



# HW 4 GROUP 5



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## Resources

Use the dataset SCM 651 Homework 4 Universal Bank.csv.

## Assignment What's due:

Submit a logit, probit, and neural network analysis of loan acquisition behavior **before the live class in week 10**. Suggested length is five pages, but should not exceed ten pages, single- spaced, 12-point font.

This is a group assignment; each student should upload a copy of the assignment to the Learning Management System. The paper must be a Microsoft Word document. You should also submit the Excel spreadsheet with the prediction models and sensitivity analyses. Name the file HW4\_Team# where # is your team number. Be sure to include the names of everyone on the team on the first page of the paper. Late assignments will not be accepted. Failure to follow directions will be penalized.

## Outline and grading criteria:

1. Perform a logit and probit analysis of the variables that affect whether a customer takes out a loan. Consider only main effects. Which variables are significant? How do the significant variables influence the likelihood of taking out a loan? Copy screen snapshots of your analysis in R to your report. (20%)

Preliminary Model to see which variables are significant:

```
call:
glm(formula = PersonalLoan ~ Age + Experience + Income + Family +
    CCAvg + Education + Mortgage + SecuritiesAccount + CDAccount +
    Online + CreditCard, family = binomial(logit), data = HW4Data)
```

Deviance Residuals:

| Min     | 1Q      | Median  | 3Q      | Max    |
|---------|---------|---------|---------|--------|
| -3.1558 | -0.2015 | -0.0796 | -0.0309 | 3.9298 |

Coefficients:

|                   | Estimate    | Std. Error | z value | Pr(> z ) |     |
|-------------------|-------------|------------|---------|----------|-----|
| (Intercept)       | -12.1926537 | 1.6451710  | -7.411  | 1.25e-13 | *** |
| Age               | -0.0536101  | 0.0613121  | -0.874  | 0.38191  |     |
| Experience        | 0.0637567   | 0.0609277  | 1.046   | 0.29536  |     |
| Income            | 0.0545810   | 0.0026201  | 20.831  | < 2e-16  | *** |
| Family            | 0.6957575   | 0.0743035  | 9.364   | < 2e-16  | *** |
| CCAvg             | 0.1239704   | 0.0396467  | 3.127   | 0.00177  | **  |
| Education         | 1.7361518   | 0.1150671  | 15.088  | < 2e-16  | *** |
| Mortgage          | 0.0004745   | 0.0005541  | 0.856   | 0.39190  |     |
| SecuritiesAccount | -0.9368084  | 0.2858666  | -3.277  | 0.00105  | **  |
| CDAccount         | 3.8225340   | 0.3239404  | 11.800  | < 2e-16  | *** |
| Online            | -0.6751707  | 0.1570775  | -4.298  | 1.72e-05 | *** |
| CreditCard        | -1.1197449  | 0.2049925  | -5.462  | 4.70e-08 | *** |

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 3162.0 on 4999 degrees of freedom  
Residual deviance: 1284.4 on 4988 degrees of freedom  
AIC: 1308.4

Number of Fisher Scoring iterations: 8

After this, the team also looked at a correlation matrix to further investigate which 2-4 variables are the most correlated with taking a personal loan:

|                   | Age           | CCAvg        | CDAccount    | CreditCard        |
|-------------------|---------------|--------------|--------------|-------------------|
| Age               | 1.0000000000  | -0.052012179 | 0.008042552  | 0.007681037       |
| CCAvg             | -0.0520121791 | 1.0000000000 | 0.136533655  | -0.006689494      |
| CDAccount         | 0.0080425521  | 0.136533655  | 1.0000000000 | 0.278644365       |
| CreditCard        | 0.0076810368  | -0.006689494 | 0.278644365  | 1.0000000000      |
| Education         | 0.0413343834  | -0.136123922 | 0.013933888  | -0.011014134      |
| Experience        | 0.9942148570  | -0.050076511 | 0.010353331  | 0.008967447       |
| Family            | -0.0464176636 | -0.109274506 | 0.014110365  | 0.011588066       |
| Income            | -0.0552686182 | 0.645983670  | 0.169738080  | -0.002385008      |
| Mortgage          | -0.0125385869 | 0.109904723  | 0.089311058  | -0.007230919      |
| Online            | 0.0137024021  | -0.003611009 | 0.175880016  | 0.004209656       |
| PersonalLoan      | -0.0077256172 | 0.366888736  | 0.316354829  | 0.002801509       |
| SecuritiesAccount | -0.0004362422 | 0.015086311  | 0.317034416  | -0.015028319      |
|                   | Education     | Experience   | Family       | Income            |
| Age               | 0.04133438    | 0.994214857  | -0.04641766  | -0.055268618      |
| CCAvg             | -0.13612392   | -0.050076511 | -0.10927451  | 0.645983670       |
| CDAccount         | 0.01393389    | 0.010353331  | 0.01411036   | 0.169738080       |
| CreditCard        | -0.01101413   | 0.008967447  | 0.01158807   | -0.002385008      |
| Education         | 1.000000000   | 0.013151813  | 0.06492891   | -0.187524257      |
| Experience        | 0.01315181    | 1.000000000  | -0.05256315  | -0.046574178      |
| Family            | 0.06492891    | -0.052563147 | 1.000000000  | -0.157500785      |
| Income            | -0.18752426   | -0.046574178 | -0.15750079  | 1.000000000       |
| Mortgage          | -0.03332712   | -0.010581552 | -0.02044493  | 0.206806228       |
| Online            | -0.01500382   | 0.013897900  | 0.01035404   | 0.014205919       |
| PersonalLoan      | 0.13672155    | -0.007413098 | 0.06136704   | 0.502462292       |
| SecuritiesAccount | -0.01081201   | -0.001232134 | 0.01999408   | -0.002616497      |
|                   | Mortgage      | Online       | PersonalLoan | SecuritiesAccount |
| Age               | -0.012538587  | 0.013702402  | -0.007725617 | -0.0004362422     |
| CCAvg             | 0.109904723   | -0.003611009 | 0.366888736  | 0.0150863114      |
| CDAccount         | 0.089311058   | 0.175880016  | 0.316354829  | 0.3170344157      |
| CreditCard        | -0.007230919  | 0.004209656  | 0.002801509  | -0.0150283189     |
| Education         | -0.033327125  | -0.015003821 | 0.136721550  | -0.0108120136     |
| Experience        | -0.010581552  | 0.013897900  | -0.007413098 | -0.0012321344     |
| Family            | -0.020444931  | 0.010354036  | 0.061367044  | 0.0199940798      |
| Income            | 0.206806228   | 0.014205919  | 0.502462292  | -0.0026164967     |
| Mortgage          | 1.000000000   | -0.005994898 | 0.142095236  | -0.0054109700     |
| Online            | -0.005994898  | 1.000000000  | 0.006277815  | 0.0126274704      |
| PersonalLoan      | 0.142095236   | 0.006277815  | 1.000000000  | 0.0219538822      |
| SecuritiesAccount | -0.005410970  | 0.012627470  | 0.021953882  | 1.0000000000      |

Looking at the correlation matrix, it's clear that Income, CCAvg and CDAccount are very highly correlated with Personal Loan. Unfortunately, after running a Logit with these three variables, CCAvg is no longer significant. As such, the team removed the CCAvg variable and replaced it with the Family variable. This variable is statistically significant in the first Logit model.



Probit:

Call:

```
glm(formula = PersonalLoan ~ Income + Family + CDAccount, family = binomial(probit)
, data = HW4Data)
```

Deviance Residuals:

| Min     | 1Q      | Median  | 3Q      | Max    |
|---------|---------|---------|---------|--------|
| -3.1917 | -0.2778 | -0.1055 | -0.0286 | 3.5996 |

Coefficients:

|             | Estimate   | Std. Error | z value | Pr(> z ) |     |
|-------------|------------|------------|---------|----------|-----|
| (Intercept) | -4.9173319 | 0.1752108  | -28.07  | <2e-16   | *** |
| Income      | 0.0239108  | 0.0009048  | 26.43   | <2e-16   | *** |
| Family      | 0.4027290  | 0.0349849  | 11.51   | <2e-16   | *** |
| CDAccount   | 1.2600334  | 0.1020413  | 12.35   | <2e-16   | *** |

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 3162.0 on 4999 degrees of freedom  
Residual deviance: 1657.7 on 4996 degrees of freedom  
AIC: 1665.7

Number of Fisher Scoring iterations: 8

| Coefficients : |          |            |         |          |     |             |
|----------------|----------|------------|---------|----------|-----|-------------|
|                | Estimate | Std. Error | z value | Pr(> z ) |     | Input       |
| (Intercept)    | -4.91733 | 0.175211   | -28.07  | <2e-16   | *** | 1           |
| Income         | 0.023911 | 0.000905   | 26.43   | <2e-16   | *** | 100         |
| Family         | 0.402729 | 0.034985   | 11.51   | <2e-16   | *** | 4           |
| CDAccount      | 1.260033 | 0.102041   | 12.35   | <2e-16   | *** | 1           |
|                |          |            |         |          |     |             |
|                |          |            |         |          |     | Sum         |
|                |          |            |         |          |     | Probability |
|                |          |            |         |          |     | 0.344698    |
|                |          |            |         |          |     | 63.5%       |

In both of these models, the significant variables are: Income, Family, CDAccount. As the customer's income increases, the probability of taking a personal loan out increases. As the customer's family increases, the probability of taking out a personal loan increases. As the customer's Average spending on Credit Cards per month increases, the probability of taking out a personal loan increases.

2. Add moderating effects (interactions of variables). Which interactions make sense conceptually? Which interactions are statistically significant? How do you interpret the coefficients on these variables? Copy screen snapshots of your analysis in R to your report. (20%)

Looking at the correlation matrix, it's clear that both Income and CCAvg are related with each other as well as statistically significant in the logit. Also, if one's Income is higher, you would expect them to spend more. However, if one's income is lower and the credit card average is higher, you would expect the probability of them taking out a loan to increase.

The final model with moderating effects is below:

```
call:
glm(formula = PersonalLoan ~ CCAvg * Income + Income + Family,
     family = binomial(logit), data = HW4Data)
```

Deviance Residuals:

```
      Min       1Q   Median       3Q      Max
-2.3362  -0.2391  -0.0780  -0.0221   3.1918
```

Coefficients:

```
              Estimate Std. Error z value Pr(>|z|)
(Intercept) -13.7771831   0.6031461  -22.84  <2e-16 ***
CCAvg        1.6469211   0.1361439   12.10  <2e-16 ***
Income       0.0750491   0.0037406   20.06  <2e-16 ***
Family       0.9395873   0.0679152   13.84  <2e-16 ***
CCAvg:Income -0.0106102   0.0008969  -11.83  <2e-16 ***
```

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signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

```
Null deviance: 3162.0  on 4999  degrees of freedom
Residual deviance: 1647.2  on 4995  degrees of freedom
AIC: 1657.2
```

Number of Fisher Scoring iterations: 8

| Coefficients | Estimate | Std. Error | z value | Pr(> z ) |     | Input       | Coeff*Value |
|--------------|----------|------------|---------|----------|-----|-------------|-------------|
| (Intercept)  | -13.7772 | 0.603146   | -22.84  | <2e-16   | *** | 1           | -13.7771831 |
| CCAvg        | 1.646921 | 0.136144   | 12.1    | <2e-16   | *** | 2.5         | 4.11730275  |
| Income       | 0.075049 | 0.003741   | 20.06   | <2e-16   | *** | 100         | 7.50491     |
| Family       | 0.939587 | 0.067915   | 13.84   | <2e-16   | *** | 4           | 3.7583492   |
| CCAvg:Income | -0.01061 | 0.000897   | -11.83  | <2e-16   | *** | 250         | -2.65255    |
|              |          |            |         |          |     |             |             |
|              |          |            |         |          |     | Sum         | -1.04917115 |
|              |          |            |         |          |     | Exp(Sum)    | 0.350227915 |
|              |          |            |         |          |     | Probability | 25.9%       |

As CC Avg spending increase, the probability of taking out a personal loan increases. As income increases, the probability of taking out a personal loan increases. As the family size increases, the probability of taking out a loan increases. As the combination of CCAvg and Income increases, the probability of taking out a personal loan decreases.

3. Create a final regression model with the variables that you feel are important (both main effects and interaction terms). Create a spreadsheet prediction of the model. Which variables have the greatest influence on the customers' loan behavior (combined main effects and interaction effects)? Perform a sensitivity analysis as seen earlier in the semester. Copy screen snapshots of your analysis in R to your report. (20%)

Call:

```
glm(formula = PersonalLoan ~ CCAvg * Income + Income + Family,
     family = binomial(logit), data = HW4Data)
```

Deviance Residuals:

```
      Min       1Q   Median       3Q      Max
-2.3362 -0.2391 -0.0780 -0.0221  3.1918
```

Coefficients:

```
              Estimate Std. Error z value Pr(>|z|)
(Intercept) -13.7771831   0.6031461  -22.84  <2e-16 ***
CCAvg        1.6469211   0.1361439   12.10  <2e-16 ***
Income       0.0750491   0.0037406   20.06  <2e-16 ***
Family       0.9395873   0.0679152   13.84  <2e-16 ***
CCAvg:Income -0.0106102   0.0008969  -11.83  <2e-16 ***
```

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

```
Null deviance: 3162.0 on 4999 degrees of freedom
Residual deviance: 1647.2 on 4995 degrees of freedom
AIC: 1657.2
```

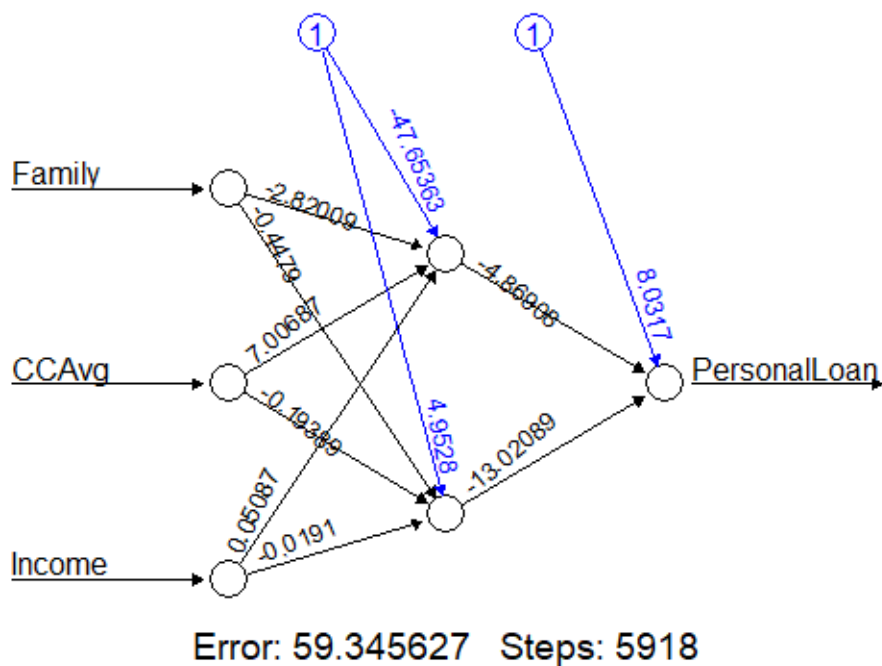
Number of Fisher Scoring iterations: 8

| Coefficients | Estimate | Std. Error | z value | Pr(> z ) |     | Input       | Coeff*Value |  | Wald Test |
|--------------|----------|------------|---------|----------|-----|-------------|-------------|--|-----------|
| (Intercept)  | -13.7772 | 0.603146   | -22.84  | <2e-16   | *** | 1           | -13.7772    |  |           |
| CCAvg        | 1.646921 | 0.136144   | 12.1    | <2e-16   | *** | 2.5         | 4.117303    |  | 146.3353  |
| Income       | 0.075049 | 0.003741   | 20.06   | <2e-16   | *** | 100         | 7.50491     |  | 402.5394  |
| Family       | 0.939587 | 0.067915   | 13.84   | <2e-16   | *** | 4           | 3.758349    |  | 191.3993  |
| CCAvg:Income | -0.01061 | 0.000897   | -11.83  | <2e-16   | *** | 250         | -2.65255    |  | 139.9455  |
|              |          |            |         |          |     | Sum         | -1.04917    |  |           |
|              |          |            |         |          |     | Exp(Sum)    | 0.350228    |  |           |
|              |          |            |         |          |     | Probability | 25.9%       |  |           |

Looking at the Wald Test, it is clear that Income and Family have the highest impact on the model. As such, the 2-way sensitivity analysis between Income and Family is below:

|        |       | Income |     |     |     |      |      |      |      |      |      |
|--------|-------|--------|-----|-----|-----|------|------|------|------|------|------|
|        | 25.9% | 25     | 50  | 75  | 100 | 125  | 150  | 175  | 200  | 225  | 250  |
| Family | 1     | 0%     | 0%  | 1%  | 2%  | 7%   | 19%  | 44%  | 73%  | 90%  | 97%  |
|        | 2     | 0%     | 0%  | 2%  | 5%  | 15%  | 38%  | 67%  | 87%  | 96%  | 99%  |
|        | 3     | 0%     | 1%  | 4%  | 12% | 32%  | 61%  | 84%  | 95%  | 98%  | 99%  |
|        | 4     | 1%     | 3%  | 9%  | 26% | 54%  | 80%  | 93%  | 98%  | 99%  | 100% |
|        | 5     | 2%     | 7%  | 21% | 47% | 75%  | 91%  | 97%  | 99%  | 100% | 100% |
|        | 6     | 6%     | 17% | 41% | 70% | 89%  | 96%  | 99%  | 100% | 100% | 100% |
|        | 7     | 13%    | 34% | 64% | 85% | 95%  | 99%  | 100% | 100% | 100% | 100% |
|        | 8     | 28%    | 57% | 82% | 94% | 98%  | 99%  | 100% | 100% | 100% | 100% |
|        | 9     | 50%    | 77% | 92% | 97% | 99%  | 100% | 100% | 100% | 100% | 100% |
|        | 10    | 72%    | 90% | 97% | 99% | 100% | 100% | 100% | 100% | 100% | 100% |

- Perform a neural network analysis of the variables found to be significant in the logit and probit analysis above. Copy screen snapshots of your final neural network model in R to your report. (20%)





5. Create a prediction model of the neural network. Using the prediction model, perform a sensitivity analysis for the neural network model similar to the logit and probit sensitivity analysis. (20%)

|                           |              |  |              |             |              |           |             |             |             |
|---------------------------|--------------|--|--------------|-------------|--------------|-----------|-------------|-------------|-------------|
| error                     | 59.34562728  |  | Hidden Node1 |             |              | Output    |             |             |             |
| reached.threshold         | 0.07654892   |  | Variable     | Coefficient | Coeff*Value  | Variables | Coefficient | Value       | Coeff*Value |
| steps                     | 5918         |  | Intercept    | -47.6536291 | -47.6536291  | Intercept | 8.03170461  | 1           | 8.03170461  |
| Intercept.to.1layhid1     | -47.65362907 |  | Family       | -2.82009272 | -11.2803709  | Hidden1   | -4.86907574 | 0%          | -2.0989E-24 |
| Family.to.1layhid1        | -2.82009272  |  | CAAvg        | 7.00686758  | 24.5240365   | Hidden2   | -13.0208892 | 52%         | -6.82125385 |
| CAAvg.to.1layhid1         | 7.00686758   |  | Income       | 0.05086553  | 6.35819125   |           |             |             |             |
| Income.to.1layhid1        | 0.05086553   |  |              |             |              |           |             | Sum         | 1.21045076  |
| Intercept.to.1layhid2     | 4.95279997   |  |              |             |              |           |             | Exp(Sum)    | 3.35499663  |
| Family.to.1layhid2        | -0.44790067  |  | Sum          |             | -28.0517722  |           |             | Probability | 77%         |
| CAAvg.to.1layhid2         | -0.19388949  |  | exp(Sum)     |             | 6.5655E-13   |           |             |             |             |
| Income.to.1layhid2        | -0.01909625  |  | Probability  |             | 0%           |           |             |             |             |
| Intercept.to.PersonalLoan | 8.03170461   |  | Hidden Node2 |             |              |           |             |             |             |
| 1layhid1.to.PersonalLoan  | -4.86907574  |  | Variable     | Coefficient | Co-eff*Value |           |             |             |             |
| 1layhid2.to.PersonalLoan  | -13.02088921 |  | Intercept    | 4.95279997  | 4.95279997   |           |             |             |             |
|                           |              |  | Family       | -0.44790067 | -1.79160268  |           |             |             |             |
| Variable                  | Input        |  | CAAvg        | -0.19388949 | -0.67861322  |           |             |             |             |
| Intercept                 | 1            |  | Income       | -0.01909625 | -2.38703125  |           |             |             |             |
| Family                    | 4            |  |              |             |              |           |             |             |             |
| CAAvg                     | 3.5          |  |              |             |              |           |             |             |             |
| Income                    | 125          |  |              |             |              |           |             |             |             |
|                           |              |  | Sum          |             | 0.09555283   |           |             |             |             |
|                           |              |  | exp(Sum)     |             | 1.10026694   |           |             |             |             |
|                           |              |  | Probability  |             | 52%          |           |             |             |             |

As the neural network prediction above shows, a customer with a family of 4, CC average spend of 3.5 thousand per month, and annual income of 125 thousand is predicted to take a personal loan 77% of the time.

|        |     | Income     |            |            |            |            |            |            |            |            |            |
|--------|-----|------------|------------|------------|------------|------------|------------|------------|------------|------------|------------|
|        | 77% | 25         | 50         | 75         | 100        | 125        | 150        | 175        | 200        | 225        | 250        |
| Family | 1   | 0.01048404 | 0.01349964 | 0.01983453 | 0.03490962 | 0.0763087  | 0.19959915 | 0.49360693 | 0.81732916 | 0.95368201 | 0.9878061  |
|        | 2   | 0.01324595 | 0.01927697 | 0.03350638 | 0.07225393 | 0.18768089 | 0.47106339 | 0.8025521  | 0.94948124 | 0.986832   | 0.99570936 |
|        | 3   | 0.01874783 | 0.03218662 | 0.06846745 | 0.17646662 | 0.44880239 | 0.7869     | 0.944891   | 0.98576728 | 0.99543768 | 0.99807841 |
|        | 4   | 0.03094466 | 0.0649307  | 0.16592926 | 0.42691556 | 0.7703787  | 0.93987894 | 0.98460303 | 0.99514362 | 0.99798852 | 0.99892674 |
|        | 5   | 0.06162634 | 0.15604    | 0.40548691 | 0.75300371 | 0.93441109 | 0.98332942 | 0.99482509 | 0.99789237 | 0.9988914  | 0.99928426 |
|        | 6   | 0.14676887 | 0.38459171 | 0.73480099 | 0.92845196 | 0.98193571 | 0.9944798  | 0.99778944 | 0.99885401 | 0.99926821 | 0.9994557  |
|        | 7   | 0.36429571 | 0.71580735 | 0.92196484 | 0.98041011 | 0.99410523 | 0.99767917 | 0.9988144  | 0.99925137 | 0.99944757 | 0.99954604 |
|        | 8   | 0.69607071 | 0.91491198 | 0.97873973 | 0.99369859 | 0.99756095 | 0.99877244 | 0.99923369 | 0.9994391  | 0.99954159 | 0.99959688 |
|        | 9   | 0.90725506 | 0.97691047 | 0.99325682 | 0.99743409 | 0.99872794 | 0.99921512 | 0.99943025 | 0.99953697 | 0.99959431 | 0.99962678 |
|        | 10  | 0.97490694 | 0.99277656 | 0.99729788 | 0.99868071 | 0.9991956  | 0.99942102 | 0.99953217 | 0.99959165 | 0.99962524 | 0.99964488 |

Justify your answers. Provide a snapshot of output from your analysis in your final paper.