Evaluate a set of hypotheses with GORIC or GORICA: Linear Regression Example

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Example: Sesame

Data preparation

First, load the required libraries (after they have been installed). These libraries contain functions, such as goric, that will be used in the R code below. Each time you reopen R, you will have to load the required libraries.

```
## First, install the packages, if you have not done this already:
if (!require("restriktor")) install.packages("restriktor")

## Then, load the packages:
library(restriktor) # for the goric function

# If you want to use restriktor from github:
#if (!require("devtools")) install.packages("devtools")
#library(devtools)
#install_github("LeonardV/restriktor")
#library(restriktor) # for goric function
```

Second, it is necessary to load the data.

Notably, it is only possible to load the data if you are using the correct working directory (with both your R script and data file). The command getwd() shows you your current working directory. You can change the working directory to the one you prefer using the function setwd() by specifying the correct location between parentheses. Alternatively, in Rstudio, you can use the "Session" tab (on top) or you can use the "Files"-pane (on top of probably the right lower box of your Rstudio-screen, this pane is located next to the panes for "Plots", "Packages", "Help", and "Viewer").

If you open the data file Data_Lucas.txt in a text editor, you can see that the variable labels have been inserted (using quotes; i.e., "...") in the first line of the file, which is called a header. Therefore, you have to specify 'header = TRUE' when loading the data:

```
# Load the sesame data from a text file
Sesame <- read.table("data/sesamesimRegression.txt", header=TRUE)
# Inspect data
head(Sesame)</pre>
```

```
prelet prenumb postnumb
       30
1
                35
2
       24
                29
                           50
3
       26
                32
                           48
4
       26
                42
                           39
5
       7
                19
                           34
6
                30
                           21
       19
```

Example hypothesis

The following hypothesis will be evaluated:

```
H1 <- 'prenumb > prelet'
# Note that the labeling of the estimates should be used
```

Standardize data

Since parameters of continuous variables (using different scales) are being compared, the data needs to be standardized (such that comparison of the parameters is meaningful / fair, since they are on the same, comparable scale then).

```
# Standardize all continuous variables (of interest) including the outcome:
Sesame_s <- as.data.frame(scale(Sesame))
#
# Or: Standardize solely the continuous predictors (of interest):
#Sesame_s <- Sesame
#Sesame_s[,2:3] <- as.data.frame(scale(Sesame[,2:3]))</pre>
```

Notes:

- Standardizing of ordinal and nominal variables is not helpful, since the estimate of the unstandardized ordinal and nominal variables reflects a group difference in the outcome (in that case, one probably does not want to standardize the outcome).
- In case there are multiple outcomes and estimates for multiple outcomes are compared, then one needs to standardize the outcome (as well).

Preparation for GORIC(A)

```
# estimate the parameters of the statistical model at hand
fit_Sesame <- lm(postnumb ~ prenumb + prelet, data = Sesame_s)
# Check names used in model
names(coef(fit_Sesame))</pre>
```

```
[1] "(Intercept)" "prenumb" "prelet"
```

```
# Specify restrictions should use these names (as done above)
#
# In case of the Intercept, one should use: .Intercept.
# E.g., when outcome is not also standardized:
# H1 <- '.Intercept. > 0'
```

GORIC & GORICA

Note: For (more) information regarding interpreting the GORIC(A) output, see 'Guidelines_output_GORIC' (https://github.com/rebeccakuiper/Tutorials).

GORIC values and weights for H1 and its complement

Here, we assume that the interest lies only in H1. In that case, it should be evaluated against its complement.

```
set.seed(123)
goric(fit_Sesame, hypotheses = list(H1 = H1))
```

restriktor (0.6-10): generalized order-restricted information criterion:

Results:

```
model
                 loglik
                                            loglik.weights
                                                             penalty.weights
                                                                              goric.weights
                         penalty
                                     goric
1
           H1
               -256.595
                            3.500
                                   520.190
                                                      1.000
                                                                       0.500
                                                                                       1.000
   complement
               -268.116
                            3.500 543.232
                                                      0.000
                                                                       0.500
                                                                                       0.000
```

Conclusion:

The order-restricted hypothesis 'H1' has 100793.25 times more support than its complement.

From the output, it is concluded that the support for H1 is many more supported / likely than its complement. Hence, there is compelling evidence in favor of H1.

GORICA values and weights for H1 and its complement

```
set.seed(123)
goric_sesam_1c <- goric(fit_Sesame, hypotheses = list(H1 = H1), type = "gorica")
#summary(goric_sesam_1c)
goric_sesam_1c</pre>
```

restriktor (0.6-10): generalized order-restricted information criterion approximation:

Results:

```
loglik.weights
        model
               loglik penalty
                                gorica
                                                         penalty.weights
                                                                          gorica.weights
                                                  1.000
                                                                   0.500
                                                                                    1.000
           H1
                6.082
                         2.500
                                -7.164
1
               -5.859
                         2.500 16.718
                                                  0.000
                                                                   0.500
                                                                                    0.000
  complement
```

Conclusion:

The order-restricted hypothesis 'H1' has 153406.68 times more support than its complement.

From the output, it is concluded that the support for H1 is many more supported / likely than its complement. Hence, there is compelling evidence in favor of H1.