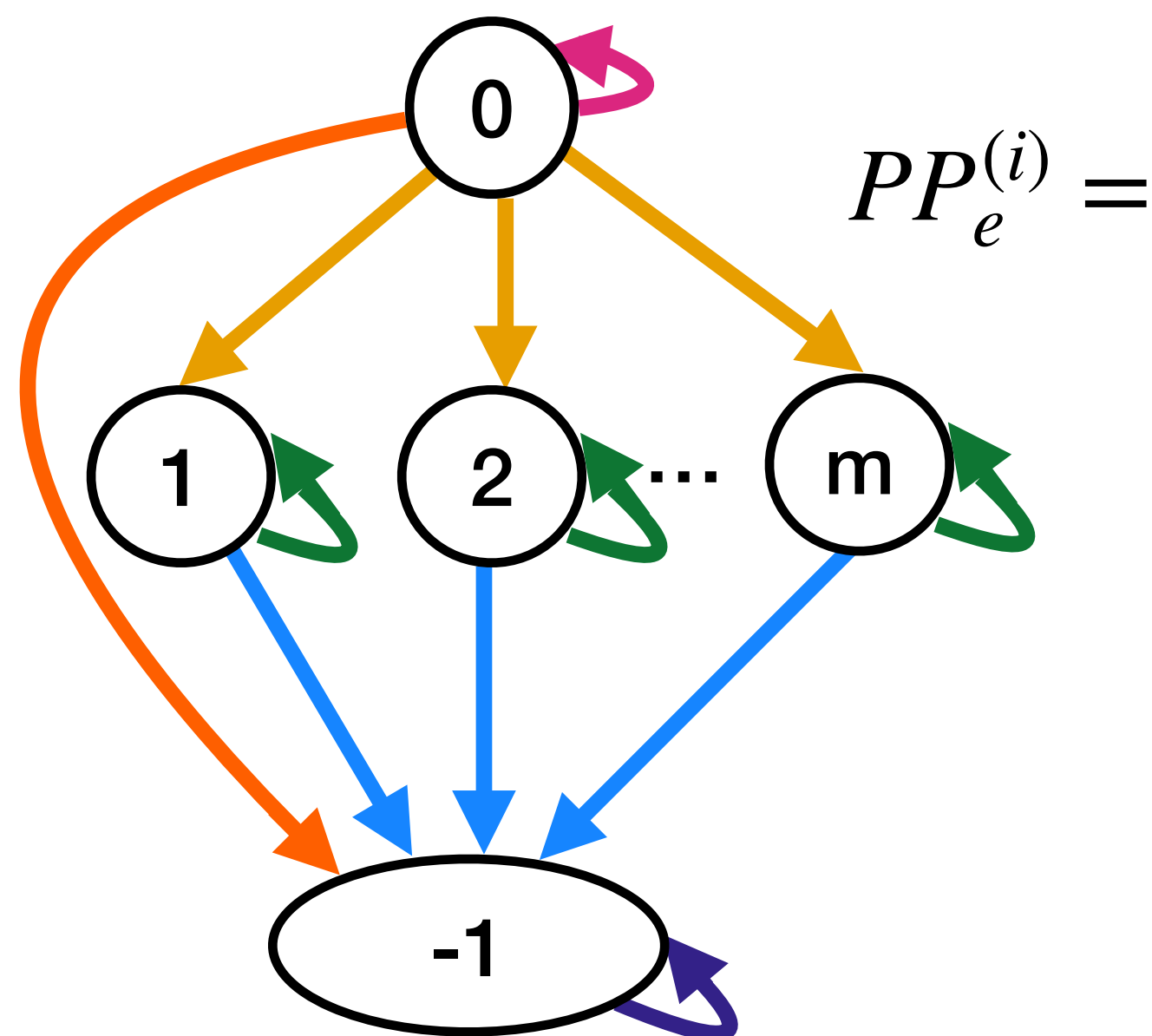


(A)

Posterior probabilities:

$$PP_e^{(i)}(\alpha, \beta) = \mathbb{P}(\chi^{(i)}(u) = \alpha, \chi^{(i)}(v) = \beta \mid \mathcal{D}^{(i)}; T, \Theta)$$



$$S_{0,0}(e, i) = PP_e^{(i)}(0, 0)$$

$$S_{0,\alpha}(e, i) = \sum_{\alpha \in \Sigma'} PP_e^{(i)}(0, \alpha)$$

$$S_{\alpha,\alpha}(e, i) = \sum_{\alpha \in \Sigma'} PP_e^{(i)}(\alpha, \alpha)$$

$$S_{\alpha,-1}(e, i) = \sum_{\alpha \in \Sigma'} PP_e^{(i)}(\alpha, -1)$$

(B)

Expectation-Maximization

E-step

 $\forall e \in E(T)$ compute:

$$S_{0,0}(e, i) \quad S_{0,\alpha}(e, i)$$

$$S_{\alpha,\alpha}(e, i) \quad S_{0,-1}(e, i)$$

$$S_{-1,-1}(e, i) \quad S_{\alpha,-1}(e, i)$$

M-step

$$\max_{\Theta} \sum_{e \in E(T)} f \left\{ \begin{array}{l} S_{0,0}(e, i) \\ S_{\alpha,\alpha}(e, i) \\ S_{0,\alpha}(e, i) \\ S_{0,-1}(e, i) \\ S_{\alpha,-1}(e, i) \end{array} \right\}$$

$$S_{-1,-1}(e, i) = PP_e^{(i)}(-1, -1)$$

$$S_{0,-1}(e, i) = PP_e^{(i)}(0, -1)$$