Eine Woche, ein Beispiel 3.30 Special loci of Ag

Ref:

I learned this from Podelski Constantin and his articles:

[PCdeg]: The Gauss Map on Theta Divisors with Transversal A_1 Singularities. Journal of Singularities 27 (2024). https://doi.org/10.5427/jsing.2024.27g.

[PCgraph]: The Gauss map for bielliptic Prym varieties. https://doi.org/10.48550/arXiv.2311.13521.

[PP21]: Piotr Pragacz. Prym Varieties and Their Moduli. EMS Press, 2021. https://doi.org/10.4171/114-1/8.

1 a list of special loci 2. invariants

1. a list of special loci
For the moduli space (a stack, but we only care about its coarse moduli space)

$$A_g = \{(A, \Theta) \text{ ppav } | \text{dim } A = g\},$$

we have the following special loci:

 $N_{k}^{(g)} = \{(A, \Theta) \in A_{g} \mid \text{dim Sing}(\Theta) \ge k\}$ Andreotti-Mayer loci

$$G_{\alpha}^{(g)} = \{(A, \emptyset) \in A_g \mid deg(P\Lambda_{\emptyset} \rightarrow Gr(g-1,g)) \leq d\}$$

$$A_{t,g-t}^{\delta} = \left\{ (A, \Theta) \in A_g \mid \exists A, A_2 \text{ abelian variety,} \\ f: A \times A, \longrightarrow A \text{ isogeny, s.t.} \right\}$$

$$\left\{ (f \circ l_A)^* \mathcal{O}_A(\Theta) \text{ is of type } \delta \right\}$$

 $S = (\alpha_1, \ldots, \alpha_k)$ ailain

Apart from that, we also have special loci induced from curves.

The following loci in the bielliptic Prym locus may use some notation in the end of the page.

$$\mathcal{B} \mathcal{E}_{g} = \text{closure of } \mathcal{P}_{rym}(\widehat{\mathbb{C}}/\mathbb{C}) \mid \mathcal{C} \text{ is bielliptic of genus } g+1]$$

$$\mathcal{E}_{g,t} = \mathcal{P}_{rym}(\widehat{\mathbb{C}}/\mathbb{C}) \in \mathcal{B}\mathcal{E}_{g} \mid \mathbb{C}' \longrightarrow \mathcal{E} \text{ ramified at 2t pts} \mathcal{E}_{g,t}^{h} = \mathcal{P}_{rym}(\widehat{\mathbb{C}}/\mathbb{C}) \in \mathcal{E}_{g,t} \mid \mathcal{C}' \text{ hyperelliptic} \mathcal{E}_{g,t}^{h} = \mathcal{P}_{rym}(\widehat{\mathbb{C}}/\mathbb{C}) \in \mathcal{E}_{g,t} \mid \mathcal{C}' \text{ hyperelliptic} \mathcal{E}_{g,t}^{h} = \mathcal{P}_{rym}(\widehat{\mathbb{C}}/\mathbb{C}) \in \mathcal{E}_{g,t} \mid \mathcal{E}_{g,t}^{h} = \mathcal{E}_{g,t}^{h} \mid \mathcal{E}_{g,t}^{h} = \mathcal{E}_{g,t}^{h} \mid \mathcal{E}$$

$$N_{ad}(\widehat{C}/C) = \# \{additional \text{ singularities of } \emptyset \}$$

= $deg((hoal_w)[W_{sing}]/2)$ [PCgraph, p13]

2 invariants

dimension

deg 0 at generic pts

possible type D counterexample 0 1 1 2 3 3 4 $\left[\frac{9-1}{2}\right]$