# 

Richard Zach $^{\dagger}$ Released 2018/04/08

#### 1 Introduction

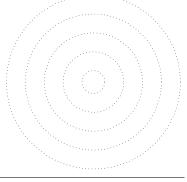
Lewis<sup>1</sup> introduced a sphere semantics for counterfactual conditionals. He jokingly referred to the diagrams depicting such sphere models as "Ptolemaic astronomy," hence the name of this package. It has nothing to do with Ptolemy or with astronomy, sorry.

The macros provided in this package aid in the construction of sphere model diagrams in the style of Lewis. The macros all make use of TikZ.

Source code can be found at https://github.com/rzach/ptolemaic-astronomy

### 2 Usage

\spheresystem To draw a sphere system with  $\langle n \rangle$  layers, say \spheresystem{ $\langle n \rangle$ }:



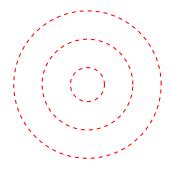
\begin{tikzpicture}
 \spheresystem{5}
\end{tikzpicture}

<sup>\*</sup>This file describes version v1.00, last revised 2018/04/08.

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<sup>&</sup>lt;sup>1</sup>David K. Lewis, Counterfactuals (Blackwell 1973)

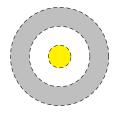
The width of each layer is determined by the TikZ parameter layerwidth and defaults to .5 TikZ units (so 0.5 cm by default). The radius of the center sphere is not layerwidth, but layerwidth  $\times$  (1 – innerfactor). innerfactor defaults to 0.4. Spheres are drawn in dotted style by default. You can change this by passing an option to \spheresystem, e.g., to get red, dashed, thick lines and wider layers:



\begin{tikzpicture}
 \spheresystem[dashed, red,
 thick, layerwidth=.75]{3}
\end{tikzpicture}

\spherelayer \spherefill

These macros shade the  $\langle n \rangle$ -th layer of the sphere model, or the entire  $\langle n \rangle$ -th sphere. The fill defaults to lightgray and can be changed with  $\lceil \langle options \rangle \rceil$ . Note that the fill extends to the center of the layer boundary line, so you should fill first and then draw the spheres. For instance:



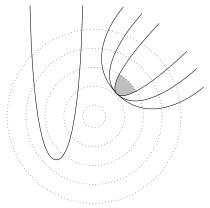
\begin{tikzpicture}
 \spherelayer{3}
 \spherefill[yellow]{1}
 \spheresystem[densely dashed]{3}
\end{tikzpicture}

\proposition \propositionintersect

A proposition is a set of worlds which (usually) intersects with a sphere system. A common way of drawing them is as a parabola, and often we want to highlight the intersection of the proposition with the closest sphere with which it intersects.  $\proposition{\langle direction \rangle}{\langle direction \rangle}{$ 

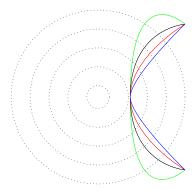
With the shift option you can also position propositions outside the center, e.g., a proposition extending from the north through the west side of the sphere system would use, say,  $shift=\{(-1,-1)\}$ .

```
\begin{tikzpicture}
  \propositionintersect{45}{3}{20}{3}
  \proposition{45}{3}{40}{3}
  \proposition{45}{3}{60}{3}
  \proposition[shift={(-1,-1)}]{90}{1}{20}{4}
  \spheresystem{5}
\end{tikzpicture}
```



The degree of "pointedness" of propositions is determined by the tension parameter, which defaults to 1.7. Larger values make the proposition more bulgy, smaller values more pointy.

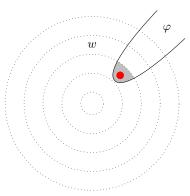
```
\begin{tikzpicture}
  \proposition[green,
      proposition/.style={tension=3}]{0}{3}{80}{3}
  \proposition{0}{3}{80}{3}
  \proposition[red,
      proposition[blue,
      proposition/.style={tension=1}]{0}{3}{80}{3}
  \proposition/.style={tension=.5}]{0}{3}{80}{3}
  \spheresystem{5}
  \end{tikzpicture}
```



#### \spherepos

\spherepos{\langle direction\rangle} \{\langle n\rangle} \{\langle code\rangle}\rangle \text{ moves to a position in the center of layer \langle n\rangle \text{ in \langle direction}\rangle \text{ and then exectures TikZ path code \langle code}\rangle. It's useful to put labels or other things into the sphere system.

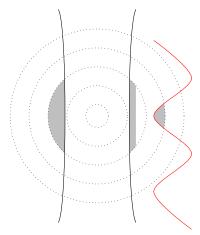
```
\begin{tikzpicture}
  \propositionintersect{45}{3}{20}{3}
  \spheresystem{5}
  \spherepos[fill,red]{45}{3}{circle[radius=.1]}
  \spherepos{90}{4}{node {$w$}}
  \spherepos{45}{6.5}{node {$\varphi$}}
\end{tikzpicture}
```



#### \sphereintersect

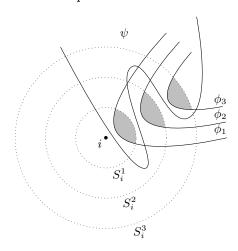
\propositionintersect uses \phereintersect[\langle options \rangle] \{\langle and \rangle \langle options \rangle] \{\langle and \rangle \rangle \langle and \rangle \rangle and \rangle and \rangle \rangle and \rangle \rangle and \rangle

to be extended, and the path drawn separately. The example below shows what happens when a very wide parabola does not completely intersect (on the right), how to use the trick to get the fill right(on the left), as well as intersecting a more complex path with a sphere layer.



Finally, a complex example: the Sobel sequence diagram, Figure 2 from Lewis, p. 11:

```
\begin{tikzpicture}[scale=.8]\small
 \tikzset{layerwidth=1,innerfactor=0,
          proposition/.style={smooth,tension=1}}
 \sphereintersect{2}{\propositionplot{30}{2.3}{45}{4}}
 \sphereintersect{1}{\propositionplot{30}{1.3}{60}{4}}
 \spheresystem{3}
 \draw \propositionplot{30}{3.3}{30}{4};
 \draw \propositionplot{30}{2.3}{45}{4};
 \draw \propositionplot{30}{1.3}{60}{4};
 \draw plot[smooth,tension=1.2]
   coordinates \{(-1.5,3)\ (1.2,-1)\ (.8,2.3)\ (2.8,.7)\ (3,4)\};
 \filldraw circle[radius=.05];
 \node at (-.2,-.2) {$i$};
 \spherepos{-70}{1.8}{node {$S^1_i$}}
 \spherepos{-70}{2.8}{node {$S^2_i$}}
 \spherepos{-70}{3.8}{node {$S^3_i$}}
 \spherepos{4}{4.3}{node {$\phi_1$}}
                    node at +(0,.5) {\frac{1}{2}}
                    node at +(0,1) {\phi_3}
 \spherepos{80}{4}{node {\scriptstyle $\psi$}}
\end{tikzpicture}
```



# 3 Implementation

```
1 \RequirePackage{tikz}
2
3 \tikzset{
4    sphere/.style = {dotted},
5    sphere intersection/.style = {fill=lightgray},
6    sphere layer/.style = {fill=lightgray},
7    proposition/.style={smooth,tension=1.7},
```

```
8 }
                     TikZ parameters used to compute the sphere radii and can be set using TikZ's
       layerwidth
     innerfactor
                     options mechanism or using \tikzset.
                      9 \pgfkeyssetvalue{/tikz/layerwidth}{.5}
                     10 \pgfkeyssetvalue{/tikz/innerfactor}{.4}
                     \sphereplot\{\langle n \rangle\} gives the plot codes for the \langle n \rangle-th sphere
     \sphereplot
                     11 \newcommand{\sphereplot}[1]{
                          circle
                     13
                             [radius=(#1)*\pgfkeysvalueof{/tikz/layerwidth}-
                               \pgfkeysvalueof{/tikz/layerwidth}*\pgfkeysvalueof{/tikz/innerfactor}]
                     14
                     15 }
                     \spheresystem[\langle options \rangle] \{\langle n \rangle\}\ draws a sphere system centered at the origin
   \spheresystem
                     with \langle n \rangle number of layers
                     16 \newcommand{\spheresystem}[2][]{
                          \foreach \i in \{1, ..., \#2\}{
                     17
                             \draw[sphere,#1] \sphereplot{\i};
                     18
                          }
                     19
                     20 }
    \spherelayer
                     21 \newcommand{\spherelayer}[2][]{
                          \begin{scope}[even odd rule]
                             \fill[#1,sphere layer]
                     23
                     24
                             \sphereplot{#2-1} \sphereplot{#2};
                          \end{scope}
     \spherefill
                     \spherefill[\langle options \rangle] {\langle n \rangle} fills the \langle n \rangle-th sphere
                     27 \newcommand{\spherefill}[2][]{
                             \fill[sphere intersection,#1]
                     28
                             \sphereplot{#2};
                     29
                     30 }
                     \sphereintersect[\langle options \rangle] {\langle n \rangle} {\langle path \rangle} shades the area between \langle path \rangle and
\sphereintersect
                     the the \langle n \rangle-th sphere layer. Options only apply to the sphere layer.
                     31 \newcommand{\sphereintersect}[3][]{
                     32
                          \begin{scope}[even odd rule]
                     33
                             \path[clip] #3;
                             \spherefill[#1]{#2}
                     34
                          \end{scope}
                     35
                     36 }
                     \propositionplot[\langle options \rangle] \{\langle direction \rangle\} \{\langle width \rangle\} \{\langle length \rangle\} \produces the
\propositionplot
                     plot code for a proposition intersecting the \langle n \rangle-th layer in angle \langle direction \rangle away
```

from the center of the sphere system, with endpoints  $\langle length \rangle$  away from the center

at an angle of  $\langle direction \rangle \pm \langle width \rangle / 2$ .

```
37 \newcommand{\propositionplot}[4]{
                                plot [proposition]
                                coordinates {+(#1+#3/2:#4)
                           39
                                  +(#1:#2*\pgfkeysvalueof{/tikz/layerwidth}-
                           40
                                  \pgfkeysvalueof{/tikz/layerwidth}*.9
                           41
                           42
                                  -\pgfkeysvalueof{/tikz/layerwidth}*\pgfkeysvalueof{/tikz/innerfactor})
                           43
                                  +(#1-#3/2:#4)}
                           44 }
          \proposition
                           \proposition[\langle options \rangle] \{\langle direction \rangle\} \{\langle n \rangle\} \{\langle width \rangle\} \{\langle length \rangle\}  actually draws
                           the proposition. Note that (options) applies to \draw, not to \plot.
                           45 \newcommand{\proposition}[5][]{
                                \draw[proposition,#1] \propositionplot {#2}{#3}{#4}{#5};
                                }
                           47
\propositionintersect
                           \spherepropositionintersect does the same as \sphereproposition but also
                           shades the area of intersection with the \langle n \rangle-th sphere.
                           48 \newcommand{\propositionintersect}[5][]{
                                \begin{scope}
                                \path[clip] \propositionplot{#2}{#3}{#4}{#5};
                           50
                           51
                                \spherefill[#1]{#3}
                           52
                                \end{scope}
                                \draw[proposition,#1] \propositionplot{#2}{#3}{#4}{#5};
                           53
                           54 }
                           \spherepos[\langle options \rangle] \{\langle direction \rangle\} \{\langle n \rangle\} \{\langle code \rangle\}  shifts the scope to a position
            \spherepos
                           in the center of the \langle n \rangle-th layer in direction angle from the center—and then puts
                           a \langle code \rangle path there.
                           55 \newcommand{\spherepos}[4][]{
                                \begin{scope} [shift=(#2:#3*\pgfkeysvalueof{/tikz/layerwidth}-
                           56
                                     \pgfkeysvalueof{/tikz/layerwidth}/2-
                           57
                                       \pgfkeysvalueof{/tikz/layerwidth}*\pgfkeysvalueof{/tikz/innerfactor})]
                           58
                                  \path[#1] #4;
                           59
                                \end{scope}
                           60
                           61 }
```

### 4 Change History

```
v1.00

General: First public release . . . . . 1
```

## 5 Index

Numbers written in italic refer to the page where the corresponding entry is described; numbers underlined refer to the code line of the definition; numbers in roman refer to the code lines where the entry is used.

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