

Verification of complex systems in Stainless

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Abstract

(TODO: Abstract)

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1 Introduction

(TODO: Introduction)

2 Program Verification with Stainless

(TODO: Describe Stainless/Inox pipeline)

3 Symbolic Evaluation of Inox Programs

3.1 Motivation

While one would expect the following program to successfully verify in a fair amount of time, Stainless is actually unable to automatically prove the verification condition corresponding to `test`'s postcondition.

```
def foldLeft[A](list: List[A], z: B)(f: (B, A) => B): B = list match {
  case Nil() => z
  case Cons(x, xs) => foldLeft(xs, f(z, x))(f)
}

def insert[A, B](values: List[(A, B)], map: Map[A, B]) = {
  foldLeft(xs, map) {
    case (acc, (k, v)) => acc.updated(k, v)
  }
}

def test(map: Map[String, Int]): Boolean = {
  val xs = List("a" -> 1, "b" -> 2, "c" -> 3, "d" -> 4)
  val res = insert(xs, map)
  res("b") == 2
}.holds
```

On the other hand, if one were to manually unfold `insert`, then unfold `foldLeft` as much as possible in the program above, one would end up with the following definition for the `test` function, the postcondition of which would then promptly verify.

```
def test(map: Map[String, Int]): Boolean = {
  val res = map.updated("a", 1).updated("b", 2).updated("c", 3).updated("d", 4)
  res("b") == 2
}.holds
```

Indeed, while the `map` variable is kept abstract, the list of values `xs` we want to insert is not, and it is thus possible to simplify the initial program, yielding to a much simpler verification condition.

It is of course unreasonable to ask users to manually perform such a transformation, especially with large programs, hence why we decided to investigate a way to do so automatically, as part of the verification pipeline.

(TODO: ...)

Let's first take a look at how the *PureScala* program above looks when expressed in Inox' input language:

```
def foldLeft[A](list: List[A], z: B)(f: (B, A) => B): B =
  if (list.isInstanceOf[Nil[A]]) {
    z
  } else {
    val x = list.asInstanceOf[Cons[A]].head
    val xs = list.asInstanceOf[Cons[A]].tail
```

```

    foldLeft(xs, f(z, x))(f)
  }
}

def insert[A, B](values: List[(A, B)], map: Map[A, B]) = {
  foldLeft(xs, map, (acc: Map[A, B], kv: (A, B)) => acc.updated(kv._1, kv._2))
}

def test(map: Map[String, Int]): Boolean = {
  val xs = List("a" -> 1, "b" -> 2, "c" -> 3, "d" -> 4)
  val res = insert(xs, map)
  res("b") == 2
}.holds

```

3.2 Semantics

The symbolic evaluator keeps track of the current *path condition*, denoted by Δ . Figure 1 lists the evaluation rules for the symbolic evaluator. Since most of those are fairly straightforward, we will only focus on rules (21), (22) and (23), which pertain to functions invocations.

$\frac{e \in \Delta}{\llbracket e; \Delta \rrbracket \rightarrow \text{true}}$	(1)
$\frac{\neg e \in \Delta}{\llbracket e; \Delta \rrbracket \rightarrow \text{false}}$	(2)
$\overline{\llbracket \lambda x_1, \dots, x_n. e; \Delta \rrbracket \rightarrow \lambda \llbracket x_1; \Delta \rrbracket, \dots, \llbracket x_n; \Delta \rrbracket. \llbracket e; \Delta \rrbracket}$	(3)
$\overline{\llbracket l ==> r; \Delta \rrbracket \rightarrow \llbracket \neg l \mid \mid r; \Delta \rrbracket}$	(4)
$\frac{\llbracket c; \Delta \rrbracket \rightarrow \text{true}}{\llbracket \text{if } (c) \ t \ \text{else } e; \Delta \rrbracket \rightarrow \llbracket t; \Delta \cup c \rrbracket}$	(5)
$\frac{\llbracket c; \Delta \rrbracket \rightarrow \text{false}}{\llbracket \text{if } (c) \ t \ \text{else } e; \Delta \rrbracket \rightarrow \llbracket e; \Delta \cup c \rrbracket}$	(6)
$\frac{\llbracket c; \Delta \rrbracket \rightarrow c' \quad \llbracket t; \Delta \cup c' \rrbracket \rightarrow t' \quad \llbracket e; \Delta \cup \neg c' \rrbracket \rightarrow e' \quad t' = e'}{\llbracket \text{if } (c) \ t \ \text{else } e; \Delta \rrbracket \rightarrow t'}$	(7)
$\frac{\llbracket c; \Delta \rrbracket \rightarrow c' \quad \llbracket t; \Delta \cup c' \rrbracket \rightarrow t' \quad \llbracket e; \Delta \cup \neg c' \rrbracket \rightarrow e' \quad t' \neq e'}{\llbracket \text{if } (c) \ t \ \text{else } e; \Delta \rrbracket \rightarrow \text{if } (c') \ t' \ \text{else } e'}$	(8)
$\frac{\llbracket p; \Delta \rrbracket \rightarrow \text{true}}{\llbracket \text{assume}(p, e); \Delta \rrbracket \rightarrow \llbracket e; \Delta \rrbracket}$	(9)
$\frac{\llbracket p; \Delta \rrbracket \rightarrow \text{false}}{\llbracket \text{assume}(p, e); \Delta \rrbracket \rightarrow \text{assume}(\text{false}, \llbracket e; \Delta \rrbracket)}$	(10)
$\frac{\llbracket p; \Delta \rrbracket \rightarrow p'}{\llbracket \text{assume}(p, e); \Delta \rrbracket \rightarrow \text{assume}(p', \llbracket e; \Delta \cup p' \rrbracket)}$	(11)
$\frac{T_2 : \text{ADTType} \quad \neg \text{isSort}(T_2)}{\llbracket C(T_1, a_1, \dots, a_n). \text{isInstanceOf}[T_2]; \Delta \rrbracket \rightarrow T_1.\text{id} == T_2.\text{id}}$	(12)
$\frac{T : \text{ADTType} \quad \text{isSort}(T)}{\llbracket e.\text{isInstanceOf}[T]; \Delta \rrbracket \rightarrow \text{true}}$	(13)
$\frac{T : \text{ADTType} \quad \llbracket e; \Delta \rrbracket \rightarrow e' \quad \text{isInstanceOf}(e', T, \Delta) == \text{Some}(b)}{\llbracket e.\text{isInstanceOf}[T]; \Delta \rrbracket \rightarrow b}$	(14)
$\frac{T : \text{ADTType} \quad \llbracket e; \Delta \rrbracket \rightarrow e' \quad \text{isInstanceOf}(e', T, \Delta) == \text{None}}{\llbracket e.\text{isInstanceOf}[T]; \Delta \rrbracket \rightarrow e'.\text{isInstanceOf}[T]}$	(15)
$\frac{T : \text{ADTType}}{\llbracket e.\text{asInstanceOf}[T]; \Delta \rrbracket \rightarrow \llbracket e; \Delta \rrbracket.\text{asInstanceOf}[T]}$	(16)

Figure 1: Operational semantics of the symbolic evaluator

$$\overline{\llbracket \text{let } x:\tau = v \text{ in } e; \Delta \rrbracket} \longrightarrow \overline{\llbracket e[x/v]; \Delta \rrbracket} \quad (17)$$

$$\overline{\llbracket \neg e; \Delta \rrbracket} \longrightarrow \neg \overline{\llbracket e; \Delta \rrbracket} \quad (18)$$

$$\frac{\llbracket f; \Delta \rrbracket \longrightarrow \lambda x_1:\tau_1, \dots, x_n:\tau_n. b \quad \llbracket e_i; \Delta \rrbracket \longrightarrow \llbracket e'_i; \Delta \rrbracket, i \in \{1 \dots n\}}{\llbracket f(e_1, \dots, e_n); \Delta \rrbracket \longrightarrow \llbracket b[x_1/e'_1, \dots, x_n/e'_n]; \Delta \rrbracket} \quad (19)$$

$$\frac{\llbracket f; \Delta \rrbracket \longrightarrow f' \quad \llbracket e_i; \Delta \rrbracket \longrightarrow \llbracket e'_i; \Delta \rrbracket, i \in \{1 \dots n\}}{\llbracket f(e_1, \dots, e_n); \Delta \rrbracket \longrightarrow f'(e'_1, \dots, e'_n)} \quad (20)$$

$$\frac{\neg \text{isRecursive}(\text{id}) \quad \text{id.params} = \langle x_1, \dots, x_n \rangle \quad \llbracket e_i; \Delta \rrbracket \longrightarrow \llbracket e'_i; \Delta \rrbracket, i \in \{1 \dots n\}}{\llbracket \text{id}(e_1, \dots, e_n); \Delta \rrbracket \longrightarrow \llbracket \text{id.body}[x_1/e'_1, \dots, x_n/e'_n]; \Delta \rrbracket} \quad (21)$$

$$\frac{\text{id.body} \Downarrow \Delta \uplus \{x_i \mapsto e'_i \mid 1 \leq i \leq n\} \quad \text{id.params} = \langle x_1, \dots, x_n \rangle \quad \llbracket e_i; \Delta \rrbracket \longrightarrow \llbracket e'_i; \Delta \rrbracket, i \in \{1 \dots n\}}{\llbracket \text{id}(e_1, \dots, e_n); \Delta \rrbracket \longrightarrow \llbracket \text{id.body}[x_1/e'_1, \dots, x_n/e'_n]; \Delta \rrbracket} \quad (22)$$

$$\frac{\llbracket e_i; \Delta \rrbracket \longrightarrow \llbracket e'_i; \Delta \rrbracket, i \in \{1 \dots n\}}{\llbracket \text{id}(e_1, \dots, e_n); \Delta \rrbracket \longrightarrow \text{id}(e'_1, \dots, e'_n)} \quad (23)$$

Figure 1: Operational semantics of the symbolic evaluator

3 Symbolic Evaluation of Inox Programs

3.3 Case Studies

(TODO: Case Studies)

3.4 Conclusion

(TODO: Conclusion)

3.5 Further Work

(TODO: Further work)

4 Verifying Actor Systems

4.1 Motivation

(TODO: Motivation)

4.2 The Actor Model

(TODO: Actor Model)

4.3 Our Framework

Message

In our framework, messages are modelled as constructors of the `Msg` abstract class.

```
abstract class Msg
case class Hello(name: String) extends Msg
```

Actor Reference

Each actor is associated with a unique and persistent reference, modelled as an instance of the `ActorRef` abstract class.

```
abstract class ActorRef
case class Primary() extends ActorRef
```

In-flight Messages

In-flight messages are represented as a product of the `ActorRef` of the destination actor, and the message itself.

```
case class Packet(dest: ActorRef, payload: Msg)
```

Actor Context

When a message is delivered to an actor, the latter is provided with a context, which holds a reference to itself, and a mutable list of `Packets` to send.

```
case class ActorContext(
  self: ActorRef,
  var toSend: List[Packet]
)
```

Behavior

A behavior specifies both the current state of an actor, and how this one should process the next incoming message. In our framework, these are modelled as a subclass of the abstract class `Behavior`, which defines a single abstract method `processMsg`, to be overridden for each defined behavior.

Using the provided `ActorContext`, the implementation of the `processMsg` method can both access its own reference, and register messages to be sent after the execution of the method is complete. It is also required to return a new `Behavior`

```
abstract class Behavior {
  def processMsg(msg: Msg)(implicit ctx: ActorContext): Behavior
}
```

Actor System

The state of the Actor system at a given point in time is modelled as a case class, holding the behavior associated with each actor reference, and the list of in-flight messages between any two actors.

```
case class ActorSystem(
  behaviors: CMap[ActorRef, Behavior],
  inboxes: CMap[(ActorRef, ActorRef), List[Msg]]
)
```

The `ActorSystem` class is equipped with a `step` method, which takes a pair of `ActorRef` as arguments, and is in charge of delivering the oldest message found in the corresponding inbox, and which returns the new state of the system after the aforementioned message has been processed.

```
def step(from: ActorRef, to: ActorRef): ActorSystem
```

4.4 Operational Semantics

We formulate the small-step operational semantics of our Actor model in Figure 2, where $s : \text{ActorSystem}$ is an Actor system, $m : \text{Msg}$ is a message, $n, n_{to}, n_{from} : \text{ActorRef}$ are references, $b, b' : \text{Behavior}$ are behaviors, $ps : \text{List}[\text{Packet}]$ a list of packets to send, $c : \text{ActorContext}$ is a context, and $\emptyset_n : \text{ActorContext}$ is the empty context for an actor whose self-reference is n , defined as $\emptyset_n := \text{ActorContext}(n, \text{Nil})$.

4.5 Proving Invariants

After having defined an Actor system with our framework, one might want to verify that this system preserves some invariant between each step of its execution. That is to say, for an `ActorSystem` s , any two `ActorRef` n, m , and an invariant $\text{inv} : \text{ActorSystem} \rightarrow \text{Boolean}$, if $\text{inv}(s)$ holds, then $\text{inv}(s.\text{step}(n, m))$ should hold as well. We express this property more formally in Figure 3. This property can be easily expressed in PureScala, as shown in Listing 1.

When encountering such a definition, Stainless will generate a verification condition equivalent to Figure 3, which will then be discharged to Inox and the underlying SMT solver.

4.6 Case studies

4.6.1 Increment-based Replicated Counter

As a first and very simple case study, we will study an Actor system which models a replicated counter, which can only be incremented by one unit. This system is composed of two actors, a primary counter whose reference is `Primary()`, and a backup counter whose reference is `Backup()`.

$\frac{\nexists m \in s.\text{inboxes}(n_{from}, n_{to})}{\langle s.\text{step}(n_{from}, n_{to}) \rangle \longrightarrow s}$	(STEP-NOMSG)
$\frac{\exists m \in s.\text{inboxes}(n_{from}, n_{to}) \quad \langle s.\text{deliverMsg}(n_{to}, n_{from}, m) \rangle \Rightarrow (b, ps, t)}{\langle s.\text{step}(n_{from}, n_{to}) \rangle \longrightarrow s \uplus (n_{to} \mapsto b, \dots, t)}$	(STEP)
$\frac{\langle s.\text{behaviors}(n_{to}).\text{processMsg}(m, \emptyset_{n_{to}}) \rangle \longrightarrow (b, c)}{\langle s.\text{deliverMsg}(n_{to}, n_{from}, m) \rangle \longrightarrow (b, c.\text{toSend}, t)}$	(DELIVER-MSG)
$\frac{b.\text{processMsg}(m, \emptyset_{n_{to}}) = [i_1, \dots, i_n, b'] \quad \emptyset_{n_{to}} \vdash \langle [i_1, \dots, i_n] \rangle \Rightarrow c}{\langle b.\text{processMsg}(m, \emptyset_{n_{to}}) \rangle \longrightarrow (b', c)}$	(PROCESS-MSG)
$\overline{\langle \text{Nil}, c \rangle \Rightarrow c}$	(I-NIL)
$\frac{\langle i, c \rangle \Rightarrow c'}{\langle i :: is, c \rangle \Rightarrow \langle is, c' \rangle}$	(I-CONS)
$\overline{\langle n ! m, c \rangle \Rightarrow (b', c.\text{copy}(\text{toSend} \mapsto (n, m) :: c.\text{toSend}))}$	(I-SEND)

Figure 2: Operational semantics

$$\forall s : \text{ActorSystem}, n : \text{ActorRef}, m : \text{ActorRef}. \text{inv}(s) \implies \text{inv}(s.\text{step}(n, m))$$

Figure 3: Invariant preservation property

```

def inv(s: ActorSystem): Boolean = {
  /* ... */
}

def preserveInv(s: ActorSystem, n: ActorRef, m: ActorRef): Boolean = {
  require(inv(s))
  inv(s.step(n, m))
} holds

```

Listing 1: Invariant preservation theorem in PureScala

Each of these reference is associated with a behavior: the primary counter reference with an instance of `PrimaryB`, and the backup counter reference with an instance of `BackupB`, both of which hold a positive integer, representing the value of the counter. Whenever the primary actor receives a message `Inc()`, it forwards that message to the backup actor, and returns a new

instance of `PrimaryB` with the counter incremented by one. When the backup actor receives an `Inc()` message, it just returns a new instance of `BackupB` with the counter incremented by one. The corresponding PureScala implementation can be found in Listing 2.

```

case class Primary() extends ActorRef
case class Backup() extends ActorRef

case class Inc() extends Msg

case class PrimaryB(counter: BigInt) extends Behavior {
  require(counter >= 0)

  def processMsg(msg: Msg)(implicit ctx: ActorContext): Behavior = msg match {
    case Inc() =>
      Backup() ! Inc()
      PrimaryB(counter + 1)
  }
}

case class BackupB(counter: BigInt) extends Behavior {
  require(counter >= 0)

  def processMsg(msg: Msg)(implicit ctx: ActorContext): Behavior = msg match {
    case Inc() => BackupB(counter + 1)
  }
}

```

Listing 2: Replicated counter implementation (increment)

Given such a system, one might want to prove that the following invariant is preserved between each step of its execution:

```

def invariant(s: ActorSystem): Boolean = {
  s.inboxes((Backup(), Backup())).isEmpty && {
    (s.behaviors(Primary()), s.behaviors(Backup())) match {
      case (PrimaryB(p), BackupB(b)) =>
        p.value == b.value + s.inboxes(Primary() -> Backup()).length
      case _ => false
    }
  }
}

```

Listing 3: Replicated counter invariant (increment)

This invariant specifies that the `Backup()` actor does not send itself any messages, that both actors have the proper corresponding behavior, and that, last but not least, the value of the primary counter is equal to the value of the backup counter added to the number of messages that are yet to be delivered to the backup actor.

```
def preserveInv(s: ActorSystem, n: ActorRef, m: ActorRef): Boolean = {
  require(invariant(s))
  invariant(s.step(n, m))
} holds
```

Listing 4: Replicated counter theorem (increment)

We can now define the actual theorem we want Stainless to prove for us:
(TODO: Rep Counter Inc Result)

4.6.2 Delivery-based Replicated Counter

Listing 5 shows a variant of the previous case study, where instead of having the primary actor forward the Inc() message to the backup actor, the former instead sends the latter the new value.

```
case class Primary() extends ActorRef
case class Backup() extends ActorRef

case class Inc() extends Msg
case class Deliver(c: BigInt) extends Msg

case class PrimaryB(counter: BigInt) extends Behavior {
  def processMsg(msg: Msg)(implicit ctx: ActorContext): Behavior = msg match {
    case Inc() =>
      Backup() ! Deliver(counter + 1)
      PrimaryB(counter + 1)

    case _ => Behavior.same
  }
}

case class BackupB(counter: BigInt) extends Behavior {
  def processMsg(msg: Msg)(implicit ctx: ActorContext): Behavior = msg match {
    case Deliver(c) => BackupB(c)
    case _ => Behavior.same
  }
}
```

Listing 5: Replicated counter implementation (deliver)

The invariant now reads slightly differently, as can be seen in Listing 6.
(TODO: Rep Counter Del Result)

4.6.3 Lock Service

Listing 7 shows the implementation of a lock service using our framework. In this case study, an actor acts as a server holding a lock on some resource, while a number of other actors (the "agents") act as clients of the lock service, each potentially trying to acquire the lock on the

```

def invariant(s: ActorSystem): Boolean = {
  validBehaviors(s)                &&
  noMsgsToSelf(Primary()).isEmpty  &&
  noMsgsToSelf(Backup()).isEmpty   &&
  noMsgsToSelf(Backup() -> Primary()).isEmpty && {
    val PrimBehav(p) = s.behaviors(Primary())
    val BackBehav(b) = s.behaviors(Backup())
    val bInbox       = s.inboxes(Primary() -> Backup())

    p.value >= b.value && isSorted(bInbox) && bInbox.forall {
      case Deliver(Counter(i)) => p.value >= i
      case _                   => true
    }
  }
}

```

Listing 6: Replicated counter implementation (deliver)

resource. To model a variable number of actors with the same implementation, we define their reference as a case class parametrized by a (TODO: unique) identifier.

An obvious property we might want to prove is that, at any time, at most one of those agents thinks that it holds the lock. Additionally, we'd like to ensure that such an agent is actually the same one that the server granted the lock too. We express this property in Listing 8.

(TODO: Lock service invariant proof)

4.7 Spawning Actors

(TODO: Name Uniqueness)

Up until now, our framework has only been able to model Actor systems with a static topology, ie. systems where no new actors besides the ones that are statically defined can be spawned. Let's now attempt to enrich our model to account for dynamic topologies.

To this end, we modify the `ActorRef` definition to include both a name and an optional field holding a reference to its parent `ActorRef` if any. We also add a new constructor of the `ActorRef` data type, which will be assigned to actors spawned from another actor.

```

abstract class ActorRef(
  name: String,
  parent: Option[ActorRef]
)

case class Child(name: String, getParent: ActorRef)
  extends ActorRef(name, Some(getParent))

```

In order for actors to spawn other actors, by specifying their name and associated initial behavior, we modify the `ActorContext` class as follows:

```

case class ActorContext(
  self: ActorRef,
  var toSend: List[Packet],

```



```

var toSpawn: List[(ActorRef, Behavior)]
) {
  def spawn(behavior: Behavior, name: String): ActorRef = {
    val id: ActorRef = Child(name, self)
    toSpawn = toSpawn :+ (id, behavior)
    id
  }
  /* ... */
}

```

As can be seen in the listing above, the context now keeps track of the names and behaviors of the actors to be spawned, and provides a `spawn` method which is in charge of constructing the `ActorRef` of the spawned actor, storing it along with the behavior within the context, and returning the newly generated reference.

Let's now update the case study in Listing 2 to accommodate these changes, while noting that we are not making use of this new feature yet. Only the two `ActorRef` definitions need to be touched, becoming:

```

case class Primary() extends ActorRef("primary", None())
case class Backup()  extends ActorRef("backup", None())

```

Unfortunately, when we now feed the updated benchmark to Stainless, the latter is be unable to prove the very same theorem it previously had no issue whatsoever with. All is not lost though, as turning on the symbolic evaluator described in Section 3 enables Stainless to verify the program in less than 10 seconds.

Listing ?? defines a simple system with a dynamic topology, where one actor, deemed `Primary`, waits for a `Spawn` message to spawn a child actor, and change its behavior from `BeforeB` to `AfterB` in order to keep track of the reference to the child. The invariant we would to verify holds here, states that, if the `Primary` actor has behavior `BeforeB()`, then the behavior associated with the `ActorRef` of its child actor must be `Stopped`. On the other hand, if the `Primary` actor has behavior `AfterB(child)`, then the behavior associated with `child` must be `ChildB`. This test case verifies promptly, provided the symbolic evaluator is enabled.

4.8 Running an Actor System on Akka

While the verification of Actor systems is in itself an interesting endeavour, it is not of much use unless one is able to run these systems, potentially in a distributed environment. In the Scala ecosystem, the most widely used real-world Actor system is Akka (TODO: REF). Listing 9 shows a shallow shim which allows to run an Actor system developed with our framework within Akka, with only a few alterations to the original program.

(TODO: Explain shim)

To this end, one must define a subclass of `ActorSystem`, and provide an implementation of its `run` method. Within this method, one can spawn new top-level actors, get a reference to those, and send them messages. Listing 10 shows such an implementation for the replicated counter described in Section 4.6.1.

4.9 Conclusion

(TODO: Conclusion)

4.10 Further Work

(TODO: Further work)

```

case class Server() extends ActorRef
object Server {
  case class Lock(agent: ActorRef) extends Msg
  case class Unlock(agent: ActorRef) extends Msg
}

sealed abstract class AgentId

case class Agent(id: AgentId) extends ActorRef
object Agent {
  case object Lock extends Msg
  case object Unlock extends Msg
  case object Grant extends Msg
}

// The head of 'agents' holds the lock, the tail are waiting for the lock
case class ServerB(agents: List[ActorRef]) extends Behavior {

  def processMsg(msg: Msg)(implicit ctx: ActorContext): Behavior = msg match {
    case Server.Lock(agent) if agents.isEmpty =>
      agent ! Agent.Grant
      ServerB(List(agent))

    case Server.Lock(agent) =>
      ServerB(agents :+ agent)

    case Server.Unlock(agent) if agents.nonEmpty =>
      val newAgents = agents.tail
      if (newAgents.nonEmpty) newAgents.head ! Agent.Grant
      ServerB(newAgents)

    case _ =>
      Behavior.same
  }
}

case class AgentB(holdsLock: Boolean) extends Behavior {

  def processMsg(msg: Msg)(implicit ctx: ActorContext): Behavior = msg match {
    case Agent.Lock =>
      Server() ! Server.Lock(ctx.self)
      Behavior.same

    case Agent.Unlock if holdsLock =>
      Server() ! Server.Unlock(ctx.self)
      AgentB(false)

    case Agent.Grant =>
      AgentB(true)

    case _ =>
      Behavior.same
  }
}

```

Listing 7: Lock service implementation

```
def hasLock(s: ActorSystem, a: ActorRef): Boolean = {
  s.behaviors(a) match {
    case AgentB(hasLock) => hasLock
    case _ => false
  }
}

def mutex(s: ActorSystem): Boolean = forall { (a: ActorRef, b: ActorRef) =>
  (a != b) ==> !(hasLock(s, a) && hasLock(s, b))
}

def hasLockThenHead(s: ActorSystem): Boolean = forall { (ref: ActorRef) =>
  hasLock(s, ref) ==> {
    s.behaviors(Server()) match {
      case ServerB(Cons(head, _)) => head == ref
      case _ => false
    }
  }
}

def invariant(s: ActorSystem): Boolean = {
  mutex(s) && hasLockThenHead(s)
}
```

Listing 8: Lock service invariant

```

case object Primary extends ActorRef("primary")
case object Spawn extends Msg

case class BeforeB() extends Behavior {
  def processMsg(msg: Msg)(implicit ctx: ActorContext): Behavior = msg match {
    case Spawn =>
      val child = ctx.spawn(ChildB(), "child")
      AfterB(child)
  }
}

case class AfterB(child: ActorRef) extends Behavior {
  def processMsg(msg: Msg)(implicit ctx: ActorContext): Behavior = msg match {
    case _ => Behavior.same
  }
}

case class ChildB() extends Behavior {
  def processMsg(msg: Msg)(implicit ctx: ActorContext): Behavior = msg match {
    case _ => Behavior.same
  }
}

def invariant(s: ActorSystem): Boolean = {
  s.behaviors(Primary) match {
    case BeforeB() =>
      s.isStopped(Child("child", Primary()))
    case AfterB(child) =>
      s.behaviors(child) == ChildB()

    case _ => false
  }
}

def theorem(s: ActorSystem, from: ActorRef, to: ActorRef): Boolean = {
  require(invariant(s))
  invariant(s.step(from, to))
} holds

```

```

import akka.actor

type ActorRef = actor.ActorRef

case class ActorContext(self: actor.ActorRef, ctx: actor.ActorContext)

class Wrapper(var behavior: Behavior)
  extends actor.Actor with actor.ActorLogging {

  implicit val ctx = ActorContext(self, context)

  def receive = {
    case msg: Msg =>
      log.info(s"${behavior}: ${msg}")
      behavior = behavior.processMsg(msg)

    case _ => ()
  }
}

abstract class ActorSystem(val name: String) {
  lazy val system = actor.ActorSystem(name)

  def spawn(behavior: Behavior, name: String): actor.ActorRef = {
    system.actorOf(actor.Props(new Wrapper(behavior)), name = name)
  }

  def run(): Unit
}

```

Listing 9: Akka shim for our Actor system framework

```

@extern
object System extends ActorSystem("rep-counter-sys") {
  def run(): Unit = {
    val backup = spawn(BackupB(0), "backup")
    val primary = spawn(PrimaryB(0, backup), "primary")

    primary ! Inc()
  }
}

@extern
def main(args: Array[String]): Unit = {
  System.run()
}

```

Listing 10: Akka shim for our Actor system framework

5 Biparty Communication Protocols

5.1 Motivation

5.1.1 Session Types

(TODO: Session Types)

5.1.2 Value-level Encoding of Sessions

(TODO: Value-level Encoding of Sessions)

5.2 Linear Types in Stainless

We now discuss our implementation of linear types in Stainless. One thing to note is that because the AST we are working with within Stainless is already typed, there is no need to write a full-fledged type checker. We will hence rather describe a *linearity checker* for PureScala programs.

We introduce a way to mark some types as *linear*. To this end, we define a covariant type constructor `Linear`, which simply holds a value of type `A`. This type provides a `!` method to consume the linear term and return the underlying value. This enables the user to call a method of the underlying type in a concise way. As the astute reader might have noticed, this effectively adds weakening to the linear type system, and, as we will see, some care will be needed to handle such conversions properly. For example, if one had a value `foo` of type `Linear[Option[A]]`, one could call the `isEmpty` method on the underlying value by writing `foo!.isEmpty`. While making the consumption of a linear value explicit in this way is good for reasoning about one's code, there is still a bit of clutter associated with it, we also introduce an opt-in implicit conversion `delinearize` from any `Linear[A]` to `A`. At last, because converting a non-linear value of type `A` to a linear value of type `Linear[A]` is always safe, we provide a such an implicit conversion by default, `linearize`. Listing 11 shows the full definitions. Because those will be extracted in a specific way, they are marked `@ignore`.

We now describe what it means for a linear term to be *consumed*: a term `t` of type `Linear[A]`, for any type `A`, is deemed *consumed* in an expression `e` when any of the following propositions is true:

- The underlying value of type `A` is extracted, via the `!` method, eg. `e = t!`.
- The term is assigned to a variable, eg. `val s:Linear[A] = t`.
- The term is supplied as an argument to function, eg. given `def f(x:Linear[A]):B`, we have `e = f(t)`.
- The term is supplied as an argument to a constructor, eg. given `case class C(x: Linear[A])`, we have `e = C(t)`.

We now must ensure that no linear term can be *consumed* more than once. To this end, we must recursively walk down the track terms that have been consumed in a context so that we can disallow subsequent uses of those terms. We will denote this context by Δ .

```

package stainless

import stainless.lang._
import stainless.annotation._

package object linear {

  @ignore
  class Linear[+A](_value: A) {
    def != _value
  }

  @ignore
  implicit def linearize[A](value: A): Linear[A] = new Linear(value)

  object implicits {
    @ignore
    implicit def delinearize[A](lin: Linear[A]): A = lin!
  }
}

```

Listing 11: Linear wrapper for Scala types and values

5.3 Sessions Library in PureScala

Listing 12 shows the PureScala implementation of the *lchannels* library. For the purpose of verification, we do not need a full-fledged implementation, but only declarations mirroring the Scala library. This way, one could run their implementation with the original library by simply linking against both it and the Stainless library, without our implementation.

5.4 Case Studies

5.4.1 ATM Protocol

Let's consider a protocol involving an ATM and its user.

1. The user authenticates herself by sending the ATM both her card number and PIN.
2. If the authentication succeeds, the ATM displays a menu to the user, who can then choose to:
 - (a) Abort the process altogether.
 - (b) Ask for her account's balance, in which case the server will reply with the balance, and displays the menu again.
 - (c) If the authentication fails, the ATM notifies the user of the failure, and the process is aborted.

Listing 13 shows the encoding of such a specification using the library described in Section 5.3, while Listing 14 shows the corresponding valid implementation.

Now, let's consider the case where the programmer made a mistake while writing this code, and forgot to send back a failure notification when the authentication fails, such as in Listing 15.


```

type In[A] = Linear[InChan[A]]
type Out[A] = Linear[OutChan[A]]

@linear @library
class InChan[A] {

  @extern
  def receive(implicit d: Duration): Linear[A] = {
    ???
  }

  def ?[B](f: Linear[A] => B)(implicit d: Duration): B = {
    f(receive)
  }
}

@linear @library
class OutChan[A] {

  @extern
  def send(msg: A): Unit = {
    ???
  }

  def !(msg: A): Unit = {
    send(msg)
  }

  @extern
  def !![B](h: Out[B] => A): In[B] = {
    ???
  }

  @extern
  def create[B]() : (In[B], Out[B]) = {
    ???
  }
}

```

Listing 12: Sessions library in PureScala

The linearity checker will realize that the linear `cont` is not consumed in every branch of the pattern match, and will pinpoint its introduction:

```

Error: linear variable 'cont' of type 'Linear[OutChan[Response]]' is never used
      case Authenticate(_, _, cont) =>
                                ^^^^^

```

```

//Authentication request from the user
case class Authenticate(card: String, pin: String, cont: Out[Response])

// Authentication response from the ATM
sealed abstract class Response
case class Failure() extends Response
case class Success(cont: Out[Menu]) extends Response

// Choices available to authenticated user
sealed abstract class Menu
case class CheckBalance(cont: Out[Balance]) extends Menu
case class Quit() extends Menu

// User account balance
case class Balance(amount: BigInt)(cont: Out[Menu])

```

Listing 13: ATM protocol description

```

def atm(c: In[Authenticate]) = {
  c ? { auth => auth! match {
    case Authenticate(card, pin, cont) if authenticated(card, pin) =>
      cont !! Success(_) ? menu(card)

    case Authenticate(_, _, cont) =>
      cont ! Failure()
  } }
}

def menu(card: String)(menu: Linear[Menu]) = {
  menu! match {
    case CheckBalance(cont) =>
      cont !! Balance(balance(card))(-) ? menu(card)

    case Quit() => ()
  }
}

@extern
def authenticated(card: String, pin: String): Boolean = {
  /* ... */
}

@extern
def balance(card: String): BigInt = {
  /* ... */
}

```

Listing 14: ATM protocol implemenation

```
def atm(c: In[Authenticate]) = {  
  c ? { auth => auth! match {  
    case Authenticate(card, pin, cont) if authenticated(card, pin) =>  
      cont !! Success(_) ? menu(card)  
  
    case Authenticate(_, _, cont) =>  
      // forgot the send back a Failure message  
  } }  
}
```

Listing 15: Wrong implementation of the ATM protocol

5.4.2 TLS 1.2 Handshake

(TODO: TLS 1.2 Handshake)

5.5 Conclusion

(TODO: Conclusion)

5.6 Further Work

(TODO: Further Work)

6 Conclusion

(TODO: Conclusion)

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