

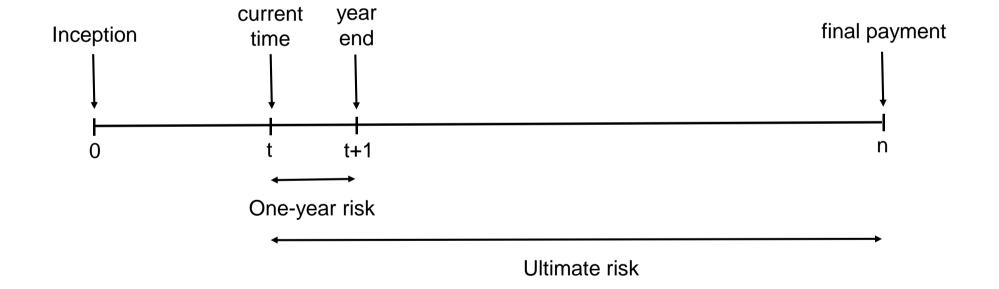
Parameterising emergence factors: how hard can it be?

Robert Scarth

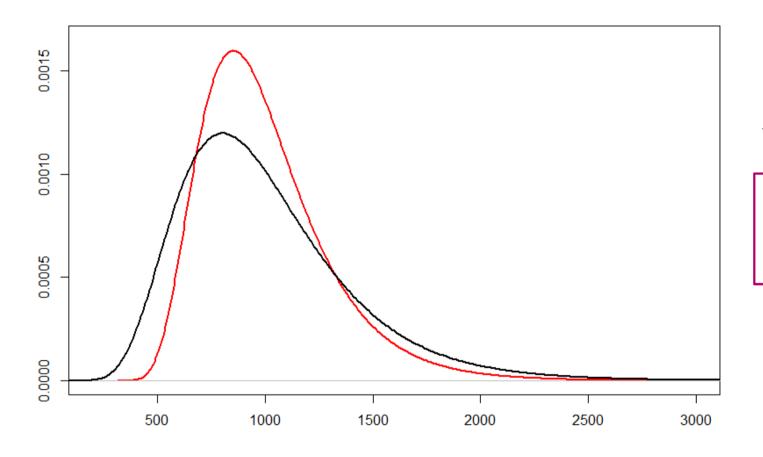
Chair, Pragmatic Stochastic Reserving Working Party

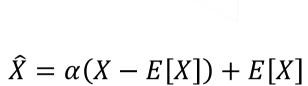
Ultimate view and one-year view





What are emergence factors?





Question: Where does the factor α come from?

Why use emergence factors?

Alternatives

- Merz-Wüthrich
- Actuary-in-the-Box
- Direct modelling

No well established model

Inflexible

Need enough data to fit model

Depends on bootstrap

Need consistent data

Computationally expensive

Difficult to explain

Emergence factors

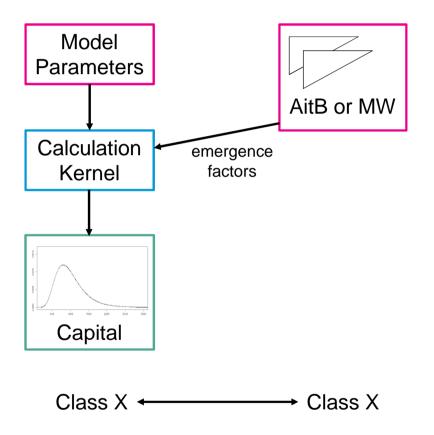
- Computationally easy
- Flexible
- Simple to explain

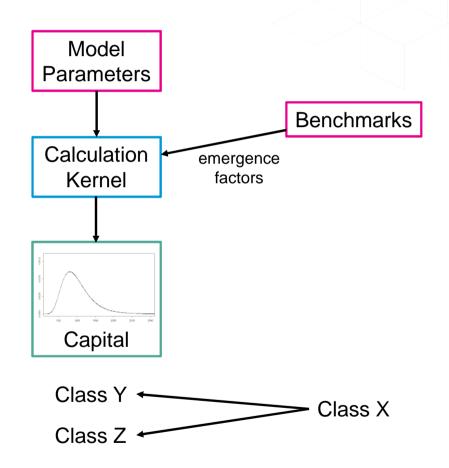
Parameterising emergence factors

	1	2	3	4	5	6	7	8	9	10
2007	357,848	1,124,788	1,735,330	2,218,270	2,745,596	3,319,994	3,466,336	3,606,286	3,833,515	3,901,463
2008	352,118	1,236,139	2,170,033	3,353,322	3,799,067	4,120,063	4,647,867	4,914,039	5,339,085	
2009	290,507	1,292,306	2,218,525	3,235,179	3,985,995	4,132,918	4,628,910	4,909,315		
2010	310,608	1,418,858	2,195,047	3,757,447	4,029,929	4,381,982	4,588,268			
2011	443,160	1,136,350	2,128,333	2,897,821	3,402,672	3,873,311				
2012	396,132	1,333,217	2,180,715	2,985,752	3,691,712					
2013	440,832	1,288,463	2,419,861	3,483,130						
2014	359,480	1,421,128	2,864,498							
2015	376,686	1,363,294								
2016	344,014									

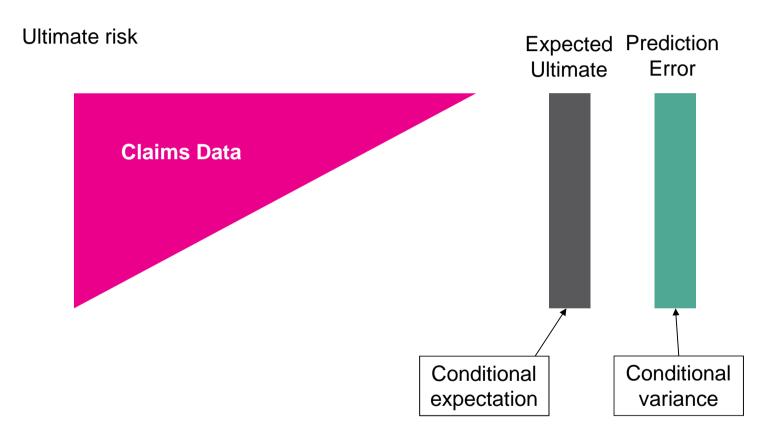
Ultimate	One-Year	Ratio
0	0	
75,535	75,535	100%
121,699	105,309	87%
133,549	79,846	60%
261,406	235,115	90%
411,010	318,427	77%
558,317	361,089	65%
875,328	629,681	72%
971,258	588,662	61%
1,363,155	1,029,925	76%
2,447,095	1,778,968	73%

Two ways of using emergence factors

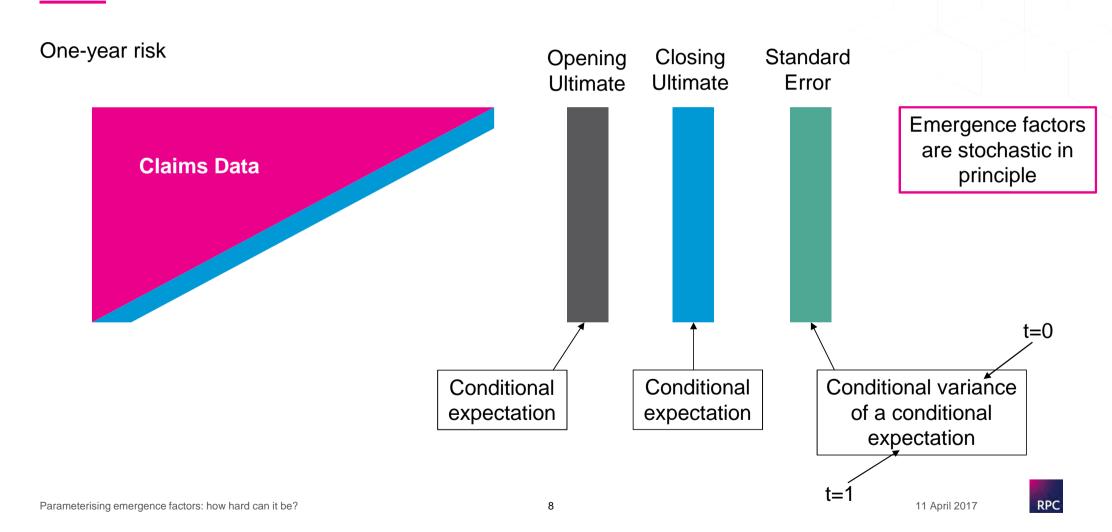




What are emergence factors, exactly? (1/2)



What are emergence factors, exactly? (2/2)



Is there a better method?

```
1 2 3 4 5 6 7 8 9 10
2007 357,848 1,124,788 1,735,330 2,218,270 2,745,596 3,319,994 3,466,336 3,606,286 3,833,515 3,901,463
2008 352,118 1,236,139 2,170,033 3,353,322 3,799,067 4,120,063 4,647,867 4,914,039 5,339,085
2009 290,507 1,292,306 2,218,525 3,235,179 3,985,995 4,132,918 4,628,910 4,909,315
2010 310,608 1,418,858 2,195,047 3,757,447 4,029,929 4,381,982 4,588,268
2011 443,160 1,136,350 2,128,333 2,897,821 3,402,672 3,873,311
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2013 440,832 1,288,463 2,419,861 3,483,130
2014 359,480 1,421,128 2,864,498
2015 376,686 1,363,294
2016 344,014
```

CDR Standard errors										
0-1	1-2	2-3	3-4	4-5	5-6	6-7	7-8	8-9	Ultimate	
0	0	0	0	0	0	0	0	0	0	
75,535	0	0	0	0	0	0	0	0	75,535	
105,309	60,996	0	0	0	0	0	0	0	121,699	
79,846	91,093	56,232	0	0	0	0	0	0	133,549	
235,115	60,577	82,068	51,474	0	0	0	0	0	261,406	
318,427	233,859	57,825	82,433	51,999	0	0	0	0	411,010	
361,089	328,989	243,412	59,162	85,998	54,343	0	0	0	558,317	
629,681	391,249	359,352	266,320	64,443	94,166	59,533	0	0	875,328	
588,662	554,574	344,763	318,493	236,576	56,543	83,645	52,965	0	971,258	
1,029,925	538,726	511,118	317,142	293,978	218,914	51,661	77,317	49,055	1,363,155	

Emergence factors from multi-year CDRs (1/2)

				CDR stand	ard errors				
0-1	1-2	2-3	3-4	4-5	5-6	6-7	7-8	8-9	Ultimate
0	0	0	0	0	0	0	0	0	0
75,535	0	0	0	0	0	0	0	0	75,535
105,309	60,996	0	0	0	0	0	0	0	121,699
79,846	91,093	56,232	0	0	0	0	0	0	133,549
235,115	60,577	82,068	51,474	0	0	0	0	0	261,406
318,427	233,859	57,825	82,433	51,999	0	0	0	0	411,010
361,089	328,989	243,412	59,162	85,998	54,343	0	0	0	558,317
629,681	391,249	359,352	266,320	64,443	94,166	59,533	0	0	875,328
588,662	554,574	344,763	318,493	236,576	56,543	83,645	52,965	0	971,258
1,029,925	538,726	511,118	317,142	293,978	218,914	51,661	77,317	49,055	1,363,155
			Cumu	lative CDR	standard (errors			
0-1	1-2	2-3	3-4	4-5	5-6	6-7	7-8	8-9	Ultimate
									0
75,535									75,535
105,309	121,699		_						121,699
79,846	121,133	133,549							133,549
235,115	242,793	256,289	261,406						261,406
318,427	395,077	399,287	407,707	411,010					411,010
361,089	488,487	545,773	548,971	555,666	558,317				558,317
629,681	741,332	823,837	865,814	868,209	873,301	875,328			875,328
588,662	808,749	879,168	935,080	964,543	966,199	969,813	971,258		971,258
1,029,925	1,162,313	1,269,729	1,308,737	1,341,348	1,359,095	1,360,076	1,362,272	1,363,155	1,363,155

Cumulate use squareroot of sum-of-squares along each origin period

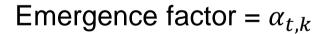
$$121,133^2 = 79,846^2 + 91,093^2$$

$$133,549^2 = 121,133^2 + 56,232^2$$

CDRs over non-overlapping periods are uncorrelated

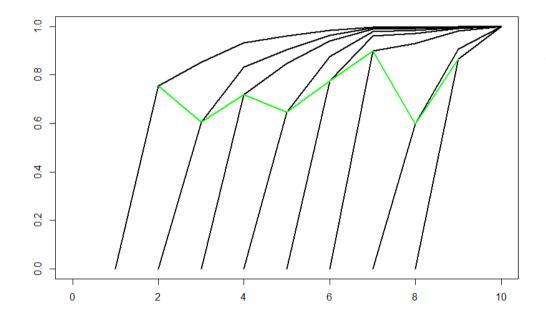
Emergence factors from multi-year CDRs (2/2)

Cumulative % CDR standard errors										
0-1	1-2	2-3	3-4	4-5	5-6	6-7	7-8	8-9		
100.0%										
86.5%	100.0%									
59.8%	90.7%	100.0%								
89.9%	92.9%	98.0%	100.0%							
77.5%	96.1%	97.1%	99.2%	100.0%						
64.7%	87.5%	97.8%	98.3%	99.5%	100.0%		_			
71.9%	84.7%	94.1%	98.9%	99.2%	99.8%	100.0%				
60.6%	83.3%	90.5%	96.3%	99.3%	99.5%	99.9%	100.0%			
75.6%	85.3%	93.1%	96.0%	98.4%	99.7%	99.8%	99.9%	100.0%		



t – prior development

k – future development

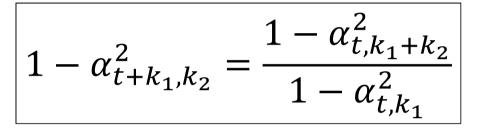


Problems to overcome

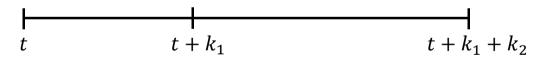
- Do different origin periods have a common emergence pattern?
- Could we assume that emergence factors are deterministic?
- Different origin periods have seen different amounts of development can the emergence factors from different origin periods be compared in a meaningful way?
- Emergence factors are ratios with this difficulty can we find an unbiased estimator for emergence factors?



Formula linking emergence factors



If emergence factors are deterministic then this equation holds



Application of formula linking emergence factors

Cumulative % CDR standard errors										
0-1	1-2	2-3	3-4	4-5	5-6	6-7	7-8	8-9		
100.0%										
86.5%	100.0%									
59.8%	90.7%	100.0%								
89.9%	92.9%	98.0%	100.0%							
77.5%	96.1%	97.1%	99.2%	100.0%						
64.7%	87.5%	97.8%	98.3%	99.5%	100.0%					
71.9%	84.7%	94.1%	98.9%	99.2%	99.8%	100.0%				
60.6%	83.3%	90.5%	96.3%	99.3%	99.5%	99.9%	100.0%			
75.6%	85.3%	93.1%	96.0%	98.4%	99.7%	99.8%	99.9%	100.0%		
			Implied or	ne-year em	ergence					
100.00/	100.00/	100.00/	100.00/	100.00/	100.00/	100.00/	100.00/	100.00/		

Implied one-year emergence										
100.0%	100.0%	100.0%	100.0%	100.0%	100.0%	100.0%	100.0%	100.0%		
86.5%	84.4%	84.5%	84.5%	84.5%	84.6%	84.7%	85.1%			
59.8%	49.1%	49.6%	50.1%	50.3%	51.0%	53.0%				
89.9%	90.1%	90.1%	90.0%	90.0%	90.0%					
77.5%	77.1%	77.2%	77.2%	77.3%						
64.7%	63.9%	64.1%	64.3%							
71.9%	71.8%	71.8%								
60.6%	60.3%									
75.6%										

Conclusions

- Emergence factors are simple to explain and calculate with
- Emergence factors can be used in different ways
- No satisfactory way of parameterising emergence factors is known
- Parameterisation is a fundamentally difficult problem
- Simplicity has been gained by packaging-up complexity into a single parameter
- Great care and judgement should be exercised if using externally parameterised emergence factors



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