Scotogenic seesaw and baryogenesis

with gauged Baryon number

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Model building
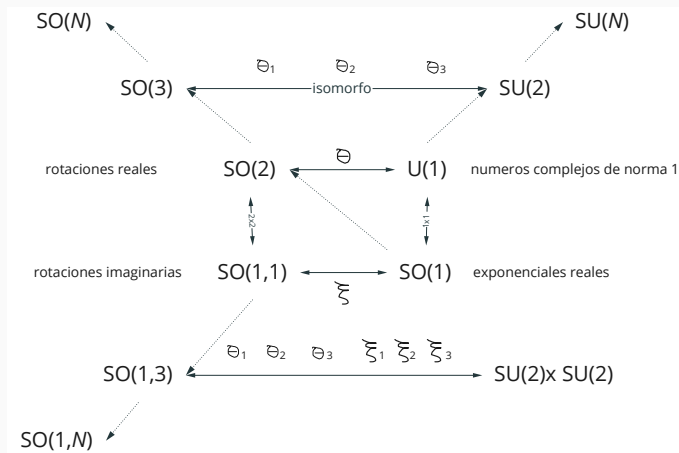
Lie groups

$$U = \exp\left(i \sum_j T_j \theta^j \right), \tag{1}$$

where θ^j are the parameters of the transformation and T_j are the generators.

Consider the 1×1

$$K = -i, \tag{2}$$

which generates an element of dilaton group , $SO(1)$, $R(\xi)$

$$\lambda(\xi) = e^{\xi}, \tag{3}$$

which are just the group of the real exponentials. Such a number can be transformed as

$$x \to x' = e^{\xi} x, \tag{4}$$

that corresponds to a boost by e^{ξ}. We can defin the invariant scalar product just as the division of real numbers, such that

$$x \cdot y \to x' \cdot y' \equiv \frac{x'}{y'} = \frac{e^{\xi} x}{e^{\xi} y} = \frac{x}{y} = x \cdot y. \tag{5}$$

Queremos obtener una representación 2×2 del álgebra

$$K^2 = -\mathbf{1}\,, \tag{6}$$

donde K es el único generador. Para hallar una representación de esta álgebra en términos de matrices 2×2 considere el generador

$$K = \begin{pmatrix} 0 & -i \\ -i & 0 \end{pmatrix}\,. \tag{7}$$

que genera un elemento del grupo $SO(1,1)$ con parámetro ξ

$$\Lambda = \exp\left(i\xi K\right) = \begin{pmatrix} \cosh\xi & \sinh\xi \\ \sinh\xi & \cosh\xi \end{pmatrix}, \,. \tag{8}$$

La transformación de una coordenada temporaloide y otra espacialoide ($c = 1$)

$$\begin{pmatrix} t \\ x \end{pmatrix} = \begin{pmatrix} x^0 \\ x^1 \end{pmatrix} \rightarrow \begin{pmatrix} x'^0 \\ x'^1 \end{pmatrix} \begin{pmatrix} \cosh\xi & \sinh\xi \\ \sinh\xi & \cosh\xi \end{pmatrix} \begin{pmatrix} x^0 \\ x^1 \end{pmatrix}$$

$$\cosh \xi = \gamma = \frac{1}{\sqrt{1 - v^2}}$$

Special: parameter ξ or v is constant, e.g, inertial system invariance: *Global* conservation of E and $\boldsymbol{p}$

General: parameter $\xi(t, \boldsymbol{x})$ or $v(t, \boldsymbol{x})$ is constant, e.g, accelerated system invariance: Local conservation of E and $\boldsymbol{p}$

Under a general Lorentz transformation we have.

$$A^{\mu}(x) \to A'^{\mu}(x) = \Lambda^{\mu}{}_{\nu} A^{\nu}(\Lambda^{-1}x). \tag{9}$$

A pure underscript 4-vector is

$$\partial_{\mu} = \frac{\partial}{\partial x^{\mu}} = \left(\frac{\partial}{\partial t}, \frac{\partial}{\partial x}, \frac{\partial}{\partial y}, \frac{\partial}{\partial z} \right) = (\partial_0, \boldsymbol{\nabla}). \tag{10}$$

From

$$\frac{1}{x'^{\mu}} = \left(\Lambda^{-1} \right)^{\nu}{}_{\mu} \frac{1}{x^{\nu}}, \tag{11}$$

the tranformation properties for a $\partial_{\mu} = \partial / \partial x^{\mu}$, are

$$\partial'_{\mu} = \left(\Lambda^{-1} \right)^{\nu}{}_{\mu} \partial_{\nu}. \tag{12}$$

In this way, the invariant scalar product between the 4-vector field and the four-gradient is just

$$\partial_\mu A^\mu \to \partial'_\mu A'^\mu = \partial_\mu A^\mu \,. \tag{13}$$

Name	Symbol	SU(N)
scalar N-plet	Ψ	$U\Psi$
scalar anti-N-plet	$\Psi^\dagger$	$\Psi^\dagger U^\dagger$

Name	Symbol	Lorentz
Photon	A^μ	$\Lambda^\mu{}_\nu A^\nu$
4-gradient	∂_μ	$\partial_\nu \left(\Lambda^{-1}\right)^\nu{}_\mu$

Table 1: Scalar products: $\Psi^\dagger\Psi$, $\quad\partial_\mu A^\mu\,,\quad A^\nu A_\nu\,,\quad \partial_\mu\partial^\mu$

Name	Symbol	Lorentz	$U(1)$
e_L: electron left	ξ_α	$S_\alpha{}^\beta \xi_\beta$	$e^{i\theta}\xi_\alpha$
$(e_L)^\dagger$: positron right	$(\xi_\alpha)^\dagger = \xi_{\dot\alpha}^\dagger$	$\xi_{\dot\beta}^\dagger [S^\dagger]^{\dot\beta}{}_{\dot\alpha}$	$\xi_{\dot\alpha}^\dagger e^{-i\theta}$
e_R: electron right	$(\eta^\alpha)^\dagger = \eta^{\dagger\,\dot\alpha}$	$\left[(S^{-1})^\dagger\right]^{\dot\alpha}{}_{\dot\beta}\eta^{\dagger\,\dot\beta}$	$e^{i\theta}\eta^{\dagger\,\dot\alpha}$
$(e_R)^\dagger$: positron left	η^α	$\eta^\beta [S^{-1}]_\beta{}^\alpha$	$e^{-i\theta}\eta^\alpha$

Table 2: electron components

Scalar products

- Majorana scalars: $\xi^\alpha \xi_\alpha + \xi_{\dot\alpha}^\dagger \xi^{\dagger\dot\alpha}$, $\eta^\alpha \eta_\alpha + \eta_{\dot\alpha}^\dagger \eta^{\dagger\dot\alpha}$.
- Dirac scalar: $\eta^\alpha \xi_\alpha + \xi_{\dot\alpha}^\dagger \eta^{\dagger\,\dot\alpha}$.
- Scalar under subgroup SL(2, C) but vector under SO(1, 3): $S^\dagger \overline\sigma^\mu S = \Lambda^\mu{}_\nu \overline\sigma^\nu$
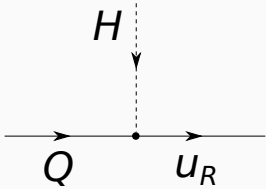
Field	Lorentz	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$
Q	ξ_α^1	**3**	**2**	$1/6$
L	ξ_α^2	**1**	**2**	$-1/2$
$\left(u_R^-\right)^\dagger$	η_1^α	$\overline{\mathbf{3}}$	**1**	$-2/3$
$\left(d_R^-\right)^\dagger$	η_2^α	$\overline{\mathbf{3}}$	**1**	$1/3$
$\left(e_R^-\right)^\dagger$	η_3^α	**1**	**1**	1
H	-	**1**	**2**	$1/2$

Table 3: Standard Model fundamental fields

like for example,

$$\eta_1^\alpha \xi_\alpha^1 \cdot H = (u_R)^\dagger \, Q \cdot H, \tag{14}$$

which can be represented by the "Kircchoff Law":

$$Y_Q + Y_H = Y_u \to \frac{1}{6} + \frac{1}{2} = \frac{2}{3}$$

Dark sectors

Local $U(1)_{\mathcal{X}}$

$$\mathcal{L} = -\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + i \sum_i \chi_i^\dagger \mathcal{D} \chi_i$$
$$-h \left(\chi_1 \chi_2 \Phi + \text{h.c} \right)$$

Anomalons: SM-singlet Dirac fermion

dark matter $m_\Psi = h\langle\Phi\rangle$

LHC production:

Gauged Symmetry: $\mathcal{X} \to B$: $q\bar{q} \to Z' \to$ jets

Gauged Symmetry: $\mathcal{X} \to L$:

$F_{\mu\nu} \ V^{\mu\nu}$

$$\overline{\Psi}\Psi = \chi_1\chi_2 + \chi_1^\dagger\chi_2^\dagger \to \chi_\alpha\chi_\beta\Phi^{(*)}, \qquad \alpha = 1, \dots N' \to N' > 4$$

12

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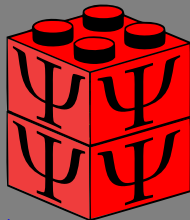
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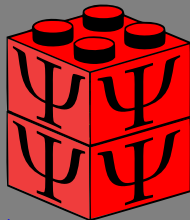
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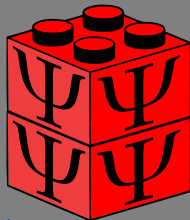
Anomalons: SM-singlet Dirac fermion

CP violation Yukawa *y*

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multi-component dark matter

$\overline{\Psi}\Psi = \chi_1\chi_2 + \chi_1^\dagger \chi_2^\dagger \to \chi_\alpha \chi_\beta \Phi^{(*)}, \qquad \alpha = 1, \ldots N' \to N' > 4$

Standard model extended with $U(1)_{\mathcal{X}=L \text{ or } B}$ gauge symmetry

Fields	$SU(2)_L$	$U(1)_Y$	$U(1)_{\mathcal{X}=B \text{ or } L}$
$Q_i^\dagger$	**2**	$-1/6$	Q
d_{Ri}	**1**	$-1/2$	d
u_{Ri}	**1**	$+2/3$	u
$L_i^\dagger$	**2**	$+1/2$	L
e_{Ri}	**1**	-1	e
H	**2**	$1/2$	$h = 0$
χ_α	**1**	0	z_α
$(L_L')^\dagger$	**2**	$1/2$	$-x'$
L_R''	**2**	$-1/2$	x''
e_R'	**1**	-1	x'
$(e_L'')^\dagger$	**1**	1	$-x''$
Φ	**1**	0	ϕ
S	**1**	0	s

Table 4: A minimal set of new fermion content: $L = e = 0$ for $\mathcal{X} = B$. Or $Q = u = d = 0$ for $\mathcal{X} = L$. $i = 1, 2, 3$, $\alpha = 1, 2, \ldots, N'$

Effective Dirac neutrino mass operator

$$\chi_1 \to \nu_{R1}, \cdots, \chi_{N_\nu} \to \nu_{R N_\nu}, \qquad 2 \leq N_\nu \leq 3, \tag{15}$$

$$\mathcal{L}_{\text{eff}} = h_\nu^{\alpha i} \, (\nu_{R\alpha})^\dagger \, \epsilon_{ab} \, L_i^a \, H^b \left(\frac{\Phi^*}{\Lambda}\right)^\delta + \text{H.c.}, \qquad \text{with } i = 1, 2, 3,$$

S is the complex singlet scalar responsible for the SSB of the anomaly-free gauge symmetry with D or X-charge

$$\phi = -(\nu + L)/\delta, \tag{16}$$

The anomaly-cancellation conditions on $[SU(3)_c]^2\, U(1)_X$, $[SU(2)_L]^2\, U(1)_X$, $[U(1)_Y]^2\, U(1)_X$, allow us to express three of the X-charges in terms of the others

$$u = -\,e - \frac{2}{3}L - \frac{1}{9}\left(x' - x''\right)\,, \quad d = e + \frac{4}{3}L - \frac{1}{9}\left(x' - x''\right)\,, \quad Q = -\frac{1}{3}L + \frac{1}{9}\left(x' - x''\right)\,, \quad (17)$$

while the $[U(1)_X]^2\, U(1)_Y$ anomaly condition reduces to

$$(e + L)(x' - x'') = 0\,. \tag{18}$$

- Previously: $x' = x''$
- We choose instead ($h = 0$):

$$e = -L\,, \tag{19}$$

so that (L is still a free parameter)

$$Q = -u = -d = -\frac{1}{3}L + \frac{1}{9}\left(x' - x''\right)\,. \tag{20}$$

If $B = 0 \rightarrow U(1)_L$

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The gravitational anomaly, $[SO(1,3)]^2\, U(1)_Y$, and the cubic anomaly, $[U(1)_X]^3$, can be written as the following system of Diophantine equations, respectively,

$$\sum_{\alpha=1}^{N} z_\alpha = 0\,, \qquad\qquad \sum_{\alpha=1}^{N} z_\alpha^3 = 0\,, \tag{21}$$

where $N = N' + 5$ and

$$z_{N'+1} = -x'\,, \qquad\qquad\qquad\qquad z_{N'+2} = x''\,,$$

$$z_{N'+2+i} = L\,, \quad i = 1,2,3 \tag{22}$$

$\rightarrow$

$$9Q = -\sum_{\alpha=N'+1}^{N'+5} z_\alpha = -x' + x'' + L + L + L\,, \tag{23}$$

$Q = 0 \not\rightarrow U(1)_L$

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`Dataset` `Open Access`

Set of N integers between -30 and 30 with sum and cubic sum up to zero for 4<N<13

Diego Restrepo

Anomalies

Solutions obtained with the python package: anomalies based on the method to find anomaly free solutions of the standard model extended with an Abelian Dark Symmetry with N right-handed singlet chiral fields described in arXiv:1905.13729 [PRL]:

Data scheme

- 'l': integer lists → input to obtain the 'solution' by using the anomalies package
- 'k': integer lists → input to obtain the 'solution' by using hte anomalies package
- 'solution': list → of integers, z_i which satisfy $\sum_{i=1}^{N} z_i = 0$ and $\sum_{i=1}^{N} z_i^3 = 0$.
- 'n': integer → number of integers in 'solution', N.

USAGE

```
#Example of JSON file usage in Python with pandas (see also json module)
>>> import pandas as pd
>>> df=pd.read_json('solutions.json')
>>> df[:2]
            l            k            solution  gcd  n
0      [1, 2]      [0, -3]   [1, 5, -7, -8, 9]    1  5
1    [-2, -1]      [0, -1]  [2, 4, -7, -9, 10]    1  5
```

Data:
390074 solutions with $5 < N \leq 12$ integers until '|32|' [JSON]

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`Gauge Symmetry`
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Versions

Version 1   Sep 24, 2021
10.5281/zenodo.5526707

U(1)$_B$ selection

- $L = 0$

$$(5, 5, -3, -2, 1, -6)$$

$\mathbb{U}(1)_B$ selection

- $L = 0$
- Effective neutrino mass: $\phi = -\nu = -5$
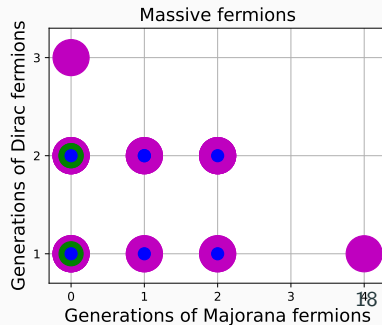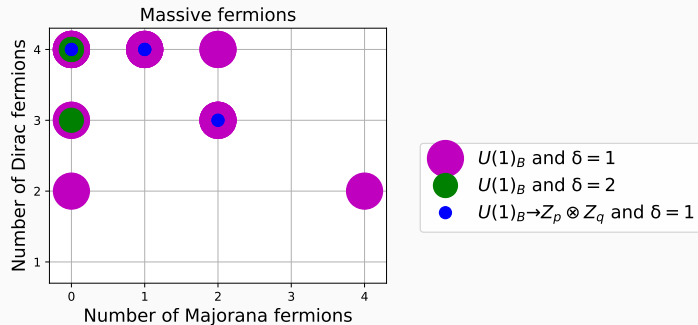
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  $(L'_L)^\dagger L''_R \Phi^* \rightarrow x' = -1, \ x'' = 6$

$$\left(5, 5, -3, -2, 1, -6\right)$$

$U(1)_B$ selection

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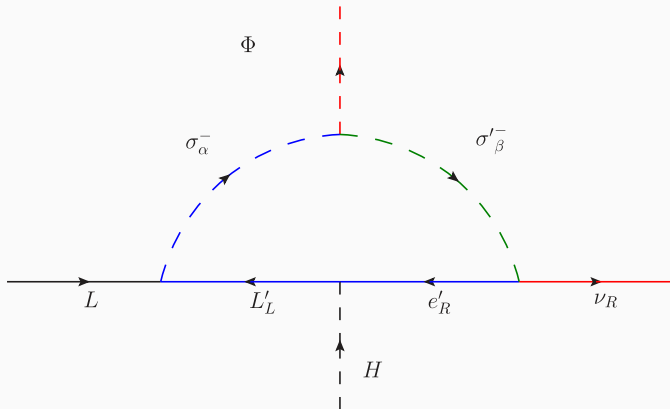- Dirac-fermionic DM: $(\chi_L)^\dagger \chi''_R \Phi^* \to z_3 = -3,\ z_4 = -2$

$$(5, 5, -3, -2, 1, -6)$$

$\mathsf{U(1)}_B$ **selection**

- $L = 0$

- Effective neutrino mass: $\phi = -\nu = -5$

- Electroweak-scale vector-like fermions:
  $(L'_L)^\dagger \, L''_R \Phi^* \to x' = -1, \; x'' = 6$

- Dirac-fermionic DM: $(\chi_L)^\dagger \, \chi''_R \Phi^* \to z_3 = -3, \; z_4 = -2$

959 solutions from $\sim 400,000$

$$(5, 5, -3, -2, 1, -6)$$

Massive fermions

Legend:
- $U(1)_B$ and $\delta = 1$
- $U(1)_B$ and $\delta = 2$
- $U(1)_B \to Z_p \otimes Z_q$ and $\delta = 1$

x-axis: Number of Majorana fermions
y-axis: Number of Dirac fermions

Massive fermions

x-axis: Generations of Majorana fermions
y-axis: Generations of Dirac fermions

Any realization which does not affect anomaly cancellation is allowed

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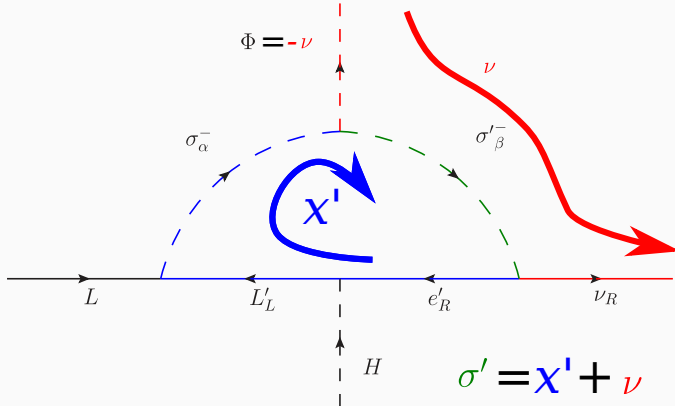
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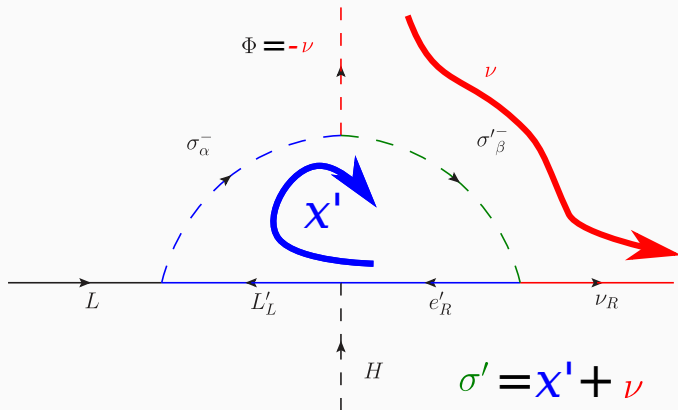
Field	$SU(2)_L$	$U(1)_Y$	$U(1)_B$
u_{Ri}	1	2/3	$u = 1/3$
d_{Ri}	1	$-1/3$	$d = 1/3$
$(Q_i)^\dagger$	2	$-1/6$	$Q = -1/3$
$(L_i)^\dagger$	2	1/2	$L = 0$
e_R	1	-1	$e = 0$
$(L'_L)^\dagger$	2	1/2	$-x' = -3/5$
e'_R	1	-1	$x' = 3/5$
L''_R	2	$-1/2$	$x'' = 18/5$
$(e''_L)^\dagger$	1	1	$-x'' = -18/5$
$\nu_{R,1}$	1	0	-3
$\nu_{R,2}$	1	0	-3
χ_R	1	0	6/5
$(\chi_L)^\dagger$	1	0	9/5
H	2	1/2	0
S	1	0	3
Φ	1	0	3
σ_α^-	1	1	3/5
σ'^-_α	1	-1	$-12/5$

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Electroweak baryogenesis

- Standard model (SM) $m_h \sim 40$ GeV. 😞
- Beyond the SM: Source of CP contains fields charged under SM
  $\rightarrow$ too large electric dipole moments 😩

- Inert SM-singlet complex scalar field which acquires vev with temperature to have strong electroweak phase transition 😊

- CP violation (CPV) triggered in dark sectors through SM gauge singlets
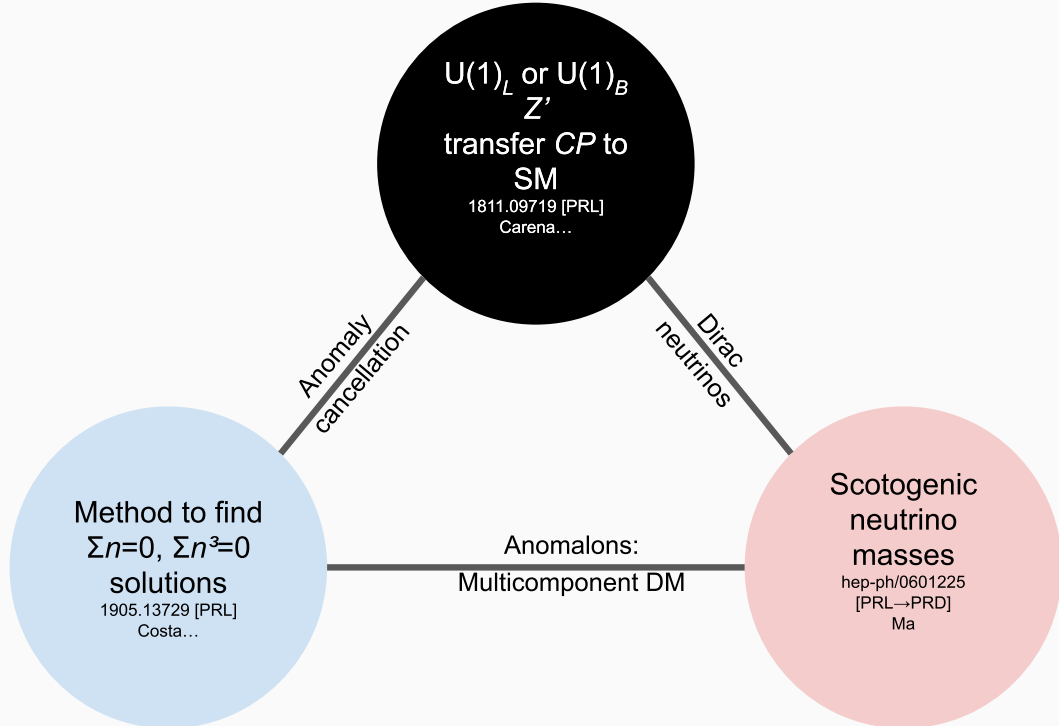 $\rightarrow$ CPV Yukawa between SM-singlet complex scalar and SM-singlet quiral fermions 😀
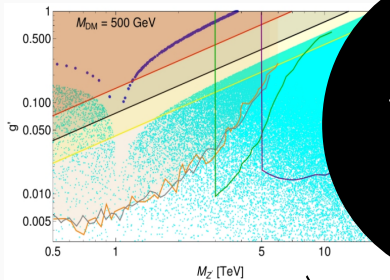
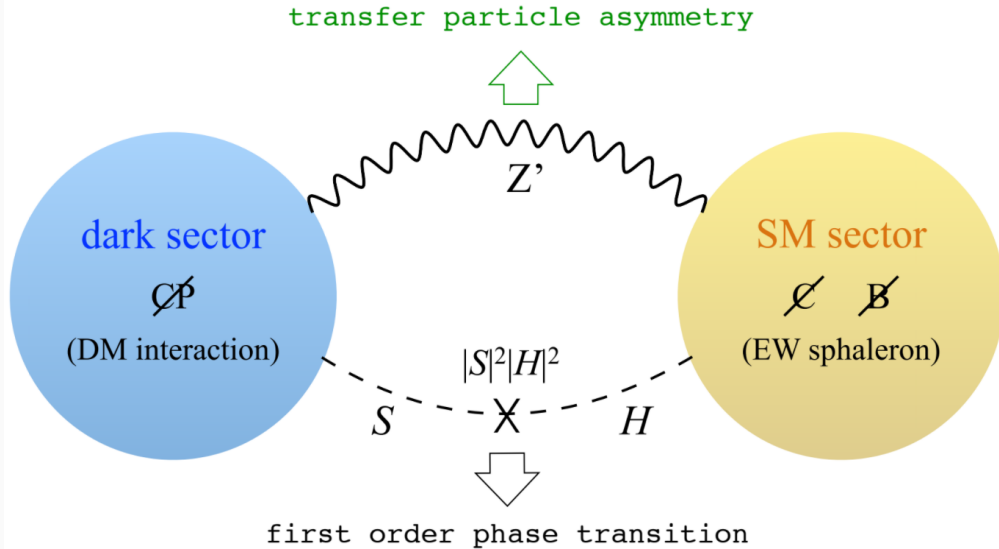U(1)$_L$ or U(1)$_B$
Z'
transfer *CP* to SM
1811.09719 [PRL]
Carena…

Anomaly cancellation

Dirac neutrinos

Anomalons:

DM

from: [1] Carena, *et al*, arXiv:1908.04818 [PRD] (see also: arXiv:1811.09719 [PRL])

CP violation occurs in the dark sector and is transmited to SM sector by the new Z' gauge boson.

- High scale fields: Φ, $\qquad$ ($\langle\Phi\rangle \to L'_L, L''_R, e'_L, e''_R$: EW-scale vector-like anomalons)
- Electroweak scale (EW) fields: $\boxed{Z'_\mu, S, \chi_L, \chi_R}$
- *CP*-violation

$$\mathcal{L}_{\text{Dirac DM}} = h\left(\chi_L\right)^\dagger \chi_R \Phi^* + y\left(\chi_L\right)^\dagger \chi_R S^* + \text{h.c}\,, \qquad\qquad y \in \mathbb{C}$$
$$\supset \left(m_\chi + |y|\, e^{i\theta}\, |S|\right)\left(\chi_L\right)^\dagger \chi_R + \text{h.c}\,.$$

- *CP*-violation Portal

$$\mathcal{L}_{\text{anomalous}} \supset g' Z'_\mu \left[3\bar{\chi}_L\gamma^\mu\chi_L - 2\bar{\chi}_R\gamma^\mu\chi_R + \bar{Q}_i\gamma^\mu Q_i + \bar{q}_{Ri}\gamma^\mu q_{Ri}\right]$$

- Strong electroweak phase transition (EWPT) portal

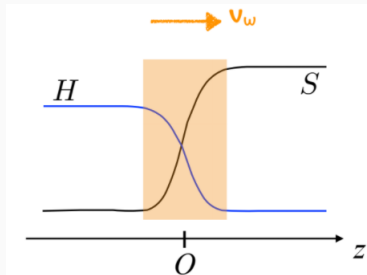$$\mathcal{L}_{\text{first order EWPT}} \supset -\lambda_{SH} H^\dagger H S^* S\,.$$

First-order phase transition: Effective potential ($T \neq 0$)

$\boxed{h = H/\sqrt{2},\ s = |S|}$ with vevs: $v(T)$ and $w(T)$ such that $v(T_c) = w(T_c)$

$$V_T(h, s) = \frac{\lambda_H v_c^4}{4}\left(\frac{h^2}{v_c^2} + \frac{s^2}{w_c^2} - 1\right)^2 + \frac{\lambda_H v_c^2}{m_{s,c}^2 w_{0,c}^4}h^2 s^2 + (T^2 - T_c^2)(c_h h^2 + c_s s^2), \qquad (24)$$

where

$$c_h = \frac{1}{48}\left(9g_2^2 + 3g_1^2 + 12y_t^2 + 24\lambda_H + \lambda_{HS}\right), \quad c_s = \frac{1}{12}\left(3\lambda_S + 2\lambda_{HS}\right). \qquad (25)$$

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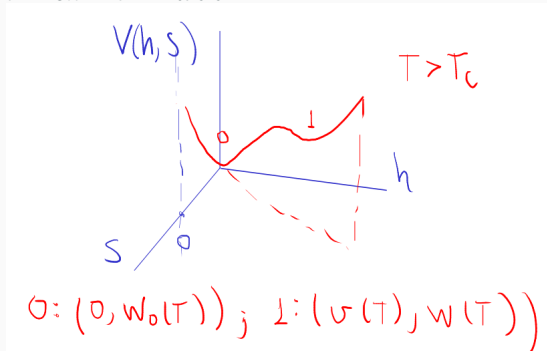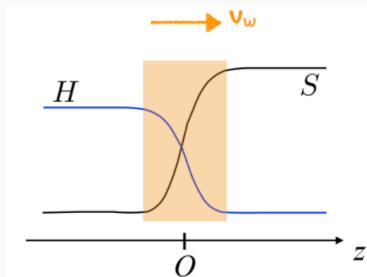# First-order phase transition: Effective potential ($T \neq 0$)

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arXiv: Sec. 4.1 arXiv:1107.5451

$0: (0, w_0(T))$; $1: (\sigma(T), w(T))$

25

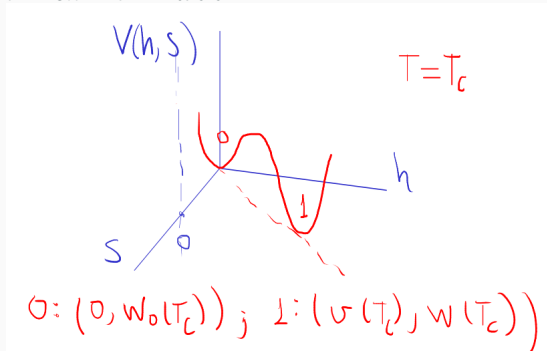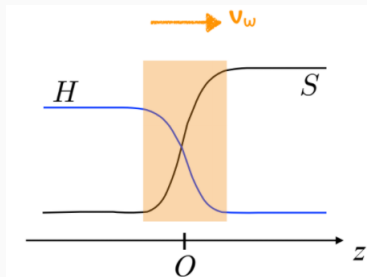# First-order phase transition: Effective potential ($T \neq 0$)

$h = H/\sqrt{2},\ s = |S|$ with vevs: $v(T)$ and $w(T)$ such that $v(T_c) = w(T_c)$

$$V_T(h, s) = \frac{\lambda_H v_c^4}{4}\left(\frac{h^2}{v_c^2} + \frac{s^2}{w_c^2} - 1\right)^2 + \frac{\lambda_H v_c^2}{m_{s,c}^2 w_{0,c}^4}h^2 s^2 + (T^2 - T_c^2)(c_h h^2 + c_s s^2),\qquad (24)$$

where

$$c_h = \frac{1}{48}\left(9g_2^2 + 3g_1^2 + 12y_t^2 + 24\lambda_H + \lambda_{HS}\right),\quad c_s = \frac{1}{12}\left(3\lambda_S + 2\lambda_{HS}\right).\qquad (25)$$
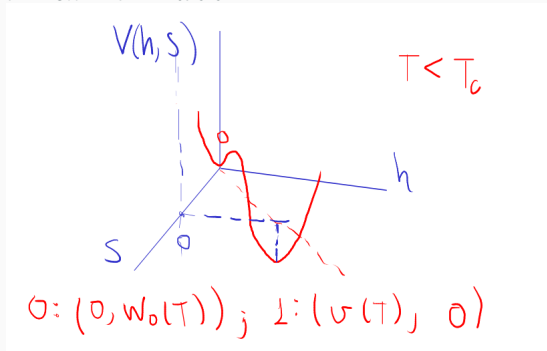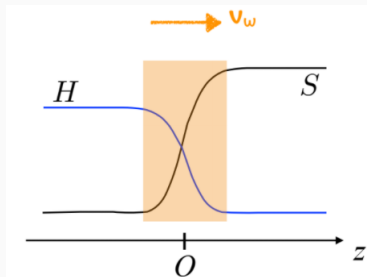
arXiv: Sec. 4.1 arXiv:1107.5451

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arXiv: Sec. 4.1 arXiv:1107.5451

$0: (0, W_0(T)) \ ; \ 1: (\sigma(T), 0)$

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Using the thin wall approximantion for the nucleation bubbles, we use the ansatz in which the space dependence of the fields is given by

$$h(z) = \frac{1}{2} v(T_n) \left(1 - \tanh\left(z/L_w\right)\right), \qquad s(z) = \frac{1}{2} w_0(T_n) \left(1 + \tanh\left(z/L_w\right)\right),$$

where z is the direction normal to the wall and L_w is the wall width.

The nucleation temperature, T_n, is defined by the condition

$$\exp\left(-S_3/T_n\right) = \frac{3}{4\pi} \left(\frac{H(T_n)}{T_n}\right)^4 \left(\frac{2\pi\, T_n}{S_3}\right)^{\frac{3}{2}},$$

where S_3 is the Euclidean action of the bubble and $H(T)$ is the Hubble rate.

Boltzmann equation i

$\xi_i(z) \equiv \mu_i(z)/T = 6\left(n_i - \overline{n}_i\right)/T^3,$

$$-D_L \xi''_{\chi_L} - v_w \xi'_{\chi_L} + \Gamma_L(\xi_{\chi_L} - \xi_{\chi_R}) = S_{\mathcal{CP}},$$

where D_L is the diffusion constant for χ_L, which is related to the scattering rate Γ_L by

$$D_L = \frac{3x+2}{x^2+3x+2}\frac{1}{3\Gamma_L}, \qquad\qquad x \equiv m_\chi/T \qquad (26)$$

and

$$S_{\mathcal{CP}} = -\frac{\lambda}{2}\frac{v_w D_L}{\frac{3x+2}{x^2+3x+2}T}\frac{(1-x)e^{-x}+x^2 E_1(x)}{4m_\chi^2 K_2(x)}\frac{m_\chi w_0(T_n)\lambda\left(-2+\cosh\left(\frac{2z}{L_w}\right)\right)\sin\theta}{L_w^3\cosh^4\left(\frac{z}{L_w}\right)}, \qquad (27)$$

where v_w is the wall's velocity $E_1(x)$ is the error function and $K_2(x)$ is the modified Bessel function of the second kind. $y = \lambda e^{i\theta - i\pi/2}$

The chiral particle give rise to a non-zero $U(1)_B$ charge density in the proximity of the wall. This results in a Z' background that couples to the SM fields with $U(1)_B$ charge,

$$\langle Z_0'(z) \rangle = \frac{g_B \left(q_{\chi_L} - q_{\chi_R} \right) T_n^3}{6 M_{Z'}} \int_{-\infty}^{\infty} \mathrm{d}\, z_1 \, \xi_{\chi_L}(z_1) \, e^{-M_{Z'}|z-z_1|},$$

which generates a chemical potential for the SM quarks,

$$\mu_Q(z) = \mu_{d_R, u_R}(z) = 3 \times \frac{5}{9} \times g_B \langle Z_0'(z) \rangle.$$

This chemical potential sources a thermal-equilibrium asymmetry in the quarks, $\Delta n_Q^{\mathrm{EQ}}(z) \sim T_n^2 \mu_Q(z)$.

From [1]

> *If the Z' is sufficiently light, it mediates a long range force that extends into the region outside the bubble wall with unbroken electroweak symmetry.*

Finally, the baryon-number asymmetry is then given by

$$n_B = \frac{\Gamma_{\mathrm{sph}}}{v_w} \int_0^\infty \mathrm{d}\, z\, n_Q^{\mathrm{EQ}}(z) \exp\left(-\frac{\Gamma_{\mathrm{sph}}}{v_w}\, z\right),$$

where Γ_{sph} is the sphaleron rate. The baryon-to-photon-number ratio is then obtained by

$$\eta_B = \frac{n_B}{s(T_n)}, \quad s(T) \equiv \frac{2\pi^2}{45} g_{*S}(T)\, T^3,$$

where $g_{*S}(T)$ is the effective number of relativistic degrees of freedom.

Our goal is to find what regions of the parameter space yield

$$0.82 \times 10^{-10} < \eta_B < 0.92 \times 10^{-10}. \tag{28}$$

- SARAH→SPheno→MicroMegas
- η_B calculation code
- Python notebook with the scan

Ten Simple Rules for Reproducible Research in Jupyter Notebook Fernando Pérez,*et al*

[...] In this paper, we address several questions about reproducibility [...] Combined with software repositories and open source licensing, notebooks are powerful tools for transparent, collaborative, reproducible, and reusable data analyses.

Results

We vary the typical Dirac-fermion DM parameter space and for each point that satisfy
neutrino oscillation data, relic density and DM direct detection constraints. For each point we
...

Parameter	Range
θ	$(-\pi/2, \pi/2)$
$w_0(T_n)/\mathrm{GeV}$	$100 - 500$
T_n/GeV	$100 - 200$
L_w/GeV^{-1}	$1/T_n - 10/T_n$
v_w	$0.05 - 0.5$

Table 5: Scan ranges for the free parameters that are involved in the baryogenesis mechanism.

Conclusions
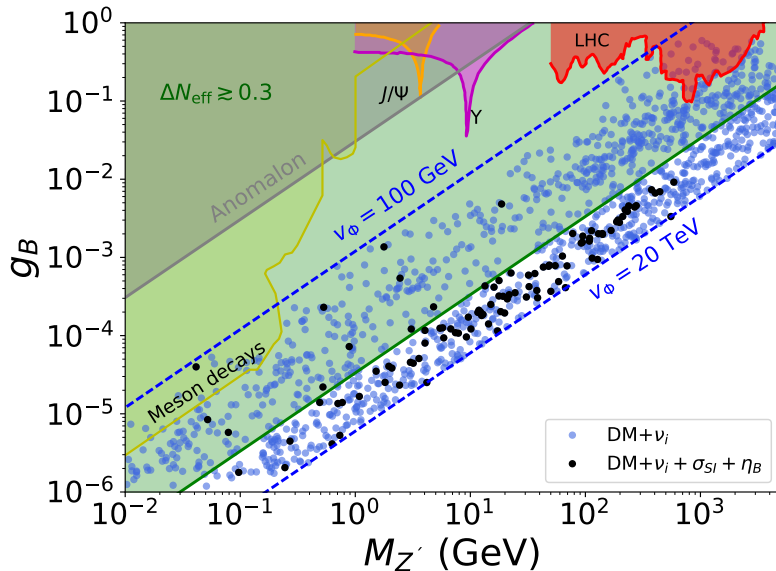
A $U(1)_B$ is presented as an example of models where all new fermions required to cancel out the anomalies are used to solve phenomenological problems of the standard model (SM):

- EW-scale fermion vector-like doublets and iso-singlet charged singlets, in conjunction with right-handed neutrinos with repeated Abelian charges, participate in the generation of small neutrino masses through the Dirac-dark Zee mechanism

- The other SM-singlets are used to explain the dark matter in the universe, while their coupling to an inert singlet scalar is the source of the CP violation.

In the presence of a strong first-order electroweak phase transition, this "dark" CP violation allows for successful electroweak baryogenesis by using long range force mediated by a sufficiently light Z' which transfers the assymmetry from the Dark sector into the SM.