

Scotogenic seesaw and baryogenesis

with gauged Baryon number



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Focus on

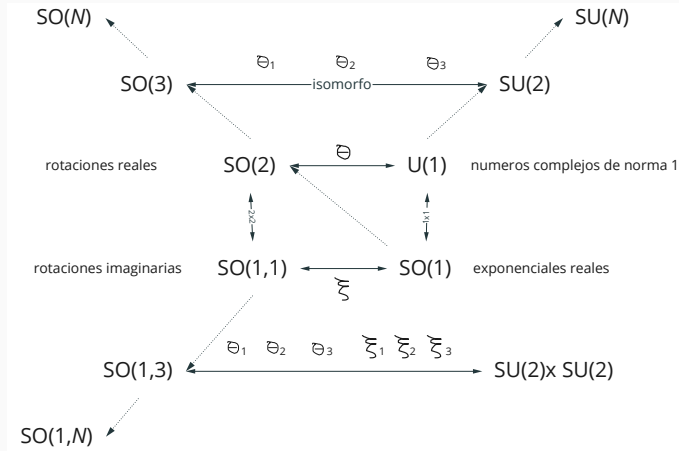
[arXiv:2205.05762](https://arxiv.org/abs/2205.05762)

In collaboration with

Andrés Rivera (UdeA), Walter Tangarife (Loyola University Chicago)

Model building

Lie groups



$$U = \exp \left(i \sum_j T_j \theta^j \right), \quad (1)$$

where θ^j are the parameters of the transformation and T_j are the generators.

Consider the 1×1

$$K = -i, \quad (2)$$

which generates an element of dilaton group, $SO(1)$, $R(\xi)$

$$\lambda(\xi) = e^{\xi}, \quad (3)$$

which are just the group of the real exponentials. Such a number can be transformed as

$$x \rightarrow x' = e^{\xi} x, \quad (4)$$

that corresponds to a boost by e^{ξ} . We can define the invariant scalar product just as the division of real numbers, such that

$$x \cdot y \rightarrow x' \cdot y' \equiv \frac{x'}{y'} = \frac{e^{\xi} x}{e^{\xi} y} = \frac{x}{y} = x \cdot y. \quad (5)$$

Queremos obtener una representación 2×2 del álgebra

$$K = \begin{pmatrix} 0 & -i \\ -i & 0 \end{pmatrix} \rightarrow K^2 = -\mathbf{1}, \quad (6)$$

que genera un elemento del grupo SO(1, 1) con *parámetro* ξ

$$\Lambda = \exp(i\xi K) = \begin{pmatrix} \cosh \xi & \sinh \xi \\ \sinh \xi & \cosh \xi \end{pmatrix}, \quad (7)$$

La transformación de una coordenada temporaloide y otra espacialoide ($c = 1$)

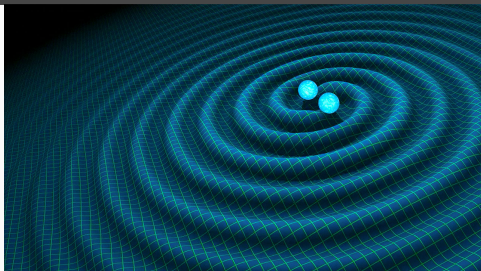
$$\begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} x^0 \\ x^1 \end{pmatrix} \rightarrow \begin{pmatrix} x'^0 \\ x'^1 \end{pmatrix} \begin{pmatrix} \cosh \xi & \sinh \xi \\ \sinh \xi & \cosh \xi \end{pmatrix} \begin{pmatrix} x^0 \\ x^1 \end{pmatrix}$$

$$\cosh \xi = \gamma = \frac{1}{\sqrt{1 - v^2}}$$

Special: parameter ξ or v is constant, e.g, inertial system invariance: *Global* conservation of E and \mathbf{p} (still action at a distance!)

General: parameter $\xi(t, \mathbf{x})$ or $v(t, \mathbf{x})$ is constant, e.g, accelerated system invariance: *Local* conservation of E and \mathbf{p}

Inestability of binary particle systems



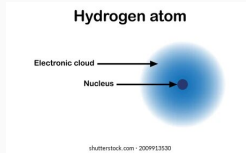
Gravitational wave discovery by LIGO



credits: science.org

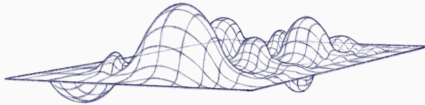
Noether's paradigm

U(1): From special θ to general $\theta(t, \mathbf{x})$



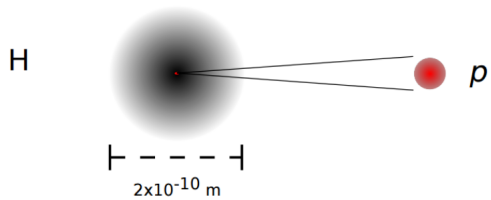
What is a *particle wavicle*? <https://www.quantamagazine.org/what-is-a-particle-20201112/>

Is a “Quantum Excitation of a Field”



Is a “Irreducible Representation of a Group”



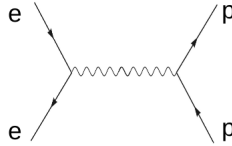
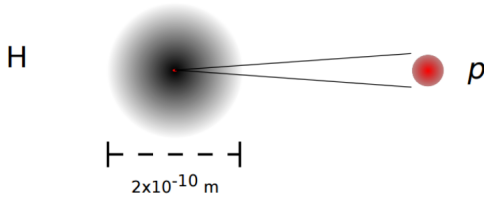


Interacción \rightarrow Fuerza = $\Delta p / \Delta t$

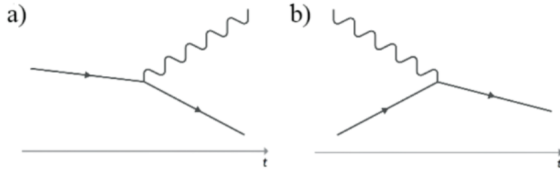
Introducción

Campos de materia \longrightarrow

Campos de radiación $\sim\sim\sim$



[doi:10.1088/1742-6596/1287/1/012045](https://doi.org/10.1088/1742-6596/1287/1/012045)



Emisión

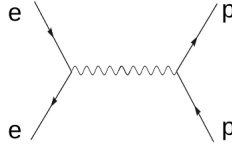
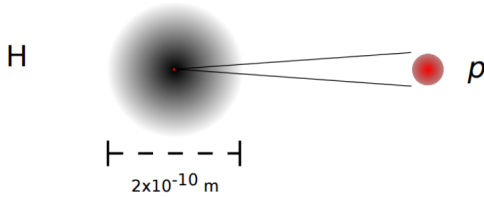
absorción

Interacción \rightarrow Fuerza = $\Delta p / \Delta t$

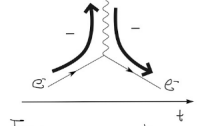
Introducción

Campos de materia \longrightarrow

Campos de radiación \sim



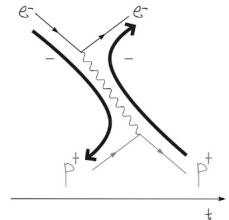
Single charge



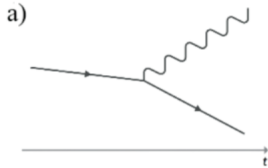
Fuerza $\frac{\Delta p}{\Delta t} \neq 0$

$$(e^-)^* = e^+$$

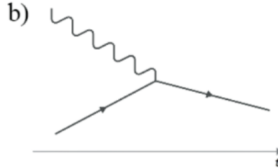
\sim fotón neutro



[doi:10.1088/1742-6596/1287/1/012045](https://doi.org/10.1088/1742-6596/1287/1/012045)



Emisión



absorción

$$e^- \rightarrow e^{-iEt}$$

$$e^+ \rightarrow e^{-iE(-t)}$$

Under a general Lorentz transformation we have.

$$A^\mu(x) \rightarrow A'^\mu(x) = \Lambda^\mu{}_\nu A^\nu(\Lambda^{-1}x). \quad (8)$$

A pure underscript 4-vector is

$$\partial_\mu = \frac{\partial}{\partial x^\mu} = \left(\frac{\partial}{\partial t}, \frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z} \right) = (\partial_0, \nabla). \quad (9)$$

From

$$\frac{1}{x'^\mu} = (\Lambda^{-1})^\nu{}_\mu \frac{1}{x^\nu}, \quad (10)$$

the tranformation properties for a $\partial_\mu = \partial/\partial x^\mu$, are

$$\partial'_\mu = (\Lambda^{-1})^\nu{}_\mu \partial_\nu. \quad (11)$$

In this way, the invariant scalar product between the 4-vector field and the four-gradient is just

$$\partial_\mu A^\mu \rightarrow \partial'_\mu A'^\mu = \partial_\mu A^\mu . \quad (12)$$

Name	Symbol	SU(N)
scalar N -plet	Ψ	$U\Psi$
scalar anti- N -plet	Ψ^\dagger	$\Psi^\dagger U^\dagger$

Name	Symbol	Lorentz
Photon	A^μ	$\Lambda^\mu{}_\nu A^\nu$
4-gradient	∂_μ	$\partial_\nu (\Lambda^{-1})^\nu{}_\mu$

Table 1: Scalar products: $\Psi^\dagger\Psi$, $\partial_\mu A^\mu$, $A^\nu A_\nu$, $\partial_\mu\partial^\mu$

Name	Symbol	Lorentz	$U(1)$
e_L : electron left	ξ_α	$S_\alpha{}^\beta \xi_\beta$	$e^{i\theta} \xi_\alpha$
$(e_L)^\dagger$: positron right	$(\xi_\alpha)^\dagger = \xi_{\dot{\alpha}}$	$\xi_{\dot{\beta}}^\dagger [S^\dagger]_{\dot{\alpha}}{}^{\dot{\beta}}$	$\xi_{\dot{\alpha}}^\dagger e^{-i\theta}$
e_R : electron right	$(\eta^\alpha)^\dagger = \eta^{\dagger\dot{\alpha}}$	$[(S^{-1})^\dagger]^{\dot{\alpha}}{}_{\dot{\beta}} \eta^{\dagger\dot{\beta}}$	$e^{i\theta} \eta^{\dagger\dot{\alpha}}$
$(e_R)^\dagger$: positron left	η^α	$\eta^\beta [S^{-1}]_\beta{}^\alpha$	$e^{-i\theta} \eta^\alpha$

Table 2: electron components

Scalar products

- ~~$U(1)$~~ Majorana scalars: $\xi^\alpha \xi_\alpha + \xi_{\dot{\alpha}}^\dagger \xi^{\dagger\dot{\alpha}}, \eta^\alpha \eta_\alpha + \eta_{\dot{\alpha}}^\dagger \eta^{\dagger\dot{\alpha}}$.
- Dirac scalar: $\eta^\alpha \xi_\alpha + \xi_{\dot{\alpha}}^\dagger \eta^{\dagger\dot{\alpha}}$.
- Tensor under subgroup $SL(2, C)$ but vector under $SO(1, 3)$: $S^{\dagger\dot{\alpha}}_{\dot{\beta}} \bar{\sigma}^\mu{}^{\dot{\beta}\beta} S_\beta{}^\alpha = \Lambda^\mu{}_\nu \bar{\sigma}^\nu{}^{\dot{\alpha}\alpha}$

Name	Symbol	Lorentz	$U(1)$
e_L : electron left	ξ_α	$S_\alpha{}^\beta \xi_\beta$	$e^{i\theta} \xi_\alpha$
$(e_L)^\dagger$: positron right	$(\xi_\alpha)^\dagger = \xi_{\dot{\alpha}}^\dagger$	$\xi_{\dot{\beta}}^\dagger [S^\dagger]{}^{\dot{\beta}}{}_{\dot{\alpha}}$	$\xi_{\dot{\alpha}}^\dagger e^{-i\theta}$
e_R : electron right	$(\eta^\alpha)^\dagger = \eta^{\dagger\dot{\alpha}}$	$[(S^{-1})^\dagger]{}^{\dot{\alpha}}{}_{\dot{\beta}} \eta^{\dagger\dot{\beta}}$	$e^{i\theta} \eta^{\dagger\dot{\alpha}}$
$(e_R)^\dagger$: positron left	η^α	$\eta^\beta [S^{-1}]{}_\beta{}^\alpha$	$e^{-i\theta} \eta^\alpha$

Table 3: electron components

General theory: QED $\rightarrow D_\mu = i\partial_\mu - ieA_\mu, F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$

$$\xi^\alpha \rightarrow \xi'^\alpha = e^{i\theta(x)} \xi^\alpha$$

$$\eta_\alpha \rightarrow \eta'_\alpha = e^{-i\theta(x)} \eta_\alpha$$

$$D_\mu \xi^\alpha \rightarrow (D_\mu \xi^\alpha)' = e^{i\theta(x)} D_\mu \xi^\alpha$$

$$D_\mu \eta_\alpha \rightarrow (D_\mu \eta_\alpha)' = e^{-i\theta(x)} D_\mu \eta_\alpha$$

$$\mathcal{L} = i\xi_{\dot{\alpha}}^\dagger \bar{\sigma}^{\mu\dot{\alpha}\alpha} D_\mu \xi_\alpha + i\eta^\alpha \sigma_{\alpha\dot{\alpha}}^\mu D_\mu \eta^{\dagger\dot{\alpha}} - m \left(\eta^\alpha \xi_\alpha + \xi_{\dot{\alpha}}^\dagger \eta^{\dagger\dot{\alpha}} \right) - \frac{1}{4} F^{\mu\nu} F_{\mu\nu}$$

Name	Symbol	Lorentz	$U(1)$
e_L : electron left	ξ_α	$S_\alpha{}^\beta \xi_\beta$	$e^{i\theta} \xi_\alpha$
$(e_L)^\dagger$: positron right	$(\xi_\alpha)^\dagger = \xi_{\dot{\alpha}}^\dagger$	$\xi_{\dot{\beta}}^\dagger [S^\dagger]{}^{\dot{\beta}}{}_{\dot{\alpha}}$	$\xi_{\dot{\alpha}}^\dagger e^{-i\theta}$
e_R : electron right	$(\eta^\alpha)^\dagger = \eta^{\dagger \dot{\alpha}}$	$[(S^{-1})^\dagger]{}^{\dot{\alpha}}{}_{\dot{\beta}} \eta^{\dagger \dot{\beta}}$	$e^{i\theta} \eta^{\dagger \dot{\alpha}}$
$(e_R)^\dagger$: positron left	η^α	$\eta^\beta [S^{-1}]{}_\beta{}^\alpha$	$e^{-i\theta} \eta^\alpha$

Table 3: electron components

General theory: QED $\rightarrow D_\mu = i\partial_\mu - ieA_\mu$, $F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu$.

Dirac spinor

$$\begin{aligned}
 \xi^\alpha &\rightarrow \xi'^\alpha = e^{i\theta(x)} \xi^\alpha & \eta_\alpha &\rightarrow \eta'_\alpha = e^{-i\theta(x)} \eta_\alpha \\
 D_\mu \xi^\alpha &\rightarrow (D_\mu \xi^\alpha)' = e^{i\theta(x)} D_\mu \xi^\alpha & D_\mu \eta_\alpha &\rightarrow (D_\mu \eta_\alpha)' = e^{-i\theta(x)} D_\mu \eta_\alpha \\
 \mathcal{L} &= i \xi_{\dot{\alpha}}^\dagger \bar{\sigma}^\mu{}^{\dot{\alpha}\alpha} D_\mu \xi_\alpha + i \eta^\alpha \sigma_{\alpha\dot{\alpha}}^\mu D_\mu \eta^{\dagger \dot{\alpha}} - m \left(\eta^\alpha \xi_\alpha + \xi_{\dot{\alpha}}^\dagger \eta^{\dagger \dot{\alpha}} \right) - \frac{1}{4} F^{\mu\nu} F_{\mu\nu} \\
 \mathcal{L} &= i \bar{\psi} \gamma^\mu D_\mu \psi - m \bar{\psi} \psi - \frac{1}{4} F^{\mu\nu} F_{\mu\nu}.
 \end{aligned}$$

$$\begin{aligned}
 \psi &= \begin{pmatrix} e_L \\ e_R \end{pmatrix} \\
 \gamma^\mu &= \begin{pmatrix} 0 & \sigma^\mu \\ \bar{\sigma}^\mu & 0 \end{pmatrix} \\
 \bar{\psi} &= \psi^\dagger \gamma^0.
 \end{aligned}$$

Not mass, not charge

Field	Lorentz	$SU(2)_L$
$L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$	ξ_α	2

Denial

$$\mathcal{L} = i(L)^\dagger \bar{\sigma}^\mu D_\mu L - \frac{1}{4} W_{\mu\nu}^i W_i^{\mu\nu}$$

$SU(2)_L \times U(1)_Y$ 17 years later... (stages of grief \rightarrow 1967)

Not mass, **hypercharge**,

Field	Lorentz	$SU(2)_L$	$U(1)_Y$
$L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$	ξ_α	2	$-1/2$

Denial

$$\mathcal{L} = i(L)^\dagger \bar{\sigma}^\mu D_\mu L - \frac{1}{4} W_{\mu\nu}^i W_i^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu}$$

$SU(2)_L \times U(1)_Y$ 17 years later... (stages of grief \rightarrow 1967)

Not mass, **hypercharge**, not **Dirac**

Field	Lorentz	$SU(2)_L$	$U(1)_Y$
$L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$	ξ_α	2	$-1/2$
$(e_R)^\dagger$	η^α	1	-1

Denial

$$\mathcal{L} = i(L)^\dagger \bar{\sigma}^\mu D_\mu L - \frac{1}{4} W_{\mu\nu}^i W_i^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - i(e_R)^\dagger \sigma^\mu D_\mu e_R$$

$SU(2)_L \times U(1)_Y$ 17 years later... (stages of grief \rightarrow 1967)

Higgs mechanism with tachyonic mass ($\mu^2 < 0$) and condensate

Field	Lorentz	$SU(2)_L$	$U(1)_Y$
$L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$	ξ_α	2	$-1/2$
$(e_R)^\dagger$	η^α	1	-1
$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} = \left[\frac{H(x)+v}{\sqrt{2}} \right] \exp \left[i \frac{\tau^i}{2} G_i(x) \right]$	-	2	$1/2$

Contempt

$$\mathcal{L} = i(L)^\dagger \bar{\sigma}^\mu D_\mu L - \frac{1}{4} W_{\mu\nu}^i W_i^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - i(e_R)^\dagger \sigma^\mu D_\mu e_R + (e_R)^\dagger \Phi^\dagger L - (D^\mu \Phi)^\dagger D_\mu \Phi - \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2$$

$SU(2)_L \times U(1)_Y$ 17 years later... (stages of grief \rightarrow 1967)

Higgs mechanism with tachyonic mass ($\mu^2 < 0$) and condensate

Field	Lorentz	$SU(2)_L$	$U(1)_Y$
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$(e_R)^\dagger$	η^α	1	-1
$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} = \left[\frac{H(x) + v}{\sqrt{2}} \right] \exp \left[i \frac{\tau^i}{2} G_i(x) \right]$	-	2	$1/2$

Contempt

$$\mathcal{L} = i(L)^\dagger \bar{\sigma}^\mu D_\mu L - \frac{1}{4} W_{\mu\nu}^i W_i^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - i(e_R)^\dagger \sigma^\mu D_\mu e_R + (e_R)^\dagger \Phi^\dagger L - (D^\mu \Phi)^\dagger D_\mu \Phi - \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2$$

$$\Phi \rightarrow \Phi' = \exp \left[i \frac{\tau^i}{2} \theta_i(x) \right] \Phi = \frac{1}{\sqrt{2}} [H(x) + v]$$

$$\mathcal{L} = i\bar{\psi}\gamma^\mu \partial_\mu \psi - m_e \bar{\psi} \psi - i(\nu_L)^\dagger \bar{\sigma}^\mu \partial_\mu \nu_L + (e_R)^\dagger \Phi^\dagger L - (D^\mu \Phi)^\dagger D_\mu \Phi - \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 - \mathcal{L}_{\text{gauge}} + Z\nu\nu + m_e \bar{\psi} \psi$$

SU(2)_L × U(1)_Y 17 years later... (stages of grief → 1971)

Z and W phenomenology and discovery

Field	Lorentz	SU(2) _L	U(1) _Y
$L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$	ξ_α	2	-1/2
$(e_R)^\dagger$	η^α	1	-1
$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} = \left[\frac{H(x) + v}{\sqrt{2}} \right] \exp \left[i \frac{\tau^i}{2} G_i(x) \right]$	-	2	1/2

Bargaining

$$\mathcal{L} = i(L)^\dagger \bar{\sigma}^\mu D_\mu L - \frac{1}{4} W_{\mu\nu}^i W_i^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - i(e_R)^\dagger \sigma^\mu D_\mu e_R + (e_R)^\dagger \Phi^\dagger L - (D^\mu \Phi)^\dagger D_\mu \Phi - \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2$$

$$\Phi \rightarrow \Phi' = \exp \left[i \frac{\tau^i}{2} \theta_i(x) \right] \Phi = \frac{1}{\sqrt{2}} [H(x) + v]$$

$$\mathcal{L} = i\bar{\psi}\gamma^\mu \partial_\mu \psi - m_e \bar{\psi}\psi - i(\nu_L)^\dagger \bar{\sigma}^\mu \partial_\mu \nu_L + (e_R)^\dagger \Phi^\dagger L - (D^\mu \Phi)^\dagger D_\mu \Phi - \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 - \mathcal{L}_{\text{gauge}} + Z\nu\nu + m_e \bar{\psi}\psi$$

$SU(2)_L \times U(1)_Y$ 17 years later... (stages of grief \rightarrow 1982)

Hierarchy problem

Field	Lorentz	$SU(2)_L$	$U(1)_Y$
$L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$	ξ_α	2	$-1/2$
$(e_R)^\dagger$	η^α	1	-1
$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} = \left[\frac{H(x) + v}{\sqrt{2}} \right] \exp \left[i \frac{\tau^i}{2} G_i(x) \right]$	-	2	$1/2$

Depression

$$\mathcal{L} = i(L)^\dagger \bar{\sigma}^\mu D_\mu L - \frac{1}{4} W_{\mu\nu}^i W_i^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - i(e_R)^\dagger \sigma^\mu D_\mu e_R + (e_R)^\dagger \Phi^\dagger L - (D^\mu \Phi)^\dagger D_\mu \Phi - \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2$$

$$\Phi \rightarrow \Phi' = \exp \left[i \frac{\tau^i}{2} \theta_i(x) \right] \Phi = \frac{1}{\sqrt{2}} [H(x) + v]$$

$$\mathcal{L} = i\bar{\psi}\gamma^\mu \partial_\mu \psi - m_e \bar{\psi}\psi - i(\nu_L)^\dagger \bar{\sigma}^\mu \partial_\mu \nu_L + (e_R)^\dagger \Phi^\dagger L - (D^\mu \Phi)^\dagger D_\mu \Phi - \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 - \mathcal{L}_{\text{gauge}} + Z\nu\nu + m_e \bar{\psi}\psi$$

$SU(2)_L \times U(1)_Y$ 17 years later... (stages of grief \rightarrow 2012)

Higgs discovery!

Field	Lorentz	$SU(2)_L$	$U(1)_Y$
$L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}$	ξ_α	2	$-1/2$
$(e_R)^\dagger$	η^α	1	-1
$\Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix} = \left[\frac{H(x) + v}{\sqrt{2}} \right] \exp \left[i \frac{\tau^i}{2} G_i(x) \right]$	-	2	$1/2$

Acceptance

$$\mathcal{L} = i(L)^\dagger \bar{\sigma}^\mu D_\mu L - \frac{1}{4} W_{\mu\nu}^i W_i^{\mu\nu} - \frac{1}{4} B_{\mu\nu} B^{\mu\nu} - i(e_R)^\dagger \sigma^\mu D_\mu e_R + (e_R)^\dagger \Phi^\dagger L - (D^\mu \Phi)^\dagger D_\mu \Phi - \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2$$

$$\Phi \rightarrow \Phi' = \exp \left[i \frac{\tau^i}{2} \theta_i(x) \right] \Phi = \frac{1}{\sqrt{2}} [H(x) + v]$$

$$\mathcal{L} = i\bar{\psi}\gamma^\mu\partial_\mu\psi - m_e\bar{\psi}\psi - i(\nu_L)^\dagger \bar{\sigma}^\mu \partial_\mu \nu_L + (e_R)^\dagger \Phi^\dagger L - (D^\mu \Phi)^\dagger D_\mu \Phi - \mu^2 \Phi^\dagger \Phi - \lambda (\Phi^\dagger \Phi)^2 - \mathcal{L}_{\text{gauge}} + Z\nu\nu + m_e\bar{\psi}\psi$$