Eine Woche, ein Beispiel

7.17 formalism

Here I collect some formalisms which enhance well-known theories.

Somehow it also explains the polularity of the abstraction in mathematics. We want to have a better understand, so we invent new languages and theories, which in turn causes more troubles for beginners. Hug those formalisms!

母题. classification, symmetry

~ Grothendieck Universe Axiomatic set Theory Both let us be away from paradoxes. The latter is more convenient Category Theory ~ Infinite Category Theory [adjoint fctor = preserve (co)limits] is some cases (Braided Symmetric) Monoidal Categories - Categorification Extract combinatorical informations from categories ~> Classification Examples Specify and generalization. $See \ https://github.com/ramified/personal_tex_collection/blob/main/\%E8\%9B\%99\%E9\%B8\%A39\sqrt[3]{latest\%20} version.pdf$ Parameter space ~> Moduli space on parameter spaces are important See https://github.com/ramified/moduli_in_algebraic_geometry

Topology
Get étale topology.

Topological space

Cet abelian category.

Scheme

Get more objects. e.g. Ind-Sch., stack,...

Snake lemma

>> homological algebra, spectral sequence

Diagram chasing all the time!

>> derived category, six-fctor formalism.

Reduce important properties to categorical non-sense.

https://www.math.uni-bonn.de/people/schwede/EnhancedSeminar-WS2223.pdf

Finite field >> ???? Should contain "field with one element".

Moreover, AR theory tells us the structure of indecomposable reps,

Bruhat-Tits theory tells us the structure of p-adic groups,

Artin-Schreier theory tells us the structure of deg p extensions. CharF=p