

Research Overview

Olalekan Ogunmolu

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Results

Treatment Types
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Solution

3DOFControl
Adaptive NeuroControl
Neural Network Model

Treatment Plan (TP)
Optimization (BOO)

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Background

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The robustness conundrum

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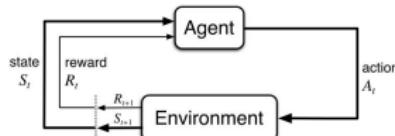
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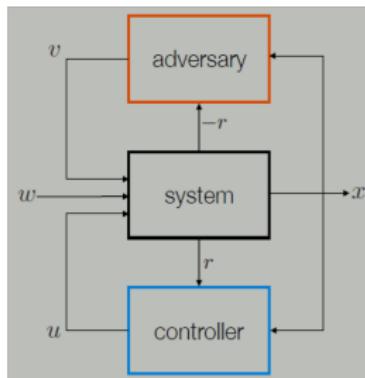
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- How to know *a priori* a policy's robustness limits?



- How to inculcate robustness into multistage decision policies?



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- To quantify the brittleness, we optimize the stage cost

$$\max_{\mathbf{v}_t \sim \psi} \left[\sum_{t=0}^T \underbrace{c(\mathbf{x}_t, \mathbf{u}_t)}_{\text{nominal}} - \gamma \underbrace{g(\mathbf{v}_t)}_{\text{adversarial}} \right]$$

- To mitigate lack of robustness, we optimize the *cost* over the control schedule U where $\mathbf{u}_t \in U$

$$\mathcal{J}_t(\mathbf{x}_t, \pi, \psi) = \min_{\mathbf{u}_t \sim \pi} \max_{\mathbf{v}_t \sim \psi} \left(\sum_{t=0}^{T-1} \ell_t(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t) + L_T(\mathbf{x}_T) \right),$$

- and seek a saddle point equilibrium policy that satisfies

$$\mathcal{J}_t(\mathbf{x}_t, \pi^*, \psi) \leq \mathcal{J}_t(\mathbf{x}_t, \pi^*, \psi^*) \leq \mathcal{J}_t(\mathbf{x}_t, \pi, \psi^*),$$

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- Suppose we have two agents interacting in an environment over an horizon T
- Let their dynamics be described as
$$\mathbf{x}_{t+1} = f_t(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t, \mathbf{w}_t), \quad t = 0, \dots, T - 1$$
 - where \mathbf{x}_t and \mathbf{u}_t are state and control variables
 - \mathbf{v}_t and \mathbf{w}_t are the respective disturbance and stochastic random variables.
 - $\mathbf{w} = \{\mathbf{w}_0, \mathbf{w}_1, \dots, \mathbf{w}_{T-1}\}$ has distribution,
 $\mathcal{P}(\mathbf{w}_t | \mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t), \quad t = 0, \dots, T - 1$.
- Furthermore, $\mathbf{u}_t \in \{\pi = \pi_0, \pi_1, \dots, \pi_T\}$,
 $\mathbf{v}_t \in \{\psi_0, \psi_1, \dots, \psi_T\}$, and $\mathbf{w}_t \in \mathcal{P}(\mathbf{w}_t | \cdot)$, $t = 0, \dots, T - 1$

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- Let a policy pair (π, ψ) is adopted, cost of a trajectory with initial condition \mathbf{x}_0 is

$$\mathcal{J}_0(\mathbf{x}_0, \pi, \psi, \mathbf{w}) = \sum_{t=0}^{T-1} \ell_t(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t) + L_T(\mathbf{x}_T) \quad (1)$$

- where $\ell_t, t = 0, \dots, T - 1$ and L_T are nonnegative instantaneous costs
- Average cost is thus

$$\mathcal{J}_0(\mathbf{x}_0, \pi, \psi) = \mathbf{E}_{\mathbf{x}_0(\mathbf{w})=\mathbf{x}_0} [\tilde{\mathcal{J}}_0(\mathbf{x}_0(\mathbf{w}), \pi, \psi, \mathbf{w})]$$

- where $\mathbf{E}_{\mathbf{x}_0(\mathbf{w})=\mathbf{x}_0}(\cdot)$ is the expectation over random variables $\mathbf{x}_1(\mathbf{w}), \dots, \mathbf{x}_T(\mathbf{w})$ having value \mathbf{x}_0 . It will sometimes be abbreviated as $\mathbf{E}_{|\mathbf{x}_t}$ for \mathbf{x}_t .

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- Define $\phi(\pi, \psi)$ as

$$\phi(\pi, \psi) = \mathbf{E}[\mathcal{J}_0(\mathbf{x}_0, \pi, \psi)] \quad (2)$$

- where \mathbf{E} has been abbreviated as $\mathbf{E}_{\mathbf{x}_0(\mathbf{w})=\mathbf{x}_0}$
so that

$$\phi(\pi, \psi) = \mathbf{E}[\tilde{\mathcal{J}}_0(\mathbf{x}_0(\mathbf{w}), \pi, \psi, \mathbf{w})] \quad (3)$$

Problem Statement

Find an admissible (saddle point equilibrium) policy pair that satisfies, $\mathcal{J}_0(\mathbf{x}_0, \pi^*, \psi) \leq \mathcal{J}_0(\mathbf{x}_0, \pi^*, \psi^*) \leq \mathcal{J}_0(\mathbf{x}_0, \pi, \psi^*), \forall \pi \in \Pi, \psi \in \Psi$ and \mathbf{x}_0 .

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- $\mathcal{J}_t(\mathbf{x}_t, \pi, \psi)$ would denote the average process cost with initial condition, \mathbf{x}_t under the policy pair, (π, ψ) , i.e.,

$$\mathcal{J}_t(\mathbf{x}_t, \pi, \psi) = \min_{\pi} \max_{\psi} \mathbf{E}_{|\mathbf{x}_t} \tilde{\mathcal{J}}_t(\mathbf{x}_t(\mathbf{w}), \pi, \psi, \mathbf{w})$$

- DP transforms the optimization over whole trajectory to a step-wise optimization over $(\mathbf{u}_t, \mathbf{v}_t)$ as

$$\mathcal{J}_t(\cdot) = \min_{\mathbf{u}_t \sim \pi} \max_{\mathbf{v}_t \sim \psi} \mathbf{E}_{|\mathbf{x}_t} \left[\sum_{t=0}^{T-1} \ell_k(\mathbf{x}_t, \pi_t(\mathbf{x}_t), \psi_t(\mathbf{x}_t)) + L(\mathbf{x}_t) \right]$$

with boundary condition $\mathcal{J}_T(\mathbf{x}_T, \pi, \psi, \mathbf{w}) = L(\mathbf{x}_T)$

Brittleness Quantification

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- Assume an agent's nominal policy, π , has been found
- Suppose that there is another agent interacting in the nominal agent's environment, so that

$$\begin{aligned} \mathbf{x}_{t+1} &= f_t(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t), \quad \mathbf{u}_t \sim \pi_t, \mathbf{v}_t \sim \psi_t \\ &:= \tilde{f}_t(\mathbf{x}_t, \mathbf{v}_t), \quad t = 0, \dots, T - 1. \end{aligned} \tag{4}$$

- We pose the stage cost as,

$$\ell_t(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t) = \max_{\mathbf{v}_t \sim \psi} \left[\sum_{t=0}^T \underbrace{c(\mathbf{x}_t, \mathbf{u}_t)}_{\text{nominal cost}} - \gamma \underbrace{g(\mathbf{v}_t)}_{\text{opponent's cost}} \right]$$

- $g_t(\cdot)$ controls the strength of the disturbing agent via the scalar term γ

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Minimax Iterative Dynamic Game

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- To mitigate lack of robustness, we optimize

$$\mathcal{J}_t(\mathbf{x}_t, \pi, \psi) = \min_{\mathbf{u}_t \sim \pi} \max_{\mathbf{v}_t \sim \psi} \left[\sum_{t=0}^{T-1} \ell_t(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t) + L_T(\mathbf{x}_T) \right]$$

- seeking a saddle point equilibrium policy that satisfies the following inequality,

$$\mathcal{J}_t(\mathbf{x}_t, \pi^*, \psi) \leq \mathcal{J}_t(\mathbf{x}_t, \pi^*, \psi^*) \leq \mathcal{J}_t(\mathbf{x}_t, \pi, \psi^*),$$

Minimax iDG: Case Study

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- Continuously solve an online trajectory optimization problem in a minimax fashion
- Essentially a meta-algorithm that is applicable to e.g. iLQG, DDP, GPS, DQN etc.
- Case study is a two-player iDG which proceeds as follows
 - approximate nonlinear system dynamics, \mathbf{x}_{t+1} , starting with a schedule of the nominal agent's local controls, $\{\bar{\mathbf{u}}_t\}$, and the opposing agent's local controls $\{\bar{\mathbf{v}}_t\}$ which are assumed to be available,

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- Case study is a two-player iDG which proceeds as follows
 - run passive dynamics with $\{\bar{\mathbf{u}}\}, \{\bar{\mathbf{v}}\}$ and generate a nominal state trajectory $\{\bar{\mathbf{x}}_t\}$, with neighboring trajectories $\{\mathbf{x}_t\}$
 - we choose a small neighborhood, $\{\delta\mathbf{x}_t\}$ of $\{\mathbf{x}_t\}$, which provides an optimal reduction in cost as the dynamics no longer represent those of $\{\mathbf{x}_t\}$
 - discretizing time, the new state and control sequence pairs become $\delta\mathbf{x}_t = \mathbf{x}_t - \bar{\mathbf{x}}_t$, $\delta\mathbf{u}_t = \mathbf{u}_t - \bar{\mathbf{u}}_t$, $\delta\mathbf{v}_t = \mathbf{v}_t - \bar{\mathbf{v}}_t$.

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- For

$$\mathcal{J}(\mathbf{x}_t, \boldsymbol{\pi}, \boldsymbol{\psi}) = \min_{\mathbf{u}_t \sim \boldsymbol{\pi}} \max_{\mathbf{v}_t \sim \boldsymbol{\psi}} [\ell(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t) + \mathcal{J}(f(\mathbf{x}_{t+1}, \mathbf{u}_{t+1}, \mathbf{v}_{t+1}))]$$

- We consider the Hamiltonian as a perturbation around $\{\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t\}$
- Cost over local neighborhood, $\{\delta\mathbf{x}_t\}$ can be approximated by a 2nd order Taylor expansion,

$$Q(\cdot) \approx \frac{1}{2} \begin{bmatrix} 1 \\ \delta\mathbf{x}_t^T \\ \delta\mathbf{u}_t^T \\ \delta\mathbf{v}_t^T \end{bmatrix}^T \begin{bmatrix} 1 & Q_{xt}^T & Q_{ut}^T & Q_{vt}^T \\ Q_{xt} & Q_{xxt} & Q_{xut} & Q_{xvt} \\ Q_{ut} & Q_{uxt} & Q_{uut} & Q_{uvt} \\ Q_{vt} & Q_{vxxt} & Q_{vut} & Q_{vvt} \end{bmatrix} \begin{bmatrix} 1 \\ \delta\mathbf{x}_t \\ \delta\mathbf{u}_t \\ \delta\mathbf{v}_t \end{bmatrix} \quad (5)$$

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■ where

$$Q_{xt} = \ell_{xt} + f_{xt}^T V_{xt+1}, \quad Q_{ut} = \ell_{ut} + f_{ut}^T V_{xt+1}$$

$$Q_{vt} = \ell_{vt} + f_{vt}^T V_{xt+1}, \quad Q_{xxt} = \ell_{xxt} + f_{xt}^T V_{xxt+1} f_{xt}$$

$$Q_{uxt} = \ell_{uxt} + f_{ut}^T V_{xxt+1} f_{xt}, \quad Q_{vxt} = \ell_{vxt} + f_{vt}^T V_{xxt+1} f_{xt}$$

$$Q_{uut} = \ell_{uut} + f_{ut}^T V_{xxt+1} f_{ut}, \quad Q_{vvt} = \ell_{vvt} + f_{vt}^T V_{xxt+1} f_{vt}$$

$$Q_{uvt} = \ell_{uvt} + f_{ut}^T V_{xxt+1} f_{vt}.$$

- it is expected that 2nd order terms will dominate the higher-order ones, consistent with linearized methods [Polycarpou and Ioannou (1992)].

Linearization of Dynamics

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- LQR approximation to dynamics becomes

$$\delta \mathbf{x}_{t+1} \approx f_{\mathbf{x}t} \delta \mathbf{x}_t + f_{\mathbf{u}t} \delta \mathbf{u}_t + f_{\mathbf{v}t} \delta \mathbf{v}_t$$
$$\ell(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t) \approx \frac{1}{2} \begin{bmatrix} 1 \\ \delta \mathbf{x}_t^T \\ \delta \mathbf{u}_t^T \\ \delta \mathbf{v}_t^T \end{bmatrix}^T \begin{bmatrix} \ell_{0t} & \ell_{\mathbf{x}t}^T & \ell_{\mathbf{u}t}^T & \ell_{\mathbf{v}t}^T \\ \ell_{\mathbf{x}t} & \ell_{\mathbf{xxt}} & \ell_{\mathbf{uxt}} & \ell_{\mathbf{vxt}} \\ \ell_{\mathbf{u}t} & \ell_{\mathbf{uxt}} & \ell_{\mathbf{uut}} & \ell_{\mathbf{uvt}} \\ \ell_{\mathbf{v}t} & \ell_{\mathbf{vxt}} & \ell_{\mathbf{vut}} & \ell_{\mathbf{vvt}} \end{bmatrix} \begin{bmatrix} 1 \\ \delta \mathbf{x}_t \\ \delta \mathbf{u}_t \\ \delta \mathbf{v}_t \end{bmatrix} \quad (6)$$

- It is easy to verify that the feedback controls are

$$\delta \mathbf{u}_t^* = -Q_{\mathbf{u}ut}^{-1} \left[Q_{\mathbf{u}t}^T + Q_{\mathbf{u}xt} \delta \mathbf{x}_t + Q_{\mathbf{u}vt} \delta \mathbf{v}_t \right], \quad (7)$$
$$\delta \mathbf{v}_t^* = -Q_{\mathbf{v}vt}^{-1} \left[Q_{\mathbf{v}t}^T + Q_{\mathbf{v}xt} \delta \mathbf{x}_t + Q_{\mathbf{v}ut} \delta \mathbf{u}_t \right].$$

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- From which we obtain the recursions,

$$\begin{aligned}\Delta V_t &= \mathbf{g}_{\mathbf{u}t} Q_{\mathbf{u}t} + \mathbf{g}_{\mathbf{v}t} Q_{\mathbf{v}t} + \mathbf{g}_{\mathbf{u}t} Q_{\mathbf{u}vt} \mathbf{g}_{\mathbf{v}t} \\ &\quad + \frac{1}{2} (\mathbf{g}_{\mathbf{u}t} Q_{\mathbf{u}ut} \mathbf{g}_{\mathbf{u}t} + \mathbf{g}_{\mathbf{v}t} Q_{\mathbf{v}vt} \mathbf{g}_{\mathbf{v}t}) \\ V_{\mathbf{x}t} &= Q_{\mathbf{x}t} + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}t} + \mathbf{G}_{\mathbf{v}t}^T Q_{\mathbf{v}t} + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}ut} \mathbf{g}_{\mathbf{u}t} + \mathbf{g}_{\mathbf{u}t} Q_{\mathbf{u}xt} \\ &\quad + \mathbf{g}_{\mathbf{v}t} Q_{\mathbf{v}xt} + \mathbf{G}_{\mathbf{v}t}^T Q_{\mathbf{v}vt} \mathbf{g}_{\mathbf{v}t} + \mathbf{G}_{\mathbf{v}t}^T Q_{\mathbf{u}vt} \mathbf{g}_{\mathbf{u}t} + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}vt} \mathbf{g}_{\mathbf{v}t} \\ V_{\mathbf{xxt}} &= \frac{1}{2} (Q_{\mathbf{xxt}} + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}ut} \mathbf{G}_{\mathbf{u}t} + \mathbf{G}_{\mathbf{v}t}^T Q_{\mathbf{v}vt} \mathbf{G}_{\mathbf{v}t}) + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}xt} \\ &\quad + \mathbf{G}_{\mathbf{v}t}^T Q_{\mathbf{v}xt} + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}vt} \mathbf{G}_{\mathbf{v}t} \end{aligned} \tag{8}$$

- NB: The gains \mathbf{g}_{it} and \mathbf{G}_{it} , $i = \mathbf{u}$ or \mathbf{v} are as defined in ([§II.B]Ogunmolu et al. (2018)).

Results: Brittleness Quantification

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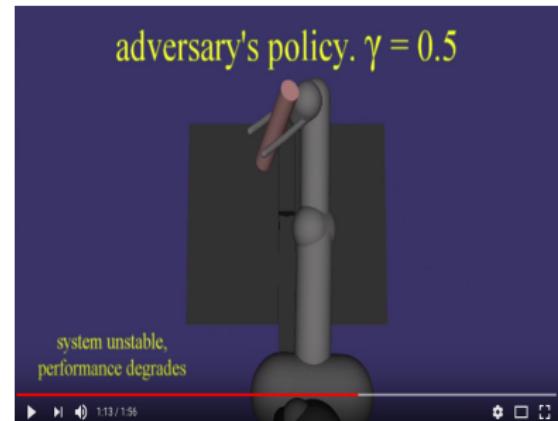
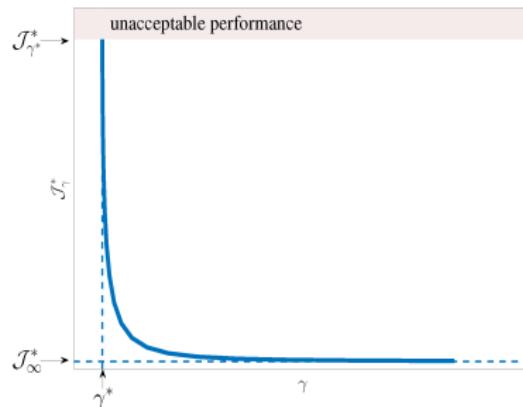
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Results: Iterative Dynamic Game

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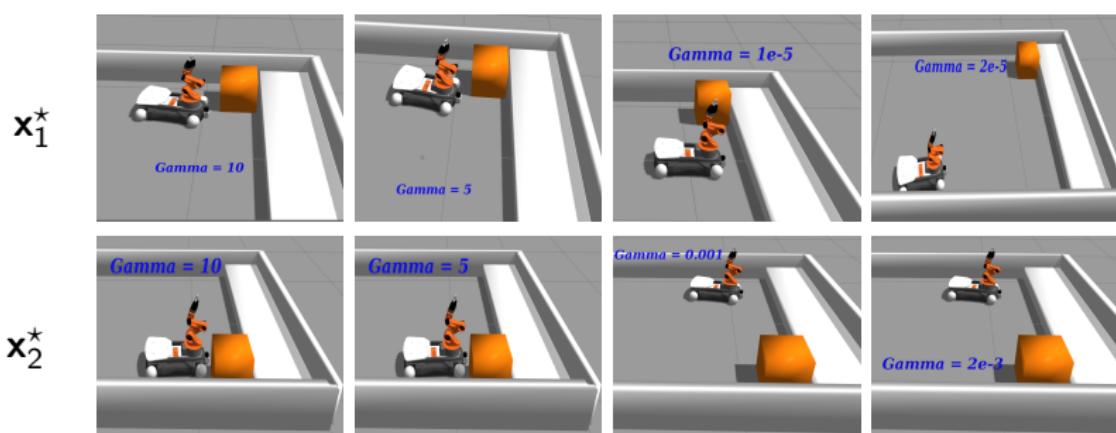
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End pose of the KUKA platform with our iDG formulation given different goal states and γ -values

Video of Results

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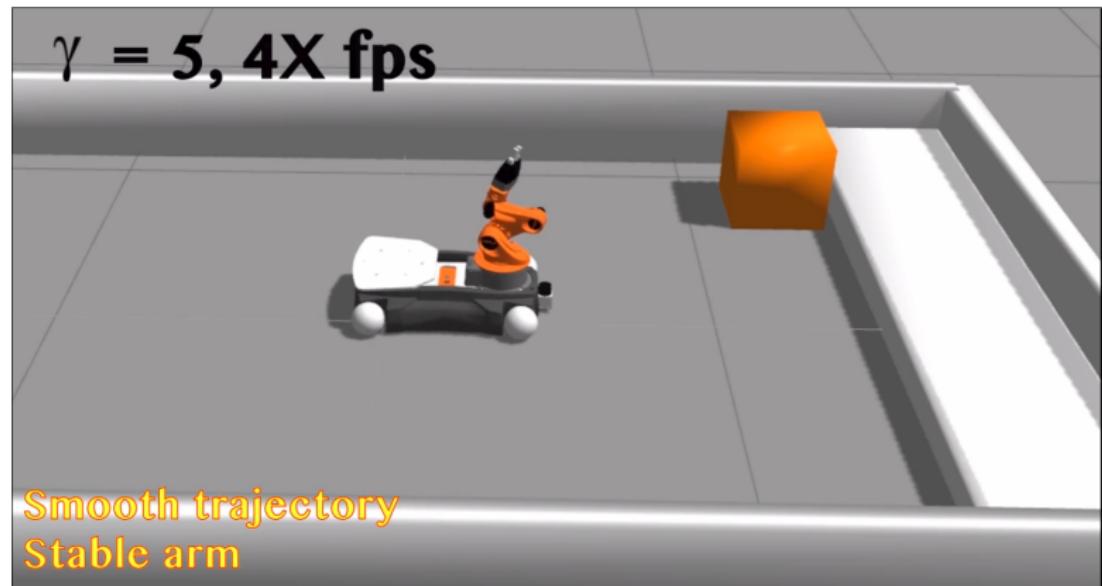
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Robotic Radiotherapy

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Treatment Options

Surgery

- Oldest technique
- Good for localized cancer cells
- Falls short of being an all-around good option



Source: National Cancer Institute

Chemotherapy

- Effective for malignant cancer cells
- Highly toxic
- Highly carcinogenic
- Kills healthy cells



Source: Cancer.gov

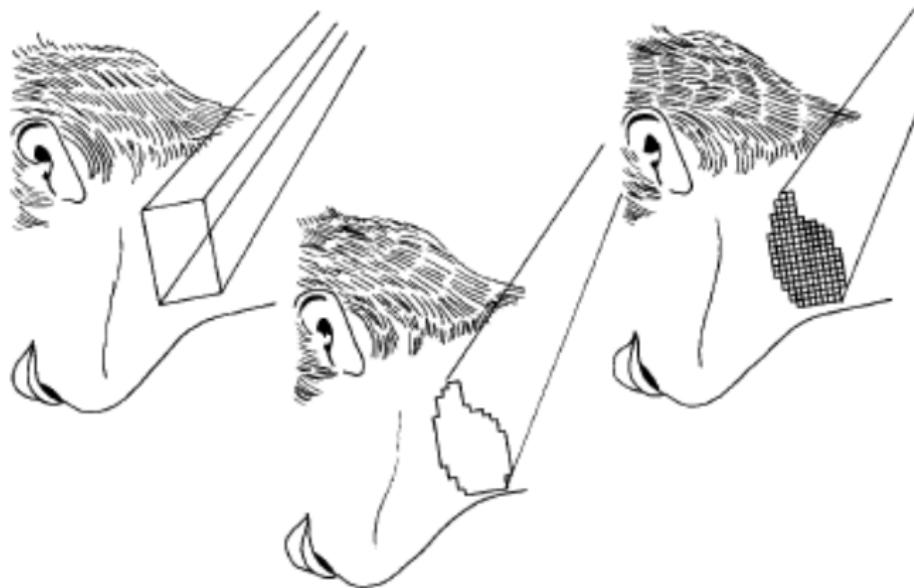
Radiosurgery

- Replaces invasive surgery
- Often used alongside surgical tumor removal
- Extremely effective in managing tumors
- Standard care in managing cancer conditions



- Radiation therapy is one of the major cancer therapy modalities
- About 2/3 of U.S. cancer patients receive radiation therapy either alone or in conjunction with surgery, chemotherapy, and immunotherapy etc.

Radiotherapy types



Left: Conventional radiotherapy.

Middle: Conformal radiotherapy (CFRT) without intensity modulation.

Right: CFRT with intensity modulation. Reprinted from Webb (2001).

Frame-based Radiotherapy Treatment

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- Fractionated radiation dose over many weeks/months



Frameless (Completely non-invasive) RT

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High-dose volumes with complex shapes [Adler and Cox (1995)]



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Image Guided Radiotherapy

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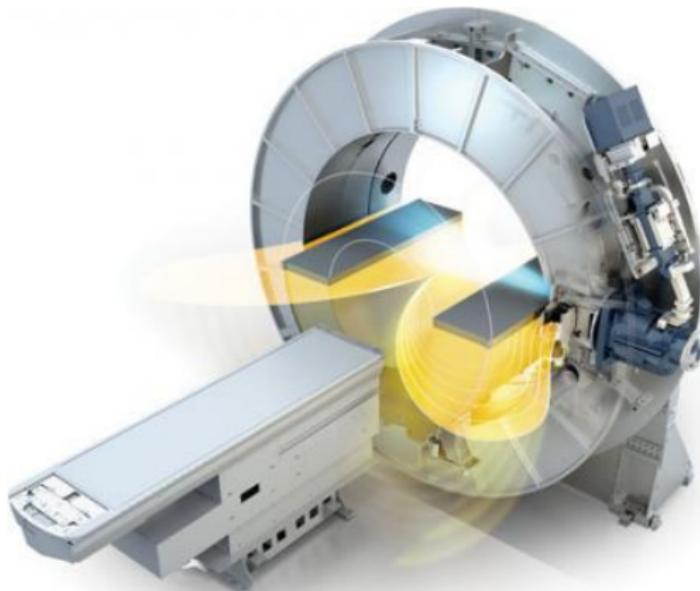
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Reprinted from Imaging Technology News

Beam Orientation Optimization

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- During treatment planning, a **beam orientation optimization problem (BOO)** is separately solved
- Radiation is delivered from $\approx (5 - 15)$ different beam orientations during IMRT
- BOO determines the best beam angle combinations for delivering radiation.
- Process of determining beamlets' intensities is termed **fluence map optimization (FMO)**

The Immobilization Problem

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NeuroControl
Neural Network
Model

Treatment
Plan (TP)
Optimization
(OO)

Cerviño et al. (2010)



Feasibility evaluation

Liu et al. (2015)



4-D robotic stage couch

Ostyn et al. (2017)



6-DoF robotic couch

Solution: Soft-Robot Position Correcting Systems

Research Overview

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Brittleness
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- Eliminate rigid frames and metallic rings
- Eliminate attenuation of X-Ray beams
- Control design
 - Feedback control + optimal regulation + robustness to disturbance ✓

Vision-based 3-DOF Control

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Simulation Testbed

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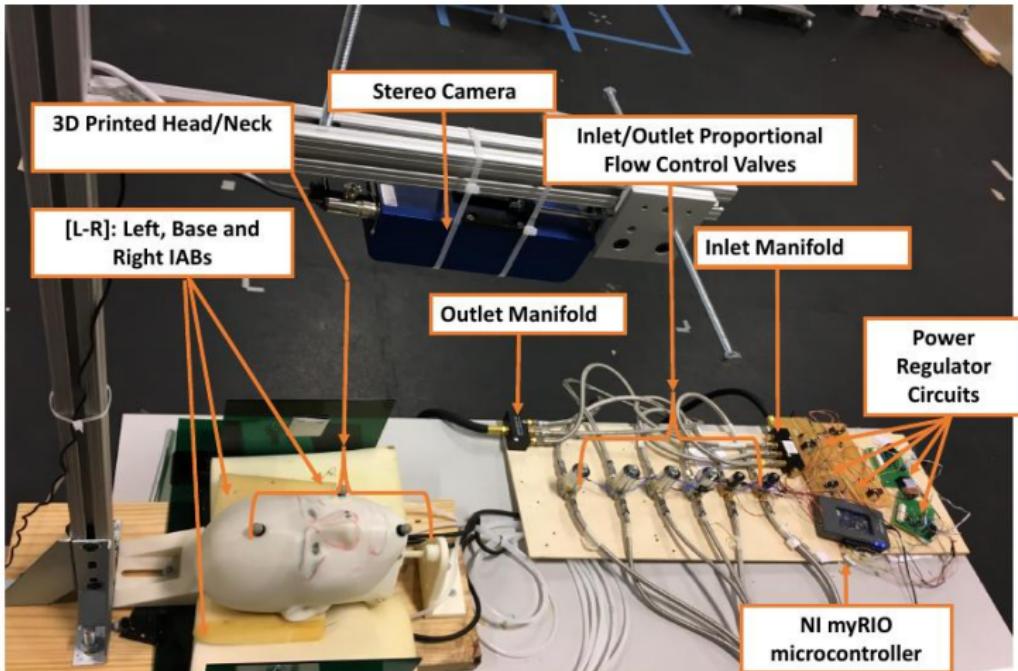
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Hardware Description

Control Proposals

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- Solve a state feedback and feedforward regulation problem
- An adaptation model based on past states and controls:
 - $Z^N = \{u(k), u(k-1), \dots, u(k-n_u), y(k), \dots, y(k-n_y)\}$
 - Let a persistently exciting input signal $u_{\text{ex}} \in L_2 \cap L_\infty$ excite the system's nonlinear modes
- Design Goal:
 - Stabilize states, $\mathbf{y} = [z, \theta, \phi]^T$

Model Reference Adaptive Control

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- Model head and bladder dynamics as
 - $\dot{\mathbf{y}} = \mathbf{A}\mathbf{y} + \mathbf{B}\Lambda(\mathbf{u} - f(\mathbf{y}, \mathbf{u})) + \mathbf{w}(k)$
 - \mathbf{A}, Λ unknown, \mathbf{B} , $\text{sgn}\Lambda$ known
 - $f(\mathbf{y}, \mathbf{u}) \triangleq$ nonlinear function to be adapted for
 - $\mathbf{x} \triangleq$ tuple containing past controls and current outputs
- Approximate $f(\mathbf{y}, \mathbf{u})$ by a neural network with continuous memory states
 - $\hat{f}(\mathbf{y}(k), \mathbf{u}(k-d))$ is realized with a *long-short term memory* cell (Horchreiter and Schmidhuber, '91, '97)
 - **purpose:** remember good adaptation gains

Assumptions

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- A dynamic RNN with N neurons, $\varphi(\mathbf{x})$, exists
 - maps from a compact input space $\mathbf{u} \subset \mathbb{U}$ to $\mathbf{y} \subset \mathbb{Y}$ on the Lebesgue integrable functions within $[0, T]$ or $[0, \infty)$
- $f(\mathbf{y}, \mathbf{u})$ is exactly $\Theta^T \Phi(\mathbf{y})$
 - f has coefficients $\Theta \in \mathbb{R}^{N \times m}$ and a Lipschitz-continuous vector of basis functions $\Phi(\mathbf{y}) \in \mathbb{R}^N$
- Inside a ball \mathbf{Y}_R with known, finite radius R ,
 - an ideal neural network (NN) approximation $f(\mathbf{y}) : \mathbb{R}^n \rightarrow \mathbb{R}^m$, is realized to a sufficient degree of accuracy, $\varepsilon_f > 0$;
- Outside \mathbf{Y}_R ,
 - the NN approximation error can be upper-bounded by a known unbounded, scalar function $\varepsilon_{max}(\mathbf{y})$;
 - $\|\varepsilon(\mathbf{y})\| \leq \varepsilon_{max}(\mathbf{y}), \quad \forall \mathbf{y} \in \mathbf{Y}_R$;
- There exists an exponentially stable reference model
 - $\dot{\mathbf{y}}_m = \mathbf{A}_m \mathbf{y}_m + \mathbf{B}_m \mathbf{r}$

Adaptive Neuro-Control Scheme

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- Set control law in terms of parameter estimates from the neural network weights and Lipschitz basis functions
 - $\Phi(\mathbf{y}) = \{\mathbf{y}(k-d), \dots, \mathbf{y}(k-d-4), \mathbf{u}(k-d) \dots \mathbf{u}(k-d-5)\}$
 - i.e. network looks back in time by 5 time steps at every instant, and then makes a prediction
- Derive adaptive adjustment mechanism from Lyapunov analysis for Adaptive Control (Parks, P., 1966)
- $\mathbf{u} = \underbrace{\hat{\mathbf{K}}_y^T \mathbf{y}}_{\text{state feedback}} + \underbrace{\hat{\mathbf{K}}_r^T \mathbf{r}}_{\text{optimal regulator}} + \underbrace{\hat{f}(\mathbf{y}, \mathbf{u})}_{\text{approximator}}$

Controller formulation

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- $\hat{\mathbf{K}}_y$ and $\hat{\mathbf{K}}_r$ are adaptive gains to be designed

Term Contributions

- $\hat{\mathbf{K}}_y^T \mathbf{y}$ term keeps the states of the approximation set $\mathbf{y} \in \mathbf{B}_R$ stable,
- $\hat{\mathbf{K}}_r^T \mathbf{r}$ term causes the states to follow a given reference trajectory
- Function approximator $\hat{f}(\mathbf{y}, \mathbf{u})$ ensures states that start outside the approximation set $\mathbf{y} \in \mathbf{B}_R$ converge to \mathbf{B}_R in finite time

Adaptive Control Formulation

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- Assume model matching conditions
 - such that $\hat{\mathbf{K}}_y = \mathbf{K}_y$, and $\hat{\mathbf{K}}_r = \mathbf{K}_r$ (ideally)
- Realize the approximator as $\hat{f}(\mathbf{y}) = \hat{\Theta}^T \Phi(\mathbf{y}) + \varepsilon_f(\mathbf{y})$
 - $\hat{\Theta}^T$ denotes the vectorized weights of the neural network
 - $\Phi(\mathbf{y})$ denotes the vector of lagged inputs and output,
 - $\varepsilon_f(\mathbf{y})$ is the approximation error.
 - $\Phi(\mathbf{y}) = \{\mathbf{y}(k-d) \cdots \mathbf{y}(k-d-4), \mathbf{u}(k-d) \cdots \mathbf{u}(k-d-5)\}$

Neural Network Model

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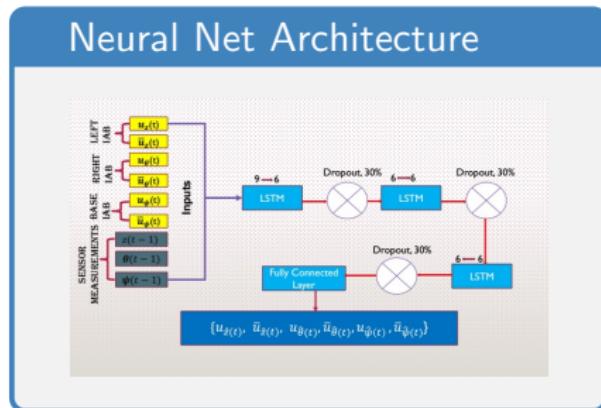
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- input: lagged vector of past observations and current control actions
- repeat $\times 3$
 - pass input through an lstm cell
 - followed by 30% dropout
- output will be control predictions directly fed as valve voltages

Lyapunov Redesign

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■ Theorem:

- Given correct choice of adaptive gains $\hat{\mathbf{K}}_y$ and $\hat{\mathbf{K}}_r$, the error state vector, $\mathbf{e}(k)$ with closed loop time derivative $\dot{\mathbf{e}}$, is **uniformly ultimately bounded**, and the state \mathbf{y} will converge to a neighborhood of \mathbf{r} .
- Please see proof in Appendix(§6).

Stability Results

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We find that

$$\begin{aligned}\dot{\mathbf{V}}(\cdot) &= -\mathbf{e}^T \mathbf{Q} \mathbf{e} - 2\mathbf{e}^T \mathbf{P} \mathbf{B} \boldsymbol{\Lambda} \boldsymbol{\varepsilon}_f \\ &\leq -\lambda_{low} \|\mathbf{e}\|^2 + 2\|\mathbf{e}\| \|\mathbf{P} \mathbf{B}\| \lambda_{high}(\boldsymbol{\Lambda}) \boldsymbol{\varepsilon}_{max}\end{aligned}$$

- $\lambda_{low}, \lambda_{high} \equiv$ minimum and maximum eigenvalues of \mathbf{Q} and $\boldsymbol{\Lambda}$ respectively.
- $\dot{\mathbf{V}}(\cdot)$ is thus negative definite outside the compact set
- $\chi = \left(\mathbf{e} : \|\mathbf{e}\| \leq \frac{2\|\mathbf{P} \mathbf{B}\| \lambda_{high}(\boldsymbol{\Lambda}) \boldsymbol{\varepsilon}_{max}(\mathbf{y})}{\lambda_{low}(\mathbf{Q})} \right)$
- thus, we conclude that the error \mathbf{e} is uniformly ultimately bounded.
 - i.e. $\mathbf{y}(t) \rightarrow 0$ as $t \rightarrow \infty$

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- Solving the general form of the Lyapunov equation, we have

$$\mathbf{P} = \begin{bmatrix} -\frac{170500}{2668} & 0 & 0 \\ 0 & -\frac{170500}{2668} & 0 \\ 0 & 0 & -\frac{170500}{2668} \end{bmatrix}$$

- Solenoid valves operate in pairs

- set

$$\mathbf{B} = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 \end{bmatrix}$$

- \mathbf{B} maps to the 3-axes controllers

$$[u_z \quad u_\theta \quad u_\psi]^T$$

- non-zero terms are the max. duty-cycle to valves

Results

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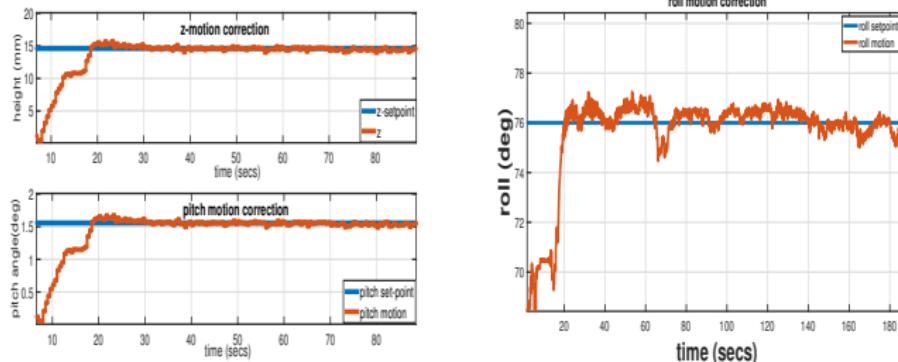
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[Left]: Goal command: $(z, \theta, \phi) = (2.5\text{mm}, 0.25^\circ, 35^\circ)$ to $(14\text{mm}, 1.6^\circ, 45^\circ)^T$. [Right]: Head roll tracking.

Treatment Plan (TP) Optimization

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IMRT TP Overview

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- IMRT delivers geometrically-shaped, high-precision photons to tumors in a beam orientation optimization (BOO) process.
- The **BOO problem** aims to find the right beam angle combinations from which to deliver radiation intensities.
 - essentially a combinatorial optimization problem
 - traditional methods fail at real-time feasible results¹.
- Afterwards, the intensity of the fluence is modulated in a **fluence map optimization** (FMO) process.

¹Current approaches take too long, and are often not optimal.



IMRT Treatment Plan Flowchart

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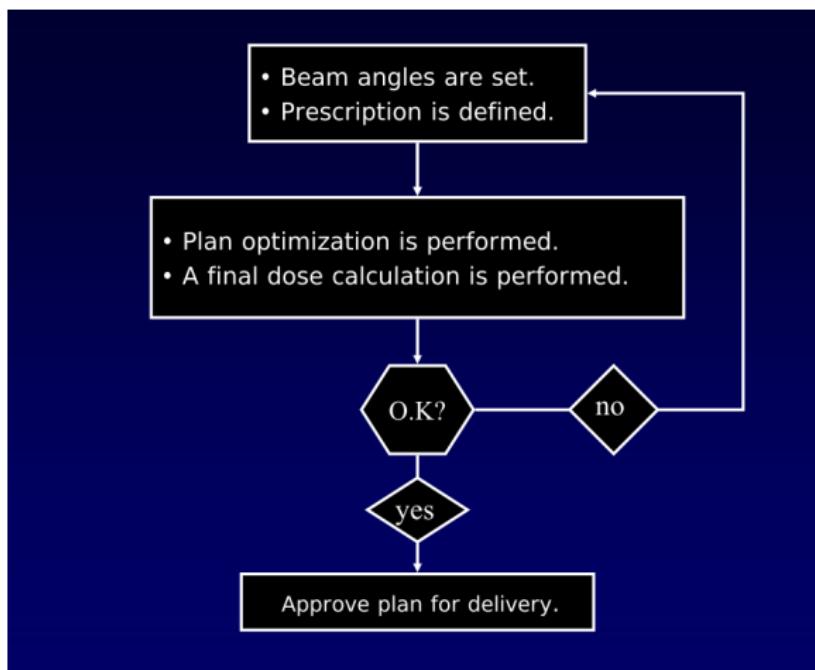
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Reprinted from "IMRT Optimization Algorithms. David Shepard. Swedish Cancer Institute. AAPM 2007."

Problem Setup

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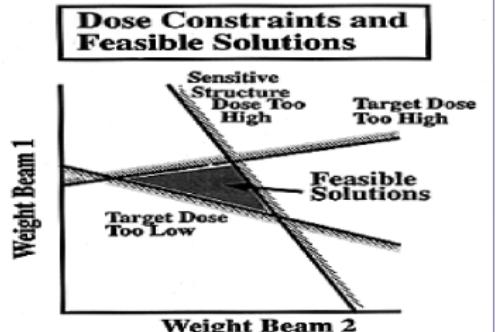
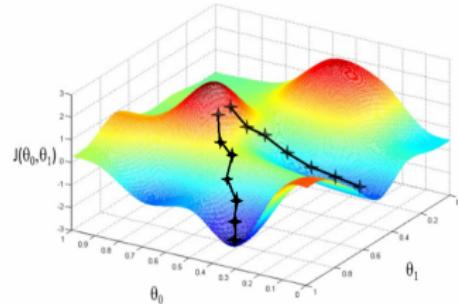
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- Given biological statement of prescriptions
 - find a numerical objective function
 - accompanied by constraints
- Challenge
 - a scalar-valued objective function usually not sufficient



Courtesy of David Shepard

Common Problem Formulation

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- Maximize weighted least square dose from for PTVs
 - Minimize weighted least square dose for OARs
 - DVH-based goal treatments
-
- Current Approaches and Limitations
 - Stochastic optimization approaches: simulated annealing; genetic algorithms and gradient search, or a combination of genetic and gradient search algorithms
 - Mixed-integer programming, branch and cut/bound algorithms, beam angle elimination algorithms
 - Commercial planners use some highly non-convex objective (actual function is proprietary and unknown to public).
 - General weakness: Feasible solution takes too long to find.

Our approach

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- Automate the **beam search** problem
- **Ultimate goal** is real-time beam angle prediction given a target volume
- Drawing ideas from
 - **pattern recognition;**
 - **monte carlo evaluations;**
 - **game simulations;** and
 - **approximate dynamic programming**

What we do

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- Formulate BOO problem into a large game planning strategy
- Neural fictitious self-play [Heinrich et al. (2015)], to refine policy predictions
 - **purpose:** drive policy weights to a **saddle equilibrium**
- a deep neural network models the nonlinear dynamical system (patient's geometry, robot-linac setup)
 - generating a policy that guides MCTS simulations for two players in a zero-sum Markov game

What we do

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- In each episodic markov decision process (MDP) setting, an MCTS lookout strategy guides transition from one beam angle set to another
- Each player in a two-player Markov game finds a best response strategy to their opponent's average strategy
 - driving the policy weights toward an approximate **saddle equilibrium** Heinrich et al. (2015).

Problem Setup

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- Let state of the dynamical system be $s \in \mathcal{S}$
- To be controlled by a discrete action $a \in \mathcal{A}$
- States evolve according to an (unknown) dynamics $p(s_{t+1}|s_t, a_t)$ (to be learned)
- Beam angle combination search task defined by a reward function, $R_t = \sum_{t=1}^N \gamma^{t-1} r(s_t, a_t)$
 - Can be found by recovering a policy, $p(a_t|s_t; \psi)$
- From now on, we will write $p(a_t|s_t; \psi)$ as $\pi_\psi(a_t|s_t)$.

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- Suppose the first player is p_1 , and the second player is p_2
- p_1 chooses its action under a (stochastic) strategy,
 $\pi^{p_1} = \{\pi_0^{p_1}, \pi_1^{p_1}, \dots, \pi_T^{p_1}\} \subseteq \Pi^{p_1}$
 - minimizing the game's outcome ζ
- p_2 's actions are governed by a policy
 $\pi^{p_2} = \{\pi_0^{p_2}, \pi_1^{p_2}, \dots, \pi_T^{p_2}\} \subseteq \Pi^{p_2}$
 - p_2 seeks to maximize ζ in order to guarantee an equilibrium solution for a game without saddle point.
- Π^{p_i} is the set of all possible nonstationary markovian policies

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- Each player bases its decision on a random event's outcome
 - generating a **mixed strategy** determined by **averaging the outcome** of individual plays.
- Both players constitute a two-player **stochastic action selection strategy**, $\pi(s, a) = Pr(a|s) := \{\pi^{P_1}, \pi^{P_2}\}$ that gives the probability of selecting moves in any given state
- Suppose the game simulation starts from an initial condition s_0 .

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- One may write the optimal **reward-to-go** value function for state s in stage t , with horizon length T as

$$V_t^*(s) = \inf_{\pi^{P_1} \in \Pi^{P_1}} \sup_{\pi^{P_2} \in \Pi^{P_2}} \mathbb{E} \left[\sum_{i=t}^{T-1} V_t(s_i, f(s_i, \pi^{P_1}, \pi^{P_2})) \right],$$
$$s \in S, t = 0, \dots, H-1$$

- where the terminal value $V_T^*(s) = 0, \forall s \in S$;
- $f(\cdot)$ represents the unknown system dynamics
- π^{P_1} and π^{P_2} contain the action/control sequences $\{a_t^{P_1}\}_{0 \leq t \leq T}$ and $\{a_t^{P_2}\}_{0 \leq t \leq T}$

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- The **saddle point strategies** for an optimal control sequence pair $\{a_t^{p_1^*}, a_t^{p_2^*}\}$ can be recursively obtained by optimizing a state-action value cost, $\mathcal{J}_t(s, a)$

$$V_t^*(s) = V_t^*(s_t, \pi_t^{p_1}, \pi_t^{p_2}) = \min_{\pi^{p_1} \in \Pi^{p_1}} \max_{\pi^{p_2} \in \Pi^{p_2}} V_t^*(s_t, \pi^{p_1}, \pi^{p_2})$$
$$\forall s_t \in \mathcal{S}, \pi^{p_1} \in \Pi^{p_1}, \pi^{p_2} \in \Pi^{p_2}.$$

such that

$$V_{p_1}^* \leq V^* \leq V_{p_2}^* \quad \forall \{\pi_t^{p_1}, \pi_t^{p_2}\}_{0 \leq t \leq T}.$$

where $V_{p_i}^*$ are the respective optimal values for each player.

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- Under ideal conditions, we'd like to find the optimal value function under perfect play
- **Caveat:** BOO exhibits Bellman's curse of dimensionality.
- What to do?
 - derive an **approximately optimal** value $V_\psi^*(s)$
 - by continually estimating the value function $v_\psi^P(s)$ using e.g. a policy parameterized by a large function approximator

State Representation

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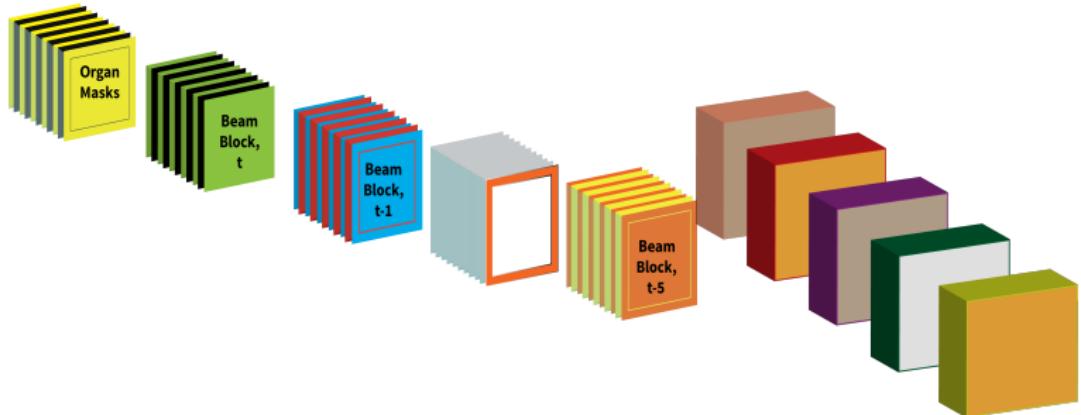
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[Left]: Concatenation of the target volume masks and the beam angles before feeding the input planes to the residual tower neural network.

[Right]: Each beam angle in a beam block is represented as shown.

Methods: Search

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- Formulated as a bandit search that imposes a regret term on the Q -value
- During the planning process, we estimate a *value*, $v(\mathbf{y}_t)$, that estimates the optimality of a beam block;
- In parallel, we refine the deep neural network policy by optimizing its weight in a separate thread.
 - Network parameters updated by a **mixed strategy** which combines its **pure strategy**,
 - It is a best response to the fictitious opponent's **average pure strategy**.

Methods: Search

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- Q -value defined as

$$\bar{Q}(s, a) = Q_j(s, a) + c \sqrt{\frac{2 \ln n(s)}{N(s, a)}}, \quad (9)$$

$$a^* = \arg \max_a \bar{Q}(s, a) \quad (10)$$

Fluence Map Optimization

- Suppose \mathcal{X} is the total discretized of voxels of interest (VOI's) in a target volume
- Let $\mathcal{B}_1 \cup \mathcal{B}_2 \cup \dots \cup \mathcal{B}_n \subseteq \mathcal{B}$ represents the partition subset of a beam \mathcal{B} ,

Methods: Fluence Map Optimization

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- Suppose further that $\mathcal{D}_{ij}(\theta_k)$ is the matrix that describes each dose influence, d_i
 - delivered to a discretized voxel, i , in a volume of interest, VOI_h ($h = 1, \dots, \mathcal{X}$), from a beam angle, θ_k ,
 $k \in \{1, \dots, n\}$
- We compute the matrix $\mathcal{D}_{ij}(\theta_k)$ by calculating each d_i for every bixel, j , at every φ° , resolution, where $j \in \mathcal{B}_k$

Methods: FMO problem definition

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- The pre-calculated dose term is given by

$$\mathbf{Ax} = \left\{ \sum_s \frac{w_s}{v_s} \mathcal{D}_{ij}^s \mathbf{x}_s \mid \mathcal{D}_{ij} \in \mathbb{R}^{n \times l}, n > l \right\}$$

- Let $w_s = \{\underline{w}_s, \bar{w}_s\}$ be the respective underdosing and overdosing weights for the OARs and PTVs
- We propose the following cost

$$\frac{1}{w_s} \sum_{s \in \text{OARs}} \|(\mathbf{b}_s - \underline{w}_s \mathcal{D}_{ij}^s \mathbf{x}_s)_+\|_2^2 + \frac{1}{v_s} \sum_{s \in \text{PTVs}} \|(\bar{w}_s \mathcal{D}_{ij}^s \mathbf{x}_s - \mathbf{b}_s)_+\|_2^2 \quad (11)$$

Methods: FMO

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- Rewriting the objective, subject to nonnegative pixel intensity constraints, we have the minimization problem

$$\min \frac{1}{2} \|Ax - b\|_2^2 \quad \text{subject to } x \geq 0.$$

- The Lagrangian becomes

$$L(x, \lambda) = \min \frac{1}{2} \|Ax - b\|_2^2 - \lambda^T x.$$

- Since we are solving a large scale problem, we use the ADMM algorithm
- Introducing an auxiliary variable z , we have

$$\min_x \frac{1}{2} \|Ax - b\|_2^2, \quad \text{subject to } z = x, \quad z \geq 0,$$

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- Solving either the \mathbf{x} and \mathbf{z} sub-problems, we have

$$\mathbf{x}^{k+1} = (\mathbf{A}^T \mathbf{A} + \rho \mathbf{I})^{-1} (\mathbf{A}^T \mathbf{b} + \rho \mathbf{z}^k - \boldsymbol{\lambda}^k). \quad (12)$$

- And using the soft-thresholding operator, $S_{\boldsymbol{\lambda}/\rho}$, we find that

$$\mathbf{z}^{k+1} = S_{\boldsymbol{\lambda}/\rho} (\mathbf{x}^{k+1} + \boldsymbol{\lambda}^k), \quad (13)$$

where $S_{\boldsymbol{\lambda}/\rho}(\tau) = (\mathbf{x} - \boldsymbol{\lambda}/\rho)_+ - (-\tau - \boldsymbol{\lambda}/\rho)_+$. $\boldsymbol{\lambda}$ is updated as

$$\boldsymbol{\lambda}^{k+1} = \boldsymbol{\lambda}^k - \gamma (\mathbf{z}^{k+1} - \mathbf{x}^{k+1}), \quad (14)$$

where γ is a parameter that controls the step length.

Game Tree Simulation

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- For b^d possible move sequences for a robot-patient setup
 - $b =$ beam angles chosen to construct a fluence
 - $d =$ is the total number of discretized angles.
- Suppose $b = 180$ and $d = 5$, we have 180^5 possible search directions
- Exhaustive search becomes real-time infeasible.

Game Tree Simulation; Approach

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- Simulate a game of **perfect recall**
 - a sequential simulation of different beam angle combinations g
 - guided by probabilities obtained from a two-player zero-sum game of neural FSP
- the probability distribution is over the possible beam angle subsets, θ^j , in the beam angle space, , Θ
- This strongly discourages classical beam s approaches

Game Tree Simulation

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- Network roll-out policy then efficiently guides the tree's game, Γ toward a *best-first* set of beam angle candidates
- Best-first leaf node encountered is the child node with the highest reward in the tree
- Essentially, a sampling-based lookout algorithm
 - Focuses learning on regions of the state space that are likely to have a good fluence

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Example Target Volumes

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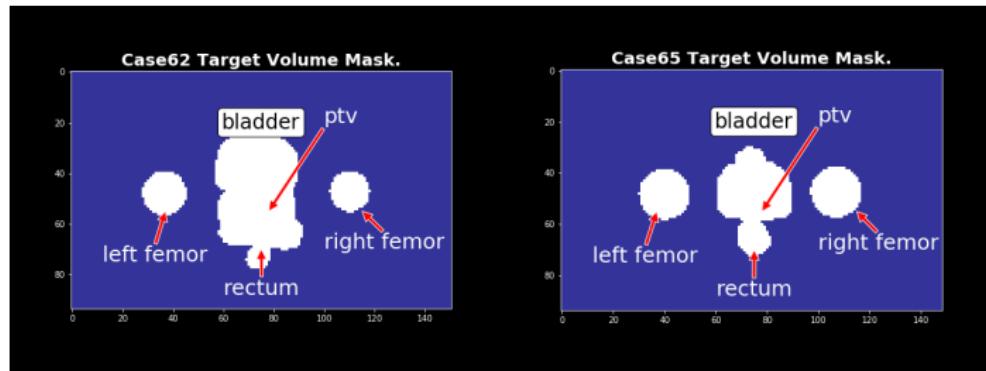
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Example Target Volumes. The PTV is engulfed within the bladder in all cases.

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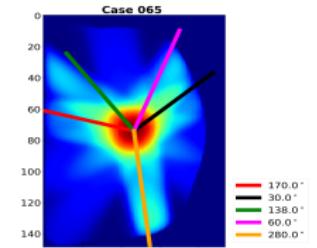
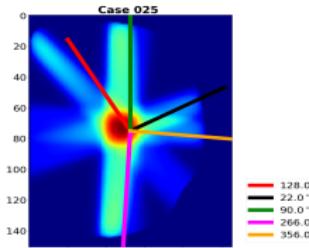
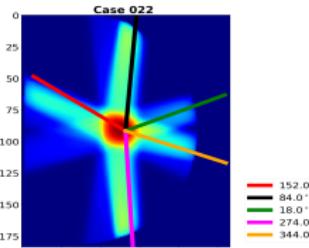
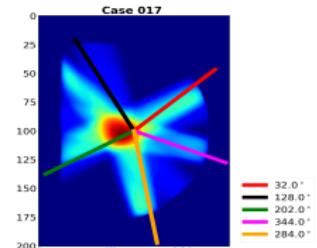
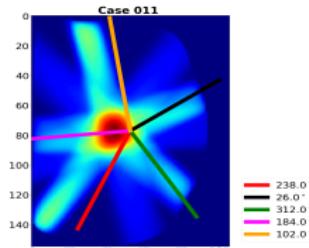
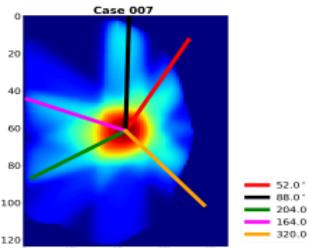
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Dose washes for select patients during training of the self-play network

Training Regime



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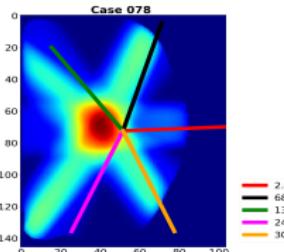
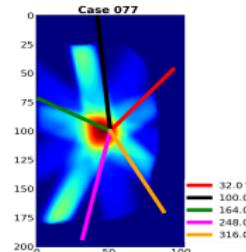
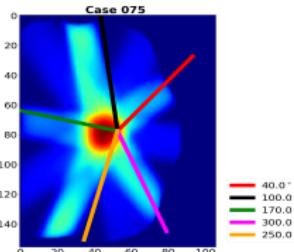
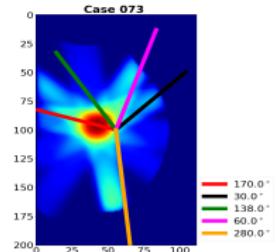
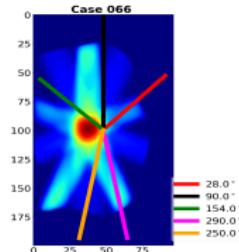
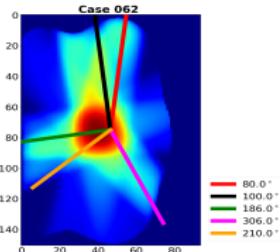
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Inference Regime



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Future Work: IMRT Immobilization

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- Adopt best practices from one of the SOTA modeling approaches viz
 - *finite element methods* [Coevoet et al. (2017); Bern et al. (2017)],
 - *constant curvature approach* [Godage et al. (2016)],
 - the *continuous Cosserat approach* [Renda et al. (2014)], and
 - the *multi-body hyper-redundant model* [Kang et al. (2012)].

Future Work

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- Robust Stabilization via inverse optimality
 - Currently working on imbibing Lyapunov stability into traditional optimal controllers
 - Build on Freeman and Kokotovic's point-wise min-norm robust control lyapunov function to realize a meaningful value function (Int. Journal of Optimal Control, 1996)
 - Simplify algorithm for real-time control
 - Carry out numerical and experimental verification and validation
 - Important in multistage decision policies, reinforcement learning controllers

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Appendix: 3-DOF Lyapunov Stability Proof

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■ Proof:

- Choose a Lyapunov function candidate \mathbf{V} in terms of the generalized error state space \mathbf{e} , gains, $\tilde{\mathbf{K}}_y^T$, $\tilde{\mathbf{K}}_r^T$, and parameter error $\varepsilon_f(\mathbf{y}(k))$ space

$$\begin{aligned}\mathbf{V}(\mathbf{e}, \tilde{\mathbf{K}}_y, \tilde{\mathbf{K}}_r^T) = & \mathbf{e}^T \mathbf{P} \mathbf{e} + \text{tr}(\tilde{\mathbf{K}}_y^T \Gamma_y^{-1} \tilde{\mathbf{K}}_y^T | \Lambda |) \\ & + \text{tr}(\tilde{\mathbf{K}}_r^T \Gamma_r^{-1} \tilde{\mathbf{K}}_r^T | \Lambda |)\end{aligned}\quad (15)$$

Appendix: Stability proof

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$$\dot{V}(\mathbf{e}, \tilde{\mathbf{K}}_y, \tilde{\mathbf{K}}_r) = \dot{\mathbf{e}}^T \mathbf{P} \mathbf{e} + \mathbf{e}^T \mathbf{P} \dot{\mathbf{e}} + 2\mathbf{tr}(\tilde{\mathbf{K}}_y^T \Gamma_y^{-1} \dot{\hat{\mathbf{K}}}_y | \Lambda |) \\ + 2\mathbf{tr}(\tilde{\mathbf{K}}_r^T \Gamma_r^{-1} \dot{\hat{\mathbf{K}}}_r | \Lambda |)$$

$$= \left[\mathbf{A}_m \mathbf{e} + \mathbf{B} \Lambda [\Delta \hat{\mathbf{K}}_r^T \mathbf{r} + \Delta \hat{\mathbf{K}}_x^T \mathbf{x}] \right]^T \mathbf{P} \mathbf{e} + \dots \\ \mathbf{e}^T \mathbf{P} \left[\mathbf{A}_m \mathbf{e} + \mathbf{B} \Lambda [\Delta \hat{\mathbf{K}}_r^T \mathbf{r} + \Delta \hat{\mathbf{K}}_x^T \mathbf{x}] \right] + \dots \\ 2\mathbf{tr}(\Delta \mathbf{K}_x^T \Gamma_x^{-1} \dot{\hat{\mathbf{K}}}_x | \Lambda |) + 2\mathbf{tr}(\Delta \mathbf{K}_r^T \Gamma_r^{-1} \dot{\hat{\mathbf{K}}}_r | \Lambda |)$$

Appendix: Stability Analysis

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$$= \mathbf{e}^T (\mathbf{P} \mathbf{A}_m + \mathbf{A}_m^T \mathbf{P}) \mathbf{e} + 2\mathbf{e}^T \mathbf{P} \mathbf{B} \Lambda \left(\tilde{\mathbf{K}}_y^T \mathbf{y} + \tilde{\mathbf{K}}_r^T \mathbf{r} \right) \\ + 2\mathbf{tr} \left(\tilde{\mathbf{K}}_y^T \Gamma_y^{-1} \dot{\tilde{\mathbf{K}}}_y |\Lambda| \right) + 2\mathbf{tr} \left(\tilde{\mathbf{K}}_r^T \Gamma_r^{-1} \dot{\tilde{\mathbf{K}}}_r |\Lambda| \right)$$

$$= -\mathbf{e}^T \mathbf{Q} \mathbf{e} - 2\mathbf{e}^T \mathbf{P} \mathbf{B} \Lambda \varepsilon_f(\mathbf{y}) + 2\mathbf{e}^T \mathbf{P} \mathbf{B} \Lambda \tilde{\mathbf{K}}_y^T \mathbf{y} \\ + 2\mathbf{tr} \left(\tilde{\mathbf{K}}_y^T \Gamma_y^{-1} \dot{\tilde{\mathbf{K}}}_y \right) + 2\mathbf{e}^T \mathbf{P} \mathbf{B} \Lambda \tilde{\mathbf{K}}_r^T \mathbf{r} + 2\mathbf{tr} \left(\Delta \mathbf{K}_r^T \Gamma_r^{-1} \dot{\tilde{\mathbf{K}}}_r \right)$$

Notice $x^T y = \mathbf{tr} (y x^T)$ from trace identity

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Therefore,

$$\begin{aligned}\dot{\mathbf{V}}(\cdot) = & -\mathbf{e}^T \mathbf{Q} \mathbf{e} - 2\mathbf{e}^T \mathbf{P} \mathbf{B} \Lambda \varepsilon_f \\ & + 2 \mathbf{tr} \left(\tilde{\mathbf{K}}_y^T (\Gamma_y^{-1} \dot{\tilde{\mathbf{K}}}_y + \mathbf{y} \mathbf{e}^T \mathbf{P} \mathbf{B} \text{sgn}(\Lambda)) \right) |\Lambda| \\ & + 2 \mathbf{tr} \left(\tilde{\mathbf{K}}_r^T (\Gamma_r^{-1} \dot{\tilde{\mathbf{K}}}_r + \mathbf{r} \mathbf{e}^T \mathbf{P} \mathbf{B} \text{sgn}(\Lambda)) \right) |\Lambda|\end{aligned}$$

where for a real-valued x , we have $x = \text{sgn}(x)|x|$.

- first two terms will be negative definite for all $\mathbf{e} \neq 0$
 - since \mathbf{A}_m is Hurwitz
- other terms will be identically null if we choose the adaptation laws

$$\dot{\tilde{\mathbf{K}}}_y = -\Gamma_y \mathbf{y} \mathbf{e}^T \mathbf{P} \mathbf{B} \text{sgn}(\Lambda), \quad \dot{\tilde{\mathbf{K}}}_r = -\Gamma_r \mathbf{r} \mathbf{e}^T \mathbf{P} \mathbf{B} \text{sgn}(\Lambda)$$

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We find that

$$\begin{aligned}\dot{\mathbf{V}}(\cdot) &= -\mathbf{e}^T \mathbf{Q} \mathbf{e} - 2\mathbf{e}^T \mathbf{P} \mathbf{B} \Lambda \varepsilon_f \\ &\leq -\lambda_{low} \|\mathbf{e}\|^2 + 2\|\mathbf{e}\| \|\mathbf{P} \mathbf{B}\| \lambda_{high}(\Lambda) \varepsilon_{max}\end{aligned}$$

- $\lambda_{low}, \lambda_{high} \equiv$ minimum and maximum characteristic roots of \mathbf{Q} and Λ respectively.
- $\dot{\mathbf{V}}(\cdot)$ is thus negative definite outside the compact set
- $\chi = \left(\mathbf{e} : \|\mathbf{e}\| \leq \frac{2\|\mathbf{P} \mathbf{B}\| \lambda_{high}(\Lambda) \varepsilon_{max}(\mathbf{y})}{\lambda_{low}(\mathbf{Q})} \right)$
- thus, we conclude that the error \mathbf{e} is uniformly ultimately bounded.
 - i.e. $\mathbf{y}(t) \rightarrow 0$ as $t \rightarrow \infty$

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■ Publications Under Review

- Olalekan Ogunmolu, Xuejun Gu, Steve Jiang, Nicholas Gans. [Nonlinear Systems Identification Using Deep Dynamic Neural Networks](#). Under review at *Physical Review Applied*, American Physical Society, Submitted September 2018.
- Olalekan Ogunmolu, Michael Folkerts, Dan Nguyen, Nicholas Gans, Steve Jiang. [Deep BOO 2.0: End-to-End Training of Beam Orientation Selection Policies for Intensity Modulated Radiation Therapy](#). Under publication invitation review at *International Journal of Robotics Research (IJRR)*, 2018.

■ Working Manuscripts

- Olalekan Ogunmolu, Ayaka Kume, Jethro Tan. [A stable Lyapunov approach for designing deep policies for complex robot motion tasks](#). *Robotics and Automation Letters/International Conference on Robotics and Automation (RA-L)*. 2019.
- Olalekan Ogunmolu, Nick Gans, Xuejun Gu, and Steve Jiang. [Simulation and control of a head and neck patient pose correction soft-robot mechanism in intensity modulated radiotherapy](#). *Transactions on Robotics (T-RO)* 2018/2019.

■ Accepted Publications

- Olalekan Ogunmolu, Michael Folkerts, Dan Nguyen, Nicholas Gans, and Steve Jiang. [Deep BOO: Automating Beam Orientation Selection in Intensity Modulated Radiation Therapy](#). To appear at *The 13th International Workshop on the Algorithmic Foundations of Robotics (WAFR)*, Mérida, Mexico. December 2018.

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■ Accepted Publications (Cont'd)

- **Olalekan Ogunmolu**, Nicholas Gans, Tyler Summers. [Minimax Iterative Dynamic Game: Application to Nonlinear Robot Control Tasks](#). *IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*, Madrid, Spain. October 2018.
- **Olalekan Ogunmolu**, Dan Nguyen, Xun Jia, Weiguo Lu, Nicholas Gans, and Steve Jiang. [Automating Beam Orientation Optimization for IMRT Treatment Planning: A Deep Reinforcement Learning Approach](#). Selected for Oral Presentation at the *John R. Cameron Young Investigators Symposium – 60th Annual Meeting of the American Association of Physicists in Medicine*, Nashville, TN (AAPM). July 2018.
- Yara Almubarak, Joshi Aniket, **Olalekan Ogunmolu**, Xuejun Gu, Steve Jiang, Nicholas Gans, and Yonas Tadesse, [Design and Development of Soft Robots for Head and Neck Cancer Radiotherapy](#). *SPIE: Smart Structures + Nondestructive Evaluation*, (SPIE), Denver, CO, U.S.A. March 2018.
- **Olalekan Ogunmolu**, Adwait Kulkarni, Yonas Tadesse, Xuejun Gu, Steve Jiang, and Nicholas Gans. [Soft-NeuroAdapt: A 3-DOF Neuro-Adaptive Pose Correction System For Frameless and Maskless Cancer Radiotherapy](#). *IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*, Vancouver, BC, Canada. September 2017. DOI: 10.1109/IROS.2017.8206211.

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- Olalekan Ogunmolu, Xuejun Gu, Steve Jiang, and Nicholas Gans. [Vision-based control of a soft-robot for Maskless Cancer Radiotherapy](#). *IEEE Conference on Automation Science and Engineering (CASE)*, Fort-Worth, Texas, August 2016. DOI: 10.1109/CoASE.2016.7743378.
- Olalekan Ogunmolu, Xuejun Gu, Steve Jiang, and Nicholas Gans. [A Real-Time Soft-Robotic Patient Positioning System for Maskless Head-and-Neck Cancer Radiotherapy](#). *IEEE Conference on Automation Science and Engineering (CASE)*, Gothenburg, Sweden, August 2015. DOI: 10.1109/CoASE.2015.7294318.

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Marios M Polycarpou and Petros A Ioannou. Modelling, Identification And Stable Adaptive Control Of Continuous-time Nonlinear Dynamical Systems Using Neural Networks. In *American Control Conference, 1992*, pages 36–40. IEEE, 1992.

Olalekan Ogunmolu, Nicholas Gans, and Tyler Summers. Minimax iterative dynamic game: Application to nonlinear robot control tasks. *IEEE International Conference on Robots and Intelligent Systems, (IROS), Madrid, 2018.*, 2018.

Steve Webb. *Intensity-Modulated Radiation Therapy*. Institute of Physics Publishing Ltd, Bristol and Philadelphia, 2001.

Laura I Cerviño, Todd Pawlicki, Joshua D Lawson, and Steve B Jiang. Frame-less and mask-less cranial stereotactic

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radiosurgery: a feasibility study. *Physics in medicine and biology*, 55(7):1863, 2010.

Xinmin Liu, Andrew H Belcher, Zachary Grelewicz, and Rodney D Wiersma. Robotic Stage for Head Motion Correction in Stereotactic Radiosurgery. In *American Control Conference (ACC)*, 2015, pages 5776–5781. IEEE, 2015.

Mark Ostyn, Thomas Dwyer, Matthew Miller, Paden King, Rachel Sacks, Ross Cruikshank, Melvin Rosario, Daniel Martinez, Siyong Kim, and Woon-Hong Yeo. An electromechanical, patient positioning system for head and neck radiotherapy. *Physics in Medicine & Biology*, 62(18):7520, 2017.

Johannes Heinrich, Marc Lanctot, and David Silver. Fictitious

self-play in extensive-form games. In *International Conference on Machine Learning*, pages 805–813, 2015.

Eulalie Coevoet, Adrien Escande, and Christian Duriez.
Optimization-based inverse model of soft robots with contact handling. *IEEE Robotics and Automation Letters*, 2(3):1413–1419, 2017.

James M Bern, Grace Kumagai, and Stelian Coros.
Fabrication, modeling, and control of plush robots. In *Intelligent Robots and Systems (IROS), 2017 IEEE/RSJ International Conference on*, pages 3739–3746. IEEE, 2017.

Isuru S Godage, Gustavo A Medrano-Cerda, David T Branson, Emanuele Guglielmino, and Darwin G Caldwell. Dynamics for variable length multisection continuum arms. *The International Journal of Robotics Research*, 35(6):695–722, 2016.

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Frame-based
RT
Cyberknife
BOO

Solution

3DOFControl
Adaptive
NeuroControl
Neural Network
Model

Treatment
Plan (TP)
Optimization
(BOO)

Federico Renda, Michele Giorelli, Marcello Calisti, Matteo Cianchetti, and Cecilia Laschi. Dynamic model of a multibending soft robot arm driven by cables. *IEEE Transactions on Robotics*, 30(5):1109–1122, 2014.

Rongjie Kang, David T Branson, Emanuele Guglielmino, and Darwin G Caldwell. Dynamic modeling and control of an octopus inspired multiple continuum arm robot. *Computers & Mathematics with Applications*, 64(5):1004–1016, 2012.