# **Gauged Lepton number**

with dark matter and dark baryogenesis



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#### Focus on

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In collaboration with

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## **Dark sectors**











# $\mathcal{L} = -\frac{1}{4}V_{\mu\nu}V^{\mu\nu} + i\sum_{i}\psi_{i}^{\dagger}\mathcal{D}\psi_{i}$

$$egin{aligned} \mathcal{L} &= -rac{1}{4} V_{\mu
u} V^{\mu
u} + i \sum_i \psi_i^\dagger \mathcal{D} \psi_i \ - h \left( \psi_1 \psi_2 \Phi + ext{h.c} 
ight) \end{aligned}$$

SSB: SM-singlet Dirac fermion dark matter  $m_{\Psi} = h \langle \Phi \rangle$ 

Gauged Symmetry:  $\mathcal{X} \to D$ :

Gauged Symmetry:  $\mathcal{X} \to X$ :



$$\overline{\Psi}\Psi = \psi_1\psi_2 + \psi_1^{\dagger}\psi_2^{\dagger} \rightarrow \psi_{\alpha}\psi_{\beta}\Phi^{(*)}, \qquad \alpha = 1, \dots N \rightarrow N > 4$$

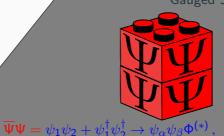


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SSB: SM-singlet Dirac fermion dark matter  $m_{\Psi} = h \langle \Phi \rangle$ 

Gauged Symmetry:  $\mathcal{X} \to B$ :  $q\overline{q} \to Z' \to \text{jets}$ Gauged Symmetry:  $\mathcal{X} \to L$ :



$$\alpha = 1, \dots N \rightarrow N > 4$$



 $\mathcal{L} = -rac{1}{4}V_{\mu
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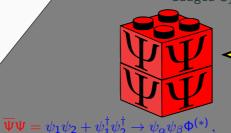
$$-h(\psi_1\psi_2\Phi+\text{h.c})$$

SSB: SM-singlet Dirac fermion dark matter  $m_{\Psi} = h \langle \Phi \rangle$ 

LHC productio

Gauged Symmetry:  $\mathcal{X} \to \mathcal{B}$ :  $q\overline{q} \to \mathcal{Z}' \to \mathsf{jets}$ 

Gauged Symmetry: 
$$\mathcal{X} \rightarrow \mathcal{L}$$
:



multi-component dark matter

 $\alpha = 1, \dots N \rightarrow N > 4$ 



 $\mathcal{L} = -rac{1}{4}V_{\mu
u}V^{\mu
u} + i\sum_{i}\psi_{i}^{\dagger}\mathcal{D}\psi_{i}$ 

$$-y(\psi_1\psi_2S+\text{h.c})$$

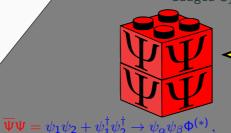
SSB: SM-singlet Dirac fermion

CP violation Yukawa y

LHC productio

Gauged Symmetry:  $\mathcal{X} \to B$ :  $q\overline{q} \to Z' \to \text{jets}$ 

Gauged Symmetry:  $\mathcal{X} \rightarrow \mathcal{L}$ :



multi-component dark matter

 $\alpha = 1, \dots N \rightarrow N > 4$ 

### **Anomaly cancellation**

Any *universal* local Abelian extension of the Standard Model can be reduced to a set of integers which must satisfy the gravitational anomaly,  $[SO(1,3)]^2 U(1)_Y$ , and the cubic anomaly,  $[U(1)_X]^3$  conditions:

$$\sum_{\alpha=1}^{N} z_{\alpha} = 0, \qquad \sum_{\alpha=1}^{N} z_{\alpha}^{3} = 0, \qquad (1)$$

• From a list of N-2 integers, e.g., for N even

$$\mathbf{q} = [l_1, l_2, \cdots, l_n, k_1, k_2, \cdots, k_n], \qquad n = (N-2)/2.$$
 (2)

in the range [-m, m], build two vector-like solutions of N integers,

$$\mathbf{x} = [l_1, k_1, \dots k_n, -l_1, -k_1, \dots - k_n,]$$
  $\mathbf{y} = [0, 0, l_1, \dots l_n, -l_1, \dots - l_n]$  (3)

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• Obtain a (some times) non vector-like solution with  $z_{max} = 2m$ 

$$\mathbf{z} = \mathbf{x} \oplus \mathbf{y} = \left(\sum_{i=1}^{N} x_i y_i^2\right) \mathbf{x} + \left(\sum_{i=1}^{N} x_i^2 y_i\right) \mathbf{y},$$
(4)

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in the range [-m, m], build two vector-like solutions of N integers,

$$\mathbf{x} = [l_1, \mathbf{k_1}, \dots \mathbf{k_n}, -l_1, -\mathbf{k_1}, \dots - \mathbf{k_n},]$$
  $\mathbf{y} = [0, 0, l_1, \dots l_n, -l_1, \dots - l_n]$  (3)

• Obtain a (some times) non vector-like solution with  $z_{max} = 2m$ 

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The parameter space to be explored with  $z_{\text{max}}=20~(m=10)$  has  $96\,153$  non vector-like solutions

# of 
$$\mathbf{q}$$
 lists =  $(2m+1)^{N-2} = \begin{cases} 9261 \to 3 & N=5 \\ 194841 \to 38 & N=6 \\ \vdots & \vdots \\ 1.6 \times 10^{13} \to 65910 & N=12 \end{cases}$ , instead  $10^{19}$ 

• From a list of N-2 integers, e.g., for N even

$$\mathbf{q} = [2, 3, -1, -3], \qquad n = 6.$$
 (2)

in the range [-3,3], build two vector-like solutions of 6 integers,

$$x = [2, -1, -3, -2, 1, 3,]$$
  $y = [0, 0, 2, \dots 3, -2, \dots -3]$  (3)

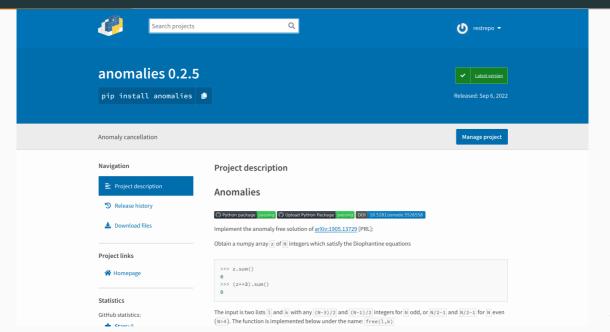
• Obtain a (some times) non vector-like solution with  $z_{\text{max}} = 2 \times 3 = 6$ 

$$\mathbf{z} = \mathbf{x} \oplus \mathbf{y} = \left(\sum_{i=1}^{N} x_i y_i^2\right) \mathbf{x} + \left(\sum_{i=1}^{N} x_i^2 y_i\right) \mathbf{y},$$
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 lists =  $(2m+1)^{N-2}$  = 
$$\begin{cases} 9261 \to 3 & N = 5 \to [1, -2, -3, 5, 5, -6] \\ 194841 \to 38 & N = 6 \\ \vdots & \vdots \\ 1.6 \times 10^{13} \to 65910 & N = 12 , \text{ instead } 10^{19} \end{cases}$$
 (5)

# https://pypi.org/project/anomalies/







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# Minimal secluded model with SM-singlet massive chiral fermions from SSB: $U(1)_D$

$$\mathcal{L} = i\psi_i^{\dagger} \mathcal{D} \psi_i - \frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \sum_{i < j} h_{ij} \psi_i \psi_j \phi^{(*)} + \text{h.c}$$
 (6)

 $96\,153 
ightarrow 5\,196$  multi-component DM ( $\emph{N}=8,12$ ) ightarrow 142 with three Dirac-fermion DM

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$$z = [1, -2, -2, 4, 5, -7, -7, 8] \rightarrow \phi = 9 \rightarrow [(1, 8), (-2, -7), (4, 5)]$$
 (7)

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$$z = [1, -2, -2, 4, 5, -7, -7, 8] \rightarrow \phi = 9 \rightarrow [(1, 8), (-2, -7), (4, 5)]$$
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$$\mathcal{L} \subset h_{(1,8)} \psi_1 \psi_8 \phi^* \phi^{(*)} + \sum_{a,b=1}^2 h_{(-2a,-7b)} \psi_4 \psi_{-7} \phi + h_{(4,5)} \psi_4 \psi_5 \phi^* \phi^{(*)} + \text{h.c.}$$
(8)

# Simplest secluded model with SM-singlet massive chiral fermions from SSB: $U(1)_D$

$$\mathcal{L} = i\psi_i^{\dagger} \mathcal{D} \psi_i - \frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \sum_{i < j} h_{ij} \psi_i \psi_j \phi^{(*)} + \text{h.c}$$
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$$z = [1, 2, 2, 4, -5, -5, -7, 8] \rightarrow \phi = 3 \rightarrow [(1, 2), (2, -5), (-5, 8), (4, -7)]$$
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# Simplest secluded model with SM-singlet massive chiral fermions from SSB: $\mathrm{U}(1)_{D}$

$$\mathcal{L} = i\psi_i^{\dagger} \mathcal{D} \psi_i - \frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \sum_{i < j} h_{ij} \psi_i \psi_j \phi^{(*)} + \text{h.c}$$
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$$\mathbf{z} = [1, 2, 2, 4, -5, -5, -7, 8] \to \phi = 3 \to [(1, 2), (2, -5), (-5, 8), (4, -7)] \tag{10}$$

$$1 \qquad 2 \qquad 2 \qquad -5 \qquad -5 \qquad 8$$

$$1 \qquad \begin{bmatrix}
0 & h_{(1,2)} & h'_{(1,2)} & 0 & 0 & 0 \\
h_{(1,2)} & 0 & 0 & h_{(2,-5)} & h_{(2,-5)} & 0 \\
h'_{(1,2)} & 0 & 0 & 0 & 0 & 0 \\
-5 & h'_{(1,2)} & 0 & 0 & 0 & 0 & h_{(-5,8)} \\
-5 & 0 & h_{(2,-5)} & 0 & 0 & 0 & h'_{(-5,8)} \\
0 & 0 & 0 & h_{(-5,8)} & h'_{(-5,8)} & 0
\end{bmatrix}$$

$$\Psi \phi^{(*)} + h_{(4,-7)} \psi_4 \psi_{-7} \phi^*$$

$$(11)$$

7

# Standard model extended with $U(1)_{\mathcal{X}=X \text{ or } \mathbf{D}}$ gauge symmetry

Fields	$SU(2)_L$	$U(1)_Y$	$U(1)_{\mathcal{X}=\mathbf{D} \text{ or } X}$
$Q_i^{\dagger}$	2	-1/6	Q
$d_{Ri}$	1	-1/2	d
$u_{Ri}$	1	+2/3	и
$L_i^{\dagger}$	2	+1/2	L
$e_{Ri}$	1	-1	e
Н	2	1/2	h
$\chi_{\alpha}$	1	0	$z_{\alpha}$

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	_	· ·	Ψ

#### Table 1:

$$i = 1, 2, 3, \ \alpha = 1, 2, \dots, N'$$

# Standard model extended with $U(1)_{\mathcal{X}=L \text{ or } \mathbf{B}}$ gauge symmetry

Fields	$SU(2)_L$	$U(1)_Y$	$U(1)_{\mathcal{X}=B \text{ or } L}$
$Q_i^{\dagger}$	2	-1/6	Q
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$u_{Ri}$	1	+2/3	и
$L_i^{\dagger}$	2	+1/2	L
$e_{Ri}$	1	-1	e
Н	2	1/2	h = 0
$\chi_{\alpha}$	1	0	$z_{\alpha}$
$(L'_L)^{\dagger}$	2	1/2	-x'
$L_R^{\prime\prime}$	2	-1/2	x''
$e_R'$	1	-1	x'
$(e_L^{\prime\prime})^\dagger$	1	1	-x''
Ф	1	0	$\phi$
S	1	0	S

**Table 1:** minimal set of new fermion content: L = e = 0 for  $\mathcal{X} = B$ . Or Q = u = d = 0 for  $\mathcal{X} = L$ .  $i = 1, 2, 3, \alpha = 1, 2, ..., N'$ 

## Anomaly cancellation: $\mathcal{X} = L$ or B

The anomaly-cancellation conditions on  $[SU(3)_c]^2 U(1)_X$ ,  $[SU(2)_L]^2 U(1)_X$ ,  $[U(1)_Y]^2 U(1)_X$ , allow us to express three of the X-charges in terms of the others

$$\mathbf{u} = -\mathbf{e} - \frac{2}{3}\mathbf{L} - \frac{1}{9}(x' - x''), \quad \mathbf{d} = \mathbf{e} + \frac{4}{3}\mathbf{L} - \frac{1}{9}(x' - x''), \quad \mathbf{Q} = -\frac{1}{3}\mathbf{L} + \frac{1}{9}(x' - x''), \quad (12)$$

while the  $[U(1)_X]^2 U(1)_Y$  anomaly condition reduces to

$$(e+L)(x'-x'')=0.$$
 (13)

- Previously: x' = x''
- We choose instead (h = 0):

$$e = -L, (14)$$

so that (L is still a free parameter)

$$Q = -u = -d = -\frac{1}{3}L + \frac{1}{9}(x' - x''). \tag{15}$$

If 
$$B = 0 \rightarrow U(1)_L$$

## Anomaly cancellation: $\mathcal{X} = L$

The gravitational anomaly,  $[SO(1,3)]^2 U(1)_Y$ , and the cubic anomaly,  $[U(1)_X]^3$ , can be written as the following system of Diophantine equations, respectively,

$$\sum_{\alpha=1}^{N} z_{\alpha} = 0, \qquad \sum_{\alpha=1}^{N} z_{\alpha}^{3} = 0, \qquad (16)$$

where

$$z_1 = -x',$$
  $z_2 = x'',$   $z_{2+i} = L, \quad i = 1, 2, 3$  (17)

 $\rightarrow$ 

$$9Q = -\sum_{\alpha=1}^{5} z_{\alpha} = -x' + x'' + L + L + L, \qquad (18)$$

$$L = 0 \rightarrow U(1)_B$$
 but  $Q = 0 \rightarrow U(1)_L$ 

• B = 0 with L = 6

$$(6,6,6,-8,-10,5,13,-9,-9)$$

- B = 0 with L = 6
- Electroweak-scale vector-like fermions with  $\Phi = 18$ :  $(L_I')^{\dagger} L_R'' \Phi \rightarrow x' = 8, \ x'' = -10$

$$(6, 6, 6, -8, -10, 5, 13, -9, -9)$$

- B = 0 with L = 6
- Electroweak-scale vector-like fermions with  $\Phi=18$ :  $(L'_L)^\dagger L''_R \Phi \to \varkappa' = 8, \ \varkappa'' = -10$
- L + L + L x' + x'' = 0

$$(6,6,6,-8,-10,5,13,-9,-9)$$

- B = 0 with L = 6
- Electroweak-scale vector-like fermions with  $\Phi = 18$ :  $(L'_L)^{\dagger} L''_R \Phi \rightarrow x' = 8, \ x'' = -10$

• 
$$L + L + L - x' + x'' = 0$$

• Dirac-fermionic DM:  $(\chi_L)^{\dagger} \chi_R' \Phi^* \rightarrow z_3 = 5, \ z_4 = 13$ 

$$(6, 6, 6, -8, -10, 5, 13, -9, -9)$$

- B = 0 with L = 6
- Electroweak-scale vector-like fermions with  $\Phi = 18$ :  $(L'_I)^{\dagger} L''_R \Phi \rightarrow \lambda' = 8, \ \lambda'' = -10$
- L + L + L x' + x'' = 0
- Dirac-fermionic DM:  $(\chi_L)^{\dagger} \chi_R' \Phi^* \rightarrow z_3 = 5, \ z_4 = 13$
- (Two generations) Majorana-fermionic DM:  $(\chi_i'')^{\dagger} \chi_i'' \Phi \rightarrow z_5 = -9, z_6 = -9$

$$(6, 6, 6, -8, -10, 5, 13, -9, -9)$$

- B = 0 with L = 6
- Electroweak-scale vector-like fermions with Φ = 18:  $(L'_L)^{\dagger} L''_{P}Φ \rightarrow x' = 8, \ x'' = -10$

$$I + I + I - x' + x'' = 0$$

Dirac-fermionic DM:

$$(\chi_L)^{\dagger} \chi_R' \Phi^* \to z_3 = 5, \ z_4 = 13$$

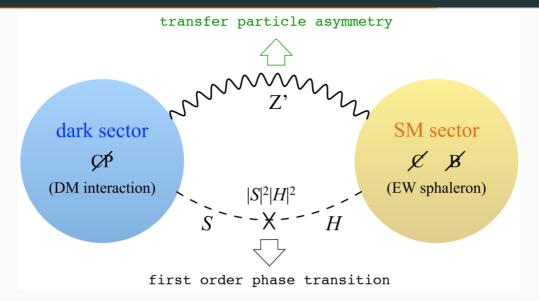
(6, 6, 6, -8, -10, 5, 13, -9, -9)

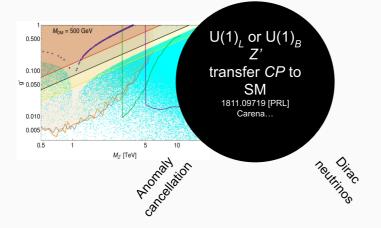
• (Two generations) Majorana-fermionic DM:  $(\chi_i'')^{\dagger} \chi_i'' \Phi \rightarrow z_5 = -9, z_6 = -9$ 

Only 4 solutions from 96 153

- 1	k	solution	gcd	n	zmax	hidden
[-2, -3, 0]	[1, 2, 3, 2]	[5, 6, 6, 6, -8, -9, -9, -10, 13]	4	9	13	[{'S': 18, 'ψ': [(-9, -9), (-8, -10), (5, 13)]}]
[2, 0, 3]	[-2, 1, -3, -1]	[2, 3, 3, 3, 6, -8, -11, -15, 17]	12	9	17	$\hbox{\tt [\{'S': 9, '\psi': [(2, -11), (6, -15), (-8, 17)]\}]}$
[-4, -2, 1]	[2, -4, 4, -2]	[1, -2, 6, 6, 6, -9, -9, -16, 17]	16	9	17	$\hbox{[('S': 18, '\psi': [(-9, -9), (1, 17), (-2, -16)])]}$
[3, -2, -4]	[-2, -1, -2, 3]	[1, 2, 3, -6, -6, -6, 15, 16, -19]	2	9	19	[{'S': 18, '\pu': [(1, -19), (3, 15), (2, 16)]}]

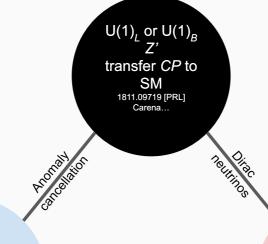
## Dark sector baryogenesis





Anomalons:

DM



Method to find  $\Sigma n=0$ ,  $\Sigma n^3=0$  solutions 1905.13729 [PRL] Costa...

Anomalons:

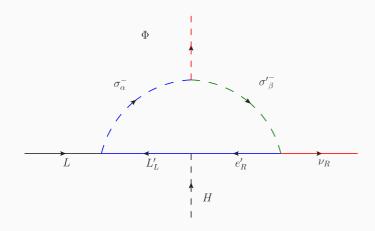
Multicomponent DM

Scotogenic neutrino masses

hep-ph/0601225 [PRL→PRD] Ma

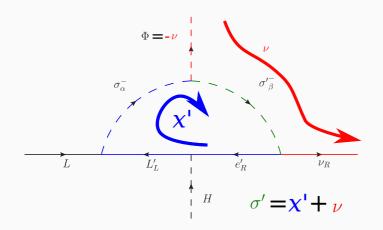
# Gauge Baryon number scotogenic realization: arXiv:2205.05762 [PRD]

with Andrés Rivera (UdeA) and Walter Tangarife (Loyola U.)



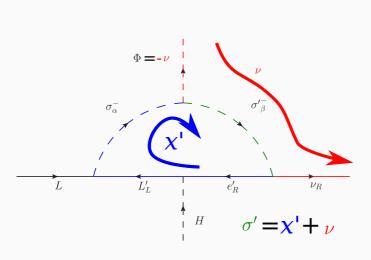
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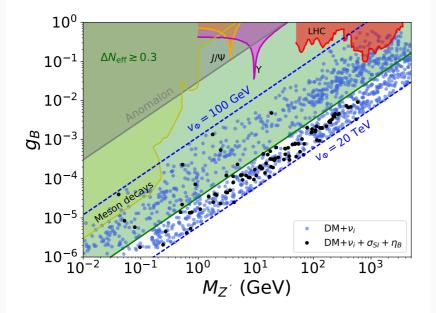


$\overline{}$	3.)					
	Field	$SU(2)_L$	$U(1)_Y$	$U(1)_B$		
	u <sub>Ri</sub>	1	2/3	u = 1/3		
	$d_{Ri}$	1	-1/3	d = 1/3		
	$(Q_i)^{\dagger}$	2	-1/6	Q = -1/3		
	$(L_i)^{\dagger}$	2	1/2	L=0		
	$e_R$	1	-1	e = 0		
	$(L'_L)^{\dagger}$	2	1/2	-x' = -3/5		
	$e'_R$	1	-1	x' = 3/5		
	$L_R^{\prime\prime}$	2	-1/2	x'' = 18/5		
	$\left(e_L^{\prime\prime} ight)^\dagger$	1	1	-x'' = -18/5		
	$ u_{R,1}$	1	0	-3		
	$\nu_{R,2}$	1	0	-3		
	$\chi_R$	1	0	6/5		
	$(\chi_L)^{\dagger}$	1	0	9/5		
	Н	2	1/2	0		
	5	1	0	3		
	Φ	1	0	3		
	$\sigma_{lpha}^-$	1	1	3/5		
	$\sigma'_{\alpha}^{-}$	1	-1	-12/5		

arXiv:2205.05762 [PRD] https://github.com/anferivera/DarkBariogenesis

- SARAH $\rightarrow$ SPheno $\rightarrow$ MicroMegas
- $\eta_B$  calculation code
- Python notebook with the scan

## Black points: Dirac neutrinos with proper DM and baryon assymetry



#### Conclusions

A methodology to find all the *universal* Abelian extensions of the standard model is designed

All of the extensions can be reformulated as the solution of

$$\sum_{\alpha=1}^{N} z_{\alpha} = 0, \qquad \sum_{\alpha=1}^{N} z_{\alpha}^{3} = 0,$$

which we fully scan until N=12 and  $|z_{\sf max}|=20$ 

Once the physical conditions are stablished, the full set of self-consistent models are found from a simple data-analysis procedure