# Package 'garma'

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```
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Title Fitting and Forecasting Gegenbauer ARMA Time Series Models
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Maintainer Richard Hunt <maint@huntemail.id.au>
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     Refer to the vignette for details of fitting these processes.
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```

2 AIC.garma\_model

# **RoxygenNote** 7.1.1 **VignetteBuilder** knitr

## **R** topics documented:

	AIC.garma_model	2
	coef.garma_model	3
	extract_arma	3
	fitted.garma_model	4
	forecast.garma_model	4
	garma	5
	garma_ggtsdisplay	8
	ggbr_semipara	8
	ggplot.garma_model	
	gg_raw_pgram	
	logLik.garma_model	
	plot.garma_model	11
	predict.garma_model	12
	print.garma_model	13
	print.garma_semipara	
	print.ggbr_factors	14
	residuals.garma_model	14
	summary.garma_model	15
	vcov.garma_model	15
	version	16
Index		17

 ${\tt AIC.garma\_model} \qquad \qquad {\tt AIC.for\ model}$ 

## Description

AIC for model if available.

## Usage

```
## S3 method for class 'garma_model'
AIC(object, ...)
```

## Arguments

object The garma\_model object
... Other parameters. Ignored.

coef.garma\_model 3

coef.garma\_model

Model Coefficients

## Description

Model Coefficients/parameters.

#### Usage

```
## S3 method for class 'garma_model'
coef(object, ...)
```

#### **Arguments**

object The garma\_model object
... Other parameters. Ignored.

extract\_arma

Extract underlying ARMA process.

#### Description

For a Gegenbauer process, transform to remove Gegenbauer long memory component to get a short memory (ARMA) process.

#### Usage

```
extract_arma(x, ggbr_factors)
```

## **Arguments**

x ggbr\_factors  $\left( num\right)$  This should be a numeric vector representing the Gegenbauer process.

(class) Each element of the list represents a Gegenbauer factor and includes f, u and fd elements.

#### Value

An object of same class as x.

```
data(AirPassengers)
ap <- as.numeric(diff(AirPassengers,12))
# find semiparametric estimates of the Gegenbauer parameters.
sp <- ggbr_semipara(ap)
# extract the underlying short-memory ARMA process
ap_arma <- extract_arma(ap,sp$ggbr_factors)
summary(arima(ap_arma,order=c(1,0,0)))</pre>
```

fitted.garma\_model Fitted values

#### **Description**

Fitted values are 1-step ahead predictions.

## Usage

```
## S3 method for class 'garma_model'
fitted(object, ...)
```

## Arguments

object The garma\_model object
... Other parameters. Ignored.

forecast.garma\_model Forecast future values.

#### **Description**

The forecast function predicts future values of a "garma\_model" object, and is exactly the same as the "predict" function with slightly different parameter values.

#### Usage

```
## S3 method for class 'garma_model'
forecast(object, h = 1, ...)
```

## Arguments

object (garma\_model) The garma\_model from which to forecast the values.

h (int) The number of time periods to predict ahead. Default: 1

Other parameters passed to the forecast function. For "garma\_model" objects, these are ignored.

#### Value

- a "ts" object containing the requested forecasts.

garma 5

#### **Examples**

```
library(forecast)

data(AirPassengers)
ap <- as.numeric(diff(AirPassengers,12))
mdl <- garma(ap,order=c(9,1,0),k=0,method='CSS',include.mean=FALSE)
forecast(mdl, h=12)</pre>
```

garma

garma: A package for estimating and foreasting Gegenbauer time series models.

## Description

The GARMA package provides the main function "garma" as well as print, summary, predict, forecast and plot/ggplot options.

The garma function is the main function for the garma package. Depending on the parameters it will calculate the parameter estimates for the GARMA process, and if available the standard errors (se's) for those parameters.

#### Usage

```
garma(
    x,
    order = list(0, 0, 0),
    k = 1,
    include.mean = (order[2] == 0),
    method = "Whittle",
    allow_neg_d = FALSE,
    opt_method = NULL,
    m_trunc = 50,
    min_freq = 0,
    max_freq = 0.5,
    control = NULL
)
```

#### **Arguments**

Х

(num) This should be a numeric vector representing the process to estimate. A minimum length of 96 is required.

order

(list) This should be a list (similar to the stats::arima order parameter) which will give the order of the process to fit. The format should be list(p,d,q) where p, d, and q are all positive integers. p represents the degree of the autoregressive process to fit, q represents the order of the moving average process to fit and d is the (integer) differencing to apply prior to any fitting. WARNING: Currently only d==0 or d==1 are allowed.

6 garma

k

(int) This is the number of (multiplicative) Gegenbauer terms to fit. Note the 'QML' method only allows k=1.

include.mean

(bool) A boolean value indicating whether a mean should be fit. Note that no mean term is fit if the series is integer differenced.

method

(character) This defines the estimation method for the routine. The valid values are 'CSS', 'Whittle', 'QML' and 'WLL'. The default (Whittle) will generally return very accurate estimates quite quickly, provided the asumption of a Gaussian distribution is even approximately correct, and is probably the method of choice for most users. For the theory behind this, refer Giraitis et. al. (2001) 'CSS' is a conditional 'sum-of-squares' technique and can be quite slow. Reference: Chung (1996). 'QML' is a Quasi-Maximum-Likelihood technique, and can also be quite slow. Reference Dissanayake (2016). (k>1 is not supported for QML) 'WLL' is a new technique which appears to work well even if the  $\epsilon_t$  are highly skewed and/or have heavy tails (skewed and/or lepto-kurtic). However the asymptotic theory for the WLL method is not complete and so standard errors are not available for most parameters.

allow\_neg\_d

(bool) A boolean value indicating if a negative value is allowed for the fractional differencing component of the Gegenbauer term is allowed. This can be set to FALSE (the default) to force the routine to find a positive value.

opt\_method

(character) This names the optimisation method used to find the parameter estimates. This may be a list of methods, in which case the methods are applied in turn, each using the results of the previous one as the starting point for the next. The default is to use c('directL', 'solnp') when k<2 and 'solnp' when k>=2. The directL algorithm is used to perform a global search for the minima, and solnp to refine the values. For some data or some models, however, other methods may work well. Supported algorithms include:

- cobyla algorithm in package nloptr
- directL algorithm in package nloptr
- BBoptim from package BB
- psoptim from package pso
- · hjkb from dfoptim package
- · nmkb from dfoptim package
- · solnp from Rsolnp package
- gosolnp from Rsolnp package
- best this option evaluates all the above options in turn and picks the one
  which finds the lowest value of the objective. This can be quite time consuming to run, particularly for the 'CSS' method.

Note further that if you specify a k>1, then inequality constraints are required, and this will further limit the list of supported routines.

m\_trunc

Used for the QML estimation method. This defines the AR-truncation point when evaluating the likelihood function. Refer to Dissanayake et. al. (2016) for details.

min\_freq

(num) When searching for Gegenbauer peaks, this is the minimum frequency used. Default 0. Note that when there is an AR(1) component, the peaks corresponding to the AR(1) can be higher than the Gegenbauer peaks. Setting this parameter to 0.05 or above can help.

garma 7

max\_freq (num) default 0.5. When searching for Gegenbauer peaks, this is the maximum frequency used.

control (list) list of optimisation routine specific values.

Details

The GARMA model is specified as

$$\phi(B) \prod_{i=1}^{k} (1 - 2u_i B + B^2)^{d_i} (X_t - \mu) = \theta(B) \epsilon_t$$

where

- $\phi(B)$  represents the short-memory Autoregressive component of order p,
- $\theta(B)$  represents the short-memory Moving Average component of order q,
- $(1-2u_iB+B^2)^{d_i}$  represents the long-memory Gegenbauer component (there may in general be k of these),
- $X_t$  represents the observed process,
- $\epsilon_t$  represents the random component of the model these are assumed to be uncorrelated but identically distributed variates. Generally the routines in this package will work best if these have an approximate Gaussian distribution.
- B represents the Backshift operator, defined by  $BX_t = X_{t-1}$ .

when k=0, then this is just a short memory model as fit by the stats "arima" function.

#### Value

An S3 object of class "garma\_model".

#### Author(s)

Richard Hunt

#### References

C Chung. A generalized fractionally integrated autoregressive moving-average process. Journal of Time Series Analysis, 17(2):111–140, 1996.

G Dissanayake, S Peiris, and T Proietti. State space modelling of Gegenbauer processes with long memory. Computational Statistics and Data Analysis, 100:115–130, 2016.

L Giraitis, J Hidalgo, and P Robinson. Gaussian estimation of parametric spectral density with unknown pole. The Annals of Statistics, 29(4):987–1023, 2001.

```
data(AirPassengers)
ap <- as.numeric(diff(AirPassengers,12))
print(garma(ap,order=c(9,1,0),k=0,method='CSS',include.mean=FALSE))
# Compare with the built-in arima function
print(arima(ap,order=c(9,1,0),include.mean=FALSE))</pre>
```

8 ggbr\_semipara

garma\_ggtsdisplay

ggtsdisplay of underlying ARMA process.

## Description

For a Gegenbauer process, use semi-parametric methods to obtain short memory version of the process, then run a ggtsdisplay().

#### Usage

```
garma_ggtsdisplay(x, k = 1, ...)
```

#### **Arguments**

x (num) This should be a numeric vector representing the process to estimate.

k (int) The number of Gegenbauer factors

... additional parameters to pass to ggtsdisplay

#### **Details**

The purpose of this function is to ease the process of identifying the underlying short memory process.

#### Value

A ggplot object.

## **Examples**

```
data(AirPassengers)
ap <- as.numeric(diff(AirPassengers,12))
garma_ggtsdisplay(ap)</pre>
```

ggbr\_semipara

Extract semiparametric estimates of the Gegenbauer factors.

#### **Description**

For a Gegenbauer process, use semi-parametric methods to estimate the Gegenbauer frequency and fractional differencing.

ggplot.garma\_model 9

#### Usage

```
ggbr_semipara(
    x,
    k = 1,
    alpha = 0.8,
    method = "gsp",
    min_freq = 0,
    max_freq = 0.5
)
```

#### **Arguments**

min\_freq (num) The minimum frequency to search through for peaks - default 0.0.

max\_freq (num) The maximum frequency to search through for peaks - default 0.5.

#### Value

An object of class "garma\_semipara".

## **Examples**

```
data(AirPassengers)
ap <- as.numeric(diff(AirPassengers,12))
sp <- ggbr_semipara(ap)
print(sp)</pre>
```

ggplot.garma\_model

ggplot of the Forecasts of the model.

#### Description

The ggplot function generates a ggplot of actuals and predicted values for a "garma\_model" object. This adds in sensible titles etc as best it can determine.

#### Usage

```
## S3 method for class 'garma_model'
ggplot(mdl, h = 24, include_fitted = FALSE, ...)
```

10 gg\_raw\_pgram

## **Arguments**

mdl (garma\_model) The garma\_model from which to ggplot the values.

h (int) The number of time periods to predict ahead. Default: 24

include\_fitted (bool) whether to include the 1-step ahead 'fitted' values in the plot. Default: FALSE

... other parameters passed to ggplot.

#### Value

A ggplot2 "ggplot" object. Note that the standard ggplot2 "+" notation can be used to enhance the default output.

#### **Examples**

```
library(ggplot2)

data(AirPassengers)
ap <- as.numeric(diff(AirPassengers,12))
mdl <- garma(ap,order=c(9,1,0),k=0,method='CSS',include.mean=FALSE)
ggplot(mdl)</pre>
```

gg\_raw\_pgram

Display raw periodogram

#### **Description**

Display the raw periodogram for a time series, and not on a log scale.

#### Usage

```
gg_raw_pgram(x, k = 1)
```

#### **Arguments**

x (num) This should be a numeric vector representing the process to estimate.

k (int) The number of Gegenbauer factors

## Details

The standard "R" functions display periodograms on a log scale which can make it more difficult to locate high peaks in the spectrum at differring frequencies. This routine will display the peaks on a raw scale.

#### Value

A ggplot object representing the raw periodogram

logLik.garma\_model 11

#### **Examples**

```
data(AirPassengers)
ap <- as.numeric(diff(AirPassengers,12))
sp <- ggbr_semipara(ap)
print(sp)</pre>
```

logLik.garma\_model

Log Likelihood

#### **Description**

Log Likelihood, or approximate likelihood or part likelihood, depending on the method.

#### Usage

```
## S3 method for class 'garma_model'
logLik(object, ...)
```

## Arguments

object The garma\_model object
... Other parameters. Ignored.

plot.garma\_model

Plot Forecasts from model.

#### **Description**

The plot function generates a plot of actuals and predicted values for a "garma\_model" object.

#### Usage

```
## S3 method for class 'garma_model'
plot(x, ...)
```

## **Arguments**

x (garma\_model) The garma\_model from which to plot the values.

... other arguments to be passed to the "plot" function, including h (int) - the number of periods ahead to forecast.

#### Value

```
An R "plot" object.
```

12 predict.garma\_model

#### **Examples**

```
data(AirPassengers)
ap <- as.numeric(diff(AirPassengers,12))
mdl <- garma(ap,order=c(9,1,0),k=0,method='CSS',include.mean=FALSE)
plot(mdl)</pre>
```

predict.garma\_model

The predict future values.

#### **Description**

Predict ahead using algorithm of Ferrara, Laurent & Guegan, Dominique, 2001. "Forecasting with k-Factor Gegenbauer Processes: Theory and Applications," Journal of Forecasting, John Wiley & Sons, Ltd., vol. 20(8), pages 581-601, December.

#### Usage

```
## S3 method for class 'garma_model'
predict(object, n.ahead = 1, ...)
```

#### **Arguments**

object (garma\_model) The garma\_model from which to predict the values.

n.ahead (int) The number of time periods to predict ahead. Default: 1

Other parameters. Ignored.

#### Value

A "ts" object containing the requested forecasts.

```
data(AirPassengers)
ap <- as.numeric(diff(AirPassengers,12))
mdl <- garma(ap,order=c(9,1,0),k=0,method='CSS',include.mean=FALSE)
predict(mdl, n.ahead=12)</pre>
```

print.garma\_model 13

print.garma\_model

print a garma\_model object.

## Description

The print function prints a summary of a "garma\_model" object.

#### Usage

```
## S3 method for class 'garma_model'
print(x, ...)
```

#### **Arguments**

x (garma\_model) The garma\_model from which to print the values.

... Other arguments. Ignored.

## **Examples**

```
data(AirPassengers)
ap <- as.numeric(diff(AirPassengers,12))
mdl <- garma(ap,order=c(9,1,0),k=0,method='CSS',include.mean=FALSE)
print(mdl)</pre>
```

```
print.garma_semipara Print Semiparametric Estimates
```

## Description

Print a semiparameteric Gegenbauer estimation object.

### Usage

```
## S3 method for class 'garma_semipara'
print(x, ...)
```

## Arguments

x An object of class garma\_semipara.

... further parameters for print function

print.ggbr\_factors

Print a 'ggbr\_factors' object.

## Description

Print a 'ggbr\_factors' object.

#### Usage

```
## S3 method for class 'ggbr_factors'
print(x, ...)
```

## Arguments

x An object of class ggbr\_factors

... further parameters for print function

residuals.garma\_model Residuals

## Description

Response Residuals from the model.

#### Usage

```
## S3 method for class 'garma_model'
residuals(object, type = "response", h = 1, ...)
```

#### **Arguments**

object The garma\_model object

type (chr) The type of residuals. Must be 'response'.

h (int) The number of periods ahead for the residuals. Must be 1.

... Other parameters. Ignored.

summary.garma\_model 15

summary.garma\_model

summarise a garma\_model object.

## Description

The summary function provides a summary of a "garma\_model" object.

## Usage

```
## S3 method for class 'garma_model'
summary(object, ...)
```

#### **Arguments**

object (garma\_model) The garma\_model from which to print the values.
... Other arguments. Ignored.

## **Examples**

```
data(AirPassengers)
ap <- as.numeric(diff(AirPassengers,12))
mdl <- garma(ap,order=c(9,1,0),k=0,method='CSS',include.mean=FALSE)
summary(mdl)</pre>
```

vcov.garma\_model

Covariance matrix

## Description

Covariance matrix of parameters if available

### Usage

```
## S3 method for class 'garma_model'
vcov(object, ...)
```

## **Arguments**

object The garma\_model object
... Other parameters. Ignored.

16 version

version

garma package version

## Description

The version function returns the garma package version.

## Usage

```
version()
```

```
library(garma)
garma::version()
```

# **Index**

```
{\tt AIC.garma\_model, 2}
coef.garma_model, 3
extract_arma, 3
fitted.garma\_model, 4
forecast.garma_model, 4
garma, 5
{\tt garma\_ggtsdisplay}, 8
gg_raw_pgram, 10
ggbr_semipara, 8
ggplot.garma\_model, 9
logLik.garma_model, 11
plot.garma_model, 11
predict.garma_model, 12
print.garma_model, 13
print.garma_semipara, 13
print.ggbr_factors, 14
residuals.garma\_model, 14
summary.garma_model, 15
vcov.garma_model, 15
version, 16
```