

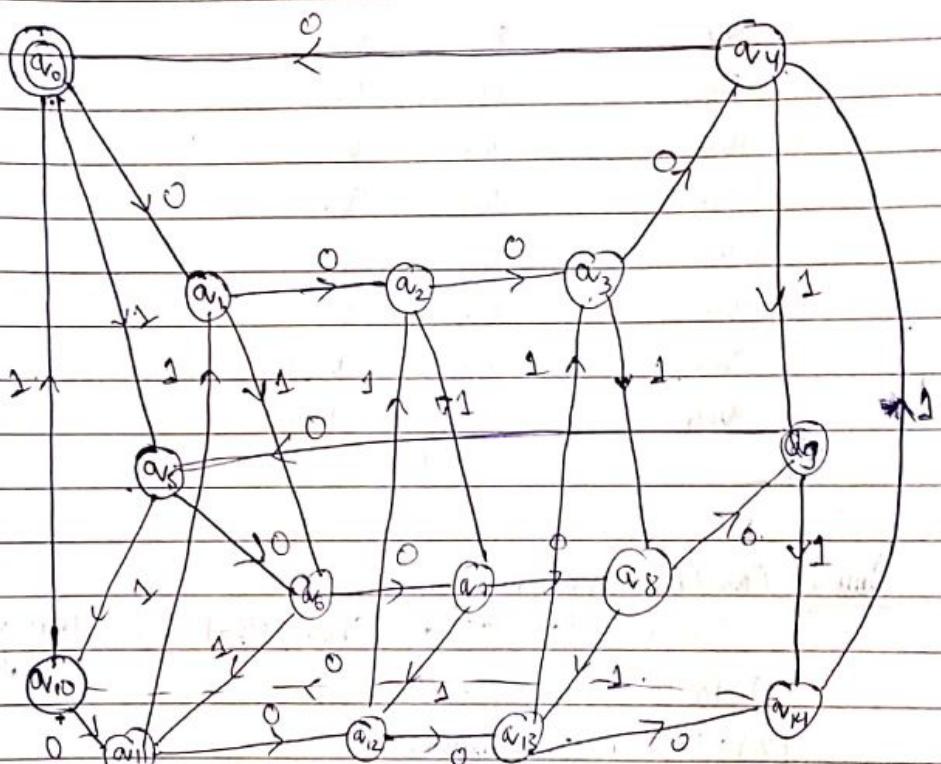
Theory of Computation

DFA-1

Ques: Design a DFA that accepts the following languages over alphabet {0,1}

{The set of strings such that the number of 0's is divisible by 5, and the number of 1's is divisible by 3.}

Ans:1.



The above DFA = $\langle Q, \Sigma, S, q_0, F \rangle$ represents no. of 0's divisible by 5 and no. of 1's divisible by 3.

State	Input	
0	1	
$\rightarrow q_0$	a_1	a_5
q_1	a_2	a_6
q_2	a_3	a_7
q_3	a_4	a_8
q_4	a_0	a_9
q_5	a_6	a_{10}
q_6	a_7	a_{11}
q_7	a_8	a_{12}
q_8	a_9	a_{13}
q_9	a_{15}	a_{14}
q_{10}	a_{11}	a_0
q_{11}	a_{12}	a_1
q_{12}	a_{13}	a_2
q_{13}	a_{14}	a_3
q_{14}	a_{10}	a_4

Ques-2 Consider the Grammar G_1 :

$S \rightarrow S+S/S*S/(S)/a$. Show that the string $a+a*a$ has to

(1) Parse trees

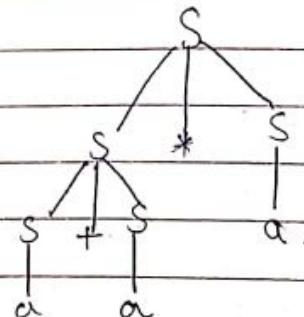
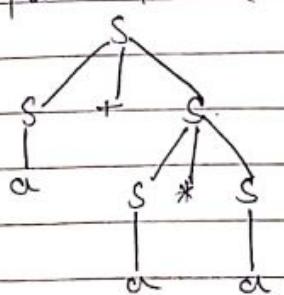
(2) Left most derivations

(3) Find the unambiguous grammar G'_1 equivalent to G_1 and show that $L(G_1) = L(G'_1)$. And G'_1 is unambiguous

Ans-2 Given the grammar $S \rightarrow S+S/S*S/(S)/a$

given string $w = a+a*a$, $\epsilon L(G_1) \rightarrow \text{①}$

(i) parse tree (using CM1).



(ii) left most derivations.

$$\begin{aligned} S &\rightarrow S+S \\ &\rightarrow a+S \\ &\rightarrow a+a*S \\ &\rightarrow a+a*a \\ &\rightarrow a+a*a. \end{aligned}$$

$$\begin{aligned} S &\rightarrow S*S \\ &\rightarrow S+S*S \\ &\rightarrow a+S*S \\ &\rightarrow a+a*S \\ &\rightarrow a+a*a. \end{aligned}$$

(iii)

$$\begin{aligned} S &\rightarrow S+T \\ T &\rightarrow T+F \\ F &\rightarrow (S)/a \end{aligned} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} G' \quad \quad \quad$$

Checking for string.

$$w = a+a*a \quad \text{in } L(G') \quad \rightarrow (2)$$

LMD

$$\begin{aligned} S &\rightarrow S+T \\ &\rightarrow T+T \\ &\rightarrow F+T \\ &\rightarrow a+T \\ &\rightarrow a+T^*F \\ &\rightarrow a+F^*F \\ &\rightarrow a+a^*f \\ &\rightarrow a+a*a \end{aligned}$$

RMD

$$\begin{aligned} S &\rightarrow S+\emptyset T \\ &\rightarrow S+S^*F \\ &\rightarrow S+T^*a \\ &\rightarrow S+F^*a \\ &\rightarrow S+a*a \\ &\rightarrow F+a*a \\ &\rightarrow F+a*a \\ &\rightarrow a+a*a \end{aligned}$$

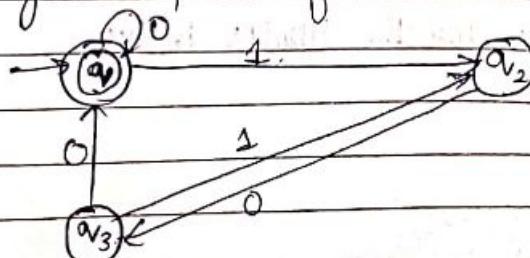
As only 1 LMD and 1 RMD exist.

$\therefore G'$ is unambiguous grammar

using (1) and (2), $L(G) \subseteq L(G')$

Ques 3

Consider the transition system of given fig. Derive the regular expression for the FA



Ans 3

Using Arden's Theorem:
find the eqns.

$$q_1 = q_{1,0} + q_{2,0} + e \quad \text{--- (1)}$$

$$q_2 = q_{1,1} + q_{2,1} + q_{3,1} \quad \text{--- (2)}$$

$$q_3 = q_{2,0} \quad \text{--- (3)}$$

Put (3) in (2)

$$q_2 = q_{1,1} + q_{2,1} + (q_{2,0})1$$

$$q_2 = q_{1,1} + q_{2,1}(1+01) \quad \text{--- (4)}$$

It is in the form $R = Q + RP$

\therefore soln is $R = QP^*$ (using Arden's)

$$q_2 = q_{1,1}(1+01)^* \quad \text{--- (5)}$$

put (3) in (1)

$$q_1 = q_{1,0} + q_{2,0}0 + e$$

put (5) in above eqn.

$$q_1 = q_{1,0} + (q_{1,1}(1+01)^*)00 + e$$

$$q_1 = e + q_{1,1}(0 + (1+01)^*00)$$

It is in the form $R = Q + RP$

\therefore soln is $R = QP^*$ (using Arden's)

$$q_1 = e(0 + (1+01)^*00)^*$$

$$\boxed{q_1 = (0 + (1+01)^*00)^*}$$

↑ this gives the RE for given FA.

Ques 4

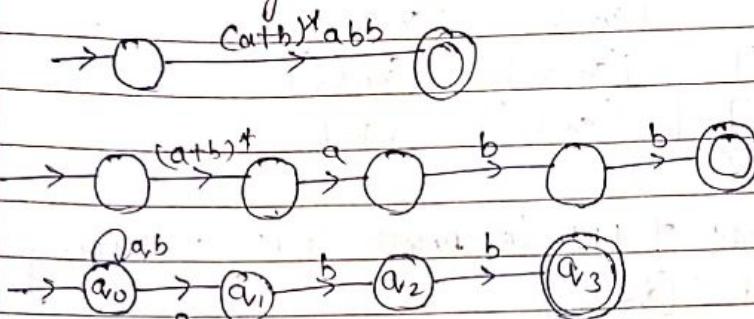
Consider the regular expression given below

$$a = (a+b)^*ab$$

- (i) Find the NFA without ϵ -moves for it
- (ii) Convert the resulted NFA in (i) into DFA.
- (iii) Find minimized DFA, for the results in (ii).

Ques: Given RE: $s = (a+b)^*abb$

(ii) constructing NFA without ϵ -moves.



(iii) Converting this NFA to DFA.

Transition table for NFA:

State	a	b
q_0	$\{q_0, q_1\}$	$\{q_0\}$
q_1	-	$\{q_2\}$
q_2	-	$\{q_3\}$
q_3	-	-

Let the DFA is $N' = \langle Q', \Sigma, S', q_0, F' \rangle$.

$$S'([q_0], a) = [q_0, q_1] - \text{new}$$

$$S'([q_0], b) = [q_0] - \text{old}$$

$$S'([q_0, q_1], a) = [q_0, q_1] \cup \emptyset = [q_0, q_1] \rightarrow \text{old}.$$

$$S'([q_0, q_1], b) = [q_0, q_2] - \text{new}$$

$$S'([q_0, q_2], a) = [q_0, q_1] - \text{old}.$$

$$S'([q_0, q_2], b) = [q_0, q_3] - \text{new}$$

$$S'([q_0, q_3], a) = [q_0, q_1] - \text{old}.$$

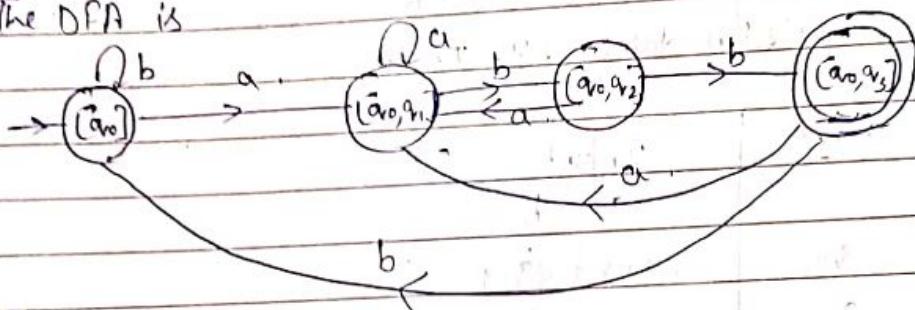
$$S'([q_0, q_3], b) = [q_0] - \text{old}.$$

Transition table for DFA:

States	a	b
$\rightarrow [q_0]$	$[q_0, q_1]$	$[q_0]$
$[q_0, q_1]$	$[q_0, q_1]$	$[q_0, q_2]$
$[q_0, q_2]$	$[q_0, q_1]$	$[q_0, q_3]$
$[q_0, q_3]$	$[q_0, q_1]$	$[q_0]$

final state of DFA is final state containing state q_3
 $f' \Rightarrow [q_0, q_3]$

The DFA is



(ii) Now, minimizing the above DFA

let $[q_0] = A$, $[q_0, q_1] = B$, $[q_0, q_2] = C$, $[q_0, q_3] = D$.

State	a	b
$\rightarrow A$	B	A
B	B	C
C	B	D
D	B	A

$$S_0 = \{ \underset{I}{\{A, B\}}, \underset{II}{\{C\}}, \underset{III}{\{D\}} \} \quad (\text{based on final and non-final states})$$

I on a.

$$\begin{cases} A \xrightarrow{a} B \\ B \xrightarrow{a} B \\ C \xrightarrow{a} B \end{cases}$$

no partition

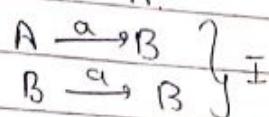
II on B

$$\begin{cases} A \xrightarrow{b} A \\ B \xrightarrow{b} C \\ C \xrightarrow{b} D \end{cases}$$

partition

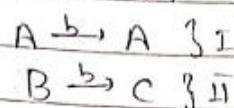
$$S_1 = \{ \underbrace{\{A, B\}}_{I}, \underbrace{\{C\}}_{II}, \underbrace{\{D\}}_{III} \}$$

I on A:



NO partition.

I on B:



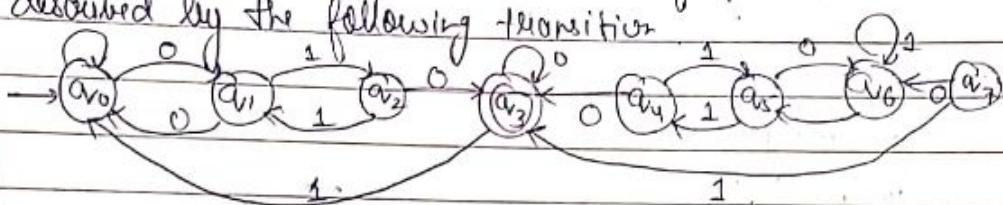
partition.

$$S_2 = \{ \{A\}, \{B\}, \{C\}, \{D\} \}$$

Since no states can be combined.

Therefore DFA obtained in (ii) is minimized DFA.

Ques 5: Find the minimum-state DFA equivalent to the DFA described by the following transition diagram.



Ans 5: Transition table for given DFA.

State	0	1
$\rightarrow q_0$	q_1	q_0
q_1	q_0	q_2
q_2	q_3	q_1
q_3	q_3	q_0
q_4	q_3	q_5
q_5	q_5	q_4
q_6	q_5	q_6
q_7	q_6	q_3

grouping on basis of non final and final states.

$$S_0 = \{ \underbrace{\{q_0, q_1, q_2, q_4, q_5, q_6, q_7\}}_I, \underbrace{\{q_3\}}_{II} \}$$

Transition on group I for all input symbols.

On 0

$$q_0 \xrightarrow{0} q_1$$

$$q_1 \xrightarrow{0} q_0$$

$$q_2 \xrightarrow{0} q_3$$

$$q_4 \xrightarrow{0} q_3$$

$$q_5 \xrightarrow{0} q_6$$

$$q_6 \xrightarrow{0} q_5$$

$$q_7 \xrightarrow{0} q_6$$

On 1

$$q_0 \xrightarrow{1} q_0$$

$$q_1 \xrightarrow{1} q_2$$

$$q_2 \xrightarrow{1} q_1$$

$$q_4 \xrightarrow{1} q_5$$

$$q_5 \xrightarrow{1} q_4$$

$$q_6 \xrightarrow{1} q_7$$

$$q_7 \xrightarrow{1} q_5$$

partition

partition

$$S_1 = \left\{ \begin{array}{l} \{q_0, q_1, q_5, q_6\}, \\ \{q_2, q_4\}, \{q_7\}, \{q_3\} \end{array} \right. \quad \text{I} \quad \text{II} \quad \text{III} \quad \text{IV}$$

Considering group I

On 0

$$q_0 \xrightarrow{0} q_1$$

$$q_1 \xrightarrow{0} q_0$$

$$q_5 \xrightarrow{0} q_6$$

$$q_6 \xrightarrow{0} q_5$$

no partition

On 1

$$q_0 \xrightarrow{1} q_0$$

$$q_1 \xrightarrow{1} q_2$$

$$q_5 \xrightarrow{1} q_4$$

$$q_6 \xrightarrow{1} q_7$$

partition

Consider group II

On 0

$$q_2 \xrightarrow{0} q_3$$

$$q_4 \xrightarrow{0} q_3$$

no partition

On 1

$$q_2 \xrightarrow{1} q_1$$

$$q_4 \xrightarrow{1} q_5$$

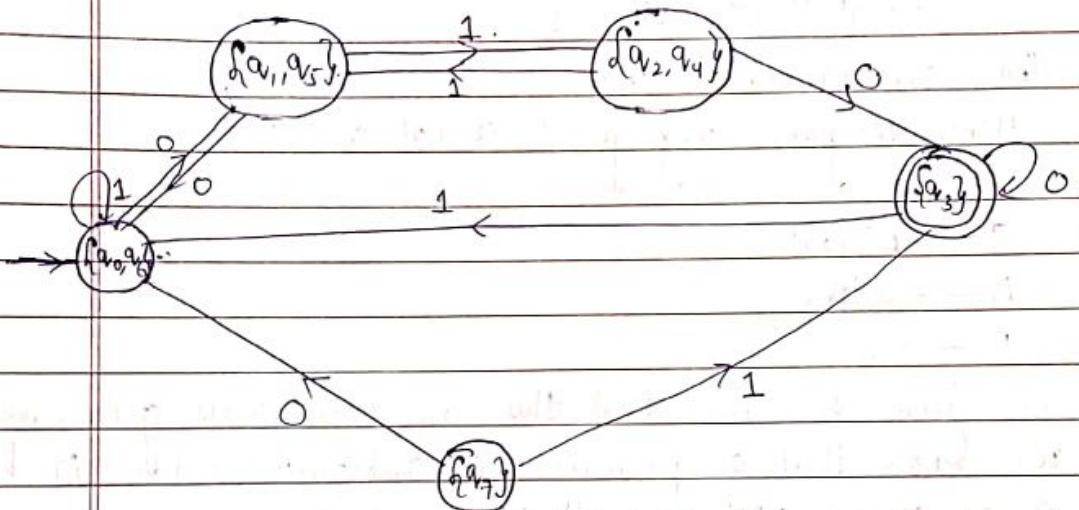
no partition

$$S_2 = \left\{ \begin{array}{l} \{q_0, q_6\}, \{q_1, q_5\}, \{q_2, q_4\}, \{q_7\}, \{q_3\} \end{array} \right.$$

No further separation possible.

$\Rightarrow S_2$ denotes states of minimized DFA.

States	0	1
$\{q_0, q_6\}$	$\{q_1, q_5\}$	$\{q_0, q_6\}$
$\{q_1, q_5\}$	$\{q_0, q_6\}$	$\{q_2, q_4\}$
$\{q_2, q_4\}$	$\{q_3\}$	$\{q_1, q_5\}$
$\{q_3\}$	$\{q_3\}$	$\{q_0, q_6\}$
$\{q_4\}$	$\{q_0, q_6\}$	$\{q_3\}$



This is minimized DFA.

- Ques-6 (i) Show that the language $L = \{ww \mid w \in \{a,b\}^*\}$ is not a context-free language by using the same
- (ii) Show that the following grammar is ambiguous.

$$S \rightarrow AB \mid aaB, A \rightarrow a \mid Aa, B \rightarrow b$$

- (iii) Construct a PDA to accept the language $L = \{0^{3n}12 \mid n \geq 0\}$ and $\Sigma = \{0,1,2\}$ by final state.

Ans-6 (i) $L = \{ww \mid w \in \{a,b\}^*\}$

we have to prove that L is not CFL.

Proof: Let L is a CFL

let L is an infinite language

if $w = a^m b^m, m > 0$

for the string $= a^m b^m a^m b^m \in L$

Case(i) Vny located in $a^m \cdot m \cdot m \cdot m$.
 $\overbrace{aa}^m \cdot \underbrace{ad}_{m-1} \cdot \overbrace{bb}^m \cdot \underbrace{ba}_{m-1} \cdots \overbrace{aa}^m \cdot \underbrace{bb}_{m-1} \cdots \overbrace{bb}^m$

Let $v = a^k$; $y = a^{k_2}$ so that $|v| \geq 1$, $|Vny| \leq m$ then
 $uv^i ny^j \in L \forall i = 0, 1, 2, 3$.

let $i=2$

$$uv^2 ny^2 \notin L$$

$$a^{m-k_1} \underbrace{a^{k_1}}_{\in L} a^{m-k_1} a^{2k_2} b^m a^m b^m \\ \rightarrow a^{m+k_2} b^m a^m b^m \notin L$$

Thus contradiction occurs.

Ques: 7

Hence the given language L is not a CFL

$$\begin{aligned} (ii) \quad S &\rightarrow AB \mid aaB \\ A &\rightarrow a \mid Aa \\ B &\rightarrow b \end{aligned}$$

We have to show that this is ambiguous grammar.

We know that a grammar is ambiguous when it has 2 or more (M) for atleast one string.

Let string be 'aab'.

Using LMD

$$\begin{array}{l} S \rightarrow AB \\ \quad \downarrow \\ \quad \rightarrow AaB \\ \quad \downarrow \\ \quad \rightarrow aAb \\ \quad \downarrow \\ \quad \rightarrow aab. \end{array}$$

$$\begin{array}{l} S \rightarrow aaB \\ \quad \downarrow \\ \quad \rightarrow aab \end{array}$$

Since 2 LMDs engg. for 'aab'

Hence given grammar is ambiguous.

$$(iii) \quad L = \{0^{3n} 1 2 \mid n \geq 0\}$$

We have to draw PDA to accept L by final state.

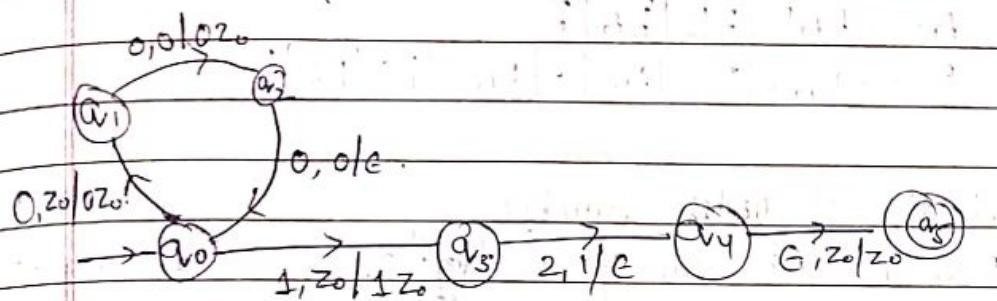
Logic: Push first 0 in stack

Perform no operation for second 0.

Pop the 0 present in stack when third 0 is read.

Push 1 in stack.

Pop 0 or 1 when 2 is read.



Ques: (i) Simplify the CFG_i and convert into CNF.

$$S \rightarrow abAB, A \rightarrow bAB/\epsilon, B \rightarrow BAa/A/\epsilon.$$

(ii) Find the Content free grammar for the following language

$$L = \{a^n b^m \mid n \leq m+3, n, m \geq 0\}$$

Ans: (i) $S \rightarrow abAB$

$$A \rightarrow bAB/\epsilon$$

$$B \rightarrow BAa/A/\epsilon$$

This is given CFG_i, we want to convert it to CNF.

(ii) Elimination of ϵ production.

$$A \rightarrow \epsilon$$

$$S \rightarrow abAB \mid abB$$

$$A \rightarrow bAB \mid bB$$

$$B \rightarrow BAa \mid A \mid Ba \mid \epsilon$$

$$B \rightarrow \epsilon$$

$$S \rightarrow abAB \mid abB \mid abA \mid ab$$

$$A \rightarrow bAB \mid bB \mid BA \mid b$$

$$B \rightarrow BAa \mid A \mid Ba \mid Aa \mid a$$

Checking with $A \rightarrow \epsilon, B \rightarrow \epsilon$.

$$S \rightarrow abAB \mid abB \mid abA \mid ab$$

$$A \rightarrow bAB \mid bB \mid BA \mid b$$

$$B \rightarrow BAa \mid A \mid Ba \mid Aa \mid a$$

(iii) Elimination of unit production

$$S \rightarrow abAB \quad abB \quad abA \quad ab \\ A \rightarrow bAB \quad bB \quad bA \quad b \\ B \rightarrow BAa \quad BA \quad Ba \quad bAB \quad bB \quad bA \quad b.$$

(iv) Elimination of useless symbol

Both A and B are generated as well as reachable
⇒ no useless symbol

(v) Converting terminal to non-terminal

$$x_a \rightarrow a$$

$$x_b \rightarrow b$$

$$S \rightarrow x_a x_b AB \quad x_a x_b B \quad x_a x_b A \quad x_a x_b \\ A \rightarrow x_b AB \quad x_b B \quad x_b A \quad b \\ B \rightarrow BAx_a \quad BX_a \quad AX_a \quad x_a AB \quad x_b B \quad x_b A \quad a \quad b.$$

(vi) Restriction on RHS to ANP¹s

$$S \rightarrow x_a P \quad x_a Q \quad x_a R \quad x_a x_b$$

$$A \rightarrow x_b U \quad x_b B \quad x_b R \quad b$$

$$B \rightarrow BT \quad BX_a \quad AX_a \quad x_b U \quad x_b B \quad x_b R \quad a \quad b$$

$$P \rightarrow x_b V$$

$$Q \rightarrow x_b B$$

$$R \rightarrow x_b A$$

$$U \rightarrow AB$$

$$T \rightarrow AX_a$$

$$x_a \rightarrow a$$

$$x_b \rightarrow b$$

This is CNF form of given grammar.

7 (ii) $L = \{a^n b^m \mid n \leq m+3, n, m \geq 0\}$

we have to find CFG for this language.

$$S \rightarrow aSb | A | B$$

$$A \rightarrow a | aa | aaaa | \epsilon$$

$$B \rightarrow bB | b$$

This is CFG for given language.

Ques 8: Given the CFG, $S \rightarrow abAB$, $A \rightarrow bAB | \lambda$, $B \rightarrow Baa | A | \lambda$, prove that the string $w = abbaa$ is the member of given Grammar (using Membership Algorithm).

$$S \rightarrow abAB$$

$$A \rightarrow bAB | \lambda$$

$$B \rightarrow Baa | A | \lambda$$

(Take $\lambda = \epsilon$).

$$A \rightarrow \epsilon$$

$$S \rightarrow abAB | abB$$

$$A \rightarrow bAB | bB$$

$$B \rightarrow Baa | A | \lambda$$

$$B \rightarrow \epsilon$$

$$S \rightarrow abAB | abB | abA | ab$$

$$A \rightarrow bAB | bB | bA | b$$

$$B \rightarrow Baa | A | aa$$

Checking with $A \rightarrow \epsilon$ and $B \rightarrow \epsilon$ gives same only.

(iii) elimination of unit production.

$$S \rightarrow abAB | abB | abA | ab$$

$$A \rightarrow bAB | bB | bA | b$$

$$B \rightarrow Baa | bAB | bB | bA | b | aa$$

(iii) No useless symbol

(iv) Converting terminals to NT.

$$x_a \rightarrow a, x_b \rightarrow b.$$

$$S \rightarrow x_a x_b A B | x_a x_b B | x_a x_b A | x_a x_b.$$

$$A \rightarrow x_b A B | x_b B | x_b A | b.$$

$$B \rightarrow B x_a x_b | x_b A B | x_b B | x_b A | b | x_a x_a.$$

(v) Restricting no. of NT in RHS to 2.

$$S \rightarrow x_a P | x_a Q | x_a R | x_a x_b.$$

$$A \rightarrow x_b T | x_b B | x_b A | b.$$

$$B \rightarrow B U | x_b T | x_b B | x_b A | b | x_a x_a.$$

$$P \rightarrow x_b T$$

$$T \rightarrow AB$$

$$Q \rightarrow x_b B$$

$$R \rightarrow x_b A$$

$$U \rightarrow x_a x_a$$

$$x_a \rightarrow a$$

$$x_b \rightarrow b$$

x₁₆

⋮

x₁₅ x₂₆

w = abbbaaa.

x₁₄ x₂₅ x₃₆

x₁₃ x₂₄ x₃₅ x₄₆

x₁₂ x₂₃ x₃₄ x₄₅ x₅₆

x₁₁ x₂₂ x₃₃ x₄₄ x₅₅ x₆₆

a a b b a a

$$X_{11} = \{X_a\}, X_{22} = \{A, B, X_B\}, X_{33} = \{A, B, X_b\}, X_{44} = \{A, B, X_b\}$$

$$X_{55} = \{X_a\}, X_{66} = \{X_a\}$$

$$X_{12} = \{S\}, X_{23} = \{T, A, B, R, Q\}, X_{34} = \{T, A, B, R, Q\}, X_{45} = \{\phi\}.$$

$$X_{56} = \{B, U\}$$

$$X_{13} = \{X_{11}, X_{23}\} \cup \{X_{12}, X_{33}\}.$$

$$= \{S\}$$

$$X_{24} = \{X_{22}, X_{34}\} \cup \{X_{23}, X_{44}\}.$$

$$= \{T, A, B, R, P, Q\}.$$

$$X_{35} = \{(X_{23}, X_{45}) \cup (X_{34}, X_{55})\}.$$

$$= \{\phi\}$$

$$X_{46} = \{(X_{44}, X_{56}) \cup (X_{45}, X_{66})\}.$$

$$= \{T, A, B, Q\}.$$

$$X_{14} = \{X_{11}, X_{24}\} \cup \{X_{12}, X_{34}\} \cup \{X_{13}, X_{44}\}$$

$$= \{S\}$$

$$X_{25} = \{X_{22}, X_{35}\} \cup \{X_{23}, X_{45}\} \cup \{X_{24}, X_{55}\}.$$

$$= \{\phi\}.$$

$$X_{36} = \{X_{33}, X_{46}\} \cup \{X_{34}, X_{56}\} \cup \{X_{35}, X_{66}\}$$

$$= \{T, A, B, P, R, Q\}$$

$$X_{15} = \{(X_{11}, X_{25}) \cup (X_{12}, X_{35}) \cup (X_{13}, X_{45}) \cup (X_{14}, X_{55})\}.$$

$$= \{\phi\}.$$

$$X_{26} = \{(X_{22}, X_{36}) \cup (X_{23}, X_{46}) \cup (X_{24}, X_{56}) \cup (X_{25}, X_{66})\}.$$

$$= \{T, A, B, P, R, Q\}.$$

$$X_{16} = \{(X_{11}, X_{26}) \cup (X_{12}, X_{36}) \cup (X_{13}, X_{46}) \cup (X_{14}, X_{56}) \cup (X_{15}, X_{66})\}.$$

$$= \{S\} \rightarrow \text{contains } S, \text{ therefore Accepted.}$$

Ques: For the given grammar check if it is LL(1) parser or SLR(0) parser or Both. (Give reason). Justify your result by constructing parse table and check for the string i) $w = \text{id}$ ii) $w = * \text{id} = \text{id}$ (Respectively for i) and ii))

is accepted or no. Check if there is any shift/Reduce or Reduce/Reduce conflicts.

$$(ii) S \rightarrow aAd/bBd/aBm/bAm$$

$$A \rightarrow e$$

$$B \rightarrow e$$

$$(iii) S \rightarrow L = R/R$$

$$L \rightarrow *R/1d$$

$$R \rightarrow L$$

Ans

$$S \rightarrow aAd/bBd/aBm/bAm$$

$$A \rightarrow e$$

$$B \rightarrow e$$

Checking for LL(1) parser

→ No left recursion

→ Eliminating left factoring

$$S \rightarrow ax/by$$

$$x \rightarrow Ad/Bm$$

$$y \rightarrow Bd/Am$$

$$A \rightarrow e$$

$$B \rightarrow e$$

Find first and follow.

	First	Follow
S	{a, b}	{e, b}
X	{e}	{f}
y	{e}	{f}
Ad	{e}	{d, m}
Bd	{e}	{d, m}

Parse Table:

	a	b	d	e	c	m	s
S	S → aX	S → bY
X				X → AAd	X → Bm	.	.
Y				Y → Bd	Y → Am	.	.
A				A → e		.	.
B			.	B → e		.	.

Since a single cell contains more than one components

Hence it is not LL(1).

Since it is not LL(1). Therefore, if we check for string:
 $w = bed$

Stack	Input	Production
S\$	bed \$	(S, b) → bY
bY\$	ed \$	
Y\$	ed \$	[Y, e] → multiple productions to choose from

Hence LL(1) fails.

Checking for SLR parser.

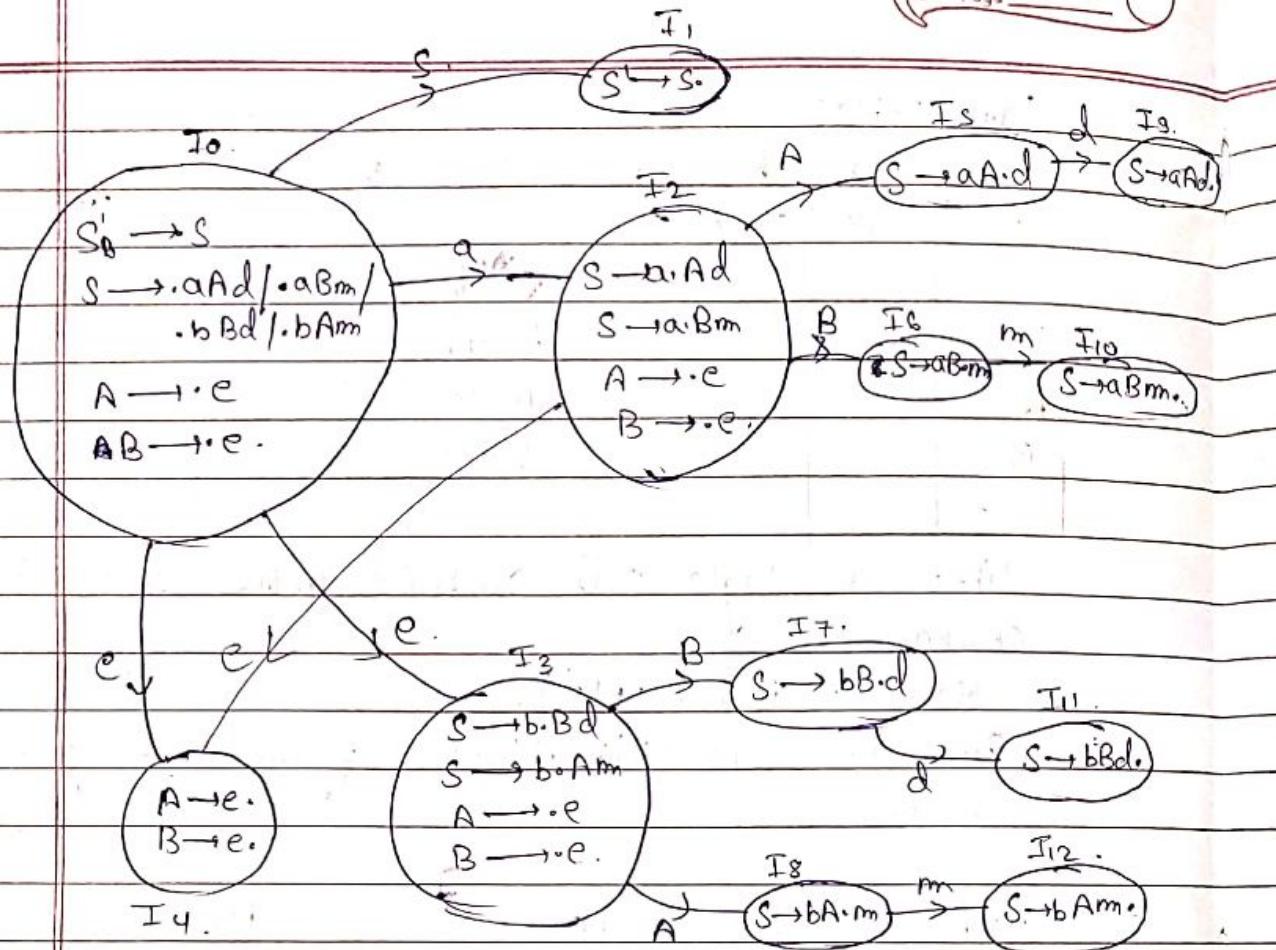
$$\begin{array}{l}
 S' \rightarrow S \quad ① \\
 S \rightarrow aAd \quad | \quad bBd \quad | \quad aBm \quad | \quad bAm \\
 A \rightarrow e \quad ⑤ \\
 B \rightarrow e \quad ⑥
 \end{array}$$

Items: $S' \rightarrow S$.

$$S \rightarrow aAd \quad | \quad bBd \quad | \quad aBm \quad | \quad bAm$$

$$A \rightarrow e$$

$$B \rightarrow e$$

Follow

S	$\{ \$ \}$
A	$\{ d, m \}$
B	$\{ d, m \}$

State	Action	Follow
	a b \bullet d, e m \bullet $\$$	S A B.
0	$S_2 S_3$	S_4
1		1
2	S_4	5 6
3	S_4	8 7
4	S_5 / S_6	S_5 / S_6
5	S_9	
6		
7		
8		
9		
10		
11		
12		

Since reduce-reduce conflict is there in the table
hence it is not SLR parser.

$w = \text{bed}$.

stack	input	rule:
\$	bed \$	$(0, b) = S_3$
\$0b3	ed \$	$(3, e) = S_4$
\$0b3e4	d \$	$(4, d) = S_5 / S_6$

conflict

therefore string not accepted

[Parsable
can't
decide]

$$(ii) \quad S \rightarrow L = R / R$$

$$L \rightarrow *R / id$$

$$R \rightarrow L$$

For LL(1) parser..

no left recursion and left factoring.

	First	Follow
S	$\{*, id\}$	$\{ \$ \}$
L	$\{*, id\}$	$\{ =, \$ \}$
R	$\{*, id\}$	$\{ =, \$ \}$

Parse Table:

	=	*	id	\$.
S		$S \rightarrow L = R$	$S \rightarrow L = R$.
		$S \rightarrow R$	$S \rightarrow R$.
L		$L \rightarrow *R$	$L \rightarrow id$		
R		$R \rightarrow L$	$R \rightarrow L$.

Since a single cell has more than one entry in a cell.

Therefore, it is not LL(1) parser.

Checking for Steing $w = * id = id$.

Stack
 $S\#$

Input
 $* id = id$

Reduction.

$(S, *) \rightarrow$ multiple production
to choose from.

Hence LL(1) fails.

For SLR parser.

$$\begin{aligned} S' &\rightarrow \cdot S. \\ S &\rightarrow \cdot L = R \quad | \quad \cdot R. \\ L &\rightarrow \cdot * R \quad | \quad \cdot id. \\ R &\rightarrow \cdot L \end{aligned}$$

I_0

$S' \rightarrow \cdot S$

$S \rightarrow \cdot L = R \quad | \quad \cdot R$

$L \rightarrow \cdot * R \quad | \quad \cdot id$

$R \rightarrow \cdot L$

I_1
 $S' \rightarrow S.$

I_2

$S \rightarrow L \cdot = R$
 $R \rightarrow L \cdot$

I_3

$S \rightarrow L = \cdot R$

$R \rightarrow \cdot L$

$\otimes L \rightarrow \cdot * R \quad | \quad \cdot id$

I_4
 $S \rightarrow R.$

$L \rightarrow id.$

I_5
 $L \rightarrow \cdot * R$
 $R \rightarrow \cdot L$
 $L \rightarrow \cdot * R \quad | \quad \cdot id$

I_6
 $R \rightarrow L \cdot$

I_7
 $S \rightarrow L = R \cdot$

I_8
 $L \rightarrow \cdot * R.$

Parse table.

	Follow:
S	\$, t, y
L	{, =, \$}
R	{, =, t, y}

States	Action				Goto		
	=	*	id	\$	S	L	R
0			$S_5 - S_8$		1	2	9
1				accept.			
2	$S_3 / S_5 -$			a_{15}			
3			$S_5 \quad S_8$			6	7
4		a_3		a_{13}			
5			S_8			6	4
6		a_5		a_{15}			
7				a_1			
8		a_4		a_{14}			
9				a_2			

Checking for string $w = *id=id$

Stack

Input

Rule

\$ 0

 $*id=id\$$ $[0, *] \rightarrow S_5$

\$ 0 * 5

 $id=id\$$ $[5, id] \rightarrow S_8$

\$ 0 * 5 id 8

 $= id \$$ $[8, =] \rightarrow a_4$

\$ 0 * 5 L 6

 $= id \$$ $[6, =] \rightarrow a_{15} -$

\$ 0 * 5 R 4

 $= id \$$ $[4, =] \rightarrow a_3$

\$ 0 L 2

 $= id \$$ $[2, =] \rightarrow \text{Conflict occurs.}$

Since shift produce conflict occurs.

Therefore it is not SLR parser.

Ques:10 Follow the given grammar construct CLR(1) parser. (Pause table also)

(i) $S \rightarrow id / B = D$

(ii) $B \rightarrow id.$

(iii) $D \rightarrow a / B.$

(iv) $S \rightarrow E$

$E \rightarrow (L) / r$

$L \rightarrow EL$

Ans:10 (i) $S \rightarrow id / B = D$

$B \rightarrow id$

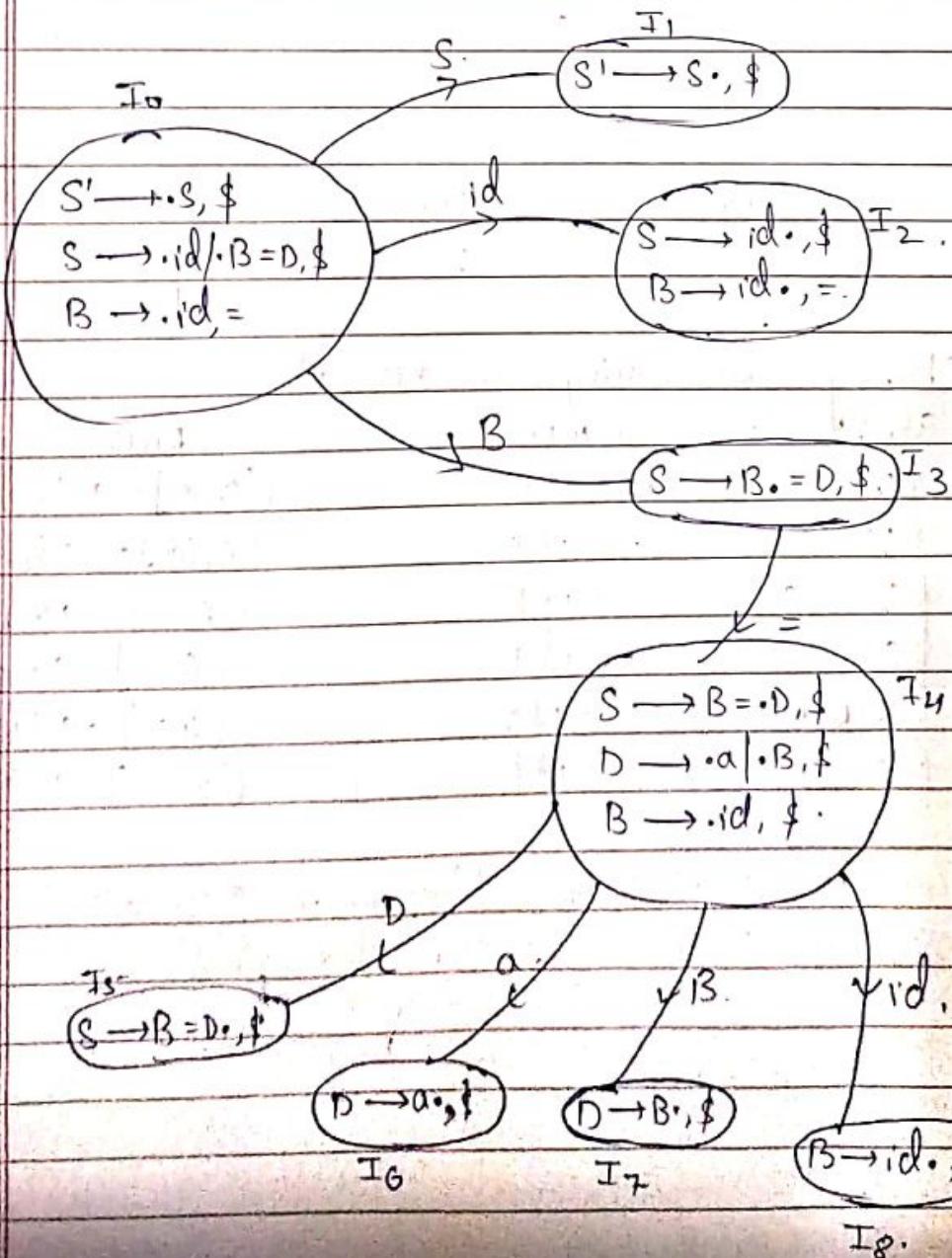
$D \rightarrow a / B.$

$S' \rightarrow \cdot S, \$$

$S \rightarrow \cdot id / \cdot B = D, \$$

$B \rightarrow \cdot id, =$

$D \rightarrow \cdot a / \cdot B,$



Parse Table for CLR(1)

State	Action				Goto.		
	id =	a	\$.	S	B	D
0	s_2				1	3..	
1				accept			
2		s_3					
3			s_4				
4	s_8				s_6	7	5..
5					s_2		
6					s_4		
7					s_5		
8					s_3		

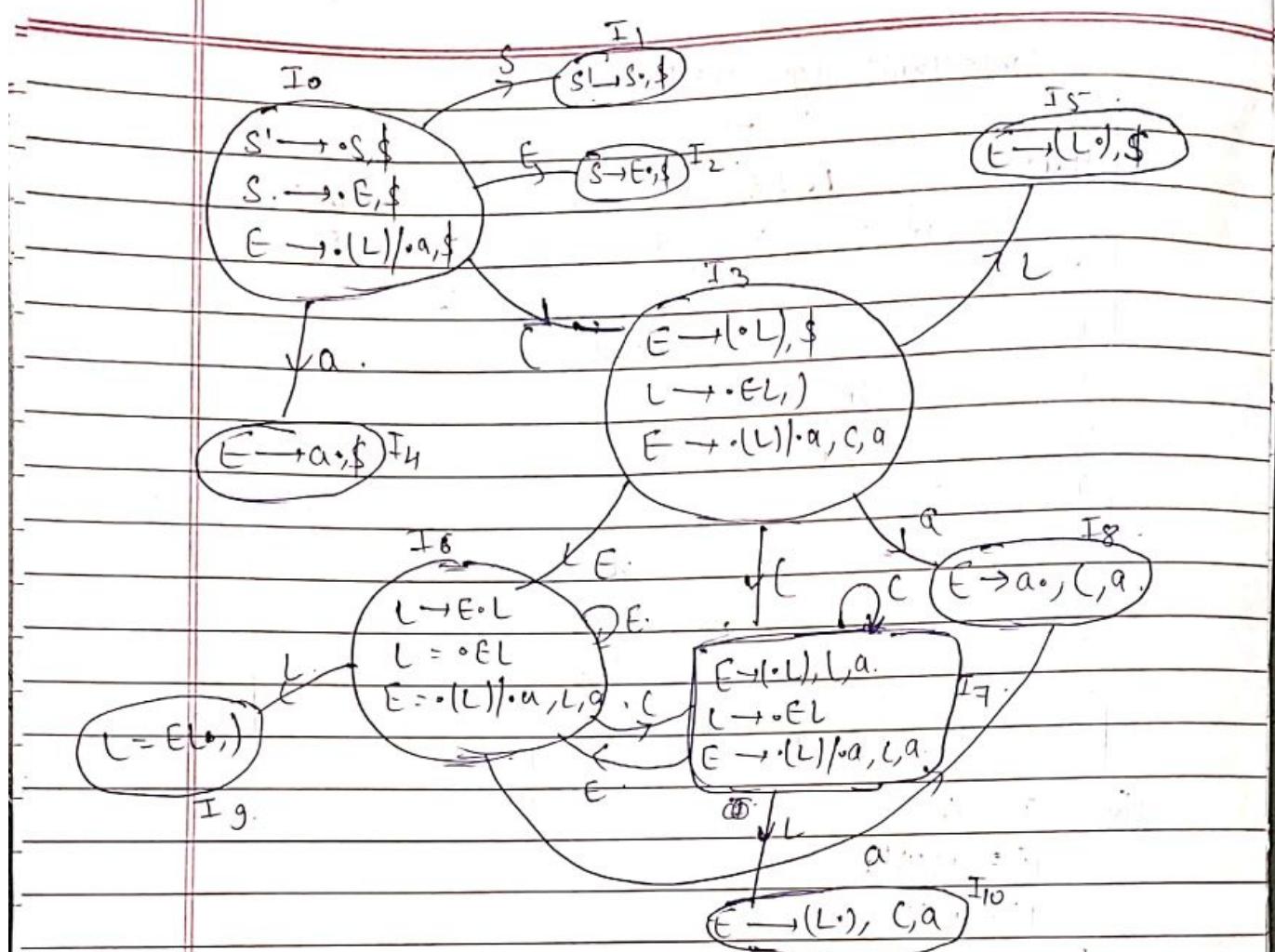
(ii) $S \rightarrow E$
 $E \rightarrow (L)/a$
 $L \rightarrow EL$

for CLR(1) \rightarrow LR(0) items + look ahead.

$S' \rightarrow S$
 $S \rightarrow \cdot E$
 $E \rightarrow \cdot (L) / a$
 $L \rightarrow \cdot EL$

{ LR(0) items }

State Diagram and Table on next
page.



Pause Table for CLR(1)

State	Action				Goto			
	(:)	a	\$	S	E	L
0	S ₃			S ₄		1	2	
1					accept.			
2					u ₁			
3	S ₇			S ₈		6	5	
4					u ₃			
5					u ₂			
6	S ₇			S ₈				
7	S ₇			S ₈				
8	u ₃			u ₃				
9				u ₄				
10	u ₂			u ₂				