Gauged Lepton number

with dark matter and dark baryogenesis



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Focus on

In collaboration with

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Dark sectors











 $\mathcal{L} = -\frac{1}{4}V_{\mu\nu}V^{\mu\nu} + i\sum_{i}\psi_{i}^{\dagger}\mathcal{D}\psi_{i}$

$$-h(\psi_1\psi_2\Phi + \text{h.c})$$

Anomalons: SM-singlet Dirac fermion dark matter $m_{\Psi}=h\langle\Phi
angle$

LHC production

Gauged Symmetry: $\mathcal{X} \to D$:

Gauged Symmetry: $\mathcal{X} \to X$:



$$\overline{\Psi}\Psi = \psi_1\psi_2 + \psi_1^{\dagger}\psi_2^{\dagger} \rightarrow \psi_{\alpha}\psi_{\beta}\Phi^{(*)}, \qquad \alpha = 1, \dots N \rightarrow N > 4$$



 $\mathcal{L} = -rac{1}{4}V_{\mu
u}V^{\mu
u} + i\sum_{i}\psi_{i}^{\dagger}\mathcal{D}\psi_{i}$

$$-h(\psi_1\psi_2\Phi+\text{h.c})$$

Anomalons: SM-singlet Dirac fermion dark matter $m_{\Psi} = h\langle \Phi \rangle$

LHC production

Gauged Symmetry: $\mathcal{X} \to B$: $q\overline{q} \to Z' \to \text{jets}$ Gauged Symmetry: $\mathcal{X} \to L$:



$$\overline{\Psi}\Psi = \psi_1\psi_2 + \psi_1^{\dagger}\psi_2^{\dagger} \to \psi_{\alpha}\psi_{\beta}\Phi^{(*)}, \qquad \alpha =$$



 $\mathcal{L} = -rac{1}{4}V_{\mu
u}V^{\mu
u} + i\sum_{i}\psi_{i}^{\dagger}\mathcal{D}\psi_{i}$

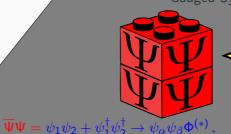
$$-h(\psi_1\psi_2\Phi + \text{h.c})$$

Anomalons: SM-singlet Dirac fermion

dark matter $m_{\Psi} = h \langle \Phi \rangle$

Gauged Symmetry: $\mathcal{X} \to \mathcal{B}$: $q\overline{q} \to \mathcal{Z}' \to \mathsf{jets}$

Gauged Symmetry: $\mathcal{X} \rightarrow \mathcal{L}$:



multi-component dark matter

 $\alpha = 1, \dots N \rightarrow N > 4$



Local $U(1)_{\mathcal{X}}$ $\mathcal{L} = -rac{1}{4}V_{\mu
u}V^{\mu
u} + i\sum_{i}\dot{\psi_{i}}^{\dagger}\mathcal{D}\psi_{i}$

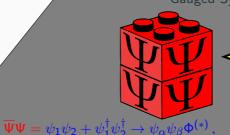
$$-y(\psi_1\psi_2S+\text{h.c})$$

Anomalons: SM-singlet Dirac fermion

CP violation Yukawa y

Gauged Symmetry: $\mathcal{X} \to B$: $q\overline{q} \to Z' \to \text{jets}$

Gauged Symmetry: $\mathcal{X} \rightarrow L$:



multi-component dark matter

 $\alpha = 1, \dots N \rightarrow N > 4$

Anomaly cancellation

Any local Abelian extension of the Standard Model can be reduced to a set of integers which must satisfy the gravitational anomaly, $[SO(1,3)]^2 U(1)_Y$, and the cubic anomaly, $[U(1)_X]^3$ conditions:

$$\sum_{\alpha=1}^{N} z_{\alpha} = 0, \qquad \sum_{\alpha=1}^{N} z_{\alpha}^{3} = 0, \qquad (1)$$

• From a list of N-2 integers, e.g., for N even

$$\mathbf{q} = [l_1, l_2, \cdots, l_n, k_1, k_2, \cdots, k_n], \qquad n = (N-2)/2.$$
 (2)

in the range [-m, m], build two vector-like solutions of N integers,

$$\mathbf{x} = [l_1, k_1, \dots k_n, -l_1, -k_1, \dots - k_n,]$$
 $\mathbf{y} = [0, 0, l_1, \dots l_n, -l_1, \dots - l_n]$ (3)

• From a list of N-2 integers, e.g., for N even

$$\mathbf{q} = [l_1, l_2, \cdots, l_n, k_1, k_2, \cdots, k_n], \qquad n = (N-2)/2.$$
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 $\mathbf{y} = [0, 0, l_1, \dots l_n, -l_1, \dots - l_n]$ (3)

• Obtain a (some times) non vector-like solution with $z_{max} = 2m$

$$\mathbf{z} = \mathbf{x} \oplus \mathbf{y} = \left(\sum_{i=1}^{N} x_i y_i^2\right) \mathbf{x} + \left(\sum_{i=1}^{N} x_i^2 y_i\right) \mathbf{y},$$
(4)

• From a list of N-2 integers, e.g., for N even

$$\mathbf{q} = [l_1, l_2, \cdots, l_n, k_1, k_2, \cdots, k_n], \qquad n = (N-2)/2.$$
 (2)

in the range [-m, m], build two vector-like solutions of N integers,

$$\mathbf{x} = [l_1, \mathbf{k_1}, \dots \mathbf{k_n}, -l_1, -\mathbf{k_1}, \dots - \mathbf{k_n},]$$
 $\mathbf{y} = [0, 0, l_1, \dots l_n, -l_1, \dots - l_n]$ (3)

• Obtain a (some times) non vector-like solution with $z_{max} = 2m$

$$\mathbf{z} = \mathbf{x} \oplus \mathbf{y} = \left(\sum_{i=1}^{N} x_i y_i^2\right) \mathbf{x} + \left(\sum_{i=1}^{N} x_i^2 y_i\right) \mathbf{y}, \tag{4}$$

The parameter space to be explored with $z_{\rm max}=20~(m=10)$ has $96\,153$ non vector-like solutions

of
$$\mathbf{q}$$
 lists = $(2m+1)^{N-2} = \begin{cases} 9261 \to 3 & N=5 \\ 194841 \to 38 & N=6 \\ \vdots & \vdots \\ 1.6 \times 10^{13} \to 65910 & N=12 \end{cases}$, instead 10^{19}

• From a list of N-2 integers, e.g., for N even

$$\mathbf{q} = [2, 3, -1, -3], \qquad n = 6.$$
 (2)

in the range [-3,3], build two vector-like solutions of 6 integers,

$$x = [2, -1, -3, -2, 1, 3,]$$
 $y = [0, 0, 2, \dots 3, -2, \dots -3]$ (3)

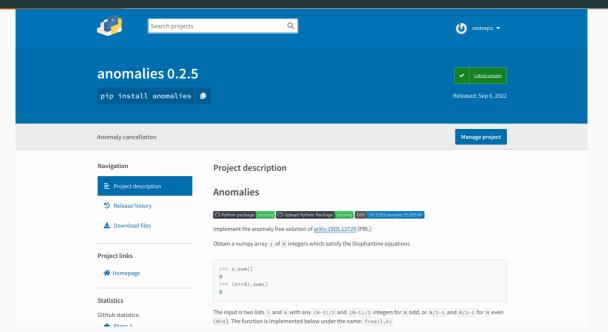
• Obtain a (some times) non vector-like solution with $z_{max} = 2 \times 3 = 6$

$$\mathbf{z} = \mathbf{x} \oplus \mathbf{y} = \left(\sum_{i=1}^{N} x_i y_i^2\right) \mathbf{x} + \left(\sum_{i=1}^{N} x_i^2 y_i\right) \mathbf{y},$$
(4)

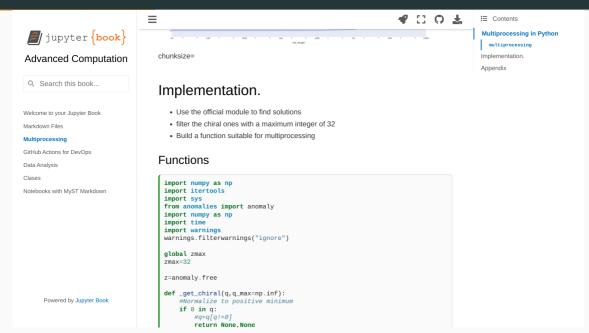
The parameter space to be explored with $z_{\text{max}}=20~(m=10)$ has $96\,153$ non vector-like solutions

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 lists = $(2m+1)^{N-2}$ =
$$\begin{cases} 9261 \to 3 & N = 5 \to [1, -2, -3, 5, 5, -6] \\ 194841 \to 38 & N = 6 \\ \vdots & \vdots \\ 1.6 \times 10^{13} \to 65910 & N = 12, \text{ instead } 10^{19} \end{cases}$$
 (5)

https://pypi.org/project/anomalies/



https://restrepo.github.io/Advanced_Computation







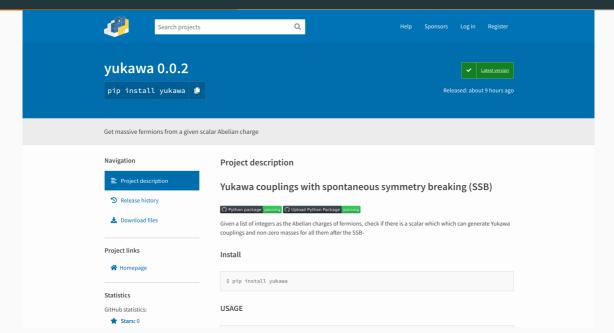
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https://pypi.org/project/yukawa/



Simplest secluded model with SM-singlet massive chiral fermions from SSB: $U(1)_{D}$

$$\mathcal{L} = i\psi_i^{\dagger} \mathcal{D} \psi_i - \frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \sum_{i \le j} h_{ij} \psi_i \psi_j \phi^{(*)} + \text{h.c}$$
 (6)

96 153 ightarrow 5 196 multi-component DM (N = 8, 12) ightarrow 28 with two Dirac-fermion DM

Simplest secluded model with SM-singlet massive chiral fermions from SSB: $U(1)_{\it D}$

$$\mathcal{L} = i\psi_i^{\dagger} \mathcal{D} \psi_i - \frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \sum_{i < j} h_{ij} \psi_i \psi_j \phi^{(*)} + \text{h.c}$$
 (6)

 $96\,153
ightarrow 5\,196$ multi-component DM (N=8,12)
ightarrow 28 with two Dirac-fermion DM

$$z = [1, 2, 2, 4, -5, -5, -7, 8] \rightarrow \phi = 3 \rightarrow [(1, 2), (2, -5), (-5, 8), (4, -7)]$$
 (7)

Simplest secluded model with SM-singlet massive chiral fermions from SSB: $U(1)_{D}$

$$\mathcal{L} = i\psi_i^{\dagger} \mathcal{D} \psi_i - \frac{1}{4} V_{\mu\nu} V^{\mu\nu} + \sum_{i < j} h_{ij} \psi_i \psi_j \phi^{(*)} + \text{h.c}$$
 (6)

 $96\,153 \rightarrow 5\,196$ multi-component DM (N=8,12) $\rightarrow 28$ with two Dirac-fermion DM

$$\mathbf{z} = [1, 2, 2, 4, -5, -5, -7, 8] \to \phi = 3 \to [(1, 2), (2, -5), (-5, 8), (4, -7)] \tag{7}$$

$$1 \qquad 2 \qquad 2 \qquad -5 \qquad -5 \qquad 8$$

$$1 \qquad \begin{bmatrix}
0 & h_{(1,2)} & h'_{(1,2)} & 0 & 0 & 0 \\
h_{(1,2)} & 0 & 0 & h_{(2,-5)} & h_{(2,-5)} & 0 \\
h'_{(1,2)} & 0 & 0 & 0 & 0 & 0 \\
0 & h_{(2,-5)} & 0 & 0 & 0 & h_{(-5,8)} \\
-5 & 0 & h_{(2,-5)} & 0 & 0 & 0 & h'_{(-5,8)} \\
0 & h_{(2,-5)} & 0 & 0 & 0 & h'_{(-5,8)}
\end{bmatrix}$$

$$\Psi \phi^{(*)} + h_{(4,-7)} \psi_4 \psi_{-7} \phi^*$$

$$(2)$$

8

Standard model extended with $U(1)_{\mathcal{X}=X \text{ or } \mathbf{D}}$ gauge symmetry

Fields	$SU(2)_L$	$U(1)_Y$	$U(1)_{\mathcal{X}=\mathbf{D} \text{ or } X}$
Q_i^{\dagger}	2	-1/6	Q
d_{Ri}	1	-1/2	d
u_{Ri}	1	+2/3	и
L_i^{\dagger}	2	+1/2	L
e_{Ri}	1	-1	e
Н	2	1/2	h
χ_{α}	1	0	Z_{α}

Ф 1	0	φ
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Table 1:

$$i = 1, 2, 3, \ \alpha = 1, 2, \dots, N'$$

Standard model extended with $U(1)_{\mathcal{X}=L \text{ or } \mathbf{B}}$ gauge symmetry

Fields	$SU(2)_L$	$U(1)_Y$	$U(1)_{\mathcal{X}=B}$ or L
Q_i^{\dagger}	2	-1/6	Q
d_{Ri}	1	-1/2	d
u_{Ri}	1	+2/3	и
L_i^{\dagger}	2	+1/2	L
e_{Ri}	1	-1	e
Н	2	1/2	h = 0
χ_{α}	1	0	z_{α}
$(L'_L)^{\dagger}$	2	1/2	-x'
$L_R^{\prime\prime}$	2	-1/2	x''
e_R'	1	-1	x'
$(e_L^{\prime\prime})^\dagger$	1	1	-x''
Ф	1	0	ϕ
S	1	0	S

Table 1: minimal set of new fermion content: L = e = 0 for $\mathcal{X} = B$. Or Q = u = d = 0 for $\mathcal{X} = L$. $i = 1, 2, 3, \alpha = 1, 2, ..., N'$

Anomaly cancellation: $\mathcal{X} = \mathbf{L}$ or \mathbf{B}

The anomaly-cancellation conditions on $[SU(3)_c]^2 U(1)_X$, $[SU(2)_L]^2 U(1)_X$, $[U(1)_Y]^2 U(1)_X$, allow us to express three of the X-charges in terms of the others

$$\mathbf{u} = -\mathbf{e} - \frac{2}{3}\mathbf{L} - \frac{1}{9}\left(x' - x''\right) , \quad \mathbf{d} = \mathbf{e} + \frac{4}{3}\mathbf{L} - \frac{1}{9}\left(x' - x''\right) , \quad \mathbf{Q} = -\frac{1}{3}\mathbf{L} + \frac{1}{9}\left(x' - x''\right) , \quad (9)$$

while the $[U(1)_X]^2 U(1)_Y$ anomaly condition reduces to

$$(e+L)(x'-x'')=0.$$
 (10)

- Previously: x' = x''
- We choose instead (h = 0):

$$e = -L, (11)$$

so that (L is still a free parameter)

$$Q = -u = -d = -\frac{1}{3}L + \frac{1}{9}(x' - x''). \tag{12}$$

If
$$B = 0 \rightarrow U(1)_L$$

Anomaly cancellation: $\mathcal{X} = L$

The gravitational anomaly, $[SO(1,3)]^2 U(1)_Y$, and the cubic anomaly, $[U(1)_X]^3$, can be written as the following system of Diophantine equations, respectively,

$$\sum_{\alpha=1}^{N} z_{\alpha} = 0, \qquad \sum_{\alpha=1}^{N} z_{\alpha}^{3} = 0, \qquad (13)$$

where

$$z_1 = -x',$$
 $z_2 = x'',$ $z_{2+i} = L, \quad i = 1, 2, 3$ (14)

 \rightarrow

$$9Q = -\sum_{\alpha=1}^{5} z_{\alpha} = -x' + x'' + L + L + L, \qquad (15)$$

$$L = 0 \rightarrow U(1)_B$$
 but $Q = 0 \rightarrow U(1)_L$

• B = 0 with L = 6

$$(6,6,6,-8,-10,5,13,-9,-9)$$

- B = 0 with L = 6
- Electroweak-scale vector-like fermions with $\Phi = 18$: $(L'_I)^{\dagger} L''_R \Phi \rightarrow x' = 8, \ x'' = -10$

$$(6, 6, 6, -8, -10, 5, 13, -9, -9)$$

- B = 0 with L = 6
- Electroweak-scale vector-like fermions with $\Phi=18$: $(L'_L)^\dagger L''_R \Phi \to x' = 8, \ x'' = -10$
- L + L + L x' + x'' = 0

$$(6,6,6,-8,-10,5,13,-9,-9)$$

- B = 0 with L = 6
- Electroweak-scale vector-like fermions with $\Phi = 18$: $(L'_I)^{\dagger} L''_R \Phi \rightarrow \chi' = 8, \ \chi'' = -10$
- L + L + L x' + x'' = 0
- Dirac-fermionic DM: $(\chi_L)^{\dagger} \chi_R' \Phi^* \rightarrow z_3 = 5, \ z_4 = 13$

$$(6, 6, 6, -8, -10, 5, 13, -9, -9)$$

- B = 0 with L = 6
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- Dirac-fermionic DM: $(\chi_L)^{\dagger} \chi_R' \Phi^* \rightarrow z_3 = 5, \ z_4 = 13$
- (Two generations) Majorana-fermionic DM: $(\chi_i'')^{\dagger} \chi_i'' \Phi \rightarrow z_5 = -9, z_6 = -9$

$$(6,6,6,-8,-10,5,13,-9,-9)$$

- B = 0 with L = 6
- Electroweak-scale vector-like fermions with $\Phi = 18$:

$$(L'_L)^{\dagger} L''_R \Phi \to x' = 8, \ x'' = -10$$

- L + L + L x' + x'' = 0
- Dirac-fermionic DM:

$$(\chi_L)^{\dagger} \chi_R' \Phi^* \to z_3 = 5, \ z_4 = 13$$

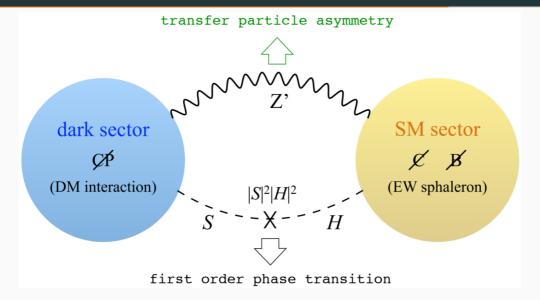
(6, 6, 6, -8, -10, 5, 13, -9, -9)

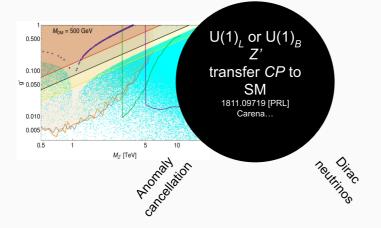
• (Two generations) Majorana-fermionic DM: $(\chi_i'')^{\dagger} \chi_i'' \Phi \rightarrow z_5 = -9, z_6 = -9$

Only 4 solutions from 96 153

- 1	k	solution	gcd	n	zmax	hidden
[-2, -3, 0]	[1, 2, 3, 2]	[5, 6, 6, 6, -8, -9, -9, -10, 13]	4	9	13	[{'S': 18, 'ψ': [(-9, -9), (-8, -10), (5, 13)]}]
[2, 0, 3]	[-2, 1, -3, -1]	[2, 3, 3, 3, 6, -8, -11, -15, 17]	12	9	17	$\hbox{\tt [\{'S': 9, '\psi': [(2, -11), (6, -15), (-8, 17)]\}]}$
[-4, -2, 1]	[2, -4, 4, -2]	[1, -2, 6, 6, 6, -9, -9, -16, 17]	16	9	17	$\hbox{[('S': 18, '\psi': [(-9, -9), (1, 17), (-2, -16)])]}$
[3, -2, -4]	[-2, -1, -2, 3]	[1, 2, 3, -6, -6, -6, 15, 16, -19]	2	9	19	[{'S': 18, '\psi': [(1, -19), (3, 15), (2, 16)]}]

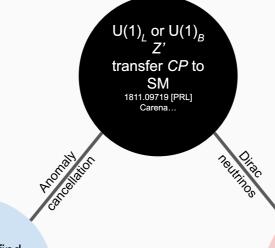
Dark sector baryogenesis





Anomalons:

DM



Method to find $\Sigma n=0$, $\Sigma n^3=0$ solutions 1905.13729 [PRL] Costa...

Anomalons:

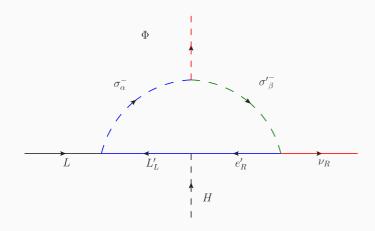
Multicomponent DM

Scotogenic neutrino masses

hep-ph/0601225 [PRL→PRD] Ma

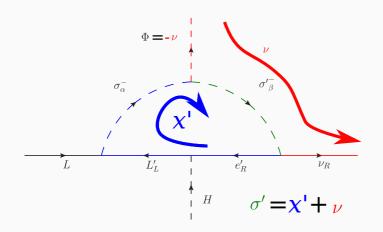
Gauge Baryon number scotogenic realization: arXiv:2205.05762 [PRD]

with Andrés Rivera (UdeA) and Walter Tangarife (Loyola U.)



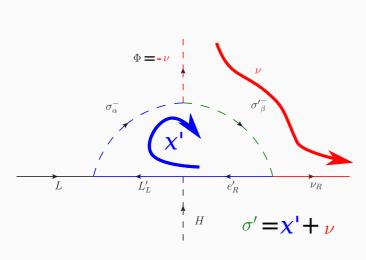
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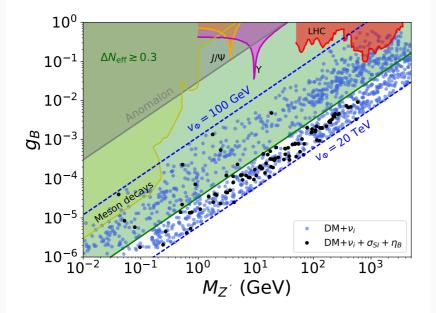


J.)			
Field	$SU(2)_L$	$U(1)_Y$	$U(1)_B$
u_{Ri}	1	2/3	u = 1/3
d_{Ri}	1	-1/3	d = 1/3
$(Q_i)^{\dagger}$	2	-1/6	Q = -1/3
$(L_i)^{\dagger}$	2	1/2	L=0
e _R	1	-1	e = 0
$(L'_L)^{\dagger}$	2	1/2	-x' = -3/5
e'_R	1	-1	x' = 3/5
$L_R^{\prime\prime}$	2	-1/2	x'' = 18/5
$\left(e_L^{\prime\prime} ight)^\dagger$	1	1	-x'' = -18/5
$ u_{R,1}$	1	0	-3
$\nu_{R,2}$	1	0	-3
χ_R	1	0	6/5
$(\chi_L)^{\dagger}$	1	0	9/5
Н	2	1/2	0
S	1	0	3
Ф	1	0	3
σ_{lpha}^-	1	1	3/5
σ'_{α}^{-}	1	-1	-12/5

arXiv:2205.05762 [PRD] https://github.com/anferivera/DarkBariogenesis

- $SARAH \rightarrow SPheno \rightarrow MicroMegas$
- η_B calculation code
- Python notebook with the scan

Black points: Dirac neutrinos with proper DM and baryon assymetry



Conclusions

A methodology to find all the *universal* Abelian extensions of the standard model is designed

All of the extensions can be reformulated as the solution of

$$\sum_{\alpha=1}^{N} z_{\alpha} = 0, \qquad \sum_{\alpha=1}^{N} z_{\alpha}^{3} = 0,$$

which we fully scan until N=12 and $|z_{\sf max}|=20$

Once the physical conditions are stablished, the full set of self-consistent models are found from a simple data-analysis procedure