

# Tunable Spin-charge Conversion in Topological Dirac Semimetals

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Based on arXiv: 2110.11823

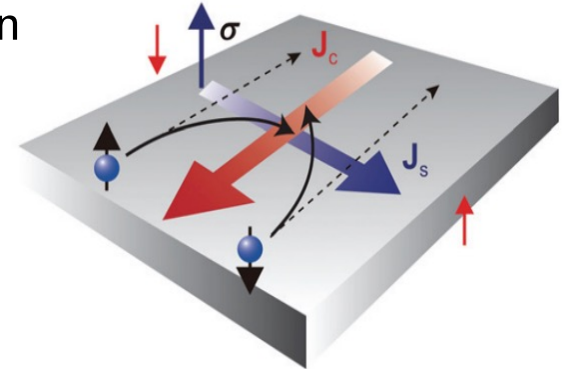
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# Spin-charge conversion

- Spin Hall effect (SHE): charge-to-spin conversion

- Intrinsic: related to the Berry curvature
- Extrinsic: induced by disorder



Ando et al., J. Appl. Phys. **109**, 103913 (2011)

- SHE in topological Dirac semimetals (TDSMs): e.g.

Taguchi et al., *PRB* **101**, 235201 (2020)

Yen and Guo, *PRB* **101**, 064430 (2020)

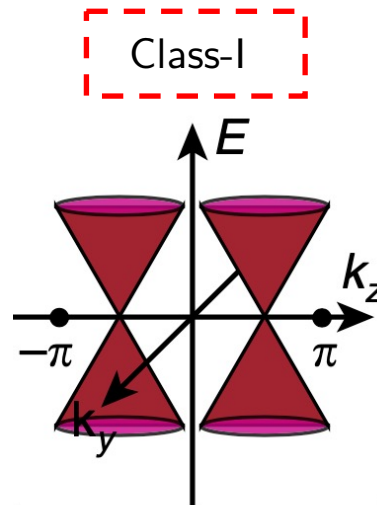
Hou et al., *npj Comput. Mater.* **7**, 37 (2021)

- Our work: Tunable spin-charge conversion in TDSMs by external fields.

# Topological Dirac semimetals (TDSMs)

- Host Dirac points (4-fold degenerate) protected by **time-reversal + inversion + uniaxial rotation symmetries**

Yang and Nagaosa, Nat. Commun. **5**, 4898 (2011)



A pair of Dirac points on the rotation axis

- Class-I TDSM materials: e.g.,  $\text{Cd}_3\text{As}_2$  ( $C_4$  symm.),  $\text{Na}_3\text{Bi}$  ( $C_3$  symm.)

# Spin Hall effect in TDSMs

Low-energy Hamiltonian for a class-I TDSM:

Wang et al., PRB **85**, 195320 (2012);  
Wang et al., PRB **88**, 125427 (2013)

$$H_D(\mathbf{k}) = \begin{pmatrix} \overset{\text{spin-up}}{\boxed{M(\mathbf{k}) \quad Ak_+ \\ Ak_- \quad -M(\mathbf{k})}} & \begin{matrix} 0 & 0 \\ 0 & 0 \end{matrix} \\ \begin{matrix} 0 & 0 \\ 0 & 0 \end{matrix} & \underset{\text{spin-down}}{\boxed{M(\mathbf{k}) \quad -Ak_- \\ -Ak_+ \quad -M(\mathbf{k})}} \end{pmatrix} = H_W^\uparrow \oplus H_W^\downarrow$$

Spin Hall current:  $\mathbf{j}^z = \frac{e}{\hbar} \sum_{s,n} s \int \frac{d^3\mathbf{k}}{(2\pi)^3} \mathbf{E} \times \overset{\text{spin Berry curvature}}{\Omega_n^s(\mathbf{k})} f_{n\mathbf{k}}^0 = \sigma_{\text{SH}}^0(\mathbf{E} \times \hat{\mathbf{z}}) \quad (s = \pm 1)$

Anisotropic SHE

with spin Hall conductivity (SHC)

$$\sigma_{\text{SH}}^0 = \frac{ek_D}{\pi^2\hbar}$$

$2k_D$  = separation of Dirac points

Charge Hall current:  $\mathbf{j} = \frac{e}{\hbar} \sum_{s,n} \int \frac{d^3\mathbf{k}}{(2\pi)^3} \mathbf{E} \times \Omega_n^s(\mathbf{k}) f_{n\mathbf{k}}^0 = 0$

Pure spin current!

# B in arbitrary directions

effective Landé g-factor  $\approx 30$

- Zeeman coupling:  $H_Z = \tilde{g}\mu_B(\mathbf{L} + 2\mathbf{S}) \cdot \mathbf{B}$

$$= \tilde{g}\mu_B \begin{pmatrix} B_z & 0 & B_- & 0 \\ 0 & 2B_z & 0 & 0 \\ B_+ & 0 & -B_z & 0 \\ 0 & 0 & 0 & -2B_z \end{pmatrix}$$

z-component of spin is NOT conserved

$\Rightarrow$  unconventional SHC tensors  $\sigma_{xy}^x, \sigma_{xy}^y \neq 0$

- Kubo-Greenwood formula:

$$\sigma_{ab}^i = -e\hbar \int \frac{d^3\mathbf{k}}{(2\pi)^3} \sum_n f_{n\mathbf{k}}^0 \sum_{n' \neq n} \frac{2 \operatorname{Im}[\langle n\mathbf{k} | J_a^i | n'\mathbf{k} \rangle \langle n'\mathbf{k} | v_b | n\mathbf{k} \rangle]}{(\varepsilon_{n'\mathbf{k}} - \varepsilon_{n\mathbf{k}})^2 + \Gamma^2}$$

$$\sigma_{ab} = -e\hbar \int \frac{d^3\mathbf{k}}{(2\pi)^3} \sum_n f_{n\mathbf{k}}^0 \sum_{n' \neq n} \frac{2 \operatorname{Im}[\langle n\mathbf{k} | v_a | n'\mathbf{k} \rangle \langle n'\mathbf{k} | v_b | n\mathbf{k} \rangle]}{(\varepsilon_{n'\mathbf{k}} - \varepsilon_{n\mathbf{k}})^2 + \Gamma^2}$$

$$J_a^i = \frac{1}{2}\{v_a, \sigma_i\}, \quad v_a = \frac{\partial \varepsilon(\mathbf{k})}{\hbar \partial k_a}$$

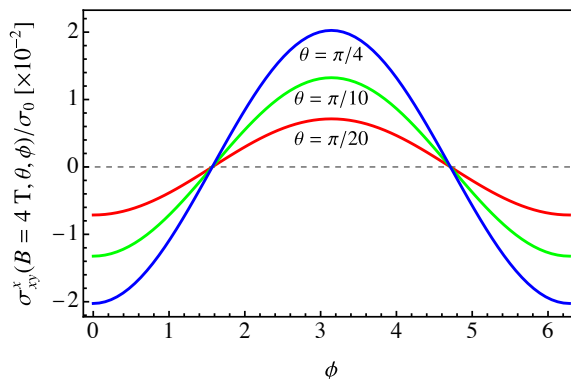
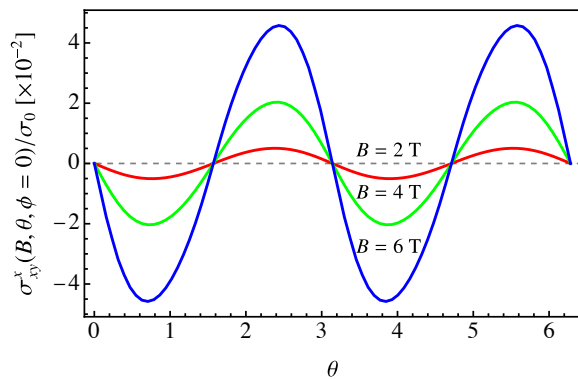
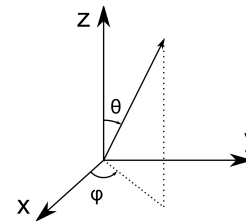
band broadening factor  $\sim \hbar/\tau \approx 10 \text{ meV}$

# Spin/charge Hall currents

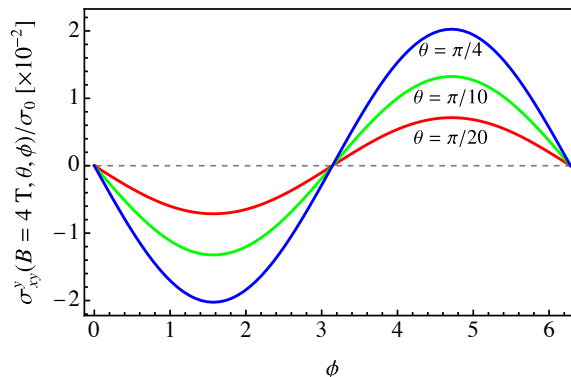
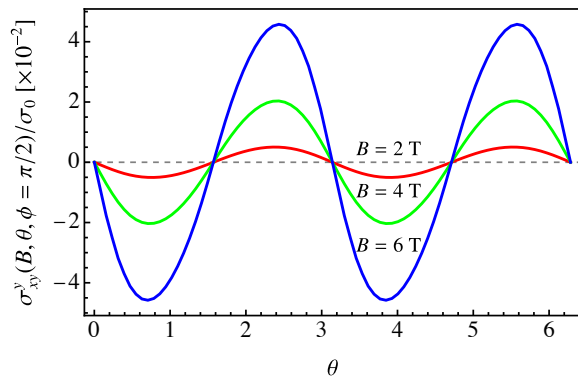
$$\begin{aligned} Q^{x(y)} &\approx \chi^{x(y)} B_z B_{x(y)} (\mathbf{E} \times \hat{\mathbf{z}}) \\ Q^z &\approx \left[ \sigma_{\text{SH}}^0 + \left( \chi_{\perp}^z B_{\perp}^2 + \chi_{\parallel}^z B_z^2 \right) \right] (\mathbf{E} \times \hat{\mathbf{z}}) \\ \mathbf{j} &\approx \kappa B_z (\mathbf{E} \times \hat{\mathbf{z}}) \end{aligned}$$

- **Electric tunability**: band topology
- **Magnetic tunability**: symmetry breaking [also seen in spin currents in ferromagnets induced by magnetization; see Amin et al., PRB **99**, 220405 (2019)]

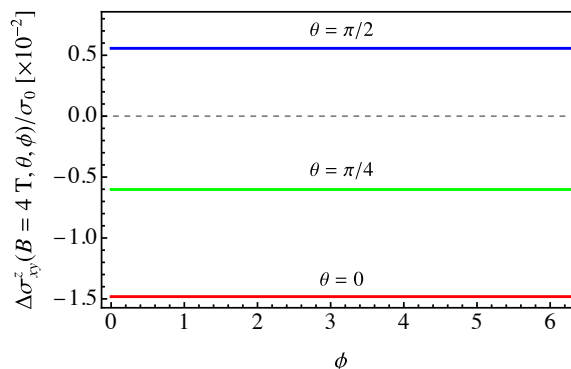
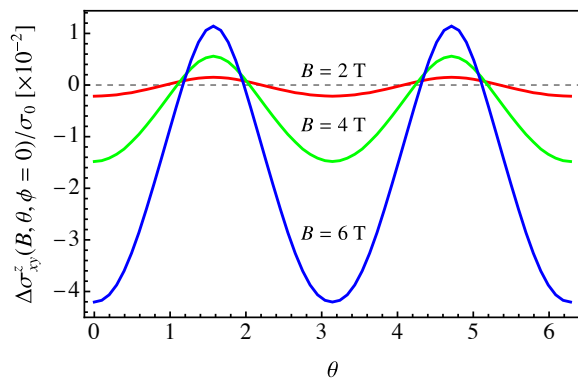
# SHC **B**-dependence



$$\begin{aligned}\sigma_{xy}^x(\mathbf{B}) &\sim B_x B_z \\ &\sim B^2 \sin(2\theta) \cos \phi\end{aligned}$$



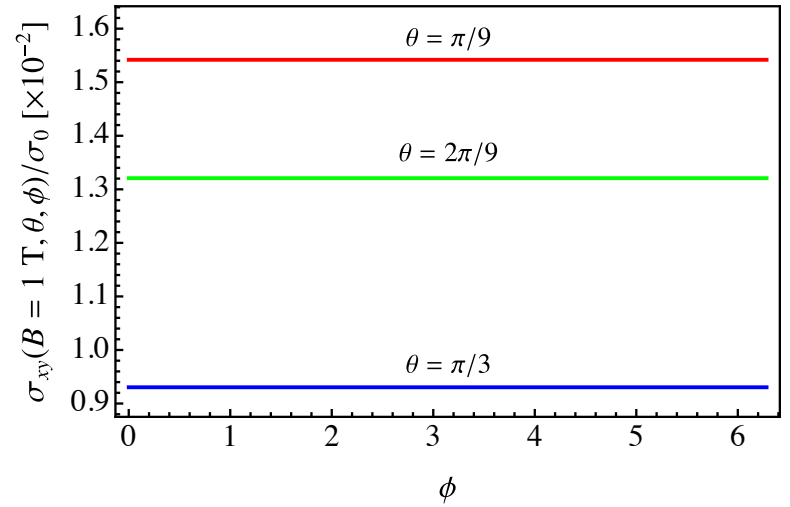
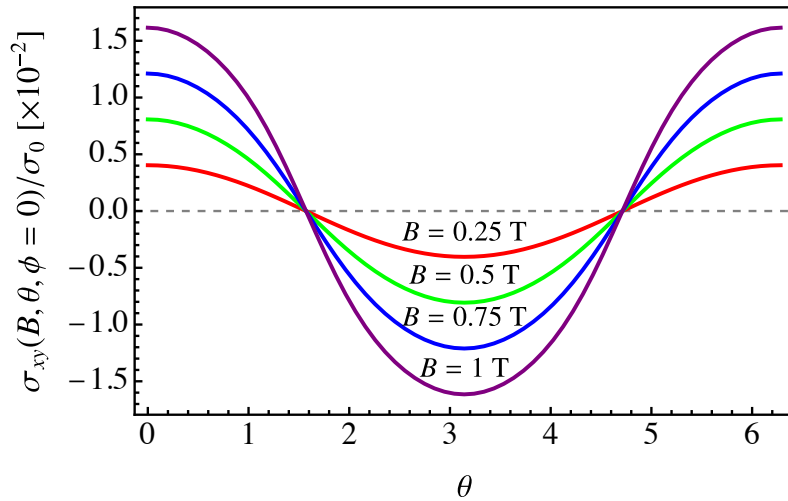
$$\begin{aligned}\sigma_{xy}^y(\mathbf{B}) &\sim B_y B_z \\ &\sim B^2 \sin(2\theta) \sin \phi\end{aligned}$$



$$\begin{aligned}\sigma_{xy}^z(\mathbf{B}) &\sim \alpha(B_x^2 + B_y^2) + \beta B_z^2 \\ &\sim B^2 (\alpha \sin^2 \theta + \beta \cos^2 \theta)\end{aligned}$$

**Tunable upon variation of magnetic field direction!**

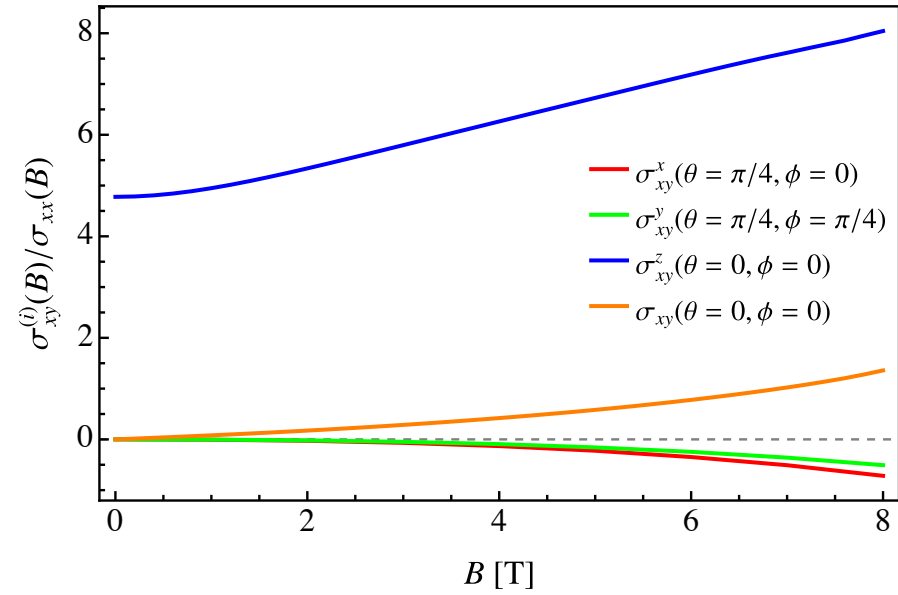
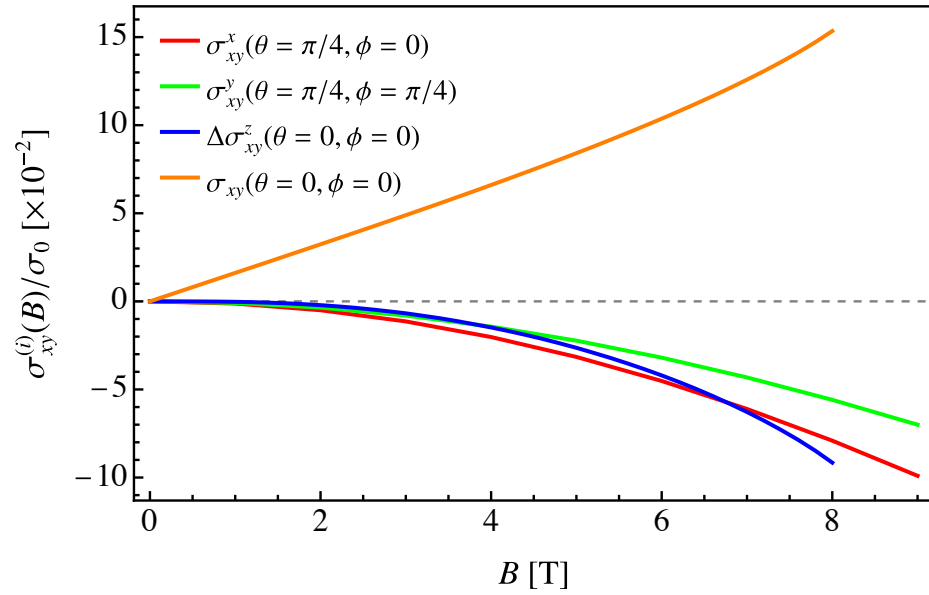
# AHC **B**-dependence



$$\sigma_{xy}(\mathbf{B}) \sim B_z \sim B \cos \theta$$



# Spin-charge conversion efficiency



# Summary & Outlook

- Take-home message:

Topological Dirac semimetals can provide another platform for realizing electrically & magnetically tunable spin-charge conversion arisen from the interplay of unique band topology and symmetry breaking.

- No magnetic field: pure spin current;

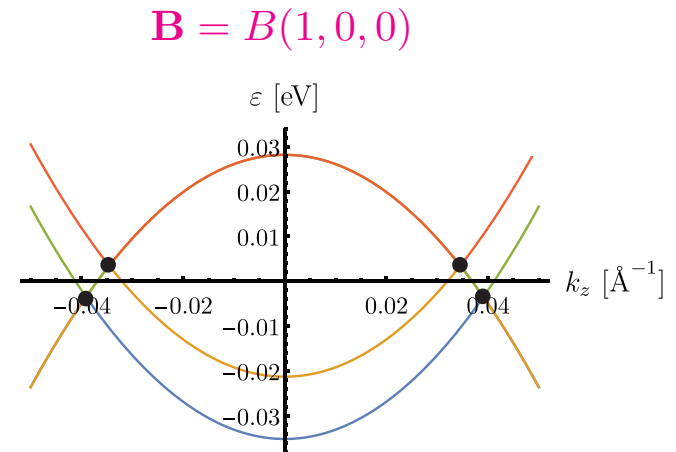
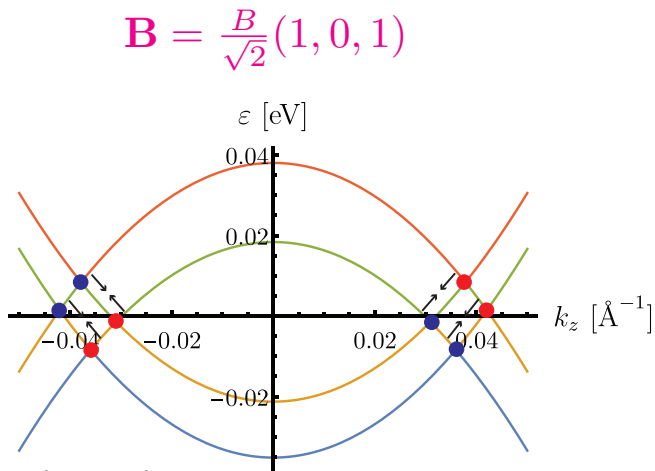
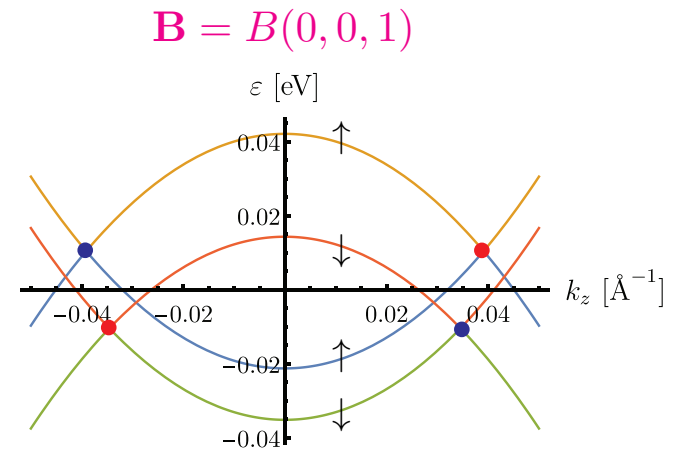
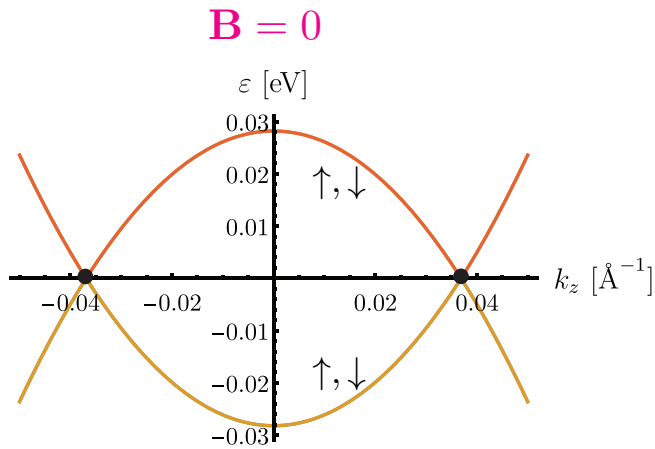
With external magnetic field: spin-to-charge conversion

- Spin-charge conversion efficiency can be enhanced by increasing the magnetic field strength.
- Possible future directions: effects of tilting and energy displacement of the Dirac cones; orbital contribution of magnetic field; etc.

# Back-up Slides

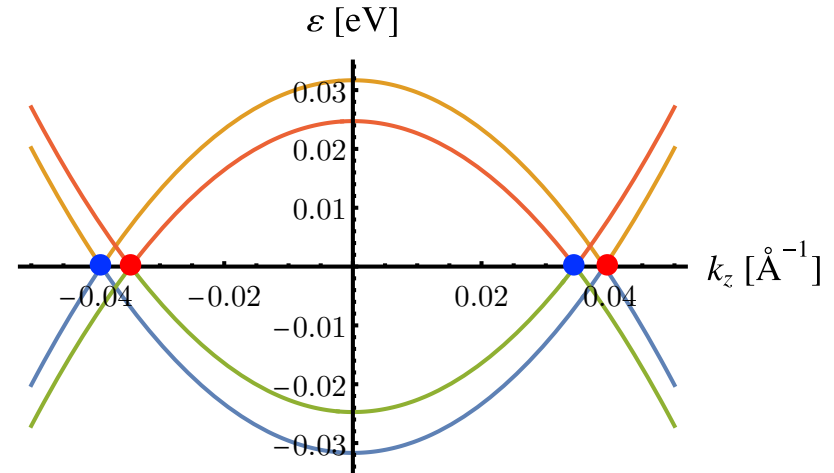
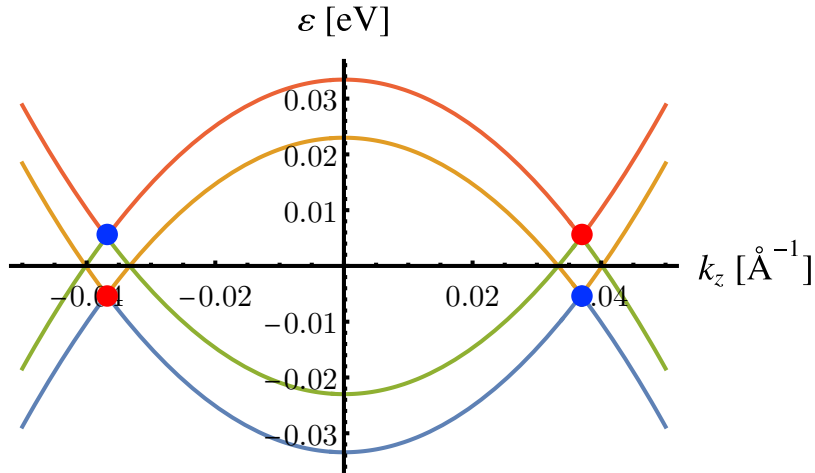
# Tunability via external magnetic field

- Spin mixing
- Symmetry breaking



# B along z-direction

Zeeman coupling:  $H_Z = h_+ \sigma_z \tau_0 + h_- \sigma_z \tau_z$



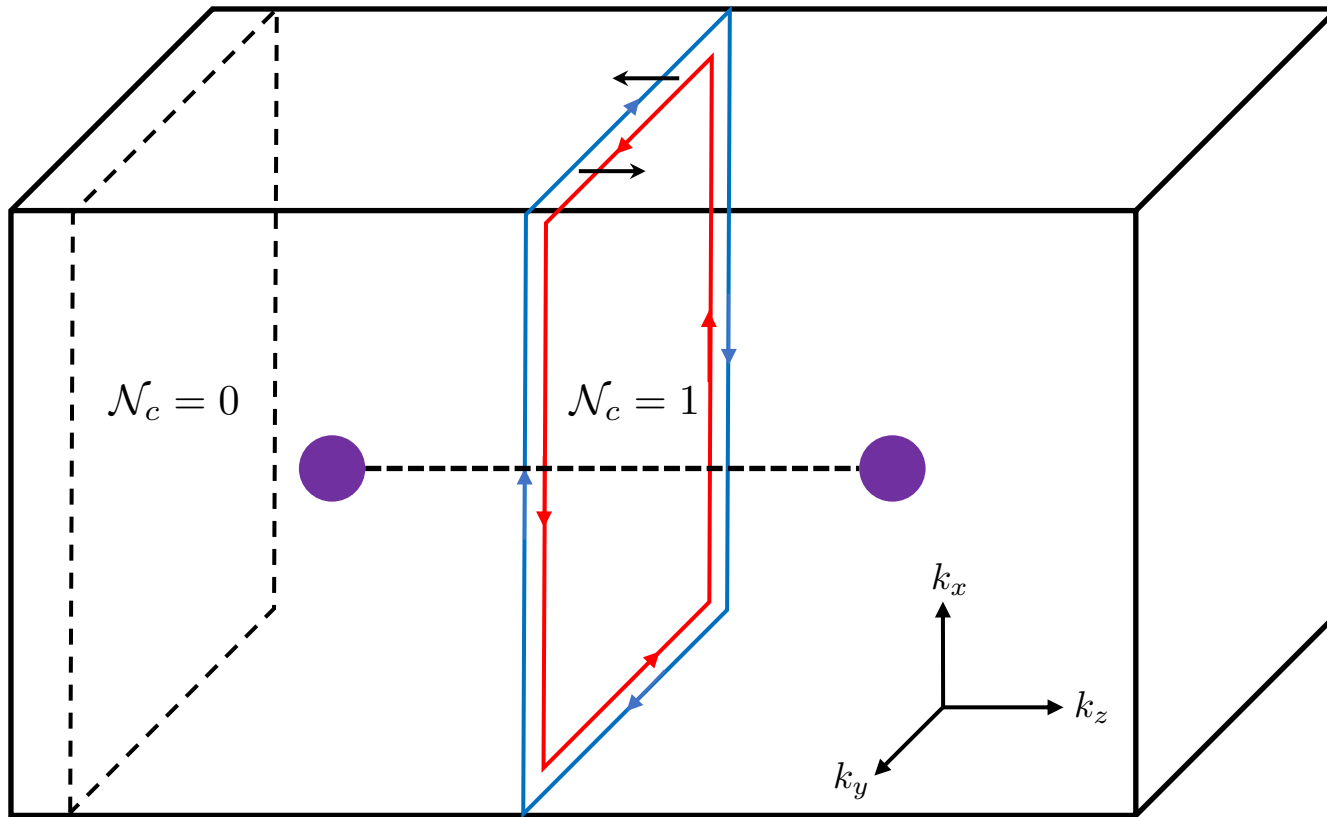
Orbital-symmetric:  $\sigma_{xy}^{z(+)} \simeq \left[ 1 - \left( \frac{1}{24M_0^2} + \frac{M_2}{3M_0A^2} \right) h_+^2 \right] \sigma_{\text{SH}}^0$

Orbital-antisymmetric:  $\sigma_{xy}^{z(-)} \simeq \left( 1 - \frac{h_-^2}{8M_0^2} \right) \sigma_{\text{SH}}^0$

$$\sigma_{xy}^{(-)} \simeq -\frac{h_-}{2|M_0|} \sigma_{\text{SH}}^0$$

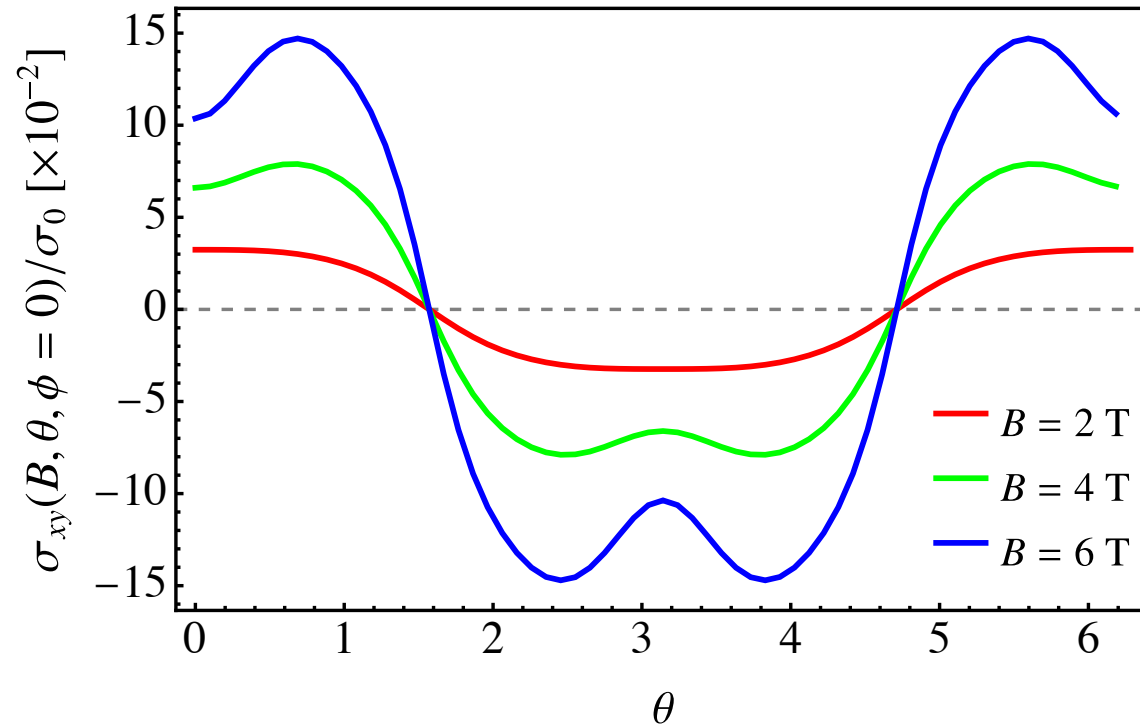
Spin-to-charge  
conversion!

# SHC in TDSMs and $Z_2$ invariant



$$\mathcal{N}_c(k_z) \equiv \frac{1}{4\pi} \sum_s s \int dk_x dk_y \Omega_{-,z}^s(\mathbf{k}) = \Theta(k_D^2 - k_z^2)$$

# High-field behavior (AHC)



# Magnitude dependence

