[CSE471: Statistical Methods in Artificial Intelligence (SMAI)]

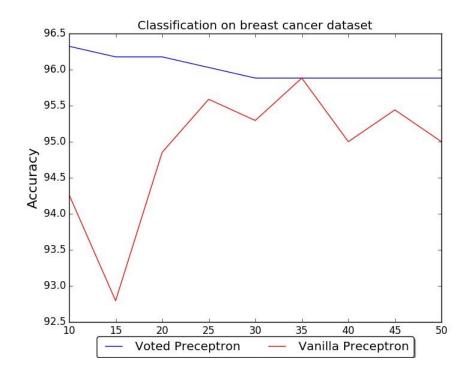
[Assignment-1]

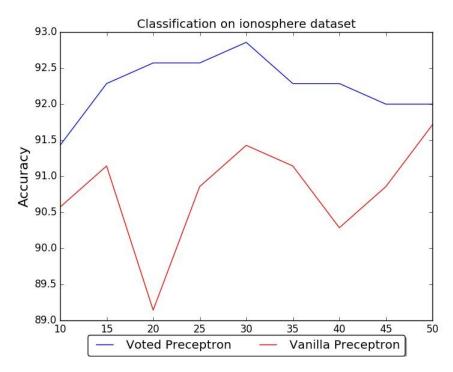
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Roll: 20172119

Q1: Compare the performance of Voted and Vanilla Perceptron Classification Models

Observation:





----Breast Cancer Dataset----

epoch = 10

Average Voted Perceptron Accuracy: 96.3235294118 Average Vanilla Perceptron Accuracy: 94.2647058824

epoch = 15

Average Voted Perceptron Accuracy: 96.1764705882 Average Vanilla Perceptron Accuracy: 92.7941176471

epoch = 20

Average Voted Perceptron Accuracy: 96.1764705882 Average Vanilla Perceptron Accuracy: 94.8529411765

epoch = 25

Average Voted Perceptron Accuracy: 96.0294117647 Average Vanilla Perceptron Accuracy: 95.5882352941

epoch = 30

Average Voted Perceptron Accuracy: 95.8823529412 Average Vanilla Perceptron Accuracy: 95.2941176471

epoch = 35

Average Voted Perceptron Accuracy: 95.8823529412 Average Vanilla Perceptron Accuracy: 95.8823529412

epoch = 40

Average Voted Perceptron Accuracy: 95.8823529412

Average Vanilla Perceptron Accuracy: 95.0

epoch = 45

Average Voted Perceptron Accuracy: 95.8823529412 Average Vanilla Perceptron Accuracy: 95.4411764706

epoch = 50

Average Voted Perceptron Accuracy: 95.8823529412

Average Vanilla Perceptron Accuracy: 95.0

----lonosphere Dataset----

epoch = 10

Average Voted Perceptron Accuracy: 91.4285714286 Average Vanilla Perceptron Accuracy: 90.5714285714

epoch = 15

Average Voted Perceptron Accuracy: 92.2857142857 Average Vanilla Perceptron Accuracy: 91.1428571429

epoch = 20

Average Voted Perceptron Accuracy: 92.5714285714 Average Vanilla Perceptron Accuracy: 89.1428571429

epoch = 25

Average Voted Perceptron Accuracy: 92.5714285714 Average Vanilla Perceptron Accuracy: 90.8571428571

epoch = 30

Average Voted Perceptron Accuracy: 92.8571428571 Average Vanilla Perceptron Accuracy: 91.4285714286

epoch = 35

Average Voted Perceptron Accuracy: 92.2857142857 Average Vanilla Perceptron Accuracy: 91.1428571429

epoch = 40

Average Voted Perceptron Accuracy: 92.2857142857 Average Vanilla Perceptron Accuracy: 90.2857142857

epoch = 45

Average Voted Perceptron Accuracy: 92.0

Average Vanilla Perceptron Accuracy: 90.8571428571

epoch = 50

Average Voted Perceptron Accuracy: 92.0

Average Vanilla Perceptron Accuracy: 91.7142857143

Comments:

The accuracy of the prediction in case of voted perceptron is better than the vanilla perceptron. Also, the accuracy of the voted one is maintaining a value within very short range for different epochs, whereas the accuracy of vanilla varies a lot depending upon the epochs. We can see the accuracy of vanilla perceptron sometime dips too much, even after giving a very high accuracy for some epoch, if we increase the epoch further. But this is not the case with the voted perceptron, it is almost invariant with respect to the epochs after an epoch value. It seems the voted perceptron converges much earlier than vanilla.

Reason:

In perceptron training, we update the weights when the used weight fails to correctly classify the data point. In vanilla, whenever we find a misclassification, we update the hyperplane and train the model for other data points using the updated weight. But the problem is we don't keep track of how many examples has been correctly classified by the old hyperplane. So, when we move the hyperplane to a new position, it might be the case that the new hyperplane fails to correctly classify the points it was correctly classifying previously, and that number of misclassifications, say the set P, may be more than

the number of correctly classified examples. So, we lose the importance of the "more" correct classifier. When, we come back again for the next round of iteration, we once again have to adjust the hyperplane to make the set P to fall into the correct class. But, this way we cannot guarantee that the classifier accuracy will be improved with increased epoch, though it is guaranteed to converge at some point of time, obviously if the data is linearly classifiable.

On the other hand, the voted perceptron has the votes for each corresponding weight. This vote signifies which hyperplane classifies more examples correctly. So, when we predict the output we take the weighted value of the hyperplanes. This way the hyperplanes which were "more" correct and survives for a longer time has more contribution in predicting the output.

```
import numpy as np
import matplotlib.pyplot as plt
from random import shuffle
from sklearn.metrics import accuracy_score

def K_Fold_Cross_Validation(X, Y, K):

Divide the whole dataset into K-folds and
perform testing for each one the fold
while train the model using other K-1 folds

'''

Y = Y.reshape(Y.shape[0],1)
sampleSize = int(X.shape[0] / K)
startPoint = 0
endPoint = startPoint + sampleSize

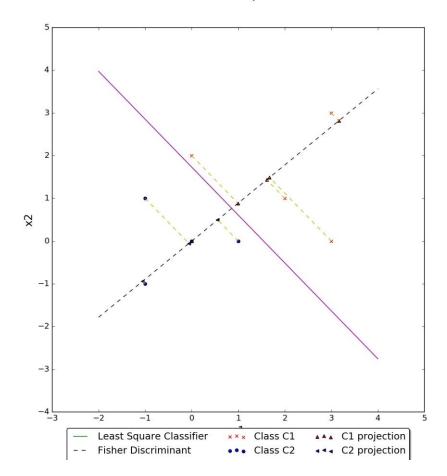
X cv = X[startPoint:endPoint,:]
Y cv = Y[startPoint:endPoint]
X_train = x[0:startPoint]
X_train = x[0:startPoint]
X_train = np.append(X_train, X[endPoint:,:],axis=0)
Y_train = Y[0:startPoint]
Y_train = y[0:startPoint]
Y_train = np.append(Y_train, X_cv, Y_train, Y_cv]]
for i in range(K-1):
    startPoint += sampleSize
endPoint=startPoint+sampleSize
X_train = x[0:startPoint:endPoint;:]
Y_cv = Y[startPoint:endPoint]
X_train = X[0:startPoint]
X_train = X[0:startPoint]
Y_train = y[0:startPoint]
```

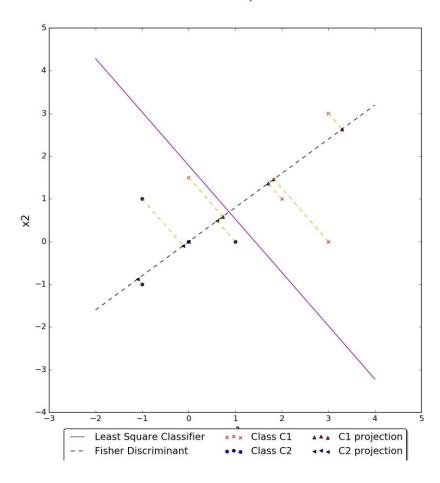
```
def votedPerceptron(X, Y, epoch):
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                                        W = np.zeros((1, A.s
B = np.zeros((1, 1))
C = np.zeros((1, 1))
                                                            np.zeros((1, X.shape[1]))
                                         n = 0
m = X.shape[0]
                                          number of features = X.shape[1]
for round in range(epoch):
    for i in range(m):
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                                                                                                     Thinge(m). Tange(m): (p.dot(W[n], X[i].reshape(number of features, 1)) + B[n]) <= 0:
W = np.append(W, np.array([W[n] + Y[i]  \overline{x} X[i]]), axis=0)
B = np.append(B, np.array([B[n] + Y[i]]), axis=0)
C = np.append(C, [[1]], axis=0)
                                                                                    else:
C[n] += 1
                                            return W[1:, :], B[1:, :], C[1:, :]
                      def votedPerceptronPredict(X, Y, W, B, C):
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                                          Y_predicted = np.zeros((1, 1))
                                         examples = Y.shape[0]
shape_w = W.shape
                                           for e in range(examples):
    temp_val = np.dot(W, X[e].T).reshape(shape_w[0], 1) + B
    temp_val[temp_val>0] = 1
    temp_val[temp_val<0] = -1
    v_predicted_np_append(Y_predicted_np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_asarray([sign(np_as
                                          Y_predicted = np.append(Y_predicted, np.asarray([sign(np.dot(C.T, temp_val))]))
Y_predicted = Y_predicted[1:]
                                            return Y_predicted.reshape(examples, 1)
```

Q2. Comparison of classifiers - Least Square Method vs Fisher's LDA

Observation:

Fisher's discriminant vs Least square - C1 vs C2 - Table 1





Comment:

The classifiers learnt using least square method and Fisher's LDA are the same. Direction of discriminant gives the direction of projection of data points in which the separation between the classes is maximum.

Reasons:

Fisher's LDA gives the direction of projection on which the data is reduced to a lower dimension and those projected data points are efficiently separable. Then we can apply any classifier on the projected points to discriminate them. The motive of Fisher's LDA is to project the data in such a way that they are also classifiable in the projected lower dimensional space and that would give the same decision boundary. This is observed in the output.

Q3. Latent Semantic Analysis

Classify documents using one-vs-rest voted perceptron after applying PCA:
 <u>Observation:</u>

The accuracy of this method when we take 1110 singular values: 93.91634980988593

**Note: Value of k depends on how many train documents we take When we vary the value of K, the following accuracies have been reported:

```
def sign(val):
    return -1 if val < 0 else 1</pre>
      def formTFMatrix(documents, terms):
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             tf_matrix = []
for words in documents:
                    doc_terms = []
                    for t in terms:
    doc_terms.append(words.count(t))
                    tf matrix.append(doc terms)
             return np.array(tf_matrix)
33
34
      def multiclass_voted_perceptron(X, Y, epoch):
35
36
             m = X.shape[0]
             number of features = X.shape[1]
            W = np.zeros((1, number_of_features))
B = np.zeros((1, 1))
C = np.zeros((1, 1))
             n = 0
             for round in range(epoch):
    for i in range(m):
        if Y[i] * (np.dot(W[n], X[i].reshape(number_of_features, 1)) + B[n]) <= 0:
        W = np.append(W, np.array(W[n] + Y[i] * X[i]), axis=0)
        B = np.append(B, np.array([B[n] + Y[i]]), axis=0)
        C = np.append(C, [[1]], axis=0)</pre>
                                 C[n] += 1
             return W[1:, :], B[1:, :], C[1:, :]
```

```
def votedPerceptronPredict(X, Y, W dict, B dict, C dict, class labels):
                Y_predicted = np.zeros((1, 1))
examples = Y.shape[0]
                 for e in range(examples):
                        predict = np.asarray([])
for x in class labels:
    W = W dict[x]
    B = B dict[x]
    C = C dict[x]
62
                                  shape^{-}w = W.shape
                                  temp val = np.dot(W, X[e].T).reshape(shape_w[0], 1) + B
                        predict = np.append(predict, np.dot(C.T, temp_val))
Y_predicted = np.append(Y_predicted, np.asarray([(np.argmax(predict))]))
                Y predicted = Y predicted[1:]
                 return Y predicted.reshape(examples, 1)
        def one vs all voted(X, Y, X test, Y test, epoch):
                class labels = np.unique(Y)
                weight = {}
bias = {}
vote = {}
                Y original = deepcopy(Y)
for x in range(class_labels.shape[0]):
    Y = deepcopy(Y_original)
    for i in range(Y.shape[0]):
                                        Y[i][0] == x:
Y[i][0] = 1
                weight[x], bias[x], vote[x] = multiclass_voted_perceptron(X, Y, epoch)
Y_predicted = votedPerceptronPredict(X_test, Y_test, weight, bias, vote, class_labels)
correct_class = 0
93
94
                 for i in range(Y_predicted.shape[0]):
    if Y_predicted[i][0] == Y_test[i][0]:
                                 correct class
                   for i in range(Y.shape[0]):
                          if Y[i][0] == x:
Y[i][0] = 1
            Y[i][0] = -1
  weight[x], bias[x], vote[x] = multiclass_voted_perceptron(X, Y, epoch)
Y_predicted = votedPerceptronPredict(X_test, Y_test, weight, bias, vote, class_labels)
correct_class = 0
for_i = rear(Y)
                        t class = 0
in range(Y_predicted.shape[0]):
Y_predicted(i][0] == Y_test[i][0]:
    correct class += 1
            correct_class += 1
print((correct_class / Y_predicted.shape[0]) * 100)
     def extractDocs(dataPath):
            documents =
            stop = set(stopwords.words('english')) # Reomoves the stop words eg the, an, a, and etc.

stemmer = PorterStemmer() # Converts the words to their root words

tokenizer = RegexpTokenizer(r'\w+') # Tokenize the document to et rid off non alphabets

folders = [dataPath + name + '/' for name in os.listdir(dataPath) if os.path.isdir(dataPath + name)]

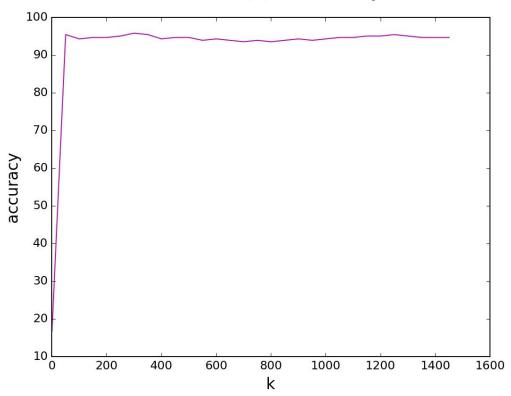
class_name = [int(name) for name in os.listdir(dataPath) if os.path.isdir(dataPath + name)]
            ctass name
it = 0
for folder in folders:
    docFiles = [folder + docName for docName in os.listdir(folder)]
    doc_words = []
    fer f in docFiles:
                          fin docFiles:
file = codecs.open(f, 'r', 'ISO-8859-1')
                          file = Couest.open(r, r, rso-boss-r)
file content = []
for document in file:
    word_list = [stemmer.stem(line) for line in tokenizer.tokenize(document.lower()) if line not in '']
    file_content.extend([w for w in word_list if w not in stop])
                          file.close()
                          documents.append(file_content)
class_labels.append(class_name[it])
            return documents, (np.array([class labels])).T
```

```
128 def getUniqueWords(documents):
                     words = [word for doc in documents for word in doc]
unique_words = list(set(words))
                      return unique words
           def classify document by perceptron(dataPath, testPath):
140
141
                     avg_accuracy = []
documents, classes = extractDocs(dataPath)
test_documents, test_classes = extractDocs(testPath)
train_data_length = len(documents)
for test_doc_in_test_documents:
    documents.append(test_doc)
    terms = netUniqueWords(documents)
142
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                     terms = getUniqueWords(documents)
                    terms = getUniqueWords(documents)
tf matrix = formTFMatrix(documents, terms)
tf = TfidfTransformer(norm='l2', use_idf=True, smooth_idf=True, sublinear_tf=False)
tf idf matrix = tf.fit_transform(tf_matrix).todense() # Form the tf-idf matrix from bag of words
test_data = tf_idf_matrix[train_data_length: , :]
tf_idf_matrix = tf_idf_matrix[:train_data_length: , :]
U, Sigma_temp, V_T = np.linalg.svd(tf_idf_matrix) # Singular Value Decomposition
Sigma = np.zeros((Sigma_temp.shape[0], Sigma_temp.shape[0]))
for i in range(Sigma_temp.shape[0]):
    Sigma[i][i] = Sigma_temp[i]
# k list = list(range(10, min(tf_idf_matrix.shape[0], tf_idf_matrix.shape[1]), 50))
k list = [1110]
154
155
                     # k_list = list(
k_list = [1110]
for k in k_list:
                               # Reducce the dimension using the eigen value which contributes the most
reduced_data = np.dot(np.dot(U[:, :k], Sigma[:k, :k]), V_T[:k, :])
                               epoch = 40 # Epoch for the perceptron gtraing
print("Accuracy using k = ", k)
                                one_vs_all_voted(reduced_data, classes, test_data, test_classes, epoch)
          dataPath = sys.argv[1] #'./LSAdata (copy)/train/
testPath = sys.argv[2] #'./LSAdata (copy)/test/'
170 classify document by perceptron(dataPath, testPath)
```

Predict the class label of the test document using cosine similarity: Observation:

As we increase the value of k, after some value the accuracy vs the values of k graph saturates, but at k = 1251 the accuracy is maximum.

Dimension (k) vs Accuracy



SVD Accuracy:

Accuracy for k = 1

16.730038022813687

Accuracy for k = 51

95.43726235741445

Accuracy for k = 101

94.29657794676807

Accuracy for k = 151

94.67680608365019

Accuracy for k = 201

94.67680608365019

Accuracy for k = 251

95.05703422053232

Accuracy for k = 301

95.81749049429658

Accuracy for k = 351

95.43726235741445

Accuracy for k = 401

94.29657794676807

Accuracy for k = 451

94.67680608365019

Accuracy for k = 501

94.67680608365019

Accuracy for k = 551

93.91634980988593

Accuracy for k = 601

94.29657794676807

Accuracy for k = 65193.91634980988593 Accuracy for k = 70193.5361216730038 Accuracy for k = 75193.91634980988593 Accuracy for k = 80193.5361216730038 Accuracy for k = 85193.91634980988593 Accuracy for k = 90194.29657794676807 Accuracy for k = 951

93.91634980988593

Accuracy for k = 1001

94.29657794676807

Accuracy for k = 1051

94.67680608365019

Accuracy for k = 1101

94.67680608365019

Accuracy for k = 1151

95.05703422053232

Accuracy for k = 1201

95.05703422053232

Accuracy for k = 1251

95.43726235741445

Accuracy for k = 1301

95.05703422053232

Accuracy for k = 1351

94.67680608365019

Accuracy for k = 1401

94.67680608365019

Accuracy for k = 1451

94.67680608365019

```
def extractDocs(dataPath):

Extract words from the documents

documents = []

class labels = []

stop = set(stopwords.words('english')) # Reomoves the stop words eg the, an, a, and etc.

stemmer = PorterStemmer() # Converts the words to their root words

tokenizer = Requesprolonizer('r'.ww') # Tokenize the document to terid off non alphabets

folders = [dataPath + name + '/' for name in os.listdir(dataPath) if os.path.isdir(dataPath + name)]

class name = [int(name) for name in os.listdir(dataPath) if os.path.isdir(dataPath + name)]

it = 0

for folder in folders:

docFiles = [folder + docName for docName in os.listdir(folder)]

doc words = []

for in docriles:

file = codecs.open(f, 'r', 'ISO-8859-1')

file content = []

for document in file:

word list = [stemmer.stem(line) for line in tokenizer.tokenize(document.lower()) if line not in '']

file.colose()

documents.append(file content)

class labels.append(file content)

class labels.append(class_name[it])

it += 1

return documents, (np.array([class_labels])).T

def getUniqueWords (documents):

Find the dictionary of words

words = [word for doc in documents for word in doc]

unique_words = list(set(words))

return unique_words

def fornIFMatrix(documents, terms):

construct the bag of words matrix for each document

where each row represents each document and

columns represent each terms

total matrix = []

for words in documents;

doc terms = []

for it in terms:
```

```
def formTFMatrix(documents, terms):

Construct the bag of words matrix for each document where each row represents each document and columns represent each terms

td. matrix = []

for words in documents:

doc terms = []

for t in terms:

doc terms.append(words.count(t))

td. matrix.append(doc terms)

return np.array(td_matrix)

def readtestDoc(testPath):

Reading the test document

documents = []

documents = []

for document in file:

word list = gegexplokenizer(r'\w')

file = codecs.open(testPath, 'r', 'ISO-8859-1')

file content = []

for document in file:

word list = [stemmer.stem(line) for line in tokenizer.tokenize(document.lower()) if line not in '']

file.close()

documents.append(file_content)

return documents;

def measure similarity by cosine(dataPath, testPath, testDocLabel):

avg accuracy = []

documents, classes = extractDocs(dataPath)

test documents, rest classes = extractDocs(testPath)

train data length = len(documents)

for test doc in test documents;

documents_append(tric documents)

tf artial data length = len(documents)

tf matrix = formFhatrix(documents, terms)

tf = fridfTransformer(norms')2: use idf-True, smooth idf=True, sublinear tf=False)

tf = fridfTransformer(norms')2: use idf-True, smooth idf=True, sublinear tf=False)

tf = fridfTransformer(norms')2: use idf-True, smooth idf=True, sublinear tf=False)

tf idf matrix = tf fit transformet fastrix).todense() # Form the tf-idf matrix from bag of words

test data = tf idf matrix(train data length): . :)
```

```
tf idf matrix = tf idf matrix[:train data length, :]

U, Sigma temp, V T = np.linalg.svd(tf idf matrix) # singular Value Decomposition

Sigma = np.zeros((Sigma temp.shape[0]); Sigma_temp.shape[0]))

Sigma[i][i] = Sigma_temp[i]

# k list = list(range(1, min(tf idf matrix.shape[0], tf idf matrix.shape[1]), 50))

k list = [1251] # Best value of k

# print(*SVD Accuracy:")

for k in k list:

correct_similarity = 0

reduced_data = np.dot(np.dot(U[:, :k], Sigma[:k, :k]), V.T[:k, :])

cosine Similarity matrix = sklearn.metrics.pairvise.cosine_similarity(reduced_data, test_data)

for x in range(test_data.shape[0]):

augmented_similarity matrix = np.concatenate(

(cosine_similarity matrix = np.concatenate(

(cosine_similarity matrix = np.concatenate()

(cosine_similarity matrix = augmented similarity_matrix[:, 0].shape[0], 1),

classes.reshape(classes.shape[0]);

sorted_similarity_matrix = sorted_similarity_matrix[:]]

sorted_similarity_matrix = sorted_similarity_matrix[::]]

sorted_similarity_matrix = sorted_similarity_matrix[::]]

sorted_similarity_matrix = sorted_similarity_matrix[::]]

top.lo_results = sorted_similarity_matrix[::0, -1]

labels = np.unique(top_lo_results).

tor l in labels:

if max_match = !1st(top_lo_results).count(l):

max_match = !1st(top_lo_results).count(l):

max_match = !1st(top_lo_results).count(l):

predicted_label = |

print("The predicted_label = int(test_classes[x]):

correct_similarity_similarity = int(test_classes[x]):

sorted_similarity_natrix = i
```