### Effective Dirac neutrino masses and baryogenesis

with gauged Baryon number



### Diego Restrepo

Instituto de Física Universidad de Antioquia Phenomenology Group & UNICAMP http://gfif.udea.edu.co



Focus on arXiv: <a href="https://www.enails.com/lincollaboration">https://www.enails.com/lincollaboration</a> with Andrés Rivera (UdeA), Walter Tangarife (Loyola University Chicago)

## Electroweak baryogenesis

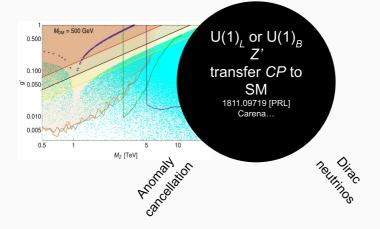
### **Problems**

- Standard model (SM)  $m_h \sim$  40 GeV.  $\bigcirc$
- Beyond the SM: Source of CP contains fields charged under SM
  - ightarrow too large electric dipole moments  $\stackrel{ ext{ iny electric}}{=}$

### Dark sectors

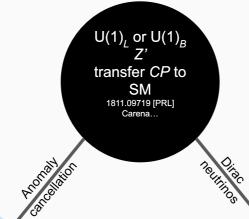
- Inert SM-singlet complex scalar field which acquires vev with temperature to have strong electroweak phase transition 😊
- CP violation (CPV) triggered in dark sectors through SM gauge singlets
  - → CPV Yukawa between SM-singlet complex scalar and SM-singlet quiral fermions \(\to\)





Anomalons:

DM



Method to find  $\Sigma n=0$ ,  $\Sigma n^3=0$  solutions 1905.13729 [PRL] Costa...

Anomalons:

Multicomponent DM

Scotogenic neutrino masses

hep-ph/0601225 [PRL→PRD] Ma

### **Dark sectors**











# $\mathcal{L} = -\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + i \sum_{i} \chi_{i}^{\dagger} \mathcal{D} \chi_{i}$

$$-h(\chi_1\chi_2\Phi + h.c)$$

Anomalons: SM-singlet Dirac fermion dark matter  $m_\Psi = h \langle \Phi \rangle$ 

LHC production

Gauged Symmetry:  $\mathcal{X} \to B$ :  $q\overline{q} \to Z' \to \text{jets}$ Gauged Symmetry:  $\mathcal{X} \to L$ :



$$\overline{\Psi}\Psi = \chi_1\chi_2 + \chi_1^{\dagger}\chi_2^{\dagger} \rightarrow \chi_{\alpha}\chi_{\beta}\Phi^{(*)}, \qquad \alpha = 1, \dots N' \rightarrow N' > 4$$



 $\mathcal{L} = -\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + i \sum_{i} \chi_{i}^{\dagger} \mathcal{D}_{\chi_{i}}$ 

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Gauged Symmetry: 
$$\chi \to L$$
:

multi-compone dark matter

$$\overline{\Psi}\Psi = \chi_1 \chi_2 + \chi_1^{\dagger} \chi_2^{\dagger} \to \chi_{\alpha} \chi_{\beta} \Phi^{(*)}, \qquad \alpha = 1, \dots N' \to \infty$$

 $\alpha = 1, \dots N' \rightarrow N' > 4$ 



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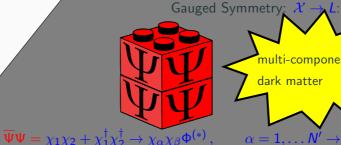
Local  $U(1)_{\mathcal{X}}$   $\mathcal{L} = -\frac{1}{4}V_{\mu\nu}V^{\mu\nu} + i\sum_{i}\chi_{i}^{\dagger}\mathcal{D}\chi_{i}$ 

$$-y\left(\chi_1\chi_2S+\text{h.c}\right)$$

Anomalons: SM-singlet Dirac fermion

CP violation Yukawa y

Gauged Symmetry:  $\mathcal{X} \to B$ :  $q\overline{q} \to Z' \to \text{jets}$ 



 $\alpha = 1, \dots N' \rightarrow N' > 4$ 

### Standard model extended with $U(1)_{\mathcal{X}=\mathbf{L} \text{ or } \mathbf{B}}$ gauge symmetry

Fields	$SU(2)_L$	$U(1)_Y$	$U(1)_{\mathcal{X}=\mathbf{B}}$ or $\mathbf{L}$
$Q_i^{\dagger}$	2	-1/6	Q
$d_{Ri}$	1	-1/2	d
$u_{Ri}$	1	+2/3	и
$L_i^{\dagger}$	2	+1/2	L
$e_{Ri}$	1	-1	e
Н	2	1/2	h = 0
$\chi_{\alpha}$	1	0	$z_{\alpha}$
$(L'_L)^{\dagger}$	2	1/2	-x'
$L_R^{\prime\prime}$	2	-1/2	x"
$e_R'$	1	-1	x'
$\left(e_L^{\prime\prime} ight)^\dagger$	1	1	-x''
Ф	1	0	$\phi$
S	1	0	S

**Table 1:** A minimal set of new fermion content: L = e = 0 for  $\mathcal{X} = B$ . Or Q = u = d = 0 for  $\mathcal{X} = L$ .

$$i = 1, 2, 3, \alpha = 1, 2, \dots, N'$$

### Effective Dirac neutrino mass operator

$$\chi_1 \to \nu_{R1}, \cdots, \chi_{N_{\nu}} \to \nu_{RN_{\nu}}, \qquad 2 \le N_{\nu} \le 3,$$
 (1)

$$\mathcal{L}_{\mathrm{eff}} = h_{
u}^{lpha i} \; (
u_{Rlpha})^{\dagger} \; \epsilon_{\mathsf{a} \mathsf{b}} \; \mathsf{L}_{i}^{\mathsf{a}} \; \mathsf{H}^{\mathsf{b}} \left( rac{\Phi^{*}}{\Lambda} 
ight)^{\delta} + \mathrm{H.c.}, \qquad \mathrm{with} \; i = 1, 2, 3 \,,$$

S is the complex singlet scalar responsible for the SSB of the anomaly-free gauge symmetry with D or X-charge

$$\phi = -(\nu + \mathbf{L})/\delta \,, \tag{2}$$

### Anomaly cancellation I

The anomaly-cancellation conditions on  $[SU(3)_c]^2 U(1)_X$ ,  $[SU(2)_L]^2 U(1)_X$ ,  $[U(1)_Y]^2 U(1)_X$ , allow us to express three of the X-charges in terms of the others

$$\mathbf{u} = -\mathbf{e} - \frac{2}{3}\mathbf{L} - \frac{1}{9}(x' - x''), \quad \mathbf{d} = \mathbf{e} + \frac{4}{3}\mathbf{L} - \frac{1}{9}(x' - x''), \quad \mathbf{Q} = -\frac{1}{3}\mathbf{L} + \frac{1}{9}(x' - x''), \quad (3)$$

while the  $[U(1)_X]^2 U(1)_Y$  anomaly condition reduces to

$$(e+L)(x'-x'')=0.$$
 (4)

- Previously: x' = x''
- We choose instead (h = 0):

$$e = -L, (5)$$

so that (*L* is still a free parameter)

$$Q = -u = -d = -\frac{1}{3}L + \frac{1}{9}(x' - x'').$$
 (6)

If 
$$L=0 \rightarrow U(1)_B$$

7

### **Anomaly cancellation II**

The gravitational anomaly,  $[SO(1,3)]^2 U(1)_Y$ , and the cubic anomaly,  $[U(1)_X]^3$ , can be written as the following system of Diophantine equations, respectively,

$$\sum_{\alpha=1}^{N} z_{\alpha} = 0, \qquad \sum_{\alpha=1}^{N} z_{\alpha}^{3} = 0, \qquad (7)$$

where N = N' + 5 and

$$z_{N'+1} = -x',$$
  $z_{N'+2+i} = L, \quad i = 1, 2, 3$  (8)

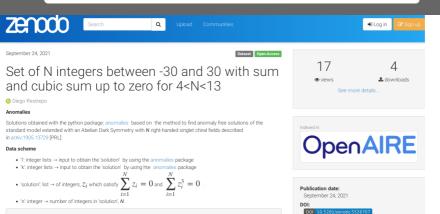
 $\rightarrow$ 

$$9Q = -\sum_{\alpha=N'+1}^{N'+5} z_{\alpha} = -x' + x'' + L + L + L, \qquad (9)$$

$$Q = 0 \rightarrow U(1)_L$$









#Example of JSON file usage in Python with pandas (see also ison module) >>> import pandas as pd >>> df=pd.read\_json('solutions.json') >>> df[:2]

solution acd n 0 [1, 2] [0, -3] [1, 5, -7, -8, 9] 1 5 1 [-2, -1] [0, -1] [2, 4, -7, -9, 10] 1 5

390074 solutions with  $5 \le N \le 12$  integers until '1321' [JSON]



Keyword(s):

License (for files):

Anomaly free | Diophantine equations | Abelian symmetry

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### $U(1)_{B}$ selection

• 
$$L = 0$$

$$(5,5,-3,-2,1,-6)$$

### $U(1)_{\mathbb{B}}$ selection

- L = 0
- Effective neutrino mass:  $\phi = -\nu = -5$

$$(5,5,-3,-2,1,-6)$$

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- L = 0
- Effective neutrino mass:  $\phi = -\nu = -5$
- Electroweak-scale vector-like fermions:

$$(L'_L)^{\dagger} L''_R \Phi^* \to x' = -1, \ x'' = 6$$

$$(5,5,-3,-2,\frac{1}{1},-\frac{6}{1})$$

### $U(1)_{\mathbb{B}}$ selection

- L = 0
- Effective neutrino mass:  $\phi = -\nu = -5$
- Electroweak-scale vector-like fermions:

$$(L'_L)^{\dagger} L''_R \Phi^* \to x' = -1, \ x'' = 6$$

• Dirac-fermionic DM:  $(\chi_L)^{\dagger} \chi_R'' \Phi^* \rightarrow z_3 = -3, \ z_4 = -2$ 

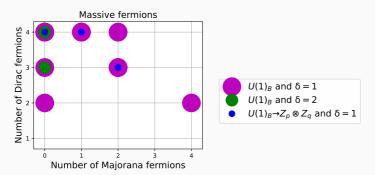
$$(5, 5, -3, -2, 1, -6)$$

### $U(1)_{\mathbf{B}}$ selection

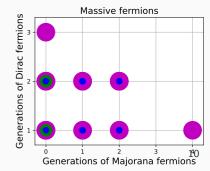
- L = 0
- Effective neutrino mass:  $\phi = -\nu = -5$
- Electroweak-scale vector-like fermions:

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- Dirac-fermionic DM:  $(\chi_L)^{\dagger} \chi_R'' \Phi^* \rightarrow z_3 = -3, \ z_4 = -2$
- 959 solutions from  $\sim$  400,000

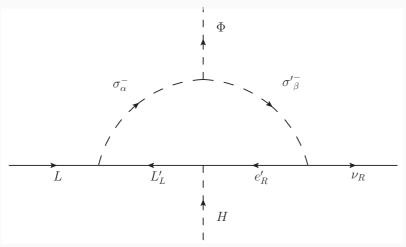


(5,5,-3,-2,1,-6)



### Scotogenic realization

Any realization which does not affect anomaly cancellation is allowed



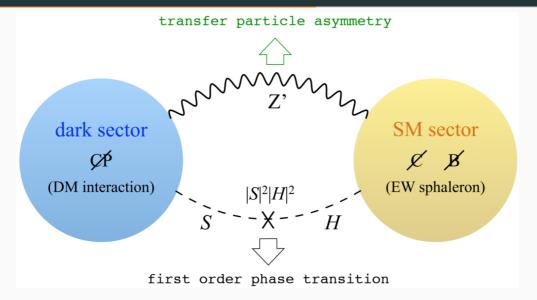
### Full $U(1)_{\mathbf{B}}$ model

Field	$SU(2)_L$	$U(1)_Y$	$U(1)_B$
$u_{Ri}$	1	2/3	u = -5/9
$d_{Ri}$	1	-1/3	d = -5/9
$(Q_i)^{\dagger}$	2	-1/6	Q = 5/9
$(L_i)^{\dagger}$	2	1/2	L=0
$e_R$	1	-1	e = 0
$(L'_L)^{\dagger}$	2	1/2	-x'=1
$e'_R$	1	-1	x' = -1
$L_R^{\prime\prime}$	2	-1/2	x'' = -6
$\left(e_L^{\prime\prime} ight)^\dagger$	1	1	-x'' = 6
$\nu_{R,1}$	1	0	5
$\nu_{R,2}$	1	0	5
XR	1	0	-2
$(\chi_L)^{\dagger}$	1	0	-3
Н	2	1/2	0
Φ	1	0	-5
S	1	0	-5
$\sigma_{\alpha}^{-}$	1	1	-1
$\sigma'_{\alpha}^{-}$	1	-1	4

**Table 2:** Fermion (top) and scalar (bottom) content and its quantum numbers,  $i = 1, 2, 3, \alpha = 1, 2$ .

### Baryogenesis

### Dark sector baryogenesis



### **Baryogenesis**

CP violation occurs in the dark sector and is transmitted to SM sector by the new Z' gauge boson.

- High scale fields:  $\Phi$ ,  $(\langle \Phi \rangle \to L'_L, L''_R, e'_L, e''_R$ : EW-scale vector-like anomalons)
- Electroweak scale (EW) fields:  $Z'_{\mu}, S, \chi_L, \chi_R$
- CP-violation

$$\mathcal{L}_{\mathsf{Dirac}\;\mathsf{DM}} = h(\chi_L)^{\dagger} \chi_R \Phi^* + y(\chi_L)^{\dagger} \chi_R S^* + \mathsf{h.c}\,, \qquad y \in \mathbb{C}$$
$$\supset \left( m_{\chi} + |y| \, \mathrm{e}^{i\theta} \, |S| \right) (\chi_L)^{\dagger} \chi_R + \mathsf{h.c}\,.$$

• CP-violation Portal

$$\mathcal{L}_{\text{anomalous}} \supset g' Z'_{\mu} \left[ 3\bar{\chi}_L \gamma^{\mu} \chi_L - 2\bar{\chi}_R \gamma^{\mu} \chi_R + \bar{Q}_i \gamma^{\mu} Q_i + \bar{q}_{Ri} \gamma^{\mu} q_{Ri} \right]$$

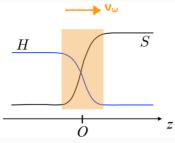
• Strong electroweak phase transition (EWPT) portal

$${\cal L}_{\sf first\ order\ EWPT} \supset -\lambda_{SH} H^\dagger H\, S^* S$$
 .

$$h = H/\sqrt{2}$$
,  $s = |S|$  with vevs:  $v(T)$  and  $w(T)$  such that  $v(T_c) = w(T_c)$ 

$$V_T(h,s) = \frac{\lambda_H v_c^4}{4} \left( \frac{h^2}{v_c^2} + \frac{s^2}{w_c^2} - 1 \right)^2 + \frac{\lambda_H v_c^2}{m_{s,c}^2 w_{0,c}^4} h^2 s^2 + (T^2 - T_c^2) (c_h h^2 + c_s s^2), \quad (10)$$

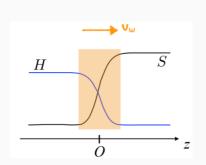
$$c_h = \frac{1}{48} \left( 9g_2^2 + 3g_1^2 + 12y_t^2 + 24\lambda_H + \lambda_{HS} \right), \quad c_s = \frac{1}{12} \left( 3\lambda_S + 2\lambda_{HS} \right).$$
 (11)

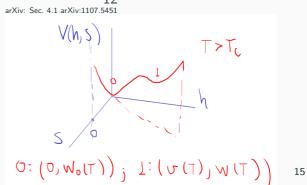


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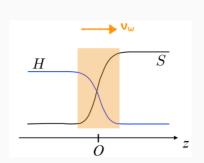


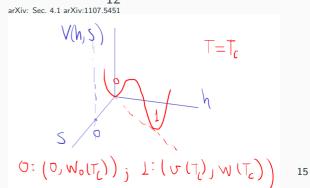


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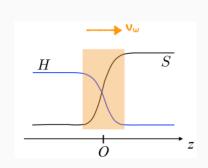


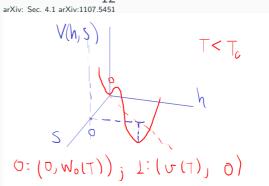


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### CP assymetry generation i

Using the thin wall approximantion for the nucleation bubbles, we use the ansatz in which the space dependence of the fields is given by

$$h(z) = \frac{1}{2}v(T_n)(1-\tanh(z/L_w)), \qquad s(z) = \frac{1}{2}s_0(1+\tanh(z/L_w)),$$

where z is the direction normal to the wall and  $L_w$  is the wall width.

### CP assymetry generation ii

The nucleation temperature,  $T_n$ , is defined by the condition

$$\exp(-S_3/T_n) = \frac{3}{4\pi} \left(\frac{H(T_n)}{T_n}\right)^4 \left(\frac{2\pi T_n}{S_3}\right)^{\frac{3}{2}},$$

where  $S_3$  is the Euclidean action of the bubble and H(T) is the Hubble rate.

The *CP* violating phase,  $\theta$ , from

$$M_{\chi}(z) = m_{\chi}(z) + |y| e^{i\theta} |S(z)|, \qquad (12)$$

### Boltzmann equation i

$$\xi_i(z) \equiv \mu_i(z)/T = 6\left(n_i - \overline{n}_i\right)/T^3,$$
 
$$-D_L \xi_{\chi_L}'' - v_w \xi_{\chi_L}' + \Gamma_L(\xi_{\chi_L} - \xi_{\chi_R}) = S_{\mathcal{QP}},$$

where  $D_L$  is the diffusion constant for  $\chi_L$ , which is related to the scattering rate  $\Gamma_L$  by  $D_L = \langle v_{p_z}^2 \rangle / 3\Gamma_L$ . Here,  $\langle \, \rangle$  means thermal average.  $S_{CP}$  is CP-violating source that results from the variation of  $\theta$ 

$$S_{\mathcal{CP}} = -\frac{\lambda}{2} \frac{v_w D_h}{\langle v_{p_z}^2 \rangle T} \left\langle \frac{|p_z|}{\omega^2} \right\rangle \left( M_{\chi}^2 \theta' \right)'' , \qquad (13)$$

where  $v_w$  is the wall's velocity and

$$\langle v_{p_z}^2 \rangle = \frac{3x+2}{x^2+3x+2} \,, \quad \left\langle \frac{|p_z|}{\omega^2} \right\rangle = \frac{(1-x)e^{-x}+x^2E_1(x)}{4m_\chi^2K_2(x)} \,, \quad x \equiv m_\chi/T \,,$$

$$\left(M_\chi^2\theta'\right)'' = \frac{m_\chi s_0 \lambda \left(-2+\cosh\left(\frac{2z}{L_w}\right)\right)\sin\theta}{L_w^3\cosh^4\left(\frac{z}{L_w}\right)} \,.$$

 $E_1(x)$  is the error function and  $K_2(x)$  is the modified Bessel function of the second kind.

### Transfer DM assymetry to SM quarks

The chiral particle give rise to a non-zero  $U(1)_B$  charge density in the proximity of the wall. This results in a Z' background that couples to the SM fields with  $U(1)_B$  charge,

$$\langle Z_0' 
angle \, = \, rac{g_B \, (q_{\chi_L} - q_{\chi_R}) \, T_n^3}{6 M_{Z'}} \int_{-\infty}^{\infty} {\sf d} \, z_1 \, \xi_{\chi_L}(z') \, {\sf e}^{-M_{Z'}|z-z'|} \, ,$$

which generates a chemical potential for the SM quarks,

$$\mu_Q(z) = \mu_{d_R,u_R}(z) = 3 \times \frac{5}{9} \times g_B \langle Z_0'(z) \rangle.$$

This chemical potential sources a thermal-equilibrium asymmetry in the quarks [?],  $\Delta n_Q^{\rm EQ}(z) \sim T_n^2 \mu_Q(z)$ .

From [1]

If the Z' is sufficiently light, it mediates a long range force that extends into the region outside the bubble wall with unbroken electroweak symmetry.

### Finally, the baryon-number asymmetry is then given by

$$n_B \,=\, rac{\Gamma_{
m sph}}{v_w} \int_0^\infty {
m d}\,z\, n_Q^{
m EQ}(z) \, \exp\left(-rac{\Gamma_{
m sph}}{v_w}\,z
ight) \,,$$

where  $\Gamma_{\mathrm{sph}}$  is the sphaleron rate. The baryon-to-photon-number ratio is then obtained by

$$\eta_B = \frac{n_B}{s(T_n)}, \quad s(T) \equiv \frac{2\pi^2}{45} g_{*S}(T) T^3,$$

where  $g_{*S}(T)$  is the effective number of relativistic degrees of freedom.

### https://github.com/anferivera/DarkBariogenesis

- SARAH $\rightarrow$ SPheno $\rightarrow$ MicroMegas
- $\eta_B$  calculation code
- Python notebook with the scan

### arXiv:1810.08055

Ten Simple Rules for Reproducible Research in Jupyter Notebook Fernando Pérez, et al

[...] In this paper, we address several questions about reproducibility [...] Combined with software repositories and open source licensing, notebooks are powerful tools for transparent, collaborative, reproducible, and reusable data analyses.

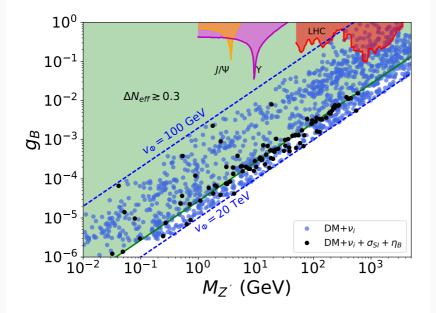
### Results

We vary the typical Dirac-fermion DM parameter space and for each point that satisfy neutrino oscillation data, relic density and DM direct detection constraints. For each point we ...

Parameter	Range	
$\theta$	$(-\pi/2,\pi/2)$	
$s_0/{ m GeV}$	100 - 500	
$T_n/{ m GeV}$	100 - 200	
$L_w/{ m GeV^{-1}}$	$1/T_n - 10/T_n$	
$V_W$	0.05 - 0.5	

**Table 3:** Scan ranges for the free parameters that are involved in the baryogenesis mechanism.

### Black points: Dirac neutrinos with proper DM and baryon assymetry



### **Conclusions**

A  $U(1)_B$  is presented as an example of models where all new fermions required to cancel out the anomalies are used to solve phenomenological problems of the standard model (SM):

- EW-scale fermion vector-like doublets and iso-singlet charged singlets, in conjunction
  with right-handed neutrinos with repeated Abelian charges, participate in the generation
  of small neutrino masses through the Dirac-dark Zee mechanism
- The other SM-singlets are used to explain the dark matter in the universe, while their coupling to an inert singlet scalar is the source of the CP violation.

In the presence of a strong first-order electroweak phase transition, this "dark" CP violation allows for successful electroweak baryogenesis by using long range force mediated by a sufficiently light Z' which transfers the assymmetry from the Dark sector into the SM.