Tutorial for goric: How to evaluate theory-based hypotheses using the GORIC and GORICA

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Introduction

Analyses

Below, you will find examples for the use of the goric function in the restriktor package.

Two types of analyses can be run:

- type = "goric" (the default), which can be applied to multivariate normal linear models;
- type = "gorica", the approximation of the GORIC which can be applied to a broad range of models.

Furthermore, there is the argument comparison = for the following three types of comparisons:

- "none'
- "unconstrained" (default)
- "complement"

If you choose "none", only the hypotheses of interest are inspected. This can lead to choosing the best out of a set of weak hypotheses. Therefore, this is only recommended when the hypotheses of interest cover the full parameter space / cover the whole set of possible theories. If "unconstrained" is chosen, then the unconstrained / unrestricted / classical alternative hypothesis is included in the set. This safeguards from choosing a weak hypothesis, that is, a hypothesis not supported by the data, as the best one. If at least one of the theory-based / informative hypotheses is not weak, one can compare those to all other hypotheses in the set. This is the default in case of multiple theory-based hypotheses.

In case of one theory-based hypothesis, "complement" is the default. Then, the complement of the hypothesis of interest is evaluated and acts like a competing hypothesis. Since there is per definition no overlap between the hypothesis and its complement, this is more powerful then using the unconstrained hypothesis as a failsafe for one theory-based hypothesis.

At the end of the file, there are three examples for the three types of comparisons.

The goric function of restriktor takes different forms of input.

For model parameter estimates:

- * enter fitted unconstrained object (lm, glm, glmer, nlmer, lmer, or lavaan object);
- * enter the (structural) parameter estimates and their covariance matrix yourself.

For constraints:

- * enter character constraints:
- * enter list with constraints matrix.

Please note that:

- * The GORIC can only be calculated for lm objects.
- * The GORIC (type = 'goric') is the default for lm objects, while GORICA (type = 'gorica') is for the other input options.
- * In the GORICA, the estimates are assumed to be normally distributed. So, for some models when sample size is low, this assumption may not hold. In that case, it is often not clear how well the GORICA performs. See Altinisik et al 2021, for some simulations regarding logistic regression and SEM models (for which the GORICA performs well).

Hypothesis specification

A few remarks on how to specify hypotheses when working with the goric function. When one uses character constraints:

- Within the restriktor and goric functions, it is possible to use the following operators: >, <, =, <=, >=, == (where the last three denote the same constraint as the first three).
- The goric and the restriktor functions can deal with:
 - pairwise restrictions separated by a semicolon; (e.g., "beta1 > beta2; beta2 > beta3") or an & sign (e.g., "beta1 > beta2 & beta2 > beta3").
 - combined restrictions consisting of more than one operator (e.g., "beta1 > beta2 > beta3"). Note that one should use the labels of the parameter estimates.
- One can also define hypothesis in terms of linear functions of parameters (For more details, see 'Extra possibility specification hypotheses' near the end of this document).

When one wish to use a list with constraints matrix (possibly together with *rhs* and *neq*), it should be done as follows: list(constraints = xxx, rhs = xxx, neq = x), with constraints being a matrix, rhs a vector with the right hand side of the restrictions, where the length of the vector equals the number of rows of constraints matrix (when not all of them are zero), and neq a scalar denoting the number of equalities in the matrix (when not zero). By default, rhs and neq are set to 0. These arguments have to be specified such that: + constraints * parameters >= rhs, + where the first neq restrictions are equalities.

In the following examples, the above methods are illustrated.

Preparation

Before starting the analyses, it is necessary to install and load the packages. Note that one needs to install the package only once, but has to load the package each time the R script is run.

```
# If you want to use restriktor from github:
#if (!require("devtools")) install.packages("devtools")
#library(devtools)
#install_github("LeonardV/restriktor")
#library(restriktor) # for goric function
#
# If from CRAN:
if (!require("restriktor")) install.packages("restriktor")
library(restriktor) # for goric function
```

Next, data is generated as example data to illustrate the functionality of the goric function. If you want to obtain the same results as obtained here, it is necessary to set the seed at a fixed number.

Then, a regression model can be fit using the lm function:

```
fit.lm \leftarrow lm(y \sim x1 + x2 + x3)
```

Below, the GORIC and GORICA are applied to this model.

To apply the GORIC(A), hypotheses need to be specified. Normally, these would be based on theory. However, since (hypothetical) data is generated, quasi-randomly two hypotheses are specified.

Notes on specifying hypotheses:

- Hypotheses in R are in terms of the labeling used for the estimates (instead of the names for the population parameters, say, beta0, ..., beta3). Thus, here: Intercept., x1, x2, and/or x3.
- In case estimates of continuous predictor variables are compared (e.g., "x1 < x2"), one should standardize the data (this is shown in more detail below) or use the standardized parameter estimates.

Model Selection using GORIC(A)

GORIC & GORICA

The upcoming analyses can be performed by means of both the GORIC and the GORICA. By default, the goric function calculates the GORIC values for lm objects (which then uses: type = "goric"). To calculate the GORICA values, the argument type has to be set to gorica (i.e., type = "gorica") within the goric function.

Note on GORIC and GORICA weights:

• The GORICA weights (asymptotically) equal the GORIC weights. The differences are minor and often not notable with 2 decimals. Because of these minor differences, the relative weights (i.e., ratio of weights) can differ. These differences in relative weights can even be large, when dividing a very large number by a very small number with minor differences in these values.

Note: For (more) information regarding interpreting the GORIC(A) output, see 'Guidelines_output_GORIC' (https://github.com/rebeccakuiper/Tutorials).

Fitted unconstrained (g)lm object + character constraints

Next, the hypotheses need to be specified. Note that the ; separates the restrictions within one hypothesis.

```
H1 \leftarrow "x1 > 0"
H2 \leftarrow "x1 > 0; x2 > 0"
```

Now, the GORIC values and weights can be calculated.

```
# GORIC
set.seed(123) # Set seed value
out <- goric(fit.lm, hypotheses = list(H1, H2))</pre>
#summary(out)
out
```

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

```
loglik.weights penalty.weights goric.weight goric.weight
          model loglik penalty
                                   goric
             H1 -3.295
                           4.500
                                                                                  0.284
1
                                 15.589
                                                  0.333
                                                                   0.284
2
             H2 -3.295
                           3.847 14.284
                                                  0.333
                                                                   0.545
                                                                                  0.545
                           5.000 16.589
3 unconstrained -3.295
                                                  0.333
                                                                   0.172
                                                                                  0.172
```

Note: Hypotheses 'H1' and 'H2' have equal likelihood values (i.e., the hypotheses overlap). The GORIC(A

The order-restricted hypothesis 'H2' is not weak, with 1.921 times more support than H1.

To obtain the GORICA values and weights instead:

```
# GORICA
set.seed(123) # Set seed value
out_gorica <- goric(fit.lm, hypotheses = list(H1, H2), type = "gorica")</pre>
#summary(out_gorica)
out_gorica
```

restriktor (0.5-90): generalized order-restricted information criterion approximation:

Results:

	model	loglik	penalty	gorica	loglik.weights	penalty.weights	gorica.weights	gorica.weigl
1	H1	3.622	3.500	-0.244	0.333	0.284	0.284	
2	H2	3.622	2.847	-1.549	0.333	0.545	0.545	
3	unconstrained	3.622	4.000	0.756	0.333	0.172	0.172	

Note: Hypotheses 'H1' and 'H2' have equal likelihood values (i.e., the hypotheses overlap). The GORIC(A

The order-restricted hypothesis 'H2' is not weak, with 1.921 times more support than H1.

Fitted unconstrained (g)lm object + list with constraints matrix

In the example above, **rhs** and **neq** are assumed to be 0, which is also the assumed default. It means that the left hand side of (in)equalities are set to 0's, and that the number of equality restrictions is equal to 0.

```
H1 <- list(constraints = c(0,1,0,0))
# "x1 > 0"
H2 <- list(constraints = rbind(c(0,1,0,0), c(0,0,1,0)))
# "x1 > 0; x2 > 0"
```

The GORIC values and weights are obtained via:

```
# GORIC
set.seed(123) # Set seed value
out <- goric(fit.lm, hypotheses = list(H1, H2))
#summary(out)
out</pre>
```

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

	model	loglik	penalty	goric	loglik.weights	penalty.weights	goric.weights	goric.weight
1	H1	-3.295	4.500	15.589	0.333	0.284	0.284	
2	H2	-3.295	3.847	14.284	0.333	0.545	0.545	
3	${\tt unconstrained}$	-3.295	5.000	16.589	0.333	0.172	0.172	

Note: Hypotheses 'H1' and 'H2' have equal likelihood values (i.e., the hypotheses overlap). The GORIC(A

The order-restricted hypothesis 'H2' is not weak, with 1.921 times more support than H1.

and the GORICA values and weights via:

```
# GORICA
set.seed(123) # Set seed value
out_gorica <- goric(fit.lm, hypotheses = list(H1, H2), type = "gorica")
#summary(out_gorica)
out_gorica</pre>
```

restriktor (0.5-90): generalized order-restricted information criterion approximation:

Results:

	model	loglik	penalty	gorica	loglik.weights	penalty.weights	gorica.weights	gorica.weigl
1	H1	3.622	3.500	-0.244	0.333	0.284	0.284	
2	H2	3.622	2.847	-1.549	0.333	0.545	0.545	
3	unconstrained	3.622	4.000	0.756	0.333	0.172	0.172	

Note: Hypotheses 'H1' and 'H2' have equal likelihood values (i.e., the hypotheses overlap). The GORIC(A

The order-restricted hypothesis 'H2' is not weak, with 1.921 times more support than H1.

Fitted unconstrained (g)lm object + list with constraints matrix (rhs and neq non-zero)

In this example, **rhs** and **neq** are not assumed to be 0. Please note that equality restrictions should be stated first in the constraints' list.

```
H1 <- list(constraints = c(0,1,0,0), rhs = 2)
# "x1 > 2"
H2 <- list(constraints = rbind(c(0,1,0,0), c(0,0,1,0)), rhs = c(1,0), neq = 1)
# "x1 = 1; x2 > 0"
```

The GORIC values and weights are obtained via:

```
# GORIC
set.seed(123) # Set seed value
out <- goric(fit.lm, hypotheses = list(H1, H2))
#summary(out)
out</pre>
```

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

```
goric loglik.weights penalty.weights goric.weights
          model loglik penalty
1
             H1 -8.212
                           4.500 25.425
                                                  0.007
                                                                   0.231
                                                                                  0.010
2
             H2 -6.197
                           3.500 19.394
                                                  0.052
                                                                   0.629
                                                                                 0.196
3
 unconstrained -3.295
                           5.000 16.589
                                                  0.941
                                                                   0.140
                                                                                 0.795
```

The unconstrained hypothesis is the best hypothesis in the set, meaning that all order-restricted hypothesis and the GORICA values and weights via:

```
# GORICA
set.seed(123) # Set seed value
out_gorica <- goric(fit.lm, hypotheses = list(H1, H2), type = "gorica")
#summary(out_gorica)
out_gorica</pre>
```

restriktor (0.5-90): generalized order-restricted information criterion approximation:

Results:

	model	loglik	penalty	gorica	loglik.weights	penalty.weights	gorica.weights
1	H1	-1.400	3.500	9.799	0.006	0.231	0.008
2	Н2	1.262	2.500	2.477	0.086	0.629	0.295
3	${\tt unconstrained}$	3.622	4.000	0.756	0.908	0.140	0.697

The unconstrained hypothesis is the best hypothesis in the set, meaning that all order-restricted hypothesis

GORICA

The upcoming analyses can only be performed by means of the *GORICA*. This is because, the GORICA only needs the parameter estimates or only those of interest (that is, those addressed in the hypotheses) and their covariance matrix. Because of this, it is applicable for a wider range of models (e.g., logistic regression and SEM models). When using this type of input, using GORICA is the default.

Numeric vector + character constraints

One needs to extract the estimates (of interest), as well as their variance-covariance matrix. Both can be extracted from the fit.lm object (also from non-(g)lm objects).

```
est <- coef(fit.lm)
VCOV <- vcov(fit.lm)</pre>
```

Next, the hypotheses need to be specified using the labels of 'est' (which can also be re-labelled as is done in the next subsection).

```
H1 <- "x1 > 0"
H2 <- "x1 > 0; x2 > 0"
```

Then, use the goric function to select the best model.

restriktor (0.5-90): generalized order-restricted information criterion approximation:

Results:

```
model loglik penalty gorica loglik.weights penalty.weights gorica.weights gorica.weig
1
            Н1
                3.622
                          3.500 -0.244
                                                 0.333
                                                                 0.284
                                                                                0.284
             H2
                 3.622
                          2.847 -1.549
                                                 0.333
                                                                 0.545
                                                                                0.545
                3.622
                          4.000 0.756
                                                 0.333
                                                                 0.172
                                                                                0.172
3 unconstrained
```

Note: Hypotheses 'H1' and 'H2' have equal likelihood values (i.e., the hypotheses overlap). The GORIC(A

The order-restricted hypothesis 'H2' is not weak, with 1.921 times more support than H1.

However, one could also use the structural parameters only, that is, the parameters used in all hypotheses in the set. In this case, the following code can be used:

restriktor (0.5-90): generalized order-restricted information criterion approximation:

Results:

100	Surus.							
	model	loglik	penalty	gorica	loglik.weights	penalty.weights	gorica.weights	gorica.weigl
1	H1	1.614	1.500	-0.227	0.333	0.284	0.284	
2	H2	1.614	0.847	-1.532	0.333	0.545	0.545	
3	unconstrained	1.614	2.000	0.773	0.333	0.172	0.172	

--

Note: Hypotheses 'H1' and 'H2' have equal likelihood values (i.e., the hypotheses overlap). The GORIC(A

The order-restricted hypothesis 'H2' is not weak, with 1.921 times more support than H1.

Now, the exact same weights are obtained. However, the penalties are two points lower than before, which is

due to the fact that two unconstrained/free parameters are left out. The log-likelihoods also change. But, when comparing the support for the hypotheses, these differences cancel out.

Relabeled numeric vector + character constraints

By default, the names/labels of the parameter estimates are based on variable names in the model (and in case of a factor, it is also based on the different levels it can take on). Using other names/labels often makes more sense. Then, one can specify the hypotheses in terms of those labels. For example, one can do the following:

restriktor (0.5-90): generalized order-restricted information criterion approximation:

Results:

```
loglik penalty gorica loglik.weights penalty.weights gorica.weights
1
              H1
                   3.622
                            3.500
                                   -0.244
                                                     0.333
                                                                       0.284
                                                                                       0.284
2
              H2
                   3.622
                            2.847
                                                     0.333
                                                                       0.545
                                                                                       0.545
                                   -1.549
3
  unconstrained
                   3.622
                            4.000
                                    0.756
                                                     0.333
                                                                       0.172
                                                                                       0.172
```

Note: Hypotheses 'H1' and 'H2' have equal likelihood values (i.e., the hypotheses overlap). The GORIC(A

The order-restricted hypothesis 'H2' is not weak, with 1.921 times more support than H1.

'Manual' numeric vector + character constraints

Sometimes, one cannot extract the coefficients and variance-covariance matrix directly from an R-object; for example, due to the fact that previous analyses were performed by means of other software, or since it stems from another article. In these situations, it is also possible to manually insert the regression coefficients and the variance-covariance matrix.

restriktor (0.5-90): generalized order-restricted information criterion approximation:

Results:

	model	loglik	penalty	gorica	loglik.weights	penalty.weights	gorica.weights	gorica.weigl
1	H1	3.622	3.500	-0.244	0.333	0.284	0.284	
2	Н2	3.622	2.847	-1.549	0.333	0.545	0.545	
3	${\tt unconstrained}$	3.622	4.000	0.756	0.333	0.172	0.172	

Note: Hypotheses 'H1' and 'H2' have equal likelihood values (i.e., the hypotheses overlap). The GORIC(A

The order-restricted hypothesis 'H2' is not weak, with 1.921 times more support than H1.

#Numeric vector + list with constraints matrix (rhs, neq)

When one only wants to use a list with a constraints matrix, the following code can be used:

restriktor (0.5-90): generalized order-restricted information criterion approximation:

Results:

	model	loglik	penalty	gorica	loglik.weights	penalty.weights	gorica.weights	gorica.weigl
1	H1	3.622	3.500	-0.244	0.333	0.284	0.284	
2	Н2	3.622	2.847	-1.549	0.333	0.545	0.545	
3	${\tt unconstrained}$	3.622	4.000	0.756	0.333	0.172	0.172	

Note: Hypotheses 'H1' and 'H2' have equal likelihood values (i.e., the hypotheses overlap). The GORIC(A

The order-restricted hypothesis 'H2' is not weak, with 1.921 times more support than H1.

Standardized data

If estimates of continuous predictor variables are compared (e.g., "x1 < x2"), then one should standardize the data. To demonstrate this, new data will be generated. In the data, the contribution of the variables to the dependent variable will differ. Below, the vector of ratios of these contributions is set to = c(1, 1.5, 2). This, then reflects (the ratios of) the population regression coefficient values. It means that the contribution to the outcome variable y, increases from x1 to x3, where that of x2 is 1.5 and that of x3 is 2 times as large as that of x1.

Note. Since there is only one outcome, the outcome does not need to be standardized.

Now, fit the regression model, and specify a hypothesis by means of character constraints.

```
fit.lm_s <- lm(y ~ -1 + x1 + x2 + x3, data = data_s)
H1 <- "x1 < x2"
# vs its complement</pre>
```

Then, calculate the GORIC values and weights:

```
# GORIC
set.seed(123) # Set seed value
out_s <- goric(fit.lm, hypotheses = list(H1))
#summary(out_s, brief = FALSE)
out_s</pre>
```

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

```
        model
        loglik
        penalty
        goric
        loglik.weights
        penalty.weights
        goric.weights

        1
        H1
        -5.447
        4.500
        19.895
        0.104
        0.500
        0.104

        2
        complement
        -3.295
        4.500
        15.589
        0.896
        0.500
        0.896
```

The order-restricted hypothesis 'H1' has 0.12 times more support than its complement.

Defining parameters

In restriktor, it is also possible to specify hypotheses in terms of linear functions of the parameters. For instance, in case of adjusted means, you can specify the restrictions in two ways:

- 1. You can write them out yourself (using the parameter/variable names from an R-object, like lm).
- 2. You can first specify the adjusted means (below called "m1" to "m4") and specify the hypotheses in terms of those:

```
H1 <- ' m1 := .Intercept.
    m2 := .Intercept. + facialBurns
    m3 := .Intercept. + gender
    m4 := .Intercept. + facialBurns + gender + gender.facialBurns
    m1 < m4
    m2 < m4
    m3 < m4 '</pre>
```

For more details, please see Vanbrabant, Van Loey, and Kuiper 2020). However, please note that this code cannot be run now, since the variables and, more importantly, the parameters are labeled differently. One can run:

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

```
        model
        loglik
        penalty
        goric
        loglik.weights
        penalty.weights
        goric.weights

        1
        H1
        -6.610
        3.879
        20.978
        0.035
        0.609
        0.054

        2
        complement
        -3.295
        4.321
        15.232
        0.965
        0.391
        0.946
```

The order-restricted hypothesis 'H1' has 0.06 times more support than its complement.

Types of comparisons

There are three types of comparisons: "none", "unconstrained", and "complement". Subsequently, it is shown, for the last type, what output can be asked for, which of course holds for all examples.

Comparison = "none""

If comparison = "none", then only the hypotheses of interest are inspected. This can lead to choosing the best hypothesis out of a set of weak hypotheses. Hence, one should only use this if the hypotheses cover the whole parameter space, that is, cover all possible theories/hypotheses.

```
H1 <- "x1 > 0"
H2 <- "x1 > 0; x2 > 0"

set.seed(123) # Set seed value
out <- goric(fit.lm, hypotheses = list(H1, H2), comparison = "none")
#summary(out)
out
```

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

```
goric loglik.weights penalty.weights goric.weights
  model loglik penalty
     H1 -3.295
                   4.500 15.589
                                           0.500
                                                            0.342
                                                                           0.342
1
2
     H2
         -3.295
                   3.847
                         14.284
                                           0.500
                                                            0.658
                                                                           0.658
```

Note: Hypotheses 'H1' and 'H2' have equal likelihood values (i.e., the hypotheses overlap). The GORIC(A

Comparison = "unconstrained"

If comparison = "unconstrained", then the unconstrained / unrestricted / classical alternative hypothesis is included in the set. This safeguards from choosing a weak hypothesis as the best one. Note that this (i.e., comparison = "unconstrained") is default in case of multiple hypotheses.

```
H1 <- "x1 > 0"
H2 <- "x1 > 0; x2 > 0"

# GORIC
set.seed(123) # Set seed value
out <- goric(fit.lm, hypotheses = list(H1, H2))
# or GORICA:
# out <- goric(fit.lm, H1, H2, type = "gorica")
#summary(out)
out</pre>
```

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

	model	loglik	penalty	goric	loglik.weights	penalty.weights	goric.weights	goric.weight
1	H1	-3.295	4.500	15.589	0.333	0.284	0.284	
2	H2	-3.295	3.847	14.284	0.333	0.545	0.545	
3	${\tt unconstrained}$	-3.295	5.000	16.589	0.333	0.172	0.172	

Note: Hypotheses 'H1' and 'H2' have equal likelihood values (i.e., the hypotheses overlap). The GORIC(A

The order-restricted hypothesis 'H2' is not weak, with 1.921 times more support than H1.

Since at least one of, even both, H1 and H2 are not weak, one can compare the support for H1 versus H2 (where H2 is 1.921 times more supported).

Comparison = "complement"

Currently, comparison = "complement" only works for one hypothesis and not for a whole set of hypotheses. However, in the latter case, most probably the interest lies in comparing the support for the theory-based hypotheses, which is the same irrespective of choice of failsafe.

When the complement of the hypothesis of interest is evaluated, it acts like the competing hypothesis. Since there is per definition no overlap between the hypothesis and its complement, this is more powerful then using the unconstrained instead. Therefore, it (i.e., comparison = "complement") is the default in case of one theory-based hypothesis.

H1 vs its complement

```
H1 <- "x1 > 0"
# us its complement
```

```
# GORIC
set.seed(123) # Set seed value
out <- goric(fit.lm, hypotheses = list(H1))</pre>
summary(out, brief = FALSE)
restriktor (0.5-90): generalized order-restricted information criterion:
Results:
       model loglik penalty goric loglik.weights penalty.weights goric.weights
                       4.500 15.589
          H1
              -3.295
                                                1.000
                                                                 0.500
                                                                               1.000
2 complement -15.009
                        4.500 39.018
                                                0.000
                                                                 0.500
                                                                               0.000
The order-restricted hypothesis 'H1' has 122335.38 times more support than its complement.
Ratio GORIC-weights:
             vs. H1 vs. complement
           1.00e+00
                          1.22e+05
complement 0.00e+00
                          1.00e+00
Ratio loglik-weights:
             vs. H1 vs. complement
           1.00e+00
                         1.22e+05
complement 0.00e+00
                          1.00e+00
Ratio penalty-weights:
           vs. H1 vs. complement
H1
               1
                               1
complement
              1
                               1
Order-restricted coefficients:
           (Intercept) x1
                                x2
                                        хЗ
                1.248 1.407 0.826 0.811
                1.144 0.000 1.488 0.645
complement
Restriction matrices:
$H1
   (Intercept) x1 x2 x3
                          op rhs active
                         >= 0
            0 1 0 0
$complement
[1] not H1
summary(out)
```

 ${\tt restriktor}\ ({\tt 0.5-90}) \colon {\tt generalized}\ {\tt order-restricted}\ {\tt information}\ {\tt criterion} \colon$

Results:

model loglik penalty goric loglik.weights penalty.weights goric.weights

```
1 H1 -3.295 4.500 15.589 1.000 0.500 1.000
2 complement -15.009 4.500 39.018 0.000 0.500 0.000
---
The order-restricted hypothesis 'H1' has 122335.38 times more support than its complement.
```

Ratio GORIC-weights:

vs. H1 vs. complement
H1 1.00e+00 1.22e+05
complement 0.00e+00 1.00e+00

--
Ratio loglik-weights:

vs. H1 vs. complement
H1 1.00e+00 1.22e+05
complement 0.00e+00 1.00e+00
--
Ratio penalty-weights:

vs. H1 vs. complement

order-restricted hypotheses:

H1: x1 > 0 out

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

 model
 loglik
 penalty
 goric
 loglik.weights
 penalty.weights
 goric.weights

 1
 H1
 -3.295
 4.500
 15.589
 1.000
 0.500
 1.000

 2
 complement
 -15.009
 4.500
 39.018
 0.000
 0.500
 0.500

The order-restricted hypothesis 'H1' has 122335.38 times more support than its complement.

H2 vs its complement

```
H2 <- "x1 > 0; x2 > 0"
# vs its complement

# GORIC
set.seed(123) # Set seed value
out <- goric(fit.lm, hypotheses = list(H2))
#summary(out)
out</pre>
```

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

model loglik penalty goric loglik.weights penalty.weights goric.weights

1	H1	-3.295	3.847	14.284	0.999	0.691	1.000
2	complement	-10.375	4.653	30.055	0.001	0.309	0.000

The order-restricted hypothesis 'H1' has 2658.77 times more support than its complement.

Note on comparisons

Please note that the obtained weights for the two hypotheses cannot be compared. If this is the goal of the analysis, one should evaluate them simultaneously in one set, as done earlier.

Different types of output

The command out gives the default results (i.e., per model / hypothesis the log-likelihood, penalty, GORIC(A), and GORIC(A)-weights).

out

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

	model	loglik	penalty	goric	loglik.weights	penalty.weights	goric.weights
1	H1	-3.295	3.847	14.284	0.999	0.691	1.000
2	complement	-10.375	4.653	30.055	0.001	0.309	0.000

The order-restricted hypothesis 'H1' has 2658.77 times more support than its complement.

The command summary(out) gives, besides the results, also the relative GORIC(A)-weights matrix.

summary(out)

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

	model	loglik	penalty	goric	loglik.weights	penalty.weights	goric.weights
1	H1	-3.295	3.847	14.284	0.999	0.691	1.000
2	complement	-10.375	4.653	30.055	0.001	0.309	0.000

The order-restricted hypothesis 'H1' has 2658.77 times more support than its complement.

Ratio GORIC-weights:

	vs. H1	vs.	complement
H1	1		2659
complement	0		1

Ratio loglik-weights:

	vs. H1	vs.	complement
H1	1.000		1188.275
complement	0.001		1.000

Ratio penalty-weights:

	vs. H1	vs.	complement
H1	1.000		2.238
complement	0.447		1.000

order-restricted hypotheses:

```
H1:
```

```
x1 > 0; x2 > 0
```

The command summary(out, brief = FALSE) gives also the order / inequality restricted coefficients (orderrestricted mle's) and constraint matrices.

```
summary(out, brief = FALSE)
```

restriktor (0.5-90): generalized order-restricted information criterion:

Results:

	model	loglik	penalty	goric	loglik.weights	penalty.weights	goric.weights
1	H1	-3.295	3.847	14.284	0.999	0.691	1.000
2	complement	-10.375	4.653	30.055	0.001	0.309	0.000

The order-restricted hypothesis 'H1' has 2658.77 times more support than its complement.

Ratio GORIC-weights:

	vs.	H1	vs.	complement
H1		1		2659
complement		0		1

Ratio loglik-weights:

	vs. H1	vs.	complement
H1	1.000		1188.275
complement	0.001		1.000

Ratio penalty-weights:

	vs. H1	vs.	complement
H1	1.000		2.238
complement	0.447		1.000

Order-restricted coefficients:

	(Intercept)	x1	x2	x3
H1	1.248	1.407	0.826	0.811
complement	1.236	1.781	0.000	0.444

Restriction matrices:

\$H1

active	rhs	op	x3	x2	x1	(Intercept)	
no	0	>=	0	0	1	0	1:
no	0	>=	0	1	0	0	2:

\$complement

[1] not H1

Furthermore, one can ask for different elements of the output by means of the following commands:

- out\$result gives results (i.e., per model / hypothesis the log-likelihood, penalty, GORIC(A), and GORIC(A)-weights).
- out\$ratio.gw gives the relative GORIC(A)-weights matrix, which gives the relative support of an hypothesis versus another.
- outsormle gives the order / inequality restricted coefficients (order-restricted mle's).
- coef(out) also gives the order / inequality restricted coefficients (order-restricted mle's).
- out\$type states what type of analysis is used (GORIC or GORICA).
- out\$comparison states what type of comparison is used (none, unconstrained, complement).
- out\$constraints gives the constraints matrices.
- out\$rhs gives the right hand side (rhs) of the constraints.
- out\$neq gives the number of equalities (neq) in the constraints, where the first neq are then equalities.

If many restrictions: Another method to calculate the penalty

Working with a lot of restrictions and a lot of parameters calculations increases the computation time, which has to do with the calculation of the level probability needed for the penalty term. There are two methods that can be used in calculating the penalty. The default method is often much faster (if the number of parameters is not too high) and needs less input specification. It can, however, not deal with hypotheses that are not of full row-rank (which easily happens if you specify many restrictions). In that case, restriktor uses automatically the other (bootstrap) method.

To use this bootstrap method, use:

restriktor (0.5-90): generalized order-restricted information criterion approximation:

Results:

```
model
                                 gorica loglik.weights penalty.weights
                                                                           gorica.weights
                loglik
                       penalty
           H1
                 3.622
                          3.502
                                 -0.240
                                                   1.000
                                                                    0.499
                                                                                     1.000
2
  complement
               -24.612
                          3.498
                                 56.220
                                                   0.000
                                                                    0.501
                                                                                     0.000
```

The order-restricted hypothesis 'H1' has 1820353968300.10 times more support than its complement.

Note on not full row-rank

If the restriction matrix is not of full row-rank, this means one of the following:

- 1. Redundant restriction, either:
 - a) leave the redundant one out (goric function does this for you), or:
 - b) use another (more time-consuming) way of obtaining the level probabilities for the penalty term: Bootstrapping, as discussed above (goric function does this by default).
- 2. Range restrictions (e.g., -2 < group1 < 2), which can be evaluated, but there is a sensitivity (like with a prior in a Bayes factor), which currently cannot be checked for.

3.	Conflicting restrictions (e.g., $2 < \text{group1} < -2$), which can evidently never hold and is thus impossible to evaluate. In this case, one should delete the incorrect restriction.	3