

Heuristic Function Analysis | Planning Search

Udacity Artificial Intelligence Nanodegree

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Abstract

In this project, we are tasked to solve deterministic logistics planning problems for an Air Cargo transport system using a planning search agent. With progression search algorithms, optimal plans for each problem are computed. There is no simple distance heuristic to aid the agent. Instead, we implemented domain-independent heuristics.

Action Schema

Problem 1 Initial State and Goal

Init($\text{At}(\text{C1}, \text{SFO}) \wedge \text{At}(\text{C2}, \text{JFK})$
 $\wedge \text{At}(\text{P1}, \text{SFO}) \wedge \text{At}(\text{P2}, \text{JFK})$
 $\wedge \text{Cargo}(\text{C1}) \wedge \text{Cargo}(\text{C2})$
 $\wedge \text{Plane}(\text{P1}) \wedge \text{Plane}(\text{P2})$
 $\wedge \text{Airport}(\text{JFK}) \wedge \text{Airport}(\text{SFO})$)
Goal($\text{At}(\text{C1}, \text{JFK}) \wedge \text{At}(\text{C2}, \text{SFO})$)

Problem 2 Initial State and Goal

Init($\text{At}(\text{C1}, \text{SFO}) \wedge \text{At}(\text{C2}, \text{JFK}) \wedge \text{At}(\text{C3}, \text{ATL})$
 $\wedge \text{At}(\text{P1}, \text{SFO}) \wedge \text{At}(\text{P2}, \text{JFK}) \wedge \text{At}(\text{P3}, \text{ATL})$
 $\wedge \text{Cargo}(\text{C1}) \wedge \text{Cargo}(\text{C2}) \wedge \text{Cargo}(\text{C3})$
 $\wedge \text{Plane}(\text{P1}) \wedge \text{Plane}(\text{P2}) \wedge \text{Plane}(\text{P3})$
 $\wedge \text{Airport}(\text{JFK}) \wedge \text{Airport}(\text{SFO}) \wedge \text{Airport}(\text{ATL})$)
Goal($\text{At}(\text{C1}, \text{JFK}) \wedge \text{At}(\text{C2}, \text{SFO}) \wedge \text{At}(\text{C3}, \text{SFO})$)

Problem 3 Initial State and Goal

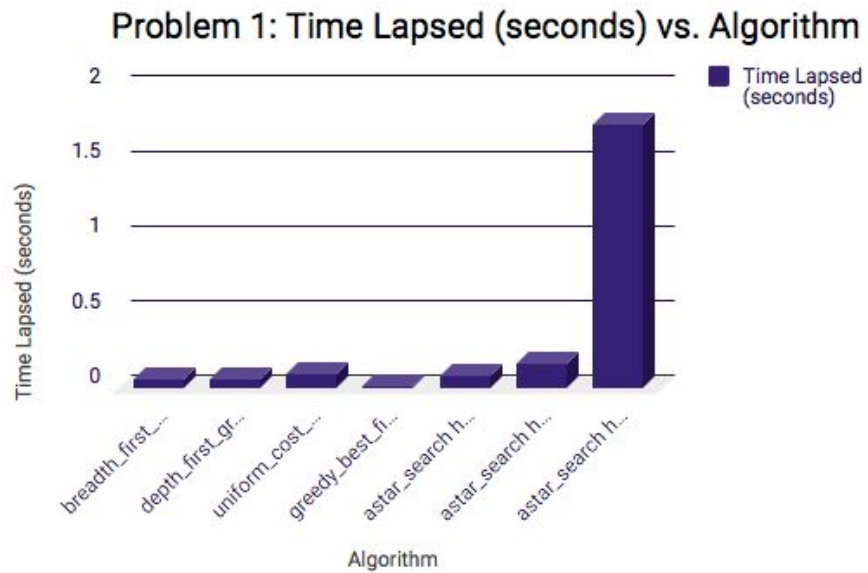
Init($\text{At}(\text{C1}, \text{SFO}) \wedge \text{At}(\text{C2}, \text{JFK}) \wedge \text{At}(\text{C3}, \text{ATL}) \wedge \text{At}(\text{C4}, \text{ORD})$
 $\wedge \text{At}(\text{P1}, \text{SFO}) \wedge \text{At}(\text{P2}, \text{JFK})$
 $\wedge \text{Cargo}(\text{C1}) \wedge \text{Cargo}(\text{C2}) \wedge \text{Cargo}(\text{C3}) \wedge \text{Cargo}(\text{C4})$
 $\wedge \text{Plane}(\text{P1}) \wedge \text{Plane}(\text{P2})$
 $\wedge \text{Airport}(\text{JFK}) \wedge \text{Airport}(\text{SFO}) \wedge \text{Airport}(\text{ATL}) \wedge \text{Airport}(\text{ORD})$)
Goal($\text{At}(\text{C1}, \text{JFK}) \wedge \text{At}(\text{C3}, \text{JFK}) \wedge \text{At}(\text{C2}, \text{SFO}) \wedge \text{At}(\text{C4}, \text{SFO})$)

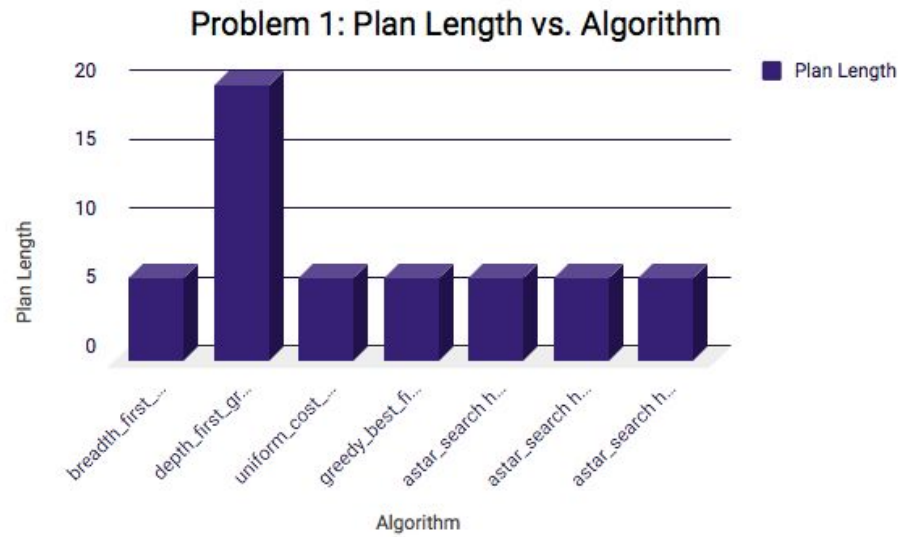
Results

Per the recommendation of Udacity, I utilized PyPy for running the searches.

Problem 1 Initial State and Goal

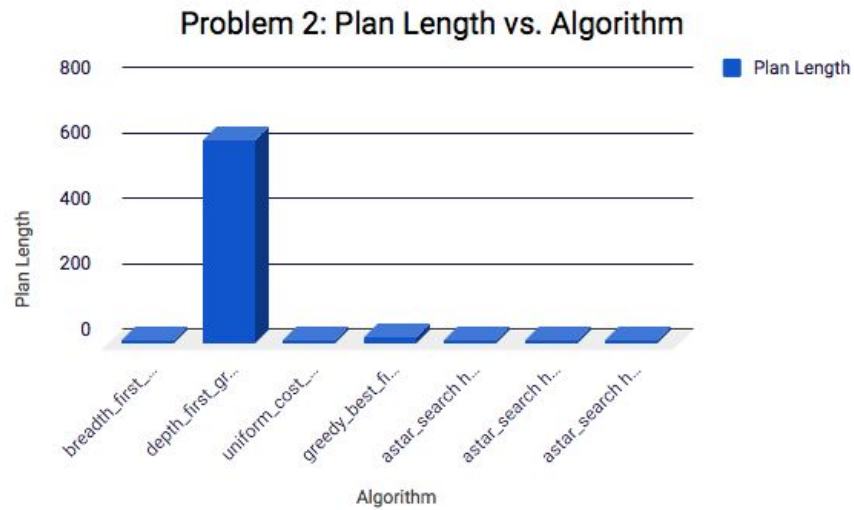
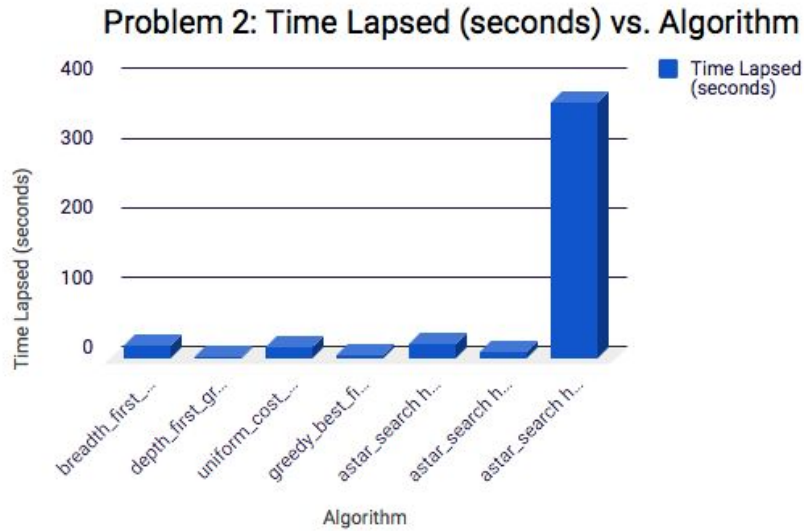
| PROBLEM 1 | | | | | |
|-------------------------------------|------------|------------|-----------|-----------------------|-------------|
| Algorithm | Expansions | Goal Tests | New Nodes | Time Lapsed (seconds) | Plan Length |
| breadth_first_search | 43 | 56 | 180 | 0.05459801201 | 6 |
| depth_first_graph_search | 21 | 22 | 84 | 0.05979764694 | 20 |
| uniform_cost_search | 55 | 57 | 224 | 0.08602173103 | 6 |
| greedy_best_first_graph_search h_1 | 7 | 9 | 28 | 0.009701812989 | 6 |
| astar_search h_1 | 55 | 57 | 224 | 0.07332619798 | 6 |
| astar_search h_ignore_preconditions | 51 | 53 | 208 | 0.162204607 | 6 |
| astar_search h_pg_levelsum | 55 | 57 | 224 | 1.759035398 | 6 |





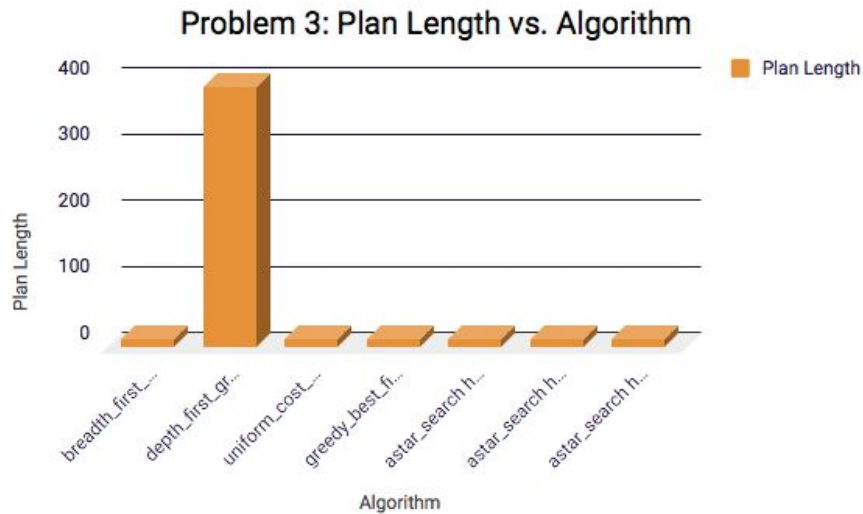
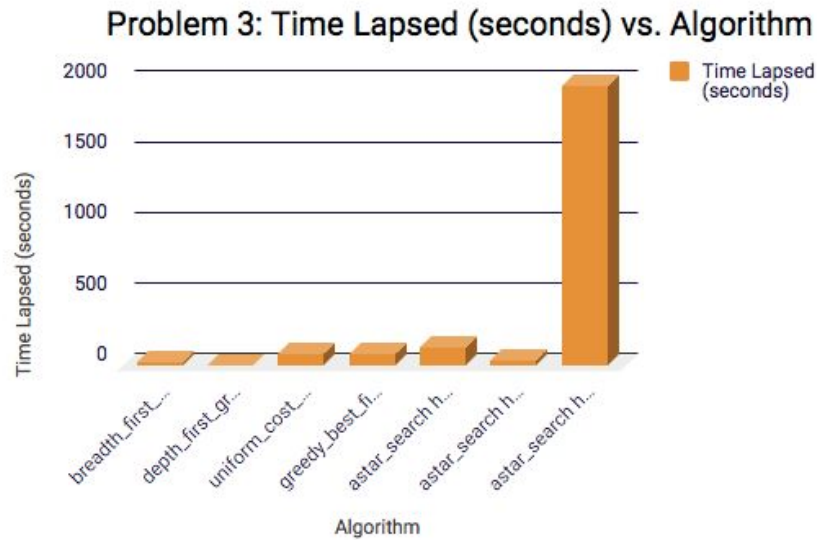
Problem 2 Initial State and Goal

| PROBLEM 2 | | | | | |
|-------------------------------------|------------|------------|-----------|-----------------------|-------------|
| Algorithm | Expansions | Goal Tests | New Nodes | Time Lapsed (seconds) | Plan Length |
| breadth_first_search | 3343 | 4609 | 30509 | 17.23337885 | 9 |
| depth_first_graph_search | 624 | 625 | 5602 | 1.410260129 | 619 |
| uniform_cost_search | 4852 | 4854 | 44030 | 15.87766461 | 9 |
| greedy_best_first_graph_search h_1 | 990 | 992 | 8910 | 3.668398147 | 17 |
| astar_search h_1 | 4852 | 4854 | 44030 | 21.41859974 | 9 |
| astar_search h_ignore_preconditions | 4297 | 4299 | 39110 | 8.666144078 | 9 |
| astar_search h_pg_levelsum | 4852 | 4854 | 44030 | 366.9104339 | 9 |



Problem 3 Initial State and Goal

| PROBLEM 3 | | | | | |
|-------------------------------------|------------|------------|-----------|-----------------------|-------------|
| Algorithm | Expansions | Goal Tests | New Nodes | Time Lapsed (seconds) | Plan Length |
| breadth_first_search | 14663 | 18098 | 129631 | 19.49652567 | 12 |
| depth_first_graph_search | 408 | 409 | 3364 | 0.648579923 | 392 |
| uniform_cost_search | 18223 | 18225 | 159618 | 78.76316557 | 12 |
| greedy_best_first_graph_search_h_1 | 18223 | 18225 | 159618 | 78.70390829 | 12 |
| astar_search_h_1 | 16993 | 16995 | 149302 | 120.3517763 | 12 |
| astar_search_h_ignore_preconditions | 16993 | 16995 | 149302 | 35.15960233 | 12 |
| astar_search_h_pg_levelsum | 18223 | 18225 | 159168 | 1972.053674 | 12 |



Optimal Plans

Optimal Plan for Problem 1

Load(C1, P1, SFO)
 Load(C2, P2, JFK)
 Fly(P1, SFO, JFK)
 Fly(P2, JFK, SFO)
 Unload(C1, P1, JFK)
 Unload(C2, P2, SFO)

Greedy Best First Graph Search was the clear winner for locating the goal state in Problem 1 by completing in the lowest amount of time and accurately locating the optimal plan. The algorithms were almost all equal in time to find the goal state except for A* search with the 'h_pg_levelsum' option (400%

longer). All algorithms except Depth First search located the minimum plan length (6) instead of DPL's return of 20.

Optimal Plan for Problem 2

```
Load(C1, P1, SFO)
Load(C2, P2, JFK)
Load(C3, P3, ATL)
Fly(P2, JFK, SFO)
Unload(C2, P2, SFO)
Fly(P1, SFO, JFK)
Unload(C1, P1, JFK)
Fly(P3, ATL, SFO)
Unload(C3, P3, SFO)
```

Greedy Best First Graph Search is the winner again by finding the optimal plan in the lowest amount of time with the least amount of expansions. Since Problem 2 increases in complexity, DPL's outlier of plans (619) versus the optimal plan (12) becomes more exacerbated.

Optimal Plan for Problem 3

```
Load(C1, P1, SFO)
Load(C2, P2, JFK)
Fly(P1, SFO, ATL)
Load(C3, P1, ATL)
Fly(P2, JFK, ORD)
Load(C4, P2, ORD)
Fly(P2, ORD, SFO)
Fly(P1, ATL, JFK)
Unload(C4, P2, SFO)
Unload(C3, P1, JFK)
Unload(C1, P1, JFK)
Unload(C2, P2, SFO)
```

Finally, for the most complex problem, Problem 3, the recommended algorithm is **A* Search (Ignore Preconditions)** clause because it was the most performant, located the goal state and minimized the nodes explored.

Analysis

Non-heuristic Planning Solution Searches

Breadth First Search (BFS) could always find optimal solution with an average number of expansions. Since BFS does not keep track of explored nodes, the number of expansions were significantly higher than uninformed graph search.

Depth First Search (DFS) kept track of all explored nodes and ended up expanding a lower number of nodes for each problem. Since DPL expands the deepest nodes first without any heuristic, it ends up going down a non-optimal path (Problem 2 and 3 were significantly sub-optimal).

Uniform Cost Search (UCS) always found the optimal path. It expanded significantly more nodes than Depth First Search (and was often far slower). but since it keeps track of explored nodes, it was faster than Breadth First Search. In a choice between BFS, DFS and USC, USC will deliver a correct result in a reasonable amount of time.

Automatic Heuristics

A* Search (Ignore Preconditions) - In this search, all preconditions are dropped. This can lead to operations achieving multiple goals and can undo the effects of others. For the Cargo problems, this algorithm always found the optimal path to the goal state.

A* Search (h_pg_levelsum) - In this search, the level sum heuristic is used which follows the subgoal independence assumption and returned the sum of the level costs of the goals. For all of the problems, it took the most amount of time to complete.

Bibliography

Russell, S. and Norvig, P. Artificial Intelligence, A Modern Approach, Third Edition, Sec 10.3.1 Planning graphs for heuristic estimation, LEVEL SUM HEURISTIC

Russell, S. and Norvig, P. Artificial Intelligence, A Modern Approach, Third Edition, Sec 10.2.3 Heuristics for planning, IGNORE PRECONDITIONS HEURISTIC