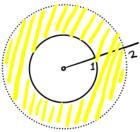
Un exemple par jour 4.1. the complex torus of form C^{\times}/Z_{\times}

 $C:=\mathbb{C}^{\times}/\mathbb{Z}_{Y}\stackrel{\text{topo}}{=}\mathbb{T}^{-1}$ is a cpt Riemannian surface of genus 1. $Y\in Aut(\mathbb{C}^{\times})$ $Y(z)=\alpha z$ $\alpha\in\mathbb{C}^{\times}$ $|\alpha|>1$

Today: a=2

1. fundamental set:



=> only need 2 local chart

2.
$$0 \rightarrow \mathbb{Z} \longleftrightarrow \mathbb{C} \xrightarrow{f: z \mapsto e^{2\pi i z}} \mathbb{C}^{\times} \longrightarrow 1$$

$$\downarrow + \frac{1}{2\pi i} \ln 2 \qquad \downarrow + \frac{1}{2\pi i} \ln 2 \qquad \downarrow \times 2$$

$$0 \rightarrow \mathbb{Z} + \frac{1}{2\pi i} \ln 2 \rightarrow \mathbb{C} \longrightarrow \mathbb{C}^{\times} \longrightarrow 1$$

$$\mathbb{C}^{\times} = \mathbb{C}/_{\mathbb{Z}} \Rightarrow \mathbb{C}^{\times}/_{\mathbb{Z}\gamma} = \mathbb{C}/_{(\mathbb{Z}' \oplus \frac{1}{2\pi i} \ln 2\mathbb{Z}')}$$

better:
$$a = e^{2\pi} \approx 535.49$$

$$a = e^{-2\pi i w} \approx -230.765$$

3. line bundle on C

bec
$$L_b = \mathbb{C}^{\times} \times \mathbb{C} /_{(2,3)} \sim (12,b)$$
 \Rightarrow 0 $L_b \in Pic_o(\mathbb{C}); (L_b \sim L_1 \simeq \mathcal{O}_{\mathbb{C}})$

$$C = \mathbb{C}^{\times} /_{2 \sim 22}$$

Reduced to: find a section s on L_b st div s = [b] - [1]Reduced to: find a meromorphic functions g on \mathbb{C}^{\times} s.t. $\mathcal{O} g(2z) = bg(z) \qquad b \in \mathbb{C}^{\times}, \ b \neq 2^{\times}; \ e.g. \ b=3$ $\mathcal{O} g \text{ has simple poles on } 2^n, \text{ and simple zeros on } 2^nb \ n \in \mathbb{Z}$ $b = e^{2\pi i c}, c \in \mathbb{C}$ $\tau := \overline{\pi i} \ln 2$ $w(z) = \frac{1}{2\pi i} \ln z$ $g(z) = \frac{\theta[i-2c](w(z), \tau)}{\theta[i](w(z), \tau)}$ is the required one. Blue — example
Orange — more than this example, slogan
Red — important results
Purple — I don't know the answer/proof
Green — sketsch of proof: in a minimal way
Grey — some supplementary explanation. Unimportant assumptions.
Hell grey — explanation on well-known notations.

Brown — small title in subsections.

My symbol collection set

1		Mathbb	Mathrsf/Mathcal	Greek	
A abelian variety	α	Aadèles	A apartment		۵
В	Ь	IB	B building	0.0	β
С	c ce	C cplx number	e chamber category	Γ ^{9P} graph Γ	8
D	d constant d	ID	9 Poincare disk	△ diag embedding	8
E elliptic curve	e ramification index	Œ	3		ε
F field fiber F formal gp law	f	IF finite field	9 sheaf		ζ
a group	9	G gp scheme	G g: Lie alg upper half plane		n
Н	h	H	Hecke alg	Θ	θ
I ideal	i	1	I ideal of sheaf		1 injection
J	į	Jī	I		k
K cos/base field	k < k	lK	$ \mathcal{X} $	1 lattice 1	λ
L	l l	LL.	え		М
M module	m	M	Mmoduli space		νοοτ of unity (ξ/ω)
Ν	n	N natural number	/ /		Sconstant
0	0	Ø	O structure sheaf O) Weierstons	TI multi	π uniformizer Projection
Р	P	IP proj space	y g; ell fet		P - P
Q	9	Q rational number	Q	Σ sum	5
Rring	r	IR real number	$ \mathcal{R} $	_	τ
S base scheme	2	2	S	Φ	ا ا
T tangent space translation	t	T torus	9	_	X character
U←U	u	V	-	$ar{arPsi}$	4
V _{1.2.} V	ν	₩	v 19	Ω Ω	w ₩≈ ₩ω
Wwitt vector	w	W	-		
X	x	X	X Y		
Y = Y	y	Y		hebrew	Russian
Z center	2	Z integer	[₹	Xcardinal	III sha gp
		ı			,

```
Green: number / basic stuffs in senior high school
Orange: scheme - related
Darkyellow: advanced algebra
                                        Don't use them simultaneously! (usually)
                                                                     1/1/v, ×/x/x/x,
Don't mix. w/w, 8/8, k/k/X/K
           \varphi/\psi , e/e , \chi/\gamma $\varpi\boldsymbol{\omega}$ (need amsbsy package)
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Japanese mathematicions and their Chiese translations.

	Matsumoto	松本	Hideya Matsumoto	松本英野
1860	Sawayama	沢山	Yuzaburo Sawayama	沢山勇三郎
1875.4	•		Teiji Takagi	高木贞治 高木 貞治
901.4	Oka	冈	Kiyoshi Oka	冈洁 岡潔
1902.7	Yamanouchi	山内	Takahiko Yamanouchi	山内恭彦
1902.8	Akizuki	朱火月	Yasuo Akizuki	秋月康夫 秋月 康夫
1904.01	•	·	Hidetaka Teresaka	寺阪英孝
1908.12	Tannakian	淡中的	Tadao Tannaka	淡中忠郎
1912.7	Nakayama	中山	Tadashi Nakayama	中山正
1915.3	Kodaira	小平	Kunihiko Kodaira	1平邦彦
1917.11	Iwasawa	岩泽	Kenkichi Iwasawa	岩泽健吉 岩澤 健吉
1924.1	Igusa	井草	Jun-Ichi Igusa	#草准一 #草 準一
1924.2	Tomita	富田	Minoru Tomita	富田稔 富田 稔
1925.1			Toichiro Kinashita	木下东-郎 木下 東一郎
1925.11	Tamagawa	玉河	Tsuneo Tamagawa	玉河恒夫
1926	Iwahori	岩堀	Nagayoshi Iwahori	岩堀长庆 岩堀 長慶
1927.11	Taniyama	谷山	Yutaka Taniyama	谷山丰 谷山 豊
1927. 12	Satake	佐武	Ichirō Satake	佐武-郎
1928,12	Fujita	藤田	Hiroshi Fujita	藤田宏 藤田 宏
1928	Toda	戸田	Hiroshi Toda	户田宏 戸田 宏
1928.4	Sato	佐藤	Mikio Sato	佐藤科 佐藤 斡夫
1930.2	Shimura	志村	Goro Shimura	志村五郎
1930.3	Yoneda	米田	Nobuo Yoneda	米田信夫
1930	Matsumura	松村	Hideyuki Matsumura	松村英之
1930	Kubota	久保田	Tomio Kubota	久保田歐佳
1931.4	Hironaka	广中	Heisuke Hironaka	广中平祐 広中 平祐
1932.1			Shoshichi Kobayashi	小林昭七 小林 昭七
1933.7	Takesaki	竹崎	Masamichi Takesaki	竹崎正道 竹崎 正道
1941	Hotta	堀田	Ryoshi Hotta	
1944.3			Toshitsune Miyake	三宅敏恒
1947.1	Kashiwara	正树	Masaki Kashiwara	柏原正树 柏原 正樹

1951.2	Mori	森	Shigefumi Mori	森重文	
1952.1	Kato	加藤	Kazuya Kato	加藤和也	
1952.8	Hida	肥田	Haruzo Hida	肥田晴三	肥田 晴三
1953,12.8	Mukai	向井	Shigeru Mukai	向井茂	
1955			Shigeru Mukai Toshiyuki Tanisaki	谷崎俊之	
1959.3	Fukaya	深谷	Kenji Fukaya	深谷贤治	
1961.9	Saito	斋藤	Takeshi Saito	斋藤毅	斎藤 毅
1962.11	Nakajima	中岛	Hiraku Nakajima	中岛启	中島啓
1969.3	•		Shinichi Mochizuki	望月新一	
1972.8			Takurō Mochizuki	望月扬即	
? 1995 P.h.D)		Kiyoshi Takeuchi	竹内潔	

Confusion list:

1. Ring has unit. Don't consider 0-Ring.

Read the diagram from top to bottom.
 countable = finite + inf countable (at most countable)

4 g fix set A. $\forall a \in A$, ga = a (use "stabilized" instead)
5 c. only mean a subset, or an injective map (uncompatible structures are allowed, e.g. $L^{\infty}([0,1]) \subset L^{1}([0,1])$)

6. definition of norm/seminorms
 7. HK ≠ H×K HK = Ig∈G | g=hk for some h∈H, k∈K]