

Minimal $B - L$ models

with total L conservation



UNIVERSIDAD DE ANTIOQUIA
1803

Diego Restrepo

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Instituto de Física
Universidad de Antioquia
Phenomenology Group
<http://gfif.udea.edu.co>



Focus on

In collaboration with

Carlos Yaguna, Julian Calle, Mario Reig, Jose Valle (IFIC Valencia), Oscar Zapata (UdeA)

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Motivation

Lepton number

- Lepton number (L) is an accidental discrete or Abelian symmetry of the standard model (SM).
- Without neutrino masses L_e, L_μ, L_τ are also conserved.
- The processes which violate individual L are called Lepton flavor violation (LFV) processes.
- All the neutrino mass models predict, to some extent, LFV processes
- Only models with Majorana neutrinos predict processes of total $L = L_e + L_\mu + L_\tau$ violation, like **neutrino less doublet beta decay** (NLDBD) or its collider equivalent at the LHC for example.
- NLDBD is experimentally challenging, specially if there is a massless neutrino in the spectrum.

with M.Reig, J.W.F Vale, O. Zapata, arXiv:806.09977

Total lepton number conservation

In the near future lepton number conservation could be established.

- If L is a conserved quantum number, it must be related to a gauge symmetry
- Z' must be massive and consequently it must be an spontaneously broken gauge symmetry
- An accidental global symmetry for L is left after symmetry breaking.

What is the minimal model with Lepton number as a gauge symmetry?

$$\text{SM} \times \text{U}(1)_{B-L} \xrightarrow[\langle S \rangle]{} \text{SM} + \text{Total Lepton number conservation} \quad (1)$$

where B is the *total baryon number*.

Exotic $B - L$

SM-like $B - L$ model

Field	$U(1)_{B-L}$
L	-1
H	0
S	s
$(\psi_R)^\dagger_\alpha$	r_α^1

Massless Majorana fermions ($n = 0, 1$)

$$L \left[(\psi_R)^\dagger_\alpha (\psi_R)^\dagger_\beta S^n \right] \Rightarrow r_\alpha + r_\beta + nS \neq 0, \quad \text{example: } r \neq 1, \text{ if } s = -2.$$

$U(1)_{B-L}$ with $3+\alpha$ zero Majorana Masses \iff SM with 3 zero Majorana masses

$$\text{For } \alpha \leq 2: (\psi_R)^\dagger_\alpha \rightarrow (\nu_R)^\dagger_\alpha \quad r_\alpha \rightarrow \nu_\alpha$$

¹Weyl notation with only left-handed fields defined; r_α restricted by anomaly cancellation

(Dirac) Neutrino masses

Seesaw mechanism

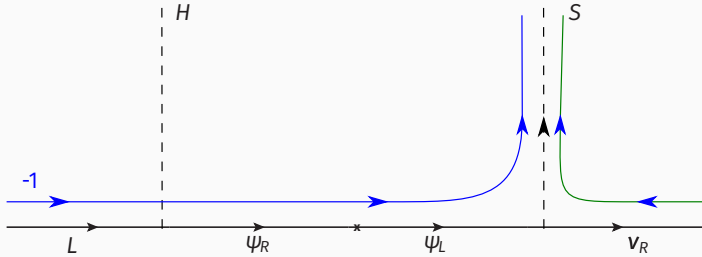
For Dirac neutrino masses: we require to introduce at least one SM-singlet heavy Dirac fermión (Weyl fermion notation)

$$\mathcal{L} = i (\psi_L)^\dagger \bar{\sigma}^\mu \partial_\mu \psi_L - m (\psi_R)^\dagger \psi_L + \text{h.c.} \quad (2)$$

Field	$U(1)_{B-L}$
L	-1
H	0
S	S
$(\nu_R)_i^\dagger$	ν_i
$(\psi_R)^\dagger$	r
ψ_L	$-r$

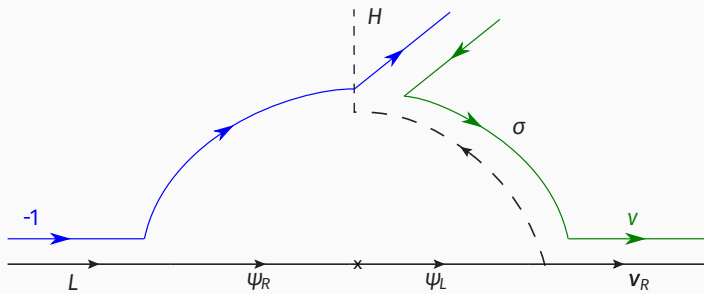
If $(\psi_R)_\alpha^\dagger$ can couple with $(\psi_R)_\beta^\dagger$, then $(\psi_R)_\beta^\dagger \rightarrow \psi_{L\alpha}$,

tree-level $r = 1, s \neq -2$

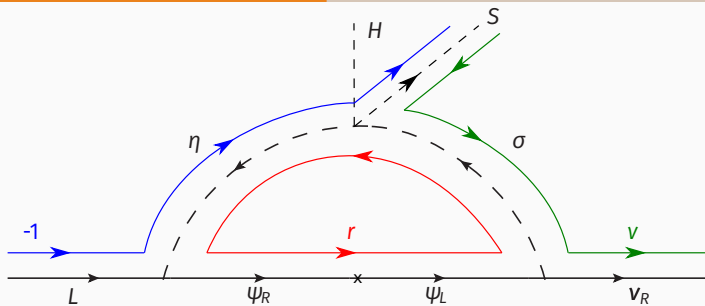


E. Ma, R. Srivastava arXiv:1411.5042 [PLB]

$$\nu \neq -1$$



Radiative Dirac seesaw

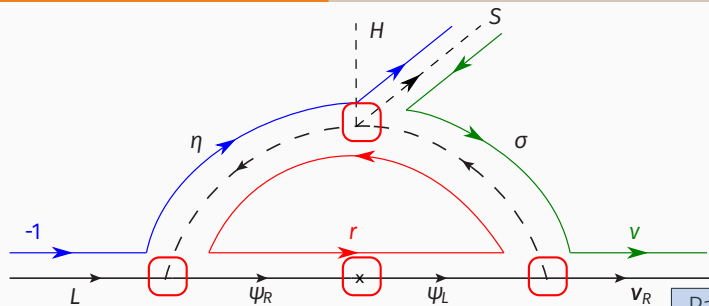


Soft breaking term induced:

$$\mathcal{L} \supset \kappa \sigma \eta^\dagger H,$$

where $\kappa = \lambda \langle S \rangle$.

Exotic $(\nu_R)^\dagger$ with $\nu \neq -1$, and vector-like Dirac fermion with $r \neq 1$



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$$\mathcal{L} \supset \kappa \sigma \eta^\dagger H,$$

where $\kappa = \lambda \langle S \rangle$.

$$-1 + \eta = -r$$

$$-r = -r$$

$$-r = -\nu + \sigma$$

$$\sigma = \eta + S$$

$$N_c = 1.$$

Particles	$U(1)_{B-L}$	$(SU(3)_c, SU(2)_L)_Y$
L_i	-1	$(1, 2)_{-1/2}$
H	0	$(1, 2)_{1/2}$
$(\nu_{Ri})^\dagger$	ν	$(1, 1)_0$
ψ_L	$-r$	$(N_c, 1)_0$
$(\psi_R)^\dagger$	r	$(N_c, 1)_0$
σ_a	$\nu - r$	$(N_c, 1)_0$
η_a	$1 - r$	$(N_c, 2)_{1/2}$
S	$\nu - 1$	$(N_c, 2)_{1/2}$

Systematic study

SM+Majorana neutrinos

$$\mathcal{L}_5 = \frac{y_{i\alpha}}{\Lambda} \epsilon_{ab} L_i^a H^b \epsilon_{cd} L_j^c H^d + \text{h.c.},$$

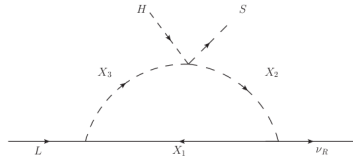
- Tree-level+one-loop+two-loops with DM, three-loops
- Dimension-7, Dimension-5 genuine topologies

Dirac

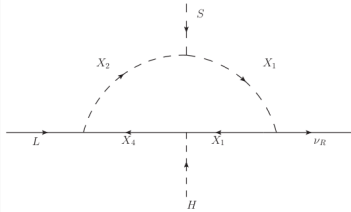
$$\mathcal{L}_5 = \frac{y_{i\alpha}}{\Lambda} \epsilon_{ab} L_i^a H^b (\nu_R)_\alpha^\dagger S + \text{h.c.},$$

- Three-level+One-loop with DM but extra Z_2 and Z'_2 for DM: Y., Chang-Yuan and D. Gui-Jun", arXiv:1802.05231 [PRD]
-

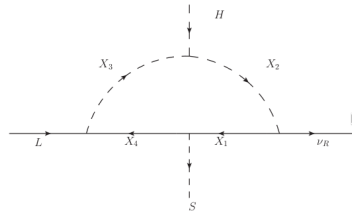
One-loop dimension-5 main Topologies



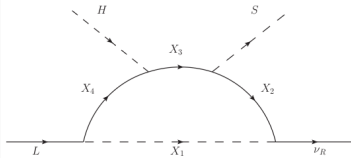
T3-1-A



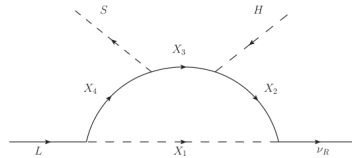
T1-3-D



T1-3-E

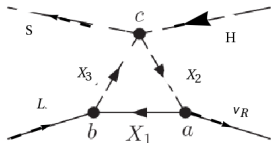


T1-2-A



T1-2-A

■ T3-1-A



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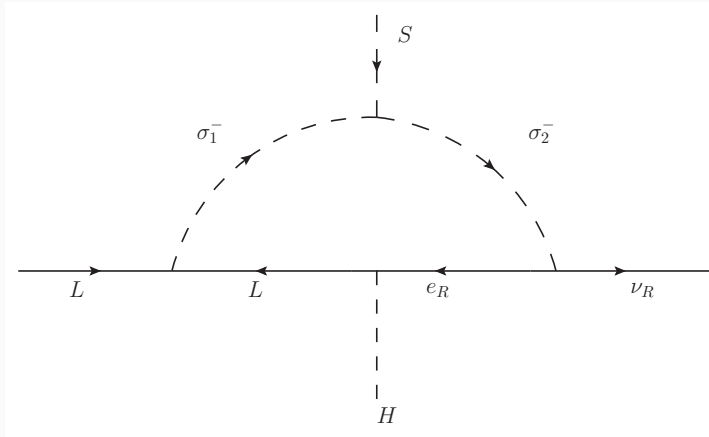
r[1]:= sol = Solve[{-v + X1 == X2, X3 == X1 + l,
  X2 + S == X3 + H}, {X3, X2, S}];
Print["Y: ", (sol /. {l -> -1, v -> 0, H -> 1}) /. X1 -> a]
Print["L: ", (sol /. {l -> -1, H -> 0}) /. X1 -> r]
Print["Full sltn: L: ", (((sol /. {l -> -1, H -> 0}) /. X1 -> r) /. v -> 4) /. {X3 -> η, X2 -> σ}]

Y: {{X3 -> -1 + α, X2 -> α, S -> 0}}
L: {{X3 -> -1 + r, X2 -> r - v, S -> -1 + v}}
Full sltn: L: {{η -> -1 + r, σ -> -4 + r, S -> 3}}

```

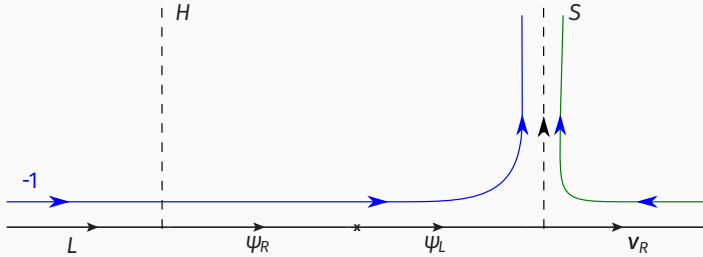
TABLE V. The finite one-loop diagrams generated from the topology T3. We show the possible quantum numbers of the messenger fields, the predictions for neutrino masses, and the dark matter candidates. The absence of tree level Dirac seesaw excludes certain values of α , where \emptyset and \cup denote empty set and universal set respectively. The dark matter Z'_2 symmetry can prevent tree level contributions to neutrino masses, such that the excluded α values become admissible and they are underlined.

Topology	Solution	X_1^F	X_2^S	X_3^S	Excluded α		Dark matter	Exotic charges
					Z_2^I	Z_2^{II}		
T3-1-A	I	$\mathbf{1}_\alpha^\mp$	$\mathbf{1}_\alpha^\pm$	$\mathbf{2}_{\alpha-1}^\mp$	<u>0, 2</u>	<u>0</u>	$[X_1, X_2, X_3]_0, [X_3]_2$	\times
	II	$\mathbf{2}_\alpha^\mp$	$\mathbf{2}_\alpha^\pm$	$\mathbf{1}_{\alpha-1}^\mp$	<u>± 1</u>	<u>± 1</u>	$[X_2]_{-1}, [X_2, X_3]_1$	\times
	III	$\mathbf{2}_\alpha^\mp$	$\mathbf{2}_\alpha^\pm$	$\mathbf{3}_{\alpha-1}^\mp$	<u>± 1</u>	<u>± 1</u>	$[X_2, X_3]_{-1}$	\checkmark
	IV	$\mathbf{3}_\alpha^\mp$	$\mathbf{3}_\alpha^\pm$	$\mathbf{2}_{\alpha-1}^\mp$	<u>0, 2</u>	\emptyset	$[X_2, X_3]_1$ $[X_1, X_2, X_3]_0$ $[X_2, X_3]_2$	\times \times \checkmark
$(m_\nu)_{\alpha\beta}/(\langle H \rangle \langle S \rangle) = M_{X_1}^{(i)} a_{\alpha i} b_{i\beta} c I_3(M_{X_2}, M_{X_3}, M_{X_1}^{(i)})$								



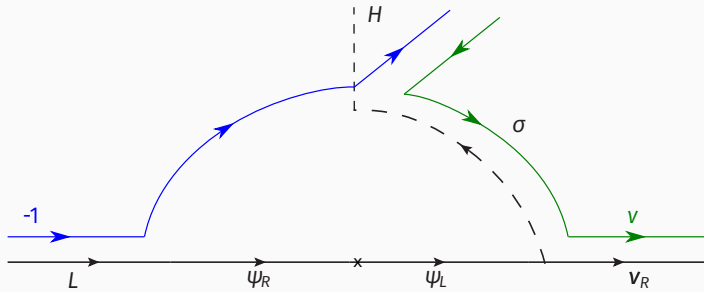
Model	$\overline{\nu_{R1}}$	$\overline{\nu_{R2}}$	$\overline{\nu_{R3}}$	σ_1^-	σ_2^-	S	$\sigma_1'^-$	$\sigma_2'^-$	S'
Dirac Zee	+4	+4	-5	-2	-5	-3	\times	\times	\times
Dirac Zee	-6	$+\frac{10}{3}$	$+\frac{17}{3}$	-2	+5	+7	-2	$-\frac{13}{3}$	$-\frac{7}{3}$

tree-level $r = 1, s \neq -2$

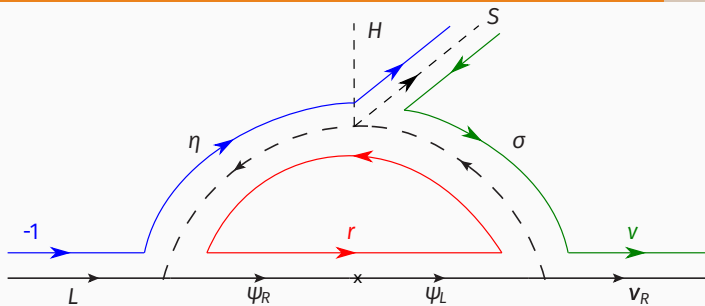


E. Ma, R. Srivastava arXiv:1411.5042 [PLB]

$$\nu \neq -1$$



Radiative Dirac seesaw

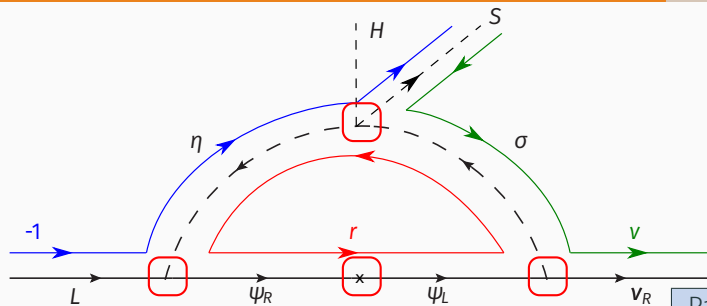


Soft breaking term induced:

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where $\kappa = \lambda \langle S \rangle$.

Exotic $(\nu_R)^\dagger$ with $\nu \neq -1$, and vector-like Dirac fermion with $r \neq 1$



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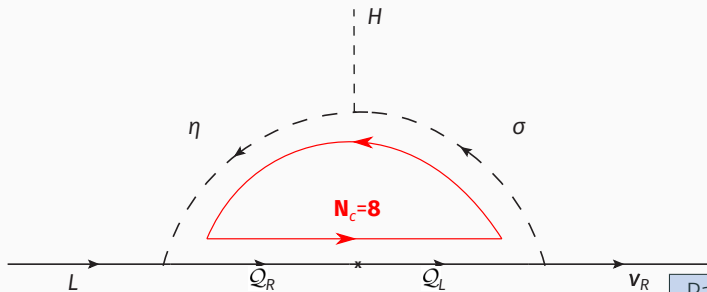
$$-r = -\nu + \sigma$$

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$$N_c = 1.$$

Particles	$U(1)_{B-L}$	$(SU(3)_c, SU(2)_L)_Y$
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S	$\nu - 1$	$(N_c, 2)_{1/2}$

The model: colored scotogenic



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$$\mathcal{L} \supset \kappa \sigma \eta^\dagger H,$$

$$-1 + \eta = -r$$

$$-r = -r$$

$$-r = -\nu + \sigma$$

$$\sigma = \eta + s$$

$$N_c = 8.$$

Particles	$U(1)_{B-L}$	$(SU(3)_c, SU(2)_L)_Y$
L_i	-1	$(1, 2)_{-1/2}$
H	0	$(1, 2)_{1/2}$
$(\nu_{Ri})^\dagger$	ν	$(1, 1)_0$
Q_L	$-r$	$(N_c, 1)_0$
$(Q_R)^\dagger$	r	$(N_c, 1)_0$
σ_a	$\nu - r$	$(N_c, 1)_0$
η_a	$1 - r$	$(N_c, 2)_{1/2}$

Neutrino masses and mixings

- ν_i are free parameter and could be fixed if we impose $U(1)_{B-L}$ to be local

$$r \neq 1,$$

$$\sum_i \nu_i = 3,$$

$$\sum_i \nu_i^3 = 3$$

	$(\nu_R)_1^\dagger$	$(\nu_R)_2^\dagger$	$(\nu_R)_3^\dagger$
$U(1)_{B-L}$	+4	+4	-5
$U(1)_{B-L}$	-6	$+\frac{10}{3}$	$+\frac{17}{3}$

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- To have at least a rank 2 neutrino mass matrix we need either:
 - At least two heavy Dirac fermions \mathcal{Q}_a , $a = 1, 2, \dots$
 - At least two sets of scalars η_a, σ_a

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Neutrino masses and mixings

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- To have at least a rank 2 neutrino mass matrix we need either:
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-

$$\mathcal{L} \supset \left[M_{\mathcal{Q}} (\mathcal{Q}_R)^\dagger \mathcal{Q}_L + h_i^a (\mathcal{Q}_R)^\dagger \tilde{\eta}_a^\dagger L_i + y_i^a \overline{\nu_{Ri}} \sigma_a^* \mathcal{Q}_L + \text{h.c.} \right] + \kappa^{ab} \sigma_a \eta_b^\dagger H + \dots$$

$$(\mathcal{M}_\nu)_{ij} = N_c \frac{M_Q}{64\pi^2} \sum_{a=1}^2 h_i^a y_j^a \frac{\sqrt{2}\kappa_{aa}v}{m_{S_{2R}^a}^2 - m_{S_{1R}^a}^2} \left[F\left(\frac{m_{S_{2R}^a}^2}{M_Q^2}\right) - F\left(\frac{m_{S_{1R}^a}^2}{M_Q^2}\right) \right] + (R \rightarrow I) \quad (3)$$

where $F(m_{S_\beta}^2/M_Q^2) = m_{S_\beta}^2 \log(m_{S_\beta}^2/M_Q^2)/(m_{S_\beta}^2 - M_Q^2)$. The four CP-even mass eigenstates are denoted as $S_{1R}^1, S_{2R}^1, S_{1R}^2, S_{2R}^2$, with a similar notation for the CP-odd ones.

If $(\mu_\eta^{aa})^2 \gg M_Q^2$ one has

$$\begin{aligned} (\mathcal{M}_\nu)_{ij} &= N_c \frac{M_Q}{32\pi^2} \sqrt{2}v \sum_{a=1}^2 \kappa^{aa} \frac{h_i^a y_j^a}{(\mu_\eta^{aa})^2} \\ &\sim 0.03 \text{ eV} \left(\frac{M_Q}{9.5 \text{ TeV}} \right) \left(\frac{\kappa^{aa}}{1 \text{ GeV}} \right) \left(\frac{50 \text{ TeV}}{\mu_\eta^{aa}} \right)^2 \left(\frac{h_i^a y_j^a}{10^{-6}} \right). \end{aligned} \quad (4)$$

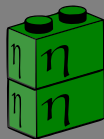
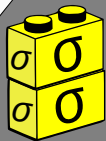
Dark matter

$U(1)_{B-L} \rightarrow$



if $r \neq 0$ (even with $N_c = 8$)





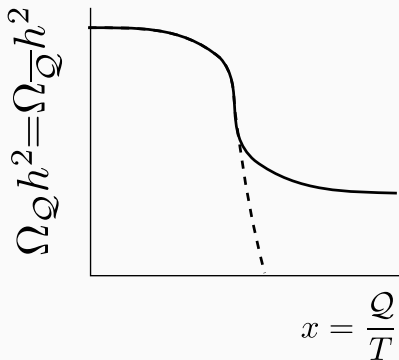


(Switch to Dirac fermions)

Because Q is a Dirac fermion, $Q\bar{Q}$ is also stable

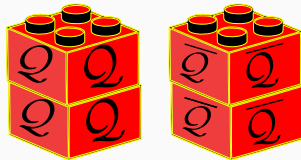
$$Q\bar{Q} \rightarrow g,$$

$$\overline{Q}Q \rightarrow g.$$



Step one

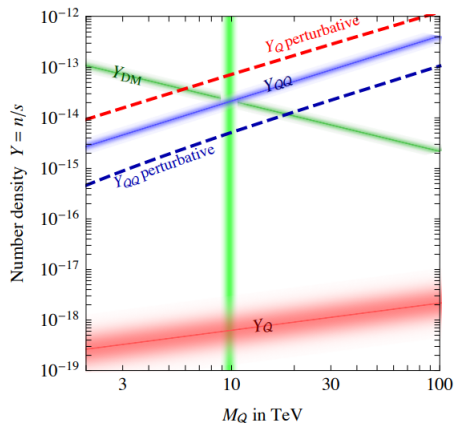
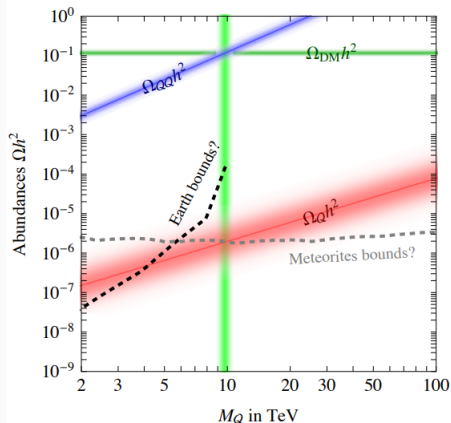
Q -onlyum



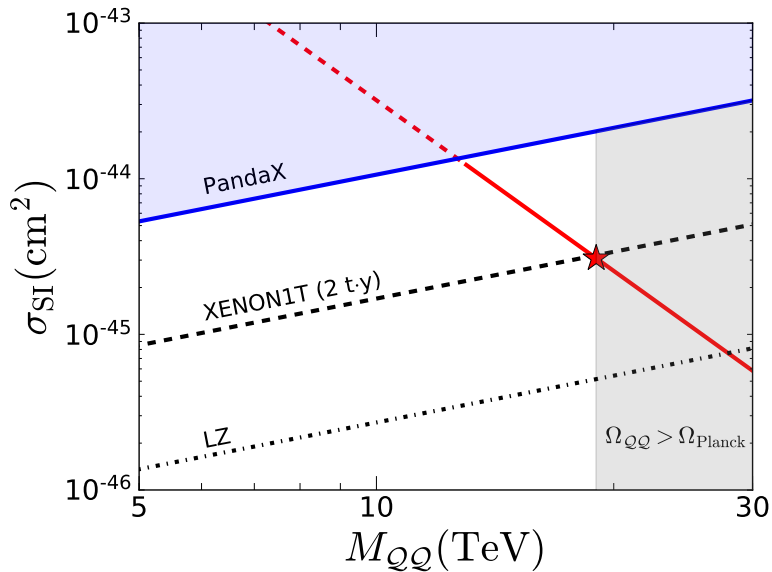
Step two

$$M_Q \simeq 9.5 \text{ TeV}$$

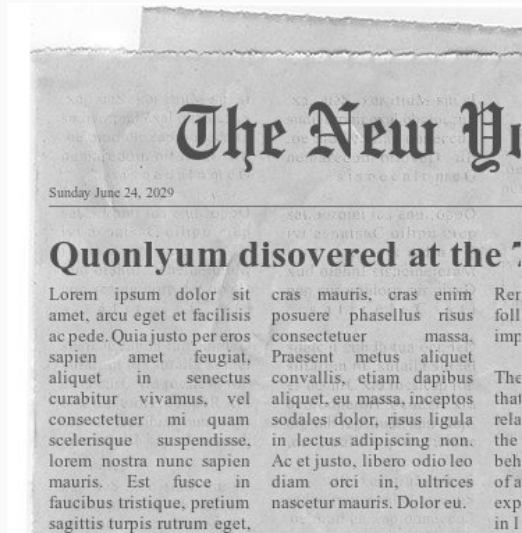
$$\Omega_{\text{hyb}} \sim 10^{-5} \Omega_{\text{DM}}$$



Direct detection







Long lived hadrons

$$p + p \longrightarrow Q + \bar{Q}$$



$$Q \rightarrow Qg$$

$$Q \rightarrow Qq\bar{q}$$

$\sqrt{s} = 65 \text{ TeV}$ needed to discover $M_Q = 9.5 \text{ TeV}$.

Conclusions

Standard Model with right-handed neutrinos of exotic $B - L$ charges



Conclusions

Standard Model with right-handed neutrinos of exotic $B - L$ charges

Dirac neutrino masses and DM

- Spontaneously broken $U(1)_{B-L}$ generates a radiative Dirac Type-I seesaw.
- A remnant symmetry makes the lightest field circulating the loop stable and good dark matter candidate.
- If color is also circulating the loop, the colored dark matter scenario can be realized

DM is made of two color octets with mass around 9.5 TeV

- For standard cosmology:
 - A single point to be discovered in Direct Detection.
 - Crosscheck at future colliders possible.