad f_{9} + f_{9} = [4, \overline{x_{1}}, \overline{1, x_{2}}, \overline{1, x_{3}}] \quad f_{9} + f_{9} = [4, \overline{x_{1}}, \overline{1, x_{2}}, \overline{1, x_{3}}] \quad f_{9} + f_{9} = [4, \overline{x_{1}}, \overline{1, x_{2}}, \overline{1, x_{3}}] \quad f_{9} + f_{9} = [4, \overline{x_{1}}, \overline{1, x_{2}}, \overline{1, x_{3}}] \quad f_{9} + f_{9} = [4, \overline{x_{1}}, \overline{1, x_{2}}, \overline{1, x_{3}}] \quad f_{9} + f_{9} = [4, \overline{x_{1}}, \overline{1, x_{2}}, \overline{1, x_{3}}] \quad f_{9} + f_{9} = [4, \overline{x_{1}}, \overline{1, x_{2}}, \overline{1, x_{3}}] \quad f_{9} + f_{9} = [4, \overline{x_{1}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x_{2}}, \overline{1, x_{2}}, \overline{1, x_{2}}] \quad f_{9} + f_{9} = [4, \overline{x$$

Computing h by class number formula  $K \subseteq Q(S_N)$ , G = Gal(K/Q) abelian

$$k = \prod_{\substack{\chi \in G \\ \chi \neq \chi_0 \\ \chi \to \text{ prim}}} L(\chi, 1) \qquad \qquad k = \frac{2^{r_1} (z\pi)^{r_2} R_k h}{|W| |\Delta_k|^{\frac{1}{2}}}$$

How to compute 
$$L(\chi, 1) \rightarrow h$$
?

$$L(\chi, 1) = -\frac{\chi(-1)\tau(\chi)}{f} \sum_{\alpha=1}^{f-1} \overline{\chi}(\alpha) \log(1-s^{\alpha})$$

$$= \begin{cases} -\frac{\tau(\chi)}{f} \sum_{\alpha=1}^{f-1} \overline{\chi}(\alpha) \log(\sin \frac{\pi \alpha}{f}) & \chi(-1) = 1 \\ \frac{\tau(\chi)\pi i}{f} \sum_{\alpha=1}^{f-1} \overline{\chi}(\alpha) & \chi(-1) = -1 \end{cases}$$

2 when K= Q(Tax), then we know Xax & T(Xax) well. with disc =  $\Delta_{K}$  : =  $\Delta$ 

(a) 
$$\chi_{o}^{(-1)} = \operatorname{Sqn}(\Delta)$$

(a) 
$$\chi_{\Delta}^{(-1)} = \operatorname{Sgn}(\Delta)$$
  
(b)  $\chi_{\Delta}^{(2)} = \begin{cases} (-1)^{\frac{\Delta^{2-1}}{8}} \\ 0 \end{cases}$   $\Delta_{k} = 1 \mod 4$   
(c)  $\chi_{\Delta}^{(p)} = \left(\frac{d_{k}}{P}\right)$   $\Delta_{k} = 3 \mod 4 \text{ or } \Delta_{k} \text{ even}$   
 $\Delta_{k} = 3 \mod 4 \text{ or } \Delta_{k} \text{ even}$ 

c) 
$$\chi_{\Delta}(p) = \left(\frac{dk}{p}\right)$$
 p odd prim

(d) 
$$\tau(\chi_{\Delta}) = J_{\Delta k} = \begin{cases} |\Delta_k|^{\frac{1}{2}} & \Delta_k > 0 \\ \frac{1}{2} |\Delta_k|^{\frac{1}{2}} & \Delta_k < 0 \end{cases}$$

$$\Rightarrow h = \begin{cases} -\frac{1}{2\log(\epsilon)} \sum_{d=1}^{|\Delta_k|-1} \chi_{\Delta}(a) \left(\log\left(\sin\frac{\pi a}{\Delta}\right) = -\frac{1}{\log(\epsilon)} \sum_{d=1}^{|\Delta_k|} \chi_{d_k}(a) \log\left(\sin\frac{\pi a}{\Delta}\right) & d_k > 0 \\ -\frac{1}{|d_k|} \sum_{a=1}^{|\Delta_k|-1} \chi_{d_k}(a) a \cdot \frac{\omega}{2} & \text{when } d_k < -4 \end{cases}$$

(3) More restriction.  $|\Delta_k| = P$  is an odd prime  $\Rightarrow \Delta_k \equiv 1 \pmod{4}$ R = Residue N = Non-residue  $T = Sin(\frac{k\pi}{n}) = \frac{n}{2^{n-1}}$ 

$$\mathcal{E}^{2h} = \frac{\prod_{b \in N} \sin \frac{\pi b}{P}}{\prod_{a \in R} \sin \frac{\pi a}{P}} \Rightarrow \mathcal{E}^{h} = \frac{\int_{P}}{2^{\frac{p}{2}}} \left( \frac{\prod_{a \in R} \sin \frac{\pi a}{P}}{a \in P} \right)^{\frac{1}{2}}$$

$$\Delta_{k} = -p$$
  $p = 3 \pmod{4}$   $p \neq 3$   
 $h = \frac{1}{p} \left( \sum_{b \in N} b - \sum_{a \in R} a \right) = \frac{p-1}{2} - \frac{2}{p} \sum_{a \in R} a$ 

$$K = Q[T]/(T^3-2) = Q(\lambda)$$
  $K/Q$  not Galois.  
1)  $Tr(\lambda) = 0$   $Tr(\lambda^2) = 0$   $N(\lambda) = 2$   $N(\lambda^2) = 4$   
2)  $Disc(1, \lambda, \lambda^2) = -N(3\lambda^2) = -3^3 \cdot 2^2$   
 $0$   $1$ ,  $\lambda, \lambda^2$  is a basis of  $Q(\lambda)$   
 $0$   $Q(\lambda) = Z[\lambda]$ ,  $\Delta Q(\lambda) = -3^3 \cdot 2^2$   
 $0$   $Y_1 = Y_2 = 1$   
3) the dual basis of  $(\lambda_1, \lambda_2, \lambda_3) = (1, \lambda_1, \lambda^2)$  is  $(\lambda_1^2, \lambda_2^2, \lambda_3^2) = (\frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ 

3) the dual basis of 
$$(a_1, a_2, a_3) = (1, a, a^2)$$
 is  $(a_1^{\vee}, a_2^{\vee}, a_3^{\vee}) = (\frac{1}{3}, \frac{1}{3a}, \frac{1}{3a^2}) = (\frac{1}{3}, \frac{a^2}{6}, \frac{1}{6})$ 

$$\delta_{\alpha(a)} = (3a^2)$$

4) ramification (d=3/2)

- 1) Q(SN)/Q Galois, Gal(Q(SN)/Q) = (Z/NZ)\*
- $Q(\S_{N}) = Q[T]/_{\Phi_{N}}(T) \qquad r_{i} = 0 \quad \text{except} \quad N = 1,2$ 2)  $\Delta_{k} \left[ \text{Disc}(1,\S, \dots \S_{N}^{N}) \right] \Rightarrow O_{Q(\S_{p^{n}})} = Z[\S_{p^{n}}]$ In general,  $O_{Q(\S_{N})} = Z[\S_{N}] \quad \text{by} \quad \text{Cor } 1.4.6.$ 3)  $\Delta_{Q(\S_{p^{n}})} = \pm p^{p^{n-1}(pn-n-1)} \quad \text{minus} \quad p = 3 \pmod{4} \quad \text{or } p^{-2}, n = 2$

when 
$$N = p_1^{n_1} \cdots p_k^{n_k}$$
, by Prop 3.3.7.3,  
 $\Delta \omega(s_N) = (-1)^t N \left[ p_1^{(n_1 - \frac{n_1 - 1}{p_1})} \cdots p_k^{(n_k - \frac{n_k - 1}{p_k})} \right]^{N}$ 
 $t_N = \int_{\infty}^{\infty} \frac{\delta(N)}{2} N > 2$ 

4) By Frobenius element,  $p \equiv 0 \pmod{N}$  ramified  $(N = p^k \text{ totally ramified})$   $p \equiv 1 \pmod{N}$  split  $p \not\equiv 0,1 \pmod{N}$  inert  $(N = p^k \text{ totally ramified})$   $(N = p^k \text{ totally ramified})$  (

 $f(\mathfrak{l}_i|l)$  is the order of l in  $(\mathbb{Z}/N\mathbb{Z})^{\times}$ , that is, the minimal integer f>0 such that  $N|(l^f-1)$ .

The minimal polynamial  $\Phi_{N}(x)$  of  $P_{N} \in \mathbb{Q}[P_{N}]$  Table[{n, Cyclotomic[n, x]}, {n, 0, 50}]  $\mathbb{Q}[P_{N}]$   $\mathbb{Q}[P_{N}]$ 

$$\begin{array}{lll}
N = 2^{n} \cdot 3 \cdot p, & p = 3 \cdot 5, 7. & \varphi(N) = 2^{mn} \cdot (p-1) \\
\Phi_{9} & 1 + x^{3} + x^{6} & \Phi_{15} & 1 - x + x^{3} - x^{4} + x^{5} - x^{7} + x^{8} & \Phi_{21} & 1 - x + x^{3} - x^{4} + x^{6} - x^{8} + x^{7} - x'' + x'^{1} \\
\Phi_{18} & 1 - x^{3} + x^{6} & \Phi_{30} & 1 + x - x^{3} - x^{4} - x^{5} + x^{7} + x^{8} & \Phi_{42} & 1 + x - x^{3} - x^{4} + x^{6} - x^{8} - x^{9} + x'' + x'^{1} \\
\Phi_{36} & 1 - x^{6} + x'^{1} & \Phi_{60} & 1 + x^{2} - x^{6} - x^{8} - x'^{0} + x'^{4} + x^{16} & \Phi_{84} & 1 + x^{2} - x^{6} - x^{8} + x'^{1} - x'^{6} - x^{8} + x^{2} + x^{2} \\
\Phi_{72} & 1 - x'^{2} + x^{24} & \Phi_{120} & 1 + x^{4} - x'^{2} - x'^{6} - x^{20} + x^{28} + x^{3} & \Phi_{168} & 1 + x^{4} - x'^{5} - x'^{6} + x^{24} - x^{3} - x^{36} + x^{44} + x^{48}
\end{array}$$

$$N = p^{2} \quad \gamma(N) = q - 1) p$$

$$= \Phi_{25} \quad 1 + x^{5} + x^{10} + x^{15} + x^{20}$$

$$= \Phi_{49} \quad 1 + x^{7} + x^{14} + x^{21} + x^{28} + x^{35} + x^{42}$$

$$= \Phi_{121} \quad 1 + x^{11} + x^{22} + x^{33} + x^{44} + x^{55} + x^{66} + \dots + x^{110}$$

50以内积, 更对更新更新更好更好

$$k = Q(F_S) \quad L = Q(F_S, i) \quad \text{purpose}, \quad L/k \quad \text{is unvaried by discuss } L/Q$$

$$1) \quad O_k = Z[F_S] \quad O_k = Z[F_S], \quad O_k =$$

## Local field

```
Teichmüller lift for K= Qs
                                                                                                                                                                                                                                                                                                                                                                                                                                                1 = [1]
                                                   [1]:1
                            · [2]= 2+ 1.5+2.52+1.53+3.54+...
                                                                                                                                                                                                                                                                                                                                                                                                                         2=[2] +[4] 5+[3] 5+[4] 5+[2] 5+...
                                                                                             (2, 1, 2, 1, 3, 4, 2, 3, 0, 3, ...
                                                                                                                                                                                                                                                                                                                                                                                                                           3=[3]+[2] + [1] -5+[4] + 53+[2] + 54+...
                        -i [3]= 3+3·5+2·5+3·53+...-
                                                                                                      (3.3,2.3,1,0,2,1,4,1,...
                   -1 [4] = 4+4.5+4.53+4.53+...
                                                                                                                                                                                                                                                                                                                                                                                              [4]=[4]+[1]5
                                                                                                     (4,4,4,4,...)
   e.g of Hensel's lemma for k = Q_s

f(x) = 5x^6 + x^5 + 3x^7 - x^3 - 2x + 3 \in \mathbb{Z}_s[x]

f(x) = (x^2 - 2) \cdot (x^3 - 2x^2 + x + 1) := \bar{g}(x) \bar{h}(x) \in [F_s[x]] \pi = 5

\begin{cases}
g_{o}(x) = \chi^{2} - 2 \\
h_{o}(x) = \chi^{2} - 2
\end{cases}

\begin{cases}
f - g_{o}h_{o} = 5(x^{b} + x^{4} - x^{2} + 1) = \pi f, & f_{i} \in \mathbb{Z}_{5}[x] \\
h_{o}(x) = x^{3} - 2x^{2} + x + 1
\end{cases}

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\begin{cases}
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\begin{cases}

                                 =) (af, +uho) go + vho = f, mod T
                                                                                                                           Po(x) = 1(x) = 22x+21
                   q_{0}(x) = \frac{1}{2} \frac
```