## Motivating Demeaning Approach

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11/2/2020

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This document analytically motivates demeaning of variables in the Yelp dataset that I use for my *Price Placebo Effect* project. The project investigates if consumers' experience with a more expensive restaurant is better even if the restaurant is similar to its competitors in other dimensions. To address the inherent endogeneity in the problem, I use Tax as an instrumental variable (IV). I also demean the variables by their *local means*<sup>1</sup> to eliminate the bias introduces by location. I assume the Directed Acyclic Graph (DAG) in Figure 1 captures the causal relationship.

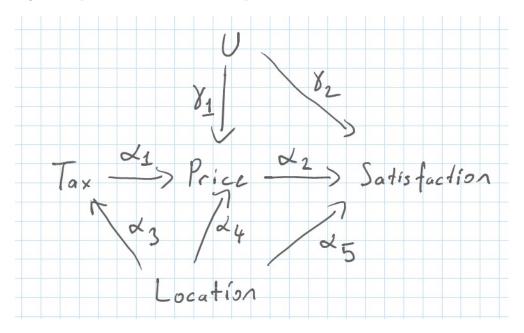


Figure 1: Causal Relationship of Variables

This graph implies the following structural equation model

 $<sup>^1{\</sup>rm Local}$  in geographical proximity.

$$\begin{aligned} &\operatorname{Tax} \ = f(\operatorname{Location}) \\ &U = m(\operatorname{Location}) + \varepsilon_1 \\ &\operatorname{Price} \ = g(\operatorname{Location}) + \alpha_1 \operatorname{Tax} \ + \gamma_1 U + \varepsilon_2 \\ &= g(\operatorname{Location}) + \alpha_1 f(\operatorname{Location}) + \gamma_1 m(\operatorname{Location}) + \gamma_1 \varepsilon_1 + \varepsilon_2 \\ &\operatorname{Satistaction} \ = \alpha_2 \operatorname{price} \ + h(\operatorname{Location}) + \gamma_2 U + \varepsilon_3 \\ &= \alpha_2 g(\operatorname{Location}) + \alpha_2 \alpha_1 f(\operatorname{Location}) + \alpha_2 \gamma_1 m(\operatorname{Location}) + \alpha_2 \gamma_1 \varepsilon_1 + \alpha_2 \varepsilon_2 \\ &\quad + h(\operatorname{Location}) + \gamma_2 m(\operatorname{Location}) + \gamma_2 \varepsilon_1 + \varepsilon_3 \end{aligned}$$

Let

$$\overline{\text{Satistaction}_{i}} = E[\text{Satistaction}|\text{Location} \in \ell_{i}(\epsilon)]$$

$$= (\alpha_{2}\alpha_{1}\alpha_{3} + \alpha_{2}\alpha_{4} + \alpha_{5}) E[\text{Location}|\text{Location} \in \ell_{i}(\epsilon)] + (\alpha_{2}\gamma_{1} + \gamma_{2}) E[U|\text{Location} \in \ell_{i}(\epsilon)]$$

$$\overline{\text{Satistaction}_{i}} = \overline{\text{Satistaction}_{i}} - \overline{\text{Satistaction}_{i}}$$

$$\approx \alpha_{2}\alpha_{1}\varepsilon_{1} + (\alpha_{2}\gamma_{1} + \gamma_{2}) \tilde{U} + \alpha_{2}\varepsilon_{2} + \varepsilon_{3}$$

where  $\ell_i$  is the  $\epsilon$ -ball around the actual location of the observation. Therefore, the approximation gets better for smaller  $\epsilon$ .

Similarly,

$$\widetilde{\operatorname{Tax}}_{i} = \operatorname{Tax}_{i} - \overline{\operatorname{Tax}_{i}}$$

$$\approx \varepsilon_{1}$$

$$\widetilde{\operatorname{Price}}_{i} = \operatorname{Price}_{i} - \overline{\operatorname{Price}_{i}}$$

$$\approx \alpha_{1}\varepsilon_{1} + \gamma_{1}\tilde{U} + \varepsilon_{2}$$

Therefore, we can approximate the DAG in Figure 1 with the one in Figure 2.

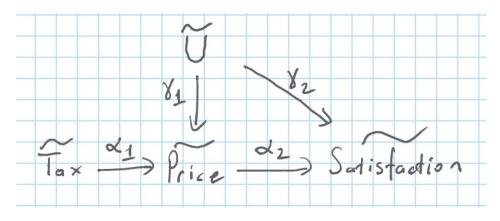


Figure 2: Alternative Causal Relationship

This analysis implies we can employ two approaches. First, we can use the DAG in Figure 2 and estimate a weighted local average for each variable to demean it. Then, we can estimate the effect with 2SLS.

Alternatively, we can directly estimate a 2SLS where we use cluster fixed-effects as an approximation to Location to control it. The DAG in Figure 1 shows that Location is the sufficient set to identify the effects of Tax on both Price and Satisfaction.