Dark matter from SM gauge extensions



with neutrino masses

Diego Restrepo

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Instituto de Física Universidad de Antioquia Phenomenology Group http://gfif.udea.edu.co



Focus on

In collaboration wit

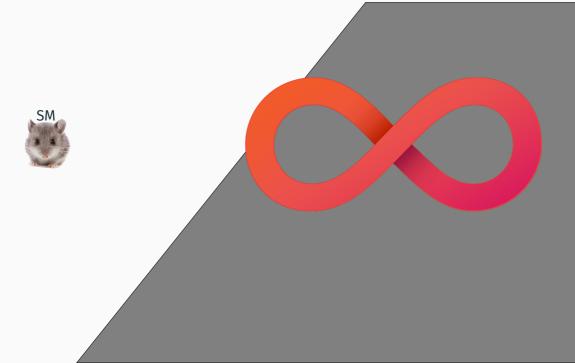
M. Hirsch (IFIC), C. Álvarez (UTFSM), A. Flórez (UniAndes), B. Dutta(Texas A& M), C. Yaguna (UPTC), J. Calle, O. Zapata, A. Rivera (UdeA), W. Tangarife (Loyola University Chicago)

Dark sectors

In the following discussion we use the following doublets in Weyl Notation

$$H = \begin{pmatrix} H^+ \\ H^0 \end{pmatrix}, \qquad L_i = \begin{pmatrix} \nu_{Li} \\ e_{Li}^- \end{pmatrix}. \tag{1}$$

corresponding to the Higgs doublet and the lepton doublets respectively.







$$m_{\text{Majorana}}^{\nu} = \frac{h_{\nu}}{\Lambda} L \cdot HL \cdot H$$
 (three-level)

Type-I arXiv:1808.03352, II arXiv:1607.04029, III arXiv:1908.04308

$$\mathcal{L} = y (N_R)^{\dagger} L \cdot H + M_N N_R N_R + \text{h.c}$$



$$m_{\text{Majorana}}^{\nu} = \frac{h_{\nu}}{\Lambda} L \cdot HL \cdot H$$

Type-I arXiv:1808.03352, with N. Bernal, C. Yaguna, and Ó. Zapata [PRD]

$$U(1)_X \rightarrow Z_7$$

$$\mathcal{L} = y(N_R)^{\dagger} L \cdot \langle H \rangle + y' \langle S \rangle N_R N_R + \text{h.c.}$$

$$m_{\rm Majorana}^{\nu} = \frac{h_{\nu}}{\Lambda} L \cdot HL \cdot H\frac{S}{\Lambda}$$
Type-I arXiv:1808.03352: Also new terms arise

2: Also new terms arise from spontaneous breakdown of a new gauge symmetry

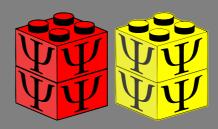
$Local U(1)_{X} \rightarrow Z_{7}$ $\mathcal{L} = y(N_{R})^{\dagger} L \cdot \langle H \rangle + y' \langle S \rangle N_{R} N_{R} + \text{h.c}$

$$\mathcal{L} = y (N_R)^{\dagger} L \cdot \langle H \rangle + y' \langle S \rangle N_R N_R + \text{h.c}$$

$$m_{\text{Majorana}}^{\nu} = \frac{h_{\nu}}{\Lambda} L \cdot HL \cdot H\frac{S}{\Lambda}$$

Type-I arXiv:1808.03352

: Also new terms arise from spontaneous breakdown of a new gauge symmetry



Fields	SU(2) _L	U(1) _Y	U(1) _X
L	2	-1/2	l
Q	2	-1/6	9
d_R	1	-1/2	d
U_R	1	+2/3	И
e_R	1	-1	е
Н	2	-1/2	h
ψ	1	0	ψ

Table 1: The new scalars and fermions with their respective charges. The SM fields have the usual $U(1)_{B-L}$ assignment. Now $\alpha=1,2$

$$[SU(3)_c]^2 U(1)_X : [3u + 3d] - [3 \cdot 2q] = 0$$

$$[SU(2)_L]^2 U(1)_X : -[2l + 3 \cdot 2q] = 0$$

$$[U(1)_Y]^2 U(1)_X : [(-2)^2 e + 3(\frac{4}{3})^2 u + 3(-\frac{2}{3})^2 d] - [2(-1)^2 l + 3 \cdot 2(\frac{1}{3})^2 q] = 0$$
 (2)

$$u=-e+\frac{2l}{3}\,,$$

$$d=e-\frac{4l}{3},$$

$$q=-\frac{l}{3}.$$

$$u=-e+\frac{2l}{3}\,,$$

$$d=e-\frac{4l}{3}\,,$$

$$q = -\frac{l}{3}. (2)$$

which satisfy

$$U(1)_{Y} \left[U(1)_{X} \right]^{2} : \qquad \left[(-2)e^{2} + 3\left(\frac{4}{3}\right)u^{2} + 3\left(-\frac{2}{3}\right)d^{2} \right] - \left[2(-1)l^{2} + 3 \cdot 2\left(\frac{1}{3}\right)q^{2} \right] = 0 \tag{3}$$

4

$$u = -e + \frac{2l}{3},$$
 $d = e - \frac{4l}{3},$ $q = -\frac{l}{3}.$ (2)

which satisfy

$$U(1)_{Y} \left[U(1)_{X} \right]^{2} : \qquad \left[\left(-2 \right) e^{2} + 3 \left(\frac{4}{3} \right) u^{2} + 3 \left(-\frac{2}{3} \right) d^{2} \right] - \left[2 \left(-1 \right) l^{2} + 3 \cdot 2 \left(\frac{1}{3} \right) q^{2} \right] = 0 \tag{3}$$

The most general cancellation for $[U(1)_X]^3$ and $[SO(1,3)]^2 U(1)_X$ is between families

$$\sum_{\alpha} \psi_{\alpha}^{3} + 3(e - 2l)^{3} = 0, \qquad \sum_{\alpha} \psi_{\alpha} + 3(e - 2l) = 0,$$
 (4)

with $\alpha = 1, 2, \dots, N$ or X = Y. We study the set of solutions with e - 2l = 1, e.g

$$\sum_{\alpha} \psi_{\alpha}^{3} = -3, \qquad \sum_{\alpha} \psi_{\alpha} = -3, \qquad (5)$$

$$u = -e + \frac{2l}{3},$$
 $d = e - \frac{4l}{3},$ $q = -\frac{l}{3}.$ (2)

which satisfy

$$U(1)_{Y} \left[U(1)_{X} \right]^{2} : \qquad \left[\left(-2 \right) e^{2} + 3 \left(\frac{4}{3} \right) u^{2} + 3 \left(-\frac{2}{3} \right) d^{2} \right] - \left[2 \left(-1 \right) l^{2} + 3 \cdot 2 \left(\frac{1}{3} \right) q^{2} \right] = 0 \tag{3}$$

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$$\sum_{\alpha} \psi_{\alpha}^{3} = -3, \qquad \sum_{\alpha} \psi_{\alpha} = -3, \qquad (5)$$

We impose $N_R = \psi_N = \psi_{N-1}$, to have at most one massless neutrino.

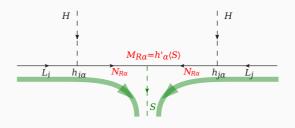
Known solutions with $\sum \psi_{lpha} = -3$ and $\sum \psi_{lpha}^3 = -3$

$(N_R, N_R, \psi_{N-2}, \cdots)$	Ref
(-1, -1, -1)	[]
(-4, -4, +5)	[?]
$\left(-\frac{2}{3}, -\frac{2}{3}, -\frac{4}{3}, -\frac{1}{3}\right)$	[?]
$\left(-\frac{8}{5}, -\frac{8}{5}, -\frac{2}{5}, -\frac{7}{5}, +2\right)$	[?]
$\left(-\frac{7}{3}, -\frac{7}{3}, +\frac{1}{3}, -\frac{5}{3}, +3\right)$	[]
$\left(-\frac{7}{10}, -\frac{7}{10}, -\frac{13}{10}, -\frac{1}{2}, +\frac{1}{5}\right)$	[]
$\left(-1,-1,-\frac{10}{7},-\frac{4}{7},-\frac{2}{7},\frac{9}{7}\right)$	[?]

Table 2: The possible solutions of the Dirac neutrino mass models with at least two repeated charges and until five chiral fermions.

Fields	SU(2) _L	U(1) _Y	U(1) _X	$U(1)_{B-L}$	U(1) _B	U(1) _D	U(1) _G
L	2	-1/2	l	-1	0	-3/2	-1/2
Q	2	-1/6	-l/3	1/3	0	1/2	1/6
d_R	1	-1/2	1 + 2l/3	1/3	1	0	2/3
U_R	1	+2/3	-1 - 4l/3	1/3	-1	1	-1/3
e_R	1	-1	1 + 2 <i>l</i>	-1	1	-2	0
Н	2	-1/2	-1 - l	0	-1	1/2	-1/2
S	1	0	$2\psi_{N}$	$2\psi_{N}$	$2\psi_N$	$2\psi_N$	$2\psi_N$
$\sum_{\alpha} \psi_{\alpha}$	1	0	-3	-3	-3	-3	-3
$\sum_{\alpha} \psi_{\alpha}^{3}$	1	0	-3	-3	-3	-3	-3

Fields	$U(1)_{B-L}$	Z_2^1	Z_2^1
L	-1	+	+
Q	1/3	+	+
d_R	1/3	+	+
U_R	1/3	+	+
e_R	-1	+	+
Н	0	+	+
S	-2	+	+
N_{R1}	-1	+	+
N_{R2}	-1	+	+
$\psi_1 o (\xi_L)^\dagger$	-10/7	_	+
$\psi_2 o \eta_R X$	-4/7	_	+
$\psi_3 o \zeta_R$	-2/7	+	_
$\psi_4 o (\chi_L)^\dagger$	+9/7	+	_
S'	1	+	+

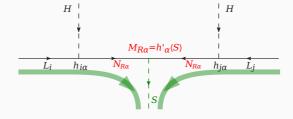


After integrating out heavy fermions, we obtain light neutrino masses

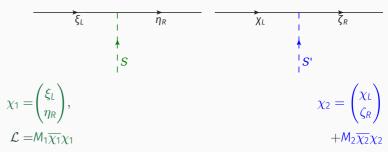
$$\mathcal{M}_{\nu}^{ij} = \sum_{\alpha=1}^{2} \left(h^{i\alpha} v \right) \frac{1}{M_{R}^{\alpha}} \left(h^{j\alpha} v \right)$$

With only two heavy fermions, one massless neutrino is left

$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Fields	Z_2^1
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	L	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Q	+
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	d_R	+
H 0 + + S -2 + +	U_R	+
S -2 + +	e_R	+
	Н	+
N 1	S	+
N_{R1} -1 + +	N_{R1}	+
N_{R2} -1 + +	N_{R2}	+
$\psi_1 ightharpoonup (\xi_L)^{\dagger} \mid -10/7 \mid - \mid +$	$\psi_1 o (\xi_L)^\dagger$	+
$\psi_2 ightarrow \eta_R X$ $-4/7$ $ +$	$\psi_2 o \eta_R X$	+
$\psi_3 ightarrow \zeta_R$ $-2/7$ $+$ $-$	$\psi_3 o \zeta_R$	-
$\psi_4 \rightarrow (\chi_L)^{\dagger}$ +9/7 + -	$\psi_4 \rightarrow (\chi_L)^{\dagger}$	_
S' 1 + +	S'	+



Two component Dirac fermion dark matter



Parameter space

$$S = \frac{1}{\sqrt{2}} \left(v_1 + h_1 \right) + \frac{i}{\sqrt{2}} x^2$$

$$S = \frac{1}{\sqrt{2}} (v_1 + h_1) + \frac{i}{\sqrt{2}} A_1$$
$$S' = \frac{1}{\sqrt{2}} (v_2 + h_2) + \frac{i}{\sqrt{2}} A_2$$

Parameter space
$$S=rac{1}{\sqrt{2}}inom{v_1}{h_1}+rac{i}{\sqrt{2}}A_1$$

$$S = \frac{1}{\sqrt{2}} \left(v_1 + h_1 \right) + \frac{i}{\sqrt{2}} A_1$$

































 $\begin{pmatrix} H_1 \\ H_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \end{pmatrix}$

 $M_{Z'}^2 = g_{RL}^2 v_2^2 \left(4 + \tan^2 \beta\right)$

 $\tan \beta = \frac{v_2}{v_1}$



Parameter space

$$S = \frac{1}{\sqrt{2}} \begin{pmatrix} v_1 + h_1 \end{pmatrix} + \frac{i}{\sqrt{2}} A_1$$

$$S' = \frac{1}{\sqrt{2}} \begin{pmatrix} v_2 + h_2 \end{pmatrix} + \frac{i}{\sqrt{2}} A_2$$

$$\begin{pmatrix} H_1 \\ H_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \end{pmatrix}$$

$$\tan \beta = \frac{v_2}{v_1}$$

$$M_{Z'}^2 = g_{BL}^2 v_2^2 \left(4 + \tan^2 \beta \right)$$

$$\mathcal{L} = M_1 \overline{\chi_1} \chi_1 + M_2 \overline{\chi_2} \chi_2 + M_{N1} \overline{N_{R1}^c} N_{R1} + M_{N2} \overline{N_{R2}^c} N_{R2}$$

Parameter space

$$S = \frac{1}{\sqrt{2}} \begin{pmatrix} v_1 + h_1 \end{pmatrix} + \frac{i}{\sqrt{2}} A_1$$

$$S' = \frac{1}{\sqrt{2}} \begin{pmatrix} v_2 + h_2 \end{pmatrix} + \frac{i}{\sqrt{2}} A_2$$

$$\begin{pmatrix} H_1 \\ H_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} h_1 \\ h_2 \end{pmatrix}$$

$$\tan \beta = \frac{v_2}{v_1}$$
11 parameters
$$M_{Z'}^2 = g_{BL}^2 v_2^2 \left(4 + \tan^2 \beta \right)$$

$$m_{\gamma} = M_1 \text{ or } M_2$$

$$\mathcal{L} = M_1 \overline{\chi_1} \chi_1 + M_2 \overline{\chi_2} \chi_2 + M_{N1} \overline{N_{R1}^c} N_{R1} + M_{N2} \overline{N_{R2}^c} N_{R2}$$

Relic abundance

 $\Omega_{\rm DM} h^2 = 0.1198 \pm 0.0015$ Planck 2015

Boltzman equation

$$\frac{dY}{dx} = -\frac{S\langle \sigma V \rangle}{xH(m_\chi)} \left(Y^2 - Y_{EQ}^2 \right)$$

$$S = \frac{2\pi^2}{45} g_\star \frac{m_\chi^3}{x^3}$$

$$H(m_\chi) = \sqrt{\frac{4\pi^3}{45}} g_\star \frac{m_\chi^2}{M_{Pl}}$$

$$SY_{EQ} = \frac{g_\chi}{2\pi^2} \frac{m_\chi^3}{x} K_2(x)$$

$$x=m_\chi/T$$
 $M_{Pl}=1.22\times 10^{19} {\rm GeV}$: the Planck mass $g_\chi=4$: the number of DM d.o.f $g_*=106.75$: for the SM particles K_2 : the modified Bessel function

sigmav

sigmav

$$\langle \sigma V \rangle = \frac{g_{\chi}^2}{64\pi^4} \left(\frac{m_{\chi}}{x}\right) \frac{1}{n_{EQ}^2} \int_{4m_{\chi}^2}^{\infty} ds \hat{\sigma}(s) \sqrt{s} K_1 \left(\frac{x\sqrt{s}}{m_{\chi}}\right)$$

where

 n_{EQ} : DM number density

*K*₁: Modified Bessel function

Reduced cross section

$$\hat{\sigma}(s) = 2\left(s - 4m_{\chi}^2 \sigma(s)\right)$$

DM annihilation cross section

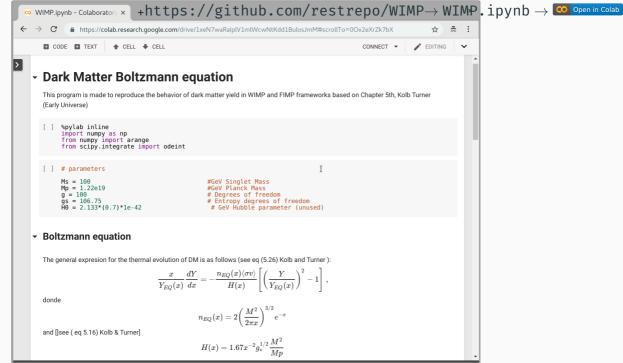
DM annihilation processes

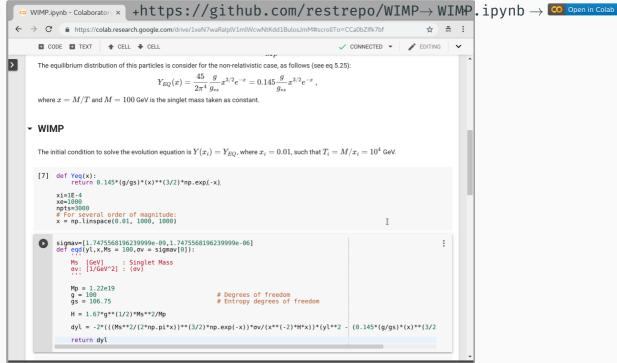


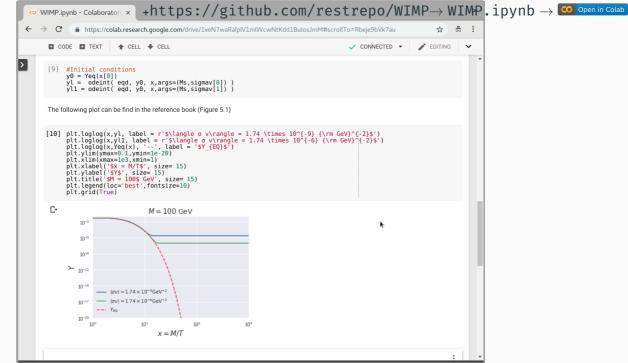
Total annihilation cross section:
$$\sigma(s) = \sigma_{SM}(s) + \sum_{i=1}^{2} \sigma_{N^{i}N^{i}}(s)$$

$$\begin{split} \sigma_{SM}(s) &= \frac{25\pi}{3} \alpha_X^2 \frac{\sqrt{s(s-4m_\chi^2)}}{(s-m_{Z'}^2)^2 + m_{Z'}^2 \Gamma_{Z'}^2} F(x_H), \\ \sigma_{N^i N^i}(s) &= \frac{400\pi}{3} \alpha_X^2 \sqrt{\frac{s-4m_{N^i}^2}{s-4m_\chi^2}} \frac{1}{(s-m_{Z'}^2)^2 + m_{Z'}^2 \Gamma_{Z'}^2} \\ &\qquad \times \frac{1}{s} \left((s-4m_\chi^2)(s-4m_{N^i}^2) + 12 \frac{m_\chi^2 - m_{N^i}^2}{m_{Z'}^4} \left(s-m_{Z'}^2 \right)^2 \right) \theta(s-4m_{N^i}^2) \end{split}$$

$$F(x_H) = 13 + 16x_H + 10x_H^2 = 10\left(x_H + \frac{4}{5}\right)^2 + \frac{33}{5}$$





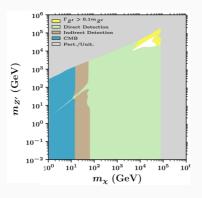


Isosinglet dark matter candidate

 χ as a isosinglet Dirac dark matter fermion charged under a local U(1)_{B-L} (SM) cuples to a SM-singlet vector mediator Z'

$$\mathcal{L}_{\text{int}} = -g_{\text{BL}} \, \overline{\chi} \gamma^{\mu} \chi \,, Z'_{\mu} - \sum_f g_f \overline{f} \gamma^{\mu} f \,, Z'_{\mu} \,,$$

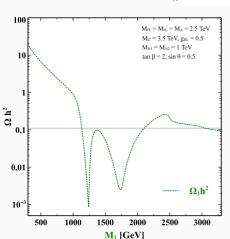
where f are the Standard Model fermions: Resonances excluded!



Additional DM annihilation processes



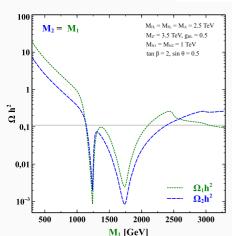




Additional DM annihilation processes



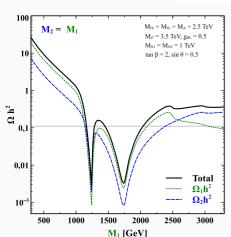




Additional DM annihilation processes

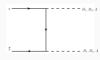


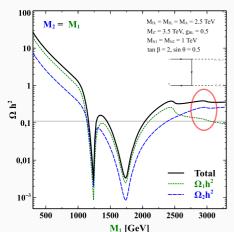




Additional DM annihilation processes

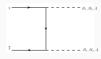


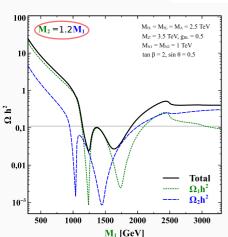


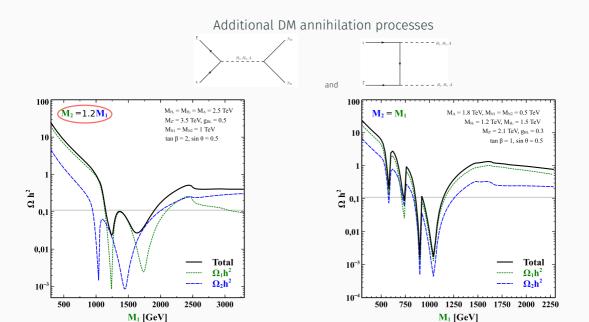


Additional DM annihilation processes



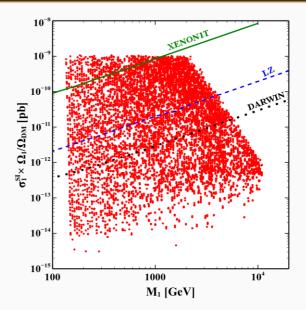






Two component Dirac fermion dark matter model

Parameter	Range
$M_{Z'}$	(0.3, 20) TeV
M _{1, 2}	(0.35, 0.65) M _{Z'}
g _{BL}	(0.001, 1)
$\sin lpha$	(0.001, 1)
aneta	(0.03, 30)
M_{R1} , M_{R2}	(0.2, 10) TeV
M_{H1} , M_{H2} , M_A	(0.2, 10) TeV



Conclusions

It makes sense to focus our attention on models tha can account for neutrino masses and dark matter (DM).

In this extension of the SM by an $U(1)_{B-L}$ gauge symmetry amomalies are are canceled partially by two right-handed neutrinos and partially by two component DM Dirac fermions. providing a connection between neutrinos and DM analogous to that one between leptons and quarks in the SM.

The model predicts the existence of three scalar fields beyond the SM Higgs: H_1 , H_2 , A

Model implemented in both LanHEP. Implemented also in

SARAH https://github.com/restrepo/BSM-Submodules/tree/B-L+DM/BSM/SARAH/Models/B-L/DM (Tested with SARAH-4.14.1) to analyse perturbativity and stability conditions and higher scales with two-loop RGEs.

After imposing the current bounds from LHC and direct detection experiments, there are regions of this model which remains unconstrained.

Easy to include an effective Z_7 breaking to get decaying dark matter.

