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■ Publications Under Review

- Olalekan Ogunmolu, Xuejun Gu, Steve Jiang, Nicholas Gans. [Nonlinear Systems Identification Using Deep Dynamic Neural Networks](#). Under review at *Physical Review Applied*, American Physical Society, Submitted September 2018.
- Olalekan Ogunmolu, Michael Folkerts, Dan Nguyen, Nicholas Gans, Steve Jiang. [Deep BOO 2.0: End-to-End Training of Beam Orientation Selection Policies for Intensity Modulated Radiation Therapy](#). Under publication invitation review at *International Journal of Robotics Research (IJRR)*, 2018.

■ Working Manuscripts

- Olalekan Ogunmolu, Ayaka Kume, Jethro Tan. [A stable Lyapunov approach for designing deep policies for complex robot motion tasks](#). *Robotics and Automation Letters/International Conference on Robotics and Automation (RA-L)*. 2019.
- Olalekan Ogunmolu, Nick Gans, Xuejun Gu, and Steve Jiang. [Simulation and control of a head and neck patient pose correction soft-robot mechanism in intensity modulated radiotherapy](#). *Transactions on Robotics (T-RO)* 2018/2019.

■ Accepted Publications

- Olalekan Ogunmolu, Michael Folkerts, Dan Nguyen, Nicholas Gans, and Steve Jiang. [Deep BOO: Automating Beam Orientation Selection in Intensity Modulated Radiation Therapy](#). To appear at *The 13th International Workshop on the Algorithmic Foundations of Robotics (WAFR)*, Mérida, Mexico. December 2018.

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■ Accepted Publications (Cont'd)

- **Olalekan Ogunmolu**, Nicholas Gans, Tyler Summers. [Minimax Iterative Dynamic Game: Application to Nonlinear Robot Control Tasks](#). *IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*, Madrid, Spain. October 2018.
- **Olalekan Ogunmolu**, Dan Nguyen, Xun Jia, Weiguo Lu, Nicholas Gans, and Steve Jiang. [Automating Beam Orientation Optimization for IMRT Treatment Planning: A Deep Reinforcement Learning Approach](#). Selected for Oral Presentation at the *John R. Cameron Young Investigators Symposium – 60th Annual Meeting of the American Association of Physicists in Medicine*, Nashville, TN (AAPM). July 2018.
- Yara Almubarak, Joshi Aniket, **Olalekan Ogunmolu**, Xuejun Gu, Steve Jiang, Nicholas Gans, and Yonas Tadesse, [Design and Development of Soft Robots for Head and Neck Cancer Radiotherapy](#). *SPIE: Smart Structures + Nondestructive Evaluation*, (SPIE), Denver, CO, U.S.A. March 2018.
- **Olalekan Ogunmolu**, Adwait Kulkarni, Yonas Tadesse, Xuejun Gu, Steve Jiang, and Nicholas Gans. [Soft-NeuroAdapt: A 3-DOF Neuro-Adaptive Pose Correction System For Frameless and Maskless Cancer Radiotherapy](#). *IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS)*, Vancouver, BC, Canada. September 2017. DOI: 10.1109/IROS.2017.8206211.

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■ Accepted Publications (Cont'd)

- Olalekan Ogunmolu, Xuejun Gu, Steve Jiang, and Nicholas Gans. [Vision-based control of a soft-robot for Maskless Cancer Radiotherapy](#). *IEEE Conference on Automation Science and Engineering (CASE)*, Fort-Worth, Texas, August 2016. DOI: 10.1109/CoASE.2016.7743378.
- Olalekan Ogunmolu, Xuejun Gu, Steve Jiang, and Nicholas Gans. [A Real-Time Soft-Robotic Patient Positioning System for Maskless Head-and-Neck Cancer Radiotherapy](#). *IEEE Conference on Automation Science and Engineering (CASE)*, Gothenburg, Sweden, August 2015. DOI: 10.1109/CoASE.2015.7294318.

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The robustness conundrum

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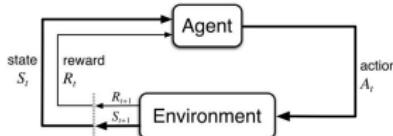
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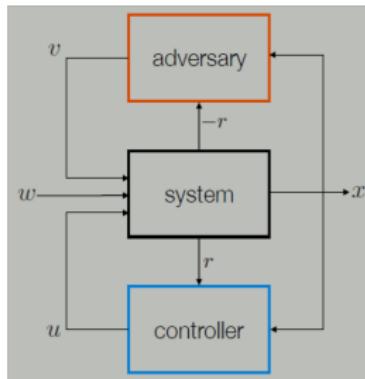
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- How to know *a priori* a policy's robustness limits?



- How to inculcate robustness into multistage decision policies?



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- Suppose we have two agents, \mathbf{u} and \mathbf{v} , interacting in an environment over an horizon T
- Let their dynamics be described as

$$\mathbf{x}_{t+1} = f_t(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t, \mathbf{w}_t), \quad t = 0, \dots, T-1$$

- where \mathbf{x}_t and \mathbf{u}_t are state and control variables
- \mathbf{v}_t and \mathbf{w}_t are the respective disturbance and stochastic random variables.
- $\mathbf{w} = \{\mathbf{w}_0, \mathbf{w}_1, \dots, \mathbf{w}_{T-1}\}$ has distribution,
 $\mathcal{P}(\mathbf{w}_t | \mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t)$, $t = 0, \dots, T-1$.
- Furthermore, $\mathbf{u}_t \in \{\pi = \pi_0, \pi_1, \dots, \pi_T\}$,
 $\mathbf{v}_t \in \{\psi_0, \psi_1, \dots, \psi_T\}$, and $\mathbf{w}_t \in \mathcal{P}(\mathbf{w}_t | \cdot)$, $i = 0, \dots, T-1$

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- When a policy pair (π, ψ) is adopted, cost of a trajectory with initial condition \mathbf{x}_0 is

$$\mathcal{J}_0(\mathbf{x}_0, \pi, \psi, \mathbf{w}) = \sum_{t=0}^{T-1} \ell_t(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t) + L_T(\mathbf{x}_T) \quad (1)$$

- where $\ell_t, t = 0, \dots, T - 1$ and L_T are nonnegative instantaneous costs
- Average cost is thus

$$\tilde{\mathcal{J}}_0(\mathbf{x}_0, \pi, \psi) = \mathbf{E}_{\mathbf{x}_0(\mathbf{w})=\mathbf{x}_0} [\tilde{\mathcal{J}}_0(\mathbf{x}_0(\mathbf{w}), \pi, \psi, \mathbf{w})]$$

- $\mathbf{E}_{\mathbf{x}_0(\mathbf{w})=\mathbf{x}_0} (\cdot)$ is the expectation over random variables $\mathbf{x}_1(\mathbf{w}), \dots, \mathbf{x}_T(\mathbf{w})$ having value \mathbf{x}_0

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- Define $\phi(\pi, \psi)$ as

$$\phi(\pi, \psi) = \mathbf{E}[\mathcal{J}_0(\mathbf{x}_0, \pi, \psi)] \quad (2)$$

- where \mathbf{E} is $\mathbf{E}_{\mathbf{x}_0(\mathbf{w})=\mathbf{x}_0}$

so that

$$\phi(\pi, \psi) = \mathbf{E}[\tilde{\mathcal{J}}_0(\mathbf{x}_0(\mathbf{w}), \pi, \psi, \mathbf{w})] \quad (3)$$

Problem Statement

Find an admissible (saddle point equilibrium) policy pair that satisfy, $\mathcal{J}_0(\mathbf{x}_0, \pi^*, \psi) \leq \mathcal{J}_0(\mathbf{x}_0, \pi^*, \psi^*) \leq \mathcal{J}_0(\mathbf{x}_0, \pi, \psi^*), \forall \pi \in \Pi, \psi \in \Psi$ and \mathbf{x}_0 .

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- $\mathcal{J}_t(\mathbf{x}_t, \boldsymbol{\pi}, \boldsymbol{\psi})$ would denote the average process cost with initial condition, \mathbf{x}_t and policy pair, $(\boldsymbol{\pi}, \boldsymbol{\psi})$, i.e.,

$$\mathcal{J}_t(\mathbf{x}_t, \boldsymbol{\pi}, \boldsymbol{\psi}) = \min_{\boldsymbol{\pi}} \max_{\boldsymbol{\psi}} \mathbf{E}_{|\mathbf{x}_t} \tilde{\mathcal{J}}_t(\mathbf{x}_t(\mathbf{w}), \boldsymbol{\pi}, \boldsymbol{\psi}, \mathbf{w})$$

- DP transforms the optimization over whole trajectory to a step-wise optimization over $(\mathbf{u}_t, \mathbf{v}_t)$ as

$$\mathcal{J}_t(\cdot) = \min_{\mathbf{u}_t \sim \boldsymbol{\pi}} \max_{\mathbf{v}_t \sim \boldsymbol{\psi}} \mathbf{E}_{|\mathbf{x}_t} \left[\sum_{k=t}^{T-1} \ell_k(\mathbf{x}_k, \boldsymbol{\pi}_k(\mathbf{x}_k), \boldsymbol{\psi}_k(\mathbf{x}_k)) + L(\mathbf{x}_k) \right]$$

with boundary condition $\mathcal{J}_T(\mathbf{x}_T, \boldsymbol{\pi}, \boldsymbol{\psi}, \mathbf{w}) = L(\mathbf{x}_T)$

- We seek a saddle point equilibrium policy that satisfies

$$\mathcal{J}_t(\mathbf{x}_t, \boldsymbol{\pi}^*, \boldsymbol{\psi}) \leq \mathcal{J}_t(\mathbf{x}_t, \boldsymbol{\pi}^*, \boldsymbol{\psi}^*) \leq \mathcal{J}_t(\mathbf{x}_t, \boldsymbol{\pi}, \boldsymbol{\psi}^*),$$

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- Assume an agent's nominal policy, π , has been found
- Suppose that there is another agent interacting in the nominal agent's environment, so that

$$\begin{aligned} \mathbf{x}_{t+1} &= f_t(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t, \mathbf{w}_t), \quad \mathbf{u}_t \sim \pi_t \\ &:= \tilde{f}_t(\mathbf{x}_t, \tilde{\mathbf{v}}_t), \quad t = 0, \dots, T-1. \end{aligned} \tag{4}$$

where we have assumed the random variable \mathbf{w}_t is part of $\tilde{\mathbf{v}}_t$

- For stage costs of the form,

$$\ell_t(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t) = \left[\sum_{t=0}^T \underbrace{c(\mathbf{x}_t, \mathbf{u}_t)}_{\text{nominal}} - \gamma \underbrace{g(\mathbf{v}_t)}_{\text{opponent}} \right]$$

- $g_t(\cdot)$ controls the strength of the disturbing agent

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Minimax Iterattive Dynamic Game

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- To mitigate lack of robustness, we optimize the *cost-to-go*

$$\mathcal{J}_t(\mathbf{x}_t, \pi, \psi) = \min_{\mathbf{u}_t \sim \pi} \max_{\mathbf{v}_t \sim \psi} \left[\sum_{t=0}^{T-1} \ell_t(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t) + L_T(\mathbf{x}_T) \right]$$

- and seek a saddle point equilibrium policy that satisfies the following inequality,

$$\mathcal{J}_t(\mathbf{x}_t, \pi^*, \psi) \leq \mathcal{J}_t(\mathbf{x}_t, \pi^*, \psi^*) \leq \mathcal{J}_t(\mathbf{x}_t, \pi, \psi^*),$$

Minimax iDG: Case Study

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- Continuously solve an online trajectory optimization problem in a minimax fashion
- Essentially a meta-algorithm that is applicable to e.g. iLQG, DDP, GPS, DQN etc.
- Case study is a two-player iDG which proceeds as follows
 - approximate nonlinear system dynamics, \mathbf{x}_{t+1} , starting with a schedule of the nominal agent's local controls, $\{\bar{\mathbf{u}}_t\}$, and the opposing agent's local controls $\{\bar{\mathbf{v}}_t\}$ which are assumed to be available,

Minimax iDG: Case Study (Cont'd)

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- Case study is a two-player iDG which proceeds as follows
 - run passive dynamics with $\{\bar{\mathbf{u}}\}, \{\bar{\mathbf{v}}\}$ and generate a nominal state trajectory $\{\bar{\mathbf{x}}_t\}$, with neighboring trajectories $\{\mathbf{x}_t\}$
 - we choose a small neighborhood, $\{\delta\mathbf{x}_t\}$ of $\{\mathbf{x}_t\}$, which provides an optimal reduction in cost as the dynamics no longer represent those of $\{\mathbf{x}_t\}$
 - discretizing time, the new state and control sequence pairs become $\delta\mathbf{x}_t = \mathbf{x}_t - \bar{\mathbf{x}}_t$, $\delta\mathbf{u}_t = \mathbf{u}_t - \bar{\mathbf{u}}_t$, $\delta\mathbf{v}_t = \mathbf{v}_t - \bar{\mathbf{v}}_t$.

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- Therefore, for

$$\mathcal{J}(\mathbf{x}_t, \boldsymbol{\pi}, \boldsymbol{\psi}) = \min_{\mathbf{u}_t \sim \boldsymbol{\pi}} \max_{\mathbf{v}_t \sim \boldsymbol{\psi}} [\ell(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t) + \mathcal{J}(f(\mathbf{x}_{t+1}, \mathbf{u}_{t+1}, \mathbf{v}_{t+1}))]$$

- Suppose we consider the Hamiltonian as a perturbation around $\{\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t\}$
- Cost over local neighborhood, $\{\delta\mathbf{x}_t\}$ can be approximated by a 2nd order Taylor expansion,

$$Q(\cdot) \approx \frac{1}{2} \begin{bmatrix} 1 \\ \delta\mathbf{x}_t^T \\ \delta\mathbf{u}_t^T \\ \delta\mathbf{v}_t^T \end{bmatrix}^T \begin{bmatrix} 1 & Q_{xt}^T & Q_{ut}^T & Q_{vt}^T \\ Q_{xt} & Q_{xxt} & Q_{xut} & Q_{xvt} \\ Q_{ut} & Q_{uxt} & Q_{uut} & Q_{uvt} \\ Q_{vt} & Q_{vxr} & Q_{vut} & Q_{vvt} \end{bmatrix} \begin{bmatrix} 1 \\ \delta\mathbf{x}_t \\ \delta\mathbf{u}_t \\ \delta\mathbf{v}_t \end{bmatrix} \quad (5)$$

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■ where

$$Q_{xt} = \ell_{xt} + f_{xt}^T V_{xt+1}, \quad Q_{ut} = \ell_{ut} + f_{ut}^T V_{xt+1}$$

$$Q_{vt} = \ell_{vt} + f_{vt}^T V_{xt+1}, \quad Q_{xxt} = \ell_{xxt} + f_{xt}^T V_{xxt+1} f_{xt}$$

$$Q_{uxt} = \ell_{uxt} + f_{ut}^T V_{xxt+1} f_{xt}, \quad Q_{vxt} = \ell_{vxt} + f_{vt}^T V_{xxt+1} f_{xt}$$

$$Q_{uut} = \ell_{uut} + f_{ut}^T V_{xxt+1} f_{ut}, \quad Q_{vvt} = \ell_{vvt} + f_{vt}^T V_{xxt+1} f_{vt}$$

$$Q_{uvt} = \ell_{uvt} + f_{ut}^T V_{xxt+1} f_{vt}.$$

- it is expected that 2nd order terms will dominate the higher-order ones, consistent with linearized methods [Polycarpou and Ioannou (1992)].

Linearization of Dynamics

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- LQR approximation to dynamics becomes

$$\delta \mathbf{x}_{t+1} \approx f_{\mathbf{x}t} \delta \mathbf{x}_t + f_{\mathbf{u}t} \delta \mathbf{u}_t + f_{\mathbf{v}t} \delta \mathbf{v}_t$$
$$\ell(\mathbf{x}_t, \mathbf{u}_t, \mathbf{v}_t) \approx \frac{1}{2} \begin{bmatrix} 1 \\ \delta \mathbf{x}_t^T \\ \delta \mathbf{u}_t^T \\ \delta \mathbf{v}_t^T \end{bmatrix}^T \begin{bmatrix} \ell_{0t} & \ell_{\mathbf{x}t}^T & \ell_{\mathbf{u}t}^T & \ell_{\mathbf{v}t}^T \\ \ell_{\mathbf{x}t} & \ell_{\mathbf{xxt}} & \ell_{\mathbf{uxt}} & \ell_{\mathbf{vxt}} \\ \ell_{\mathbf{u}t} & \ell_{\mathbf{uxt}} & \ell_{\mathbf{uut}} & \ell_{\mathbf{uvt}} \\ \ell_{\mathbf{v}t} & \ell_{\mathbf{vxt}} & \ell_{\mathbf{vut}} & \ell_{\mathbf{vvt}} \end{bmatrix} \begin{bmatrix} 1 \\ \delta \mathbf{x}_t \\ \delta \mathbf{u}_t \\ \delta \mathbf{v}_t \end{bmatrix} \quad (6)$$

- It is easy to verify that the feedback controls are

$$\delta \mathbf{u}_t^* = -Q_{\mathbf{u}ut}^{-1} [Q_{\mathbf{u}t}^T + Q_{\mathbf{u}xt} \delta \mathbf{x}_t + Q_{\mathbf{u}vt} \delta \mathbf{v}_t], \quad (7)$$
$$\delta \mathbf{v}_t^* = -Q_{\mathbf{v}vt}^{-1} [Q_{\mathbf{v}t}^T + Q_{\mathbf{v}xt} \delta \mathbf{x}_t + Q_{\mathbf{v}ut} \delta \mathbf{u}_t].$$

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- From which we obtain the recursions,

$$\begin{aligned}\Delta V_t &= \mathbf{g}_{\mathbf{u}t} Q_{\mathbf{u}t} + \mathbf{g}_{\mathbf{v}t} Q_{\mathbf{v}t} + \mathbf{g}_{\mathbf{u}t} Q_{\mathbf{u}vt} \mathbf{g}_{\mathbf{v}t} \\ &\quad + \frac{1}{2} (\mathbf{g}_{\mathbf{u}t} Q_{\mathbf{u}ut} \mathbf{g}_{\mathbf{u}t} + \mathbf{g}_{\mathbf{v}t} Q_{\mathbf{v}vt} \mathbf{g}_{\mathbf{v}t}) \\ V_{\mathbf{x}t} &= Q_{\mathbf{x}t} + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}t} + \mathbf{G}_{\mathbf{v}t}^T Q_{\mathbf{v}t} + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}ut} \mathbf{g}_{\mathbf{u}t} + \mathbf{g}_{\mathbf{u}t} Q_{\mathbf{u}xt} \\ &\quad + \mathbf{g}_{\mathbf{v}t} Q_{\mathbf{v}xt} + \mathbf{G}_{\mathbf{v}t}^T Q_{\mathbf{v}vt} \mathbf{g}_{\mathbf{v}t} + \mathbf{G}_{\mathbf{v}t}^T Q_{\mathbf{u}vt}^T \mathbf{g}_{\mathbf{u}t} + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}vt} \mathbf{g}_{\mathbf{v}t} \\ V_{\mathbf{xxt}} &= \frac{1}{2} (Q_{\mathbf{xxt}} + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}ut} \mathbf{G}_{\mathbf{u}t} + \mathbf{G}_{\mathbf{v}t}^T Q_{\mathbf{v}vt} \mathbf{G}_{\mathbf{v}t}) + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}xt} \\ &\quad + \mathbf{G}_{\mathbf{v}t}^T Q_{\mathbf{v}xt} + \mathbf{G}_{\mathbf{u}t}^T Q_{\mathbf{u}vt} \mathbf{G}_{\mathbf{v}t} \end{aligned} \tag{8}$$

- NB: The gains \mathbf{g}_{it} and \mathbf{G}_{it} , $i = \mathbf{u}$ or \mathbf{v} are as defined in ([§II.B]Ogunmolu et al. (2018)).

Results: Brittleness Quantification

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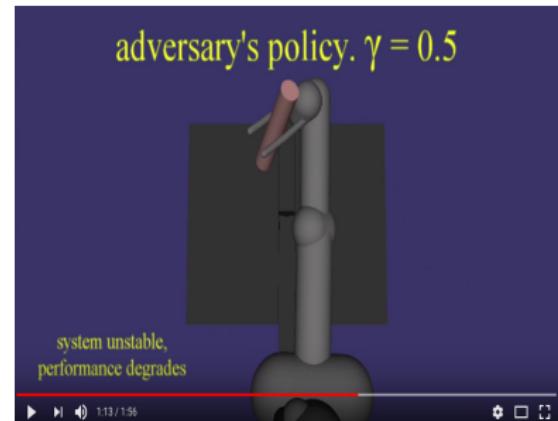
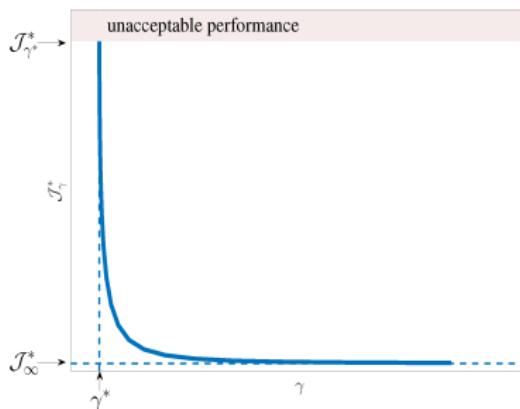
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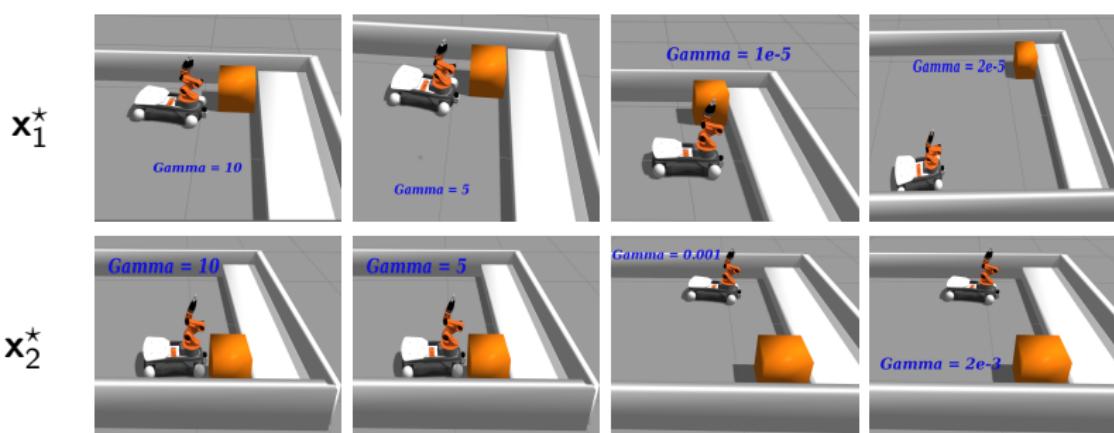
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End pose of the KUKA platform with our iDG formulation given different goal states and γ -values

Video of Results

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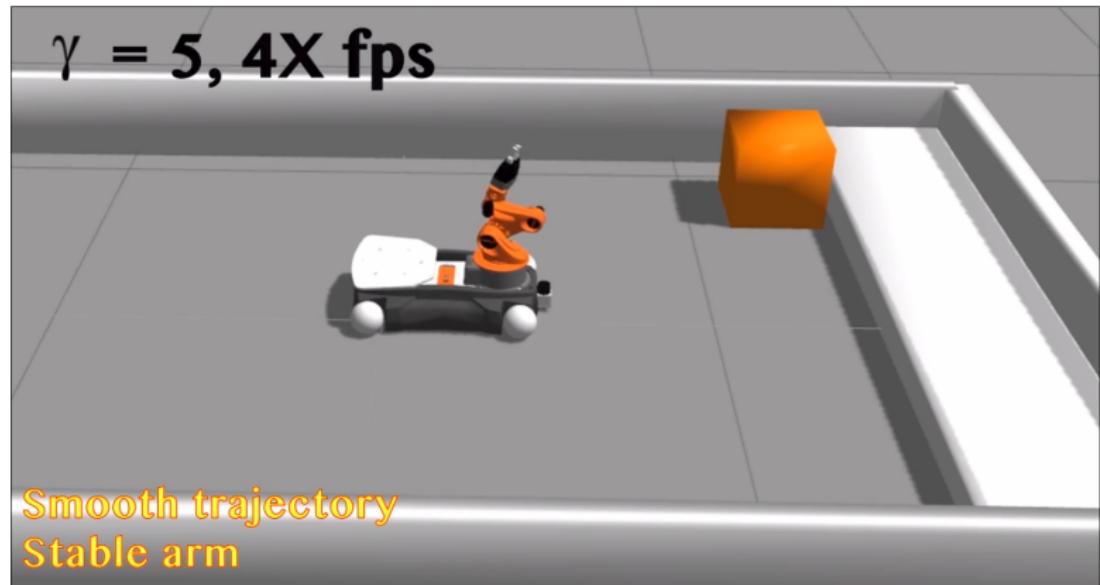
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Treatment Options

Surgery

- Oldest technique
- Good for localized cancer cells
- Falls short of being an all-around good option



Source: National Cancer Institute

Chemotherapy

- Effective for malignant cancer cells
- Highly toxic
- Highly carcinogenic
- Kills health cells



Source: Cancer.gov

Radiosurgery

- Replaces invasive surgery
- Often used alongside surgical tumor removal
- Extremely effective in managing tumors
- Standard care in managing cancer conditions



■ Radiotherapy treatment is the most effective

Radiotherapy types

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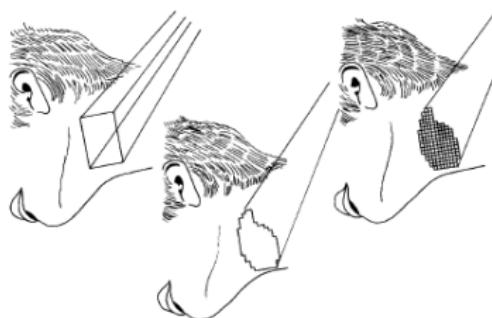
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Neural Network Model

- Conventional Radiation Therapy
- Conformal Radiation Therapy (CFRT)
- Intensity-Modulated Radiation Therapy (IMRT)



Left: Conventional radiotherapy.

Middle: Conformal radiotherapy (CFRT) without intensity modulation.

Right: CFRT with intensity modulation. Reprinted from Webb (2001).

Frame-based Radiotherapy Treatment

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- Fractionated radiation dose over many weeks/months



Frameless (Completely non-invasive) RT

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High-dose volumes with complex shapes [Adler and Cox (1995)]



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Image Guided Radiotherapy

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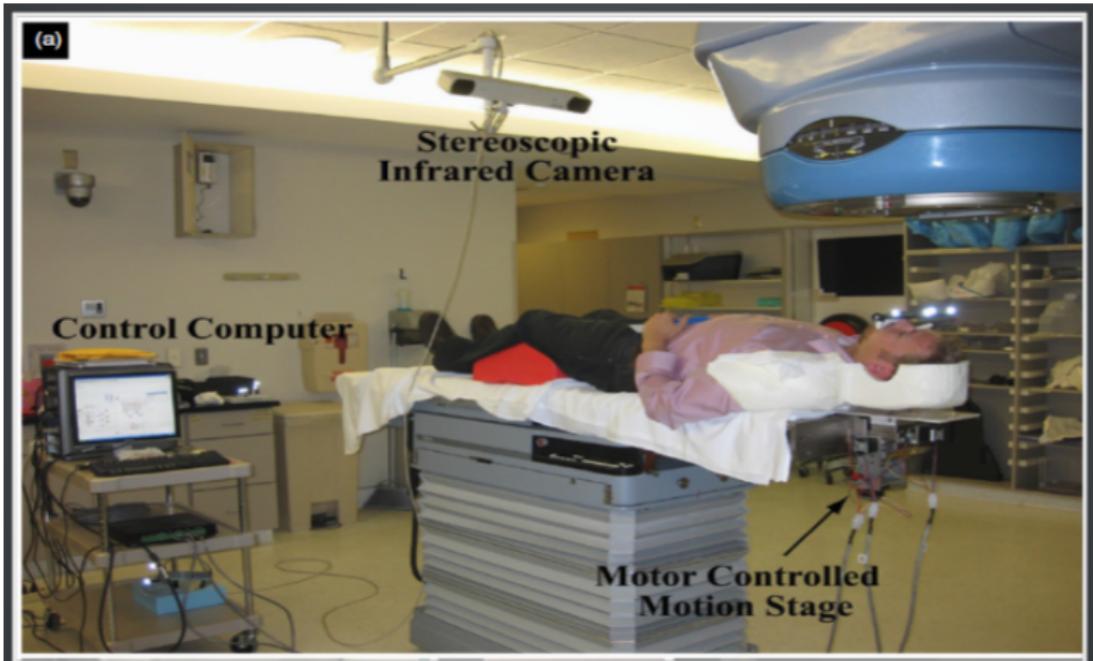
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© Wiersma et al. (2009)

Beam Orientation Optimization

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- During treatment planning, a **beam orientation optimization** problem (BOO) is separately solved
- Radiation is delivered from $\approx (5 - 15)$ different beam orientations during IMRT
- BOO determines the best beam angle combinations for delivering radiation.
- Process of determining beamlets' intensities is termed **fluence map optimization** (FMO)

The Immobilization Problem

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Cerviño et al. (2010)



Feasibility evaluation

Liu et al. (2015)



4-D robotic stage couch

Ostyn et al. (2017)



6-DoF robotic couch

Solution: Soft-Robot Position Correcting Systems

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- Eliminate rigid frames and metallic rings
- Eliminate attenuation of X-Ray beams
- Control design
 - Feedback control + optimal regulation + robustness to disturbance ✓

Vision-based 3-DOF Control

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Simulation Testbed

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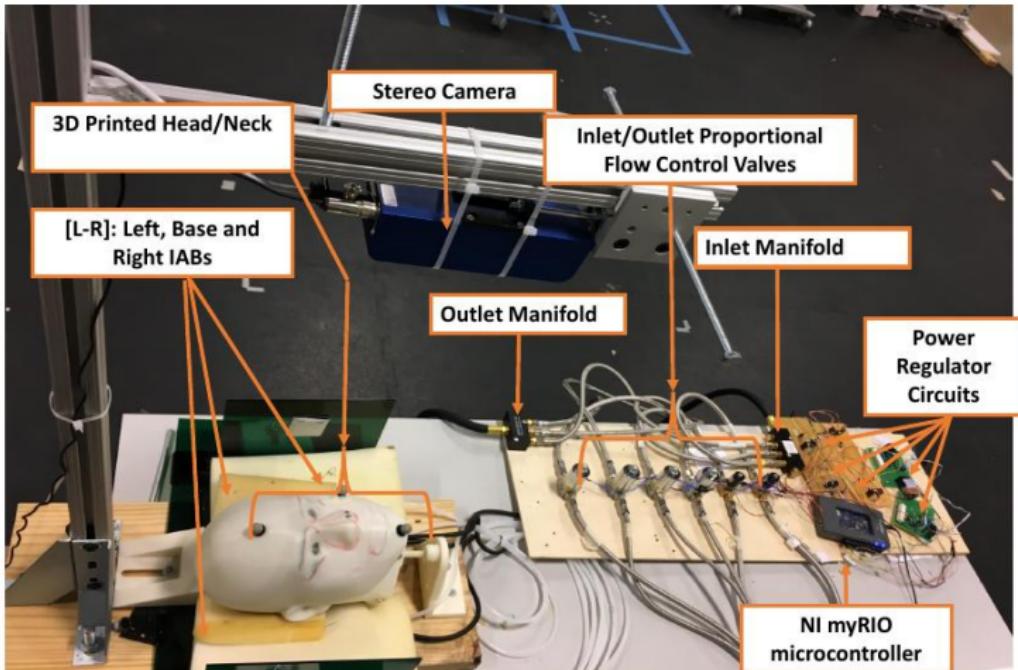
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Control Proposals

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Neural Network Model

- Solve a state feedback and feedforward regulation problem
- An adaptation model based on head pose estimate given past states and past control inputs:
 - $Z^N = \{u(k), u(k-1), \dots, u(k-n_u), y(k), \dots, y(k-n_y)\}$
 - Let a persistently exciting input signal $u_{ex} \in L_2 \cap L_\infty$ excite the system's nonlinear modes
- Design Goal:
 - Stabilize states, $\mathbf{y} = [z, \theta, \phi]^T$ out of $[x, y, z, \theta, \phi, \psi]^T$

Model Reference Adaptive Control

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Neural Network Model

- Model head and bladder dynamics as
 - $\dot{\mathbf{y}} = \mathbf{A}\mathbf{y}, \mathbf{u} + \mathbf{B}\Lambda(\mathbf{u} - f(\mathbf{y})) + \mathbf{w}(k)$
 - \mathbf{A}, Λ unknown, \mathbf{B} , $\text{sgn}\Lambda$ known
 - $f(\mathbf{y}, \mathbf{u}) \triangleq$ nonlinear function to be adapted for
 - $\mathbf{x} \triangleq$ tuple containing past controls and current outputs
- Approximate $f(\mathbf{y}, \mathbf{u})$ by a neural network with continuous memory states
 - $\hat{f}(\mathbf{y}(k), \mathbf{u}(k-d))$ is realized with a *long-short term memory* cell (Horchreiter and Schmidhuber, '91, '97)
 - **purpose:** remember good adaptation gains

Assumptions

- A dynamic RNN with N neurons, $\varphi(\mathbf{x})$, exists
 - maps from a compact input space $\mathbf{u} \subset \mathbb{U}$ to $\mathbf{y} \subset \mathbb{Y}$ on the Lebesgue integrable functions within $[0, T]$ or $[0, \infty)$
- $f(\mathbf{y}, \mathbf{u})$ is exactly $\Theta^T \Phi(\mathbf{y})$
 - f has coefficients $\Theta \in R^{N \times m}$ and a Lipschitz-continuous vector of basis functions $\Phi(\mathbf{y}) \in R^N$
- Inside a ball \mathbf{Y}_R with known, finite radius R ,
 - an ideal neural network (NN) approximation $f(\mathbf{y}) : R^n \rightarrow R^m$, is realized to a sufficient degree of accuracy, $\varepsilon_f > 0$;
- Outside \mathbf{Y}_R ,
 - the NN approximation error can be upper-bounded by a known unbounded, scalar function $\varepsilon_{max}(\mathbf{y})$;
 - $\|\varepsilon(\mathbf{y})\| \leq \varepsilon_{max}(\mathbf{y}), \quad \forall \mathbf{y} \in \mathbf{Y}_R$;
- There exists an exponentially stable reference model
 - $\dot{\mathbf{y}}_m = \mathbf{A}_m \mathbf{y}_m + \mathbf{B}_m \mathbf{r}$

Adaptive Neuro-Control Scheme

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- Set control law in terms of parameter estimates from the neural network weights and Lipschitz basis functions
 - $\Phi(\mathbf{y}) = \{\mathbf{y}(k-d), \dots, \mathbf{y}(k-d-4), \mathbf{u}(k-d) \dots \mathbf{u}(k-d-5)\}$
 - i.e. network looks back in time by 5 time steps at every instant, and then makes a prediction
- Derive adaptive adjustment mechanism from Lyapunov analysis for Adaptive Control (Parks, P., 1966)
- $\mathbf{u} = \underbrace{\hat{\mathbf{K}}_y^T \mathbf{y}}_{\text{state feedback}} + \underbrace{\hat{\mathbf{K}}_r^T \mathbf{r}}_{\text{optimal regulator}} + \underbrace{\hat{f}(\mathbf{y}, \mathbf{u})}_{\text{approximator}}$

Controller formulation

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- \hat{K}_y and \hat{K}_r are adaptive gains to be designed

Term Contributions

- $\hat{K}_y^T \mathbf{y}$ term keeps the states of the approximation set $\mathbf{y} \in \mathbf{B}_R$ stable,
- $\hat{K}_r^T \mathbf{r}$ term causes the states to follow a given reference trajectory
- Function approximator $\hat{f}(\mathbf{y}, \mathbf{u})$ ensures states that start outside the approximation set $\mathbf{y} \in \mathbf{B}_R$ converge to \mathbf{B}_R in finite time

Adaptive Control Formulation

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Neural Network Model

- Assume model matching conditions
 - such that $\hat{\mathbf{K}}_y = \mathbf{K}_y$, and $\hat{\mathbf{K}}_r = \mathbf{K}_r$ (ideally)
- Realize the approximator as $\hat{f}(\mathbf{y}) = \hat{\Theta}^T \Phi(\mathbf{y}) + \varepsilon_f(\mathbf{y})$
 - $\hat{\Theta}^T$ denotes the vectorized weights of the neural network
 - $\Phi(\mathbf{y})$ denotes the vector of lagged inputs and output,
 - $\varepsilon_f(\mathbf{y})$ is the approximation error.
 - $\Phi(\mathbf{y}) = \{\mathbf{y}(k-d) \cdots \mathbf{y}(k-d-4), \mathbf{u}(k-d) \cdots \mathbf{u}(k-d-5)\}$

Neural Network Model

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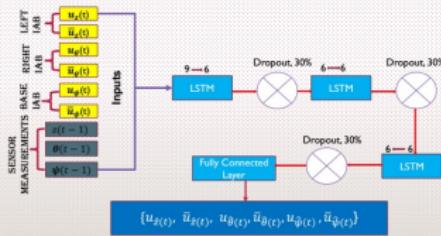
BOO

Solution

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Neural Network Model

Neural Net Architecture



- input: lagged vector of past observations and current control actions
- repeat $\times 3$
 - pass input through an lstm cell
 - followed by 30% dropout
- output will be control predictions directly fed as valve voltages

Lyapunov Redesign

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■ Theorem:

- Given correct choice of adaptive gains $\hat{\mathbf{K}}_y$ and $\hat{\mathbf{K}}_r$, the error state vector, $\mathbf{e}(k)$ with closed loop time derivative $\dot{\mathbf{e}}$, is **uniformly ultimately bounded**, and the state \mathbf{y} will converge to a neighborhood of \mathbf{r} .
- Please see proof in §V.A of Ogunmolu et al. (2017).

Stability Results

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We find that

$$\begin{aligned}\dot{\mathbf{V}}(\cdot) &= -\mathbf{e}^T \mathbf{Q} \mathbf{e} - 2\mathbf{e}^T \mathbf{P} \mathbf{B} \Lambda \varepsilon_f \\ &\leq -\lambda_{low} \|\mathbf{e}\|^2 + 2\|\mathbf{e}\| \|\mathbf{P} \mathbf{B}\| \lambda_{high}(\Lambda) \varepsilon_{max}\end{aligned}$$

- $\lambda_{low}, \lambda_{high} \equiv$ minimum and maximum characteristic roots of Q and Λ respectively.
- $\dot{\mathbf{V}}(\cdot)$ is thus negative definite outside the compact set
- $\chi = \left(\mathbf{e} : \|\mathbf{e}\| \leq \frac{2\|\mathbf{P} \mathbf{B}\| \lambda_{high}(\Lambda) \varepsilon_{max}(\mathbf{y})}{\lambda_{low}(Q)} \right)$
- thus, we conclude that the error \mathbf{e} is uniformly ultimately bounded.
 - i.e. $\mathbf{y}(t) \rightarrow 0$ as $t \rightarrow \infty$

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- Solving the general form of the Lyapunov equation, we have

$$\mathbf{P} = \begin{bmatrix} -\frac{170500}{2668} & 0 & 0 \\ 0 & -\frac{170500}{2668} & 0 \\ 0 & 0 & -\frac{170500}{2668} \end{bmatrix}$$

- Solenoid valves operate in pairs
 - two valves create a difference in air mass within each IAB at any given time
 - set

$$\mathbf{B} = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 \end{bmatrix}$$

- \mathbf{B} maps to the 3-axes controllers

$$[u_z \quad u_\theta \quad u_\psi]^T$$

- non-zero terms are the max. duty-cycle to valves based on the software configuration of the NI RIO PWM generator

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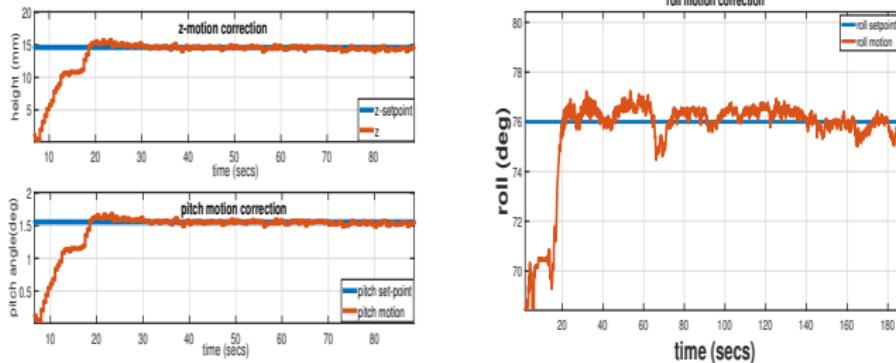
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[Left]: Goal command: $(z, \theta, \phi) = (2.5\text{mm}, 0.25^\circ, 35^\circ)$ to $(14\text{mm}, 1.6^\circ, 45^\circ)^T$. [Right]: Head roll tracking.

Treatment Plan (TP) Optimization

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IMRT TP Overview

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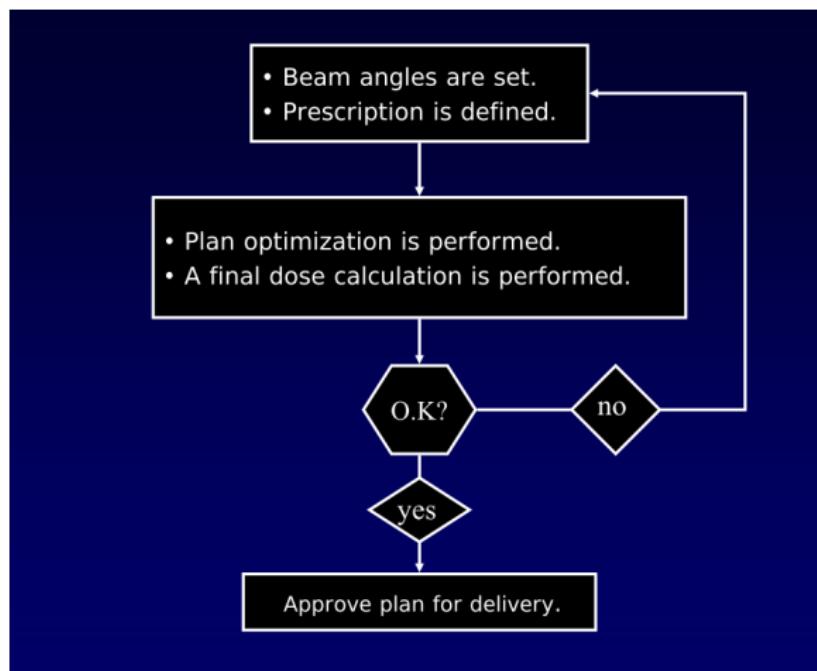
Neural Network Model

- IMRT delivers geometrically-shaped, high-precision photons to tumors in a beam orientation optimization (BOO) process.
- The **BOO problem** aims to find the right beam angle combinations from which to deliver radiation intensities.
 - essentially a combinatorial optimization problem
 - traditional methods fail at real-time feasible results¹.
- Afterwards, the intensity of the fluence is modulated in a **fluence map optimization** (FMO) process.

¹Current approaches take too long, and are often not optimal.



IMRT Treatment Plan Flowchart



Reprinted from "IMRT Optimization Algorithms. David Shepard. Swedish Cancer Institute. AAPM 2007."

Problem Setup

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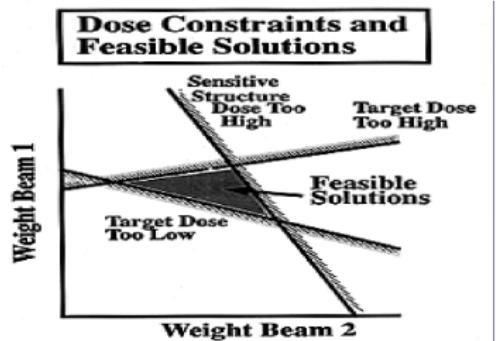
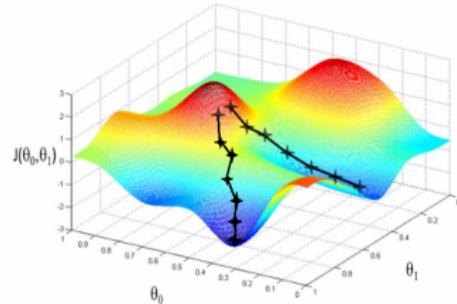
3DOFControl

Adaptive

NeuroControl

Neural Network Model

- Given biological statement of prescriptions
 - find a numerical **objective function**
 - accompanied by **constraints**
- Challenge
 - a scalar-valued objective function usually not sufficient



Courtesy of David Shepard

Common Problem Formulation

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Neural Network Model

- Maximize weighted least square dose from for PTVs
- Minimize weighted least square dose for OARs
- DVH-based goal treatments

- Current Approaches and Limitations

- Stochastic optimization approaches: simulated annealing; genetic algorithms and gradient search, or a combination of genetic and gradient search algorithms
- Mixed-integer programming, branch and cut/bound algorithms, beam angle elimination algorithms
- General weakness: Feasible solution takes too long to find.

Our approach

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- Automate the **beam search** problem
- **Ultimate goal** is real-time beam angle prediction given a target volume
- Drawing ideas from
 - **pattern recognition;**
 - **monte carlo evaluations;**
 - **game simulations;** and
 - **approximate dynamic programming**

What we do

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Neural Network Model

- Formulate BOO problem into a large game planning strategy
- Neural fictitious self-play [Heinrich et al. (2015)], to refine policy predictions
 - **purpose:** drive policy weights to a **saddle equilibrium**
- a deep neural network models the nonlinear dynamical system (patient's geometry, robot-linac setup)
 - generating a policy that guides MCTS simulations for two players in a zero-sum Markov game

What we do

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- In each episodic markov decision process (MDP) setting, an MCTS lookout strategy guides transition from one beam angle set to another
- Each player in a two-player Markov game finds a best response strategy to their opponent's average strategy
 - driving the policy weights toward an approximate **saddle equilibrium** Heinrich et al. (2015).

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- Let state of the dynamical system be $s \in \mathcal{S}$
- To be controlled by a discrete action $a \in \mathcal{A}$
- States evolve according to an (unknown) dynamics $p(s_{t+1}|s_t, a_t)$ (to be learned)
- Beam angle combination search task defined by a reward function, $R_t = \sum_{t=1}^N \gamma^{t-1} r(s_t, a_t)$
 - Can be found by recovering a policy, $p(a_t|s_t; \psi)$
- From now on, we will write $p(a_t|s_t; \psi)$ as $\pi_\psi(a_t|s_t)$.

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- Suppose the first player is p_1 , and the second player is p_2
- p_1 chooses its action under a (stochastic) strategy,
 $\pi^{p_1} = \{\pi_0^{p_1}, \pi_1^{p_1}, \dots, \pi_T^{p_1}\} \subseteq \Pi^{p_1}$
 - minimizing the game's outcome ζ
- p_2 's actions are governed by a policy
 $\pi^{p_2} = \{\pi_0^{p_2}, \pi_1^{p_2}, \dots, \pi_T^{p_2}\} \subseteq \Pi^{p_2}$
 - p_2 seeks to maximize ζ in order to guarantee an equilibrium solution for a game without saddle point.
- Π^{p_i} is the set of all possible nonstationary markovian policies

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Neural Network Model

- Each player bases its decision on a random event's outcome
 - generating a **mixed strategy** determined by **averaging the outcome** of individual plays.
- Both players constitute a two-player **stochastic action selection strategy**, $\pi(s, a) = Pr(a|s) := \{\pi^{P_1}, \pi^{P_2}\}$ that gives the probability of selecting moves in any given state
- Suppose the game simulation starts from an initial condition s_0 .

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- One may write the optimal **reward-to-go** value function for state s in stage t , with horizon length T as

$$V_t^*(s) = \inf_{\pi^{P_1} \in \Pi^{P_1}} \sup_{\pi^{P_2} \in \Pi^{P_2}} \mathbb{E} \left[\sum_{i=t}^{T-1} V_t(s_0, f(s_t, \pi^{P_1}, \pi^{P_2})) \right],$$
$$s \in S, t = 0, \dots, H-1$$

- where the terminal value $V_T^*(s) = 0, \forall s \in S$;
- $f(\cdot)$ represents the unknown system dynamics
- π^{P_1} and π^{P_2} contain the action/control sequences $\{a_t^{P_1}\}_{0 \leq t \leq T}$ and $\{a_t^{P_2}\}_{0 \leq t \leq T}$

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- The **saddle point strategies** for an optimal control sequence pair $\{a_t^{p_1^*}, a_t^{p_2^*}\}$ can be recursively obtained by optimizing a state-action value cost, $\mathcal{J}_t(s, a)$

$$V_t^*(s) = V_t^*(s_t, \pi_t^{p_1}, \pi_t^{p_2}) = \min_{\pi^{p_1} \in \Pi^{p_1}} \max_{\pi^{p_2} \in \Pi^{p_2}} V_t^*(s_t, \pi^{p_1}, \pi^{p_2})$$
$$\forall s_t \in \mathcal{S}, \pi^{p_1} \in \Pi^{p_1}, \pi^{p_2} \in \Pi^{p_2}.$$

such that

$$V_{p_1}^* \leq V^* \leq V_{p_2}^* \quad \forall \{\pi_t^{p_1}, \pi_t^{p_2}\}_{0 \leq t \leq T}.$$

where $V_{p_i}^*$ are the respective optimal values for each player.

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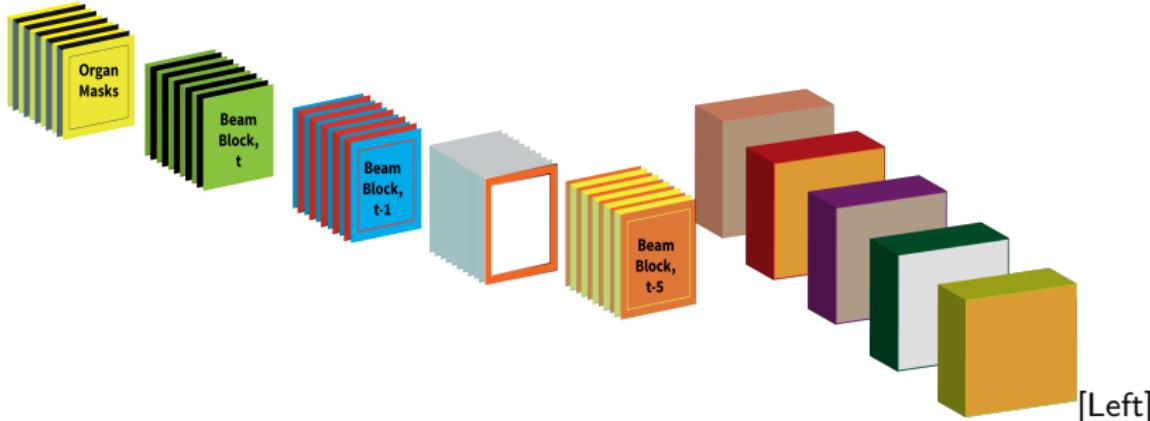
Adaptive

NeuroControl

Neural Network Model

- Under ideal conditions, we'd like to find the optimal value function under perfect play
- **Caveat:** BOO exhibits Bellman's curse of dimensionality.
- What to do?
 - derive an **approximately optimal** value $V_\psi^*(s)$
 - by continually estimating the value function $v_\psi^P(s)$ using e.g. a policy parameterized by a large function approximator

State Representation



Concatenation of the target volume masks and the beam angles before feeding the input planes to the residual tower neural network. The first six planes (top-most mask of left figure) contain the delineated organs and the PTV. This is concatenated with a block of m beams from the current time step, regressed to the previous 5 time steps (here, 5 was heuristically chosen). [Right]: Each beam angle in a beam block is represented as shown. Together with the target volume, these form an input plane of size $36 \times N \times W \times H$ to the policy/value neural network tower of residual blocks.

Methods: Search

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- Formulated as a bandit search that imposes a regret term on the Q -value
- During the planning process, we estimate a *value*, $v(\mathbf{y}_t)$, that estimates the optimality of a beam block;
- In parallel, we refine the deep neural network policy by optimizing its weight in a separate thread.
 - This player's weights are continually written to a shared memory such that its values are available to the MCTS search thread.
 - Network parameters updated by a **mixed strategy** which combines its **pure strategy**, which is a best response to the **average pure strategy** of a fictitious opponent.

Methods: Search

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- Q -value defined as

$$\bar{Q}(s, a) = Q_j(s, a) + c \sqrt{\frac{2 \ln n(s)}{N(s, a)}}, \quad (9)$$

$$a^* = \arg \max_a \bar{Q}(s, a) \quad (10)$$

Fluence Map Optimization

- Suppose \mathcal{X} is the total discretized of voxels of interest (*VOI's*) in a target volume
- Suppose $\mathcal{B}_1 \cup \mathcal{B}_2 \cup \dots \cup \mathcal{B}_n \subseteq \mathcal{B}$ represents the partition subset of a beam \mathcal{B} ,
 - where n is the total number of beams from which radiation can be delivered

Methods: Fluence Map Optimization

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- Suppose further that $\mathcal{D}_{ij}(\theta_k)$ is the matrix that describes each dose influence, d_i .
 - delivered to a discretized voxel, i , in a volume of interest, VOI_h ($h = 1, \dots, \mathcal{X}$), from a beam angle, θ_k ,
 $k \in \{1, \dots, n\}$
- We compute the matrix $\mathcal{D}_{ij}(\theta_k)$ by calculating each d_i for every bixel, j , at every φ° , resolution, where $j \in \mathcal{B}_k$
 - ending up with an ill-conditioned (*sparse*) matrix, $\mathcal{D}_{ij}(\theta_k)$, which consists of the dose to every voxel, i , incident from a beam angle, θ_k at every $360^\circ/\varphi^\circ$

Methods: FMO problem definition

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- The pre-calculated dose term is given by
$$\mathbf{Ax} = \left\{ \sum_s \frac{w_s}{v_s} \mathcal{D}_{ij}^s \mathbf{x}_s \mid \mathcal{D}_{ij} \in \mathbb{R}^{n \times l}, n > l \right\}$$
- Let $w_s = \{\underline{w}_s, \bar{w}_s\}$ be the respective underdosing and overdosing weights for the OARs and PTVs, and v_s represents the total number of voxels in each structure.
- We propose the following cost

$$\frac{1}{v_s} \sum_{s \in \text{OARs}} \|(\mathbf{b}_s - \underline{w}_s \mathcal{D}_{ij}^s \mathbf{x}_s)_+\|_2^2 + \frac{1}{v_s} \sum_{s \in \text{PTVs}} \|(\bar{w}_s \mathcal{D}_{ij}^s \mathbf{x}_s - \mathbf{b}_s)_+\|_2^2 \quad (11)$$

Methods: FMO

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- Rewriting the objective, subject to nonnegative pixel intensity constraints, we have the minimization problem

$$\min \frac{1}{2} \|Ax - b\|_2^2 \quad \text{subject to } x \geq 0.$$

- The Lagrangian becomes

$$L(x, \lambda) = \min \frac{1}{2} \|Ax - b\|_2^2 - \lambda^T x.$$

- Since we are solving a large scale problem, we use the ADMM algorithm
- Introducing an auxiliary variable z , we have

$$\min_x \frac{1}{2} \|Ax - b\|_2^2, \quad \text{subject to } z = x, \quad z \geq 0,$$

Methods: FMO

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- Solving either the \mathbf{x} and \mathbf{z} sub-problems, we have

$$\mathbf{x}^{k+1} = (\mathbf{A}^T \mathbf{A} + \rho \mathbf{I})^{-1} (\mathbf{A}^T \mathbf{b} + \rho \mathbf{z}^k - \boldsymbol{\lambda}^k). \quad (12)$$

- And using the soft-thresholding operator, $S_{\boldsymbol{\lambda}/\rho}$, we find that

$$\mathbf{z}^{k+1} = S_{\boldsymbol{\lambda}/\rho} (\mathbf{x}^{k+1} + \boldsymbol{\lambda}^k), \quad (13)$$

where $S_{\boldsymbol{\lambda}/\rho}(\tau) = (\mathbf{x} - \boldsymbol{\lambda}/\rho)_+ - (-\tau - \boldsymbol{\lambda}/\rho)_+$. $\boldsymbol{\lambda}$ is updated as

$$\boldsymbol{\lambda}^{k+1} = \boldsymbol{\lambda}^k - \gamma (\mathbf{z}^{k+1} - \mathbf{x}^{k+1}), \quad (14)$$

where γ is a parameter that controls the step length.

Game Tree Simulation

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- For b^d possible move sequences for a robot-patient setup
 - b = beam angles chosen to construct a fluence
 - d = is the total number of discretized angles.
- Suppose $b = 180$ and $d = 5$, we have 180^5 possible search directions
- Exhaustive search becomes real-time infeasible.

Game Tree Simulation; Approach

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- Simulate a game of **perfect recall**
 - a sequential simulation of different beam angle combinations g
 - guided by probabilities obtained from a two-player zero-sum game of neural FSP
- the probability distribution is over the possible beam angle subsets, θ^j , in the beam angle space, , Θ
- This strongly discourages classical beam s approaches

Game Tree Simulation

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- Network roll-out policy then efficiently guides the tree's game, Γ toward a *best-first* set of beam angle candidates
- Best-first leaf node encountered is the child node with the highest reward in the tree
- Essentially, a sampling-based lookout algorithm
 - Focuses learning on regions of the state space that are likely to have a good fluence

MCTS Simulation

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- After each simulation iteration, a ‘best move’ for the current beam block is selected, as computed by the tree search
- Four steps are applied at each iteration of the simulation for each player in $\{p_1, p_2\}$, viz,
 - *Selection*: starting at a root node, we recursively apply a child selection policy to navigate the branches of the tree until an expandable node is encountered.
 - *Expansion*: we iteratively add one or more children to the current node, based on the available move probabilities

MCTS

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■ MCTS Steps (cont'd)

- *Simulation*: a simulation from the beam angles in the new node is carried out to determine the optimal fluence objective function
- *Back-up*: from the *leaf node* (encountered during the expansion procedure), the lookout simulation is “backed up” through its direct nodal ancestors – updating each node’s statistics as we traverse the current node up to the root node.

Deep BOO MCTS Algorithm

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Algorithm 1 Deep BOO Monte Carlo Tree Search

```
function MCTS( $x_0, c$ )
     $x_0 \leftarrow x_0(s_0)$ 
    while search_time < budget
    do
         $\bar{x} \leftarrow EXPAND\_POLICY(x_0, c)$ 
         $\bar{x}.r \leftarrow FMO\_POLICY(\bar{x})$ 
        BACKUP( $\bar{x}, \bar{x}.r$ )
    end while
    return BEST_CHILD( $x_0$ )
end function

function FULLY_EXPANDED( $x, d$ )
     $d_i \leftarrow pairwise\_distance(x.s)$ 
    min_elem  $\leftarrow \min(d_i)$ 
    if min_elem < d then
        return True
    else
        return False
    end if
end function

function EXPAND( $x, c$ )
     $\tilde{a} = SELECT\_MOVE(x, c)$ 
    sample  $\tilde{f}$  with  $x.p(s, a)$ 
    update  $\tilde{\theta} \leftarrow \tilde{\theta} + \tilde{a}$ 
    with  $\pi_{t-1}$ , create  $\tilde{x}.p(\tilde{x}, \tilde{a})$ 
    while not  $\tilde{x} \in x_0$  do
        add  $\tilde{x}$  to  $x$ 
    end while
    return  $\tilde{x}$ 
end function

function EXPAND_POLICY( $x, c$ )
    while  $x$  nonterminal do
        if  $x$  not f_expanded then
            return EXPAND( $x, c$ )
        else
             $x \leftarrow BEST\_CHILD(x)$ 
        end if
    end while
    return  $x$ 
end function

function BACK_UP( $x, \bar{x}.r$ )
    while  $\bar{x}$  not null do
         $N(\bar{x}) \leftarrow \bar{x} + 1$ 
         $Q(\bar{x}) \leftarrow Q(\bar{x}) + \bar{x}.r$ 
         $\bar{x} = parent of \bar{x}$ 
    end while
end function

function BEST_CHILD( $x_0$ )
    if  $p_1$  to play then
        return  $x_0[\arg\min children of x_0.r]$ 
    else
        return  $x_0[\arg\max children of x_0.r]$ 
    end if
end function
```

where $K(\bar{x}) = c\sqrt{\frac{2 \ln n(\bar{x}.s)}{N(\bar{x}.s, a)}}$ and $\bar{x} \in x$ implies $\bar{x} \in children of x$.

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- Start by randomly adding five beam blocks to the state queue
- Input planes are passed through the tower residual network, from which probability distributions and a value are predicted
- Add a random walk sequence to the generated pure strategy
- Construct tree with this mixed strategy
- As new beam angle combinations are found according to the MCTS Algorithm, the FIFO queue is updated

Example Target Volumes

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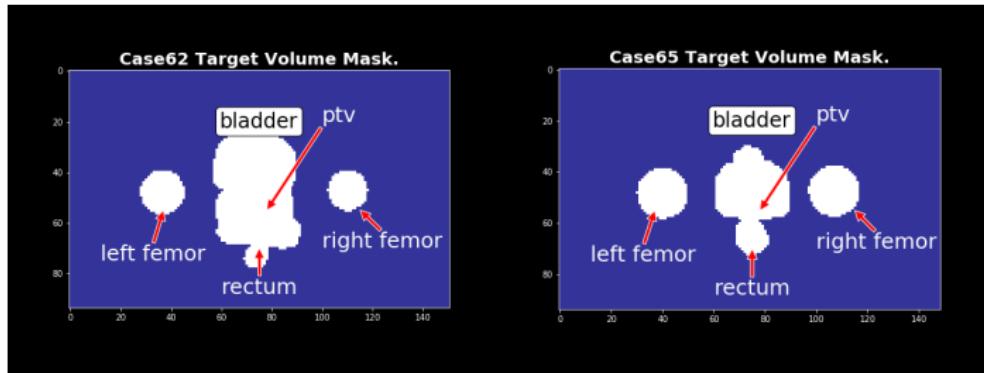
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Example Target Volumes. The PTV is engulfed within the bladder in all cases.

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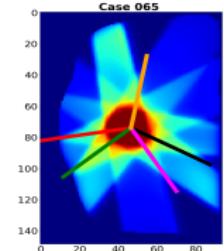
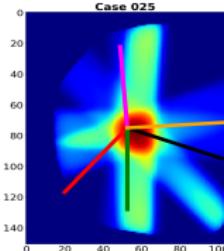
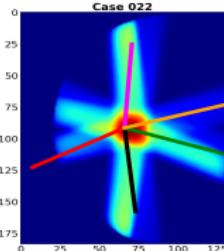
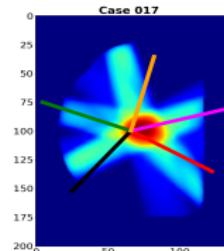
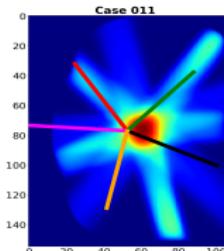
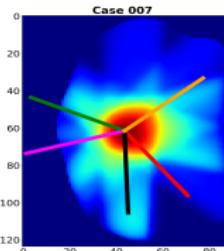
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Dose washes for select patients during training of the self-play network

Training Regime



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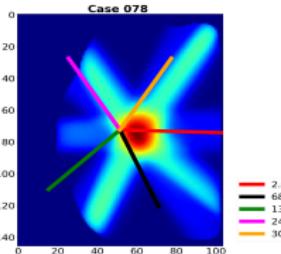
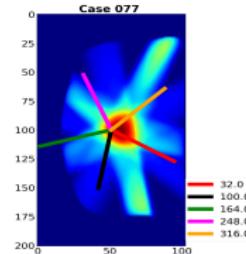
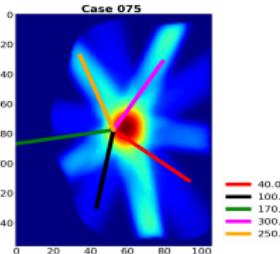
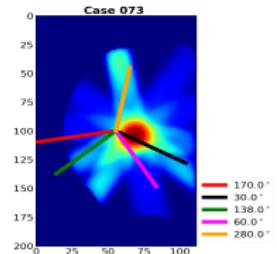
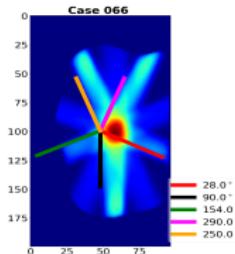
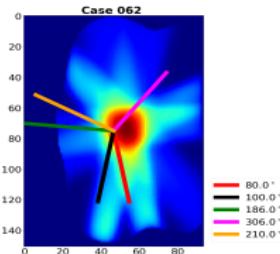
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Inference Regime



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- Adopt best practices from one of the SOTA modeling approaches viz
 - *finite element methods* Coevoet et al. (2017); Bern et al. (2017),
 - constant curvature approach Godage et al. (2016),
 - the continuous Cosserat approach Renda et al. (2014), and
 - the multi-body hyper-redundant model Kang et al. (2012).

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Marios M Polycarpou and Petros A Ioannou. Modelling, Identification And Stable Adaptive Control Of Continuous-time Nonlinear Dynamical Systems Using Neural Networks. In *American Control Conference, 1992*, pages 36–40. IEEE, 1992.

Olalekan Ogunmolu, Nicholas Gans, and Tyler Summers. Minimax iterative dynamic game: Application to nonlinear robot control tasks. *IEEE International Conference on Robots and Intelligent Systems, (IROS), Madrid, 2018.*, 2018.

Steve Webb. *Intensity-Modulated Radiation Therapy*. Institute of Physics Publishing Ltd, Bristol and Philadelphia, 2001.

Rodney D Wiersma, Zhifei Wen, Meredith Sadinski, Karl Farrey, and Kamil M Yenice. Development of a frameless stereotactic radiosurgery system based on real-time 6d



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position monitoring and adaptive head motion compensation. *Physics in Medicine & Biology*, 55(2):389, 2009.

Laura I Cerviño, Todd Pawlicki, Joshua D Lawson, and Steve B Jiang. Frame-less and mask-less cranial stereotactic radiosurgery: a feasibility study. *Physics in medicine and biology*, 55(7):1863, 2010.

Xinmin Liu, Andrew H Belcher, Zachary Grelewicz, and Rodney D Wiersma. Robotic Stage for Head Motion Correction in Stereotactic Radiosurgery. In *American Control Conference (ACC)*, 2015, pages 5776–5781. IEEE, 2015.

Mark Ostyn, Thomas Dwyer, Matthew Miller, Paden King, Rachel Sacks, Ross Cruikshank, Melvin Rosario, Daniel Martinez, Siyong Kim, and Woon-Hong Yeo. An



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electromechanical, patient positioning system for head and neck radiotherapy. *Physics in Medicine & Biology*, 62(18): 7520, 2017.

Olalekan Ogunmolu, Adwait Kulkarni, Yonas Tadesse, Xuejun Gu, Steve Jiang, and Nicholas Gans. Soft-neuroadapt: A 3-dof neuro-adaptive patient pose correction system for frameless and maskless cancer radiotherapy. In *Intelligent Robots and Systems (IROS), 2017 IEEE/RSJ International Conference on*, pages 3661–3668. IEEE, 2017.

Johannes Heinrich, Marc Lanctot, and David Silver. Fictitious self-play in extensive-form games. In *International Conference on Machine Learning*, pages 805–813, 2015.

Eulalie Coevoet, Adrien Escande, and Christian Duriez. Optimization-based inverse model of soft robots with



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contact handling. *IEEE Robotics and Automation Letters*, 2(3):1413–1419, 2017.

James M Bern, Grace Kumagai, and Stelian Coros.

Fabrication, modeling, and control of plush robots. In *Intelligent Robots and Systems (IROS), 2017 IEEE/RSJ International Conference on*, pages 3739–3746. IEEE, 2017.

Isuru S Godage, Gustavo A Medrano-Cerda, David T Branson, Emanuele Guglielmino, and Darwin G Caldwell. Dynamics for variable length multisection continuum arms. *The International Journal of Robotics Research*, 35(6):695–722, 2016.

Federico Renda, Michele Giorelli, Marcello Calisti, Matteo Cianchetti, and Cecilia Laschi. Dynamic model of a multibending soft robot arm driven by cables. *IEEE Transactions on Robotics*, 30(5):1109–1122, 2014.

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Rongjie Kang, David T Branson, Emanuele Guglielmino, and Darwin G Caldwell. Dynamic modeling and control of an octopus inspired multiple continuum arm robot. *Computers & Mathematics with Applications*, 64(5):1004–1016, 2012.

Federico Renda, Vito Cacucciolo, Jorge Dias, and Lakmal Seneviratne. Discrete cosserat approach for soft robot dynamics: A new piece-wise constant strain model with torsion and shears. In *Intelligent Robots and Systems (IROS), 2016 IEEE/RSJ International Conference on*, pages 5495–5502. IEEE, 2016.

Federico Renda and Lakmal Seneviratne. A Geometric and Unified Approach for Modeling Soft-Rigid Multi-body Systems with Lumped and Distributed Degrees of Freedom. *2018 IEEE International Conference on Robotics and Automation (ICRA)*, pages 1567 – 1574, 2018.



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Juan Carlos Simo and Loc Vu-Quoc. On the dynamics in space of rods undergoing large motions—a geometrically exact approach. *Computer methods in applied mechanics and engineering*, 66(2):125–161, 1988.