Constraining new physics from Higgs measurements with Lilith: update to LHC Run 2 results

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Abstract

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Lilith is public python library for constraining new physics from Higgs signal 11 strength measurements. We here present version 2.0 of Lilith together with an 12 updated database which includes the full set of ATLAS and CMS Run 2 Higgs 13 results for 36 fb⁻¹. Both the code and the XML database where extended from the ordinary Gaussian approximation employed in Lilith-1.1 to using variable Gaussian and Poisson distributions. Moreover, Lilith can now make use of correlation matrices of arbitrary dimension. We provide detailed validations 17 of the implemented experimental results as well as a status of global fits for 18 i) reduced Higgs couplings and ii) Two-Higgs-doublet models of Type-I and Type-II. Lilith-2.0 is available on GitHub and ready to be used to constrain a wide class of new physics scenarios.

$_{\scriptscriptstyle 12}$ Introduction

23 Introduce Higgs couplings fits and Lilith [1]
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Extended XML format for experimental input

In the Lilith database, every single experimental result is stored in a separate XML file.
This allows to easily select the results to use in a fit, and it also makes maintaining and updating the database rather easy.

The root tag of each XML file is $\langle \text{expmu} \rangle$, which has two mandatory attributes, dim and type to specify the type of signal strength result. Production and decay modes are specified via prod and decay attributes either directly in the $\langle \text{expmu} \rangle$ tag or as efficiencies in $\langle \text{eff} \rangle$ tags. Additional (optional) information can be provided in $\langle \text{experiment} \rangle$, $\langle \text{source} \rangle$, $\langle \text{sqrts} \rangle$, $\langle \text{CL} \rangle$ and $\langle \text{mass} \rangle$ tags. Taking the $H \to \gamma \gamma$ result from the combined ATLAS and CMS Run 1 analysis [2] as a concrete example, the structure of the XML file is

```
<expmu decay="gammagamma" dim="2" type="n">
41
     <experiment>ATLAS-CMS</experiment>
42
     <source type="publication">CMS-HIG-15-002; ATLAS-HIGG-2015-07</source>
     <sqrts>7+8</sqrts>
44
     <mass>125.09</mass>
45
     <CL>68%</CL>
46
47
     <eff axis="x" prod="ggH">1.</eff>
     <eff axis="y" prod="VVH">1.</eff>
49
50
     <!-- (...) -->
51
   </expmu>
52
```

where <!-- (...) --> is a placeholder for the actual likelihood information. For a detailed description, we refer to the original Lilith manual [1]. In the following, we assume that the reader is familiar with the basic syntax.

So far, the likelihood information could be specified in one or two dimensions in the form of [1]: 1D intervals given as best fit with 1σ error; 2D likelihood contours described as best fit point and parameters a, b, c which parametrize the inverse of the covariance matrix; or full likelihood information as 1D or 2D grids of $-2 \log L$. The first two options, 1D intervals and 2D likelihood contours, declared as type="n" in the <expmu> tag, employ an ordinary Gaussian approximation; in the 1D case, asymmetric errors are accounted for by putting together two one-sided Gaussians with the same mean but different variances, while the 2D case assumes symmetric errors. This does does not always allow to describe the experimental data (i.e. the true likelihood) very well. Full 2D likelihood grids would be much better but are rarely available.

In order to treat asymmetric uncertainties in a better way, we have extended the XML format and fitting procedure in Lilith to Gaussian distributions of variable width ("variable Gaussian") as well as generalized Poisson distributions. The declaration is type="vn" for variable Gaussian or type="p" for Poisson distribution in the expmu> tag. Both work for 1D and 2D data with the same syntax. Moreover, in order to make use of the N-dimensional (N>2) correlation matrices which both ATLAS and CMS have started to provide, we have added a new XML format for correlated signal strengths in more than two dimensions. This can be used with the ordinary or variable Gaussian approximation for the likelihood. In the following we give explicit examples for the different possibilities.

1D likelihood parameterization

```
For 1D data, the format remains the same as in [1]. For example, a signal strength
   \mu(ZH,\,b\bar{b})=1.12^{+0.50}_{-0.45} is implemented as
77
      <bestfit>1.12</bestfit>
78
      <param>
79
        <uncertainty side="left">-0.45</uncertainty>
80
        <uncertainty side="right">0.50</uncertainty>
81
      </param>
82
   The <bestfit> tag contains the best-fit value, while the <uncertainty> tag contains the
   left (negative) and right (positive) 1\sigma errors. The choice of likelihood function is done
   by setting type="n" for ordinary, 2-sided Gaussian (as in Lilith-1.1); type="vn" for a
   variable Gaussian; or type="p" for a Poisson distribution in the <expmu> tag.
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2D likelihood parameterization

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For type="vn" and type="p", signal strengths in 2D with a correlation are now described in an analogous way as 1D data. For example, \mu(ggH, WW) = 1.10^{+0.21}_{-0.20} and \mu(VBF, WW) = 0.62^{+0.36}_{-0.35} with a correlation of \rho = -0.08 can be implemented as
```

```
<expmu decay="WW" dim="2" type="vn">
91
92
      <eff axis="x" prod="ggH">1.0</eff>
93
      <eff axis="y" prod="VBF">1.0</eff>
95
      <bestfit>
96
        < x > 1.10 < / x >
97
        < y > 0.62 < / y >
98
      </bestfit>
100
      <param>
101
        <uncertainty axis="x" side="left">-0.20</uncertainty>
102
        <uncertainty axis="x" side="right">+0.21</uncertainty>
103
        <uncertainty axis="y" side="left">-0.35</uncertainty>
104
        <uncertainty axis="y" side="right">+0.36</uncertainty>
        <correlation>-0.08</correlation>
106
      </param>
107
   </expmu>
108
```

Here, the <eff> tag is used to declare the x and y axes. The <bestfit> tag specifies the location of the best-fit point in the (x,y) plane. The <uncertainty> tags contain the left (negative) and right (positive) 1σ errors for the x and y axes, and finally the <correlation> tag specifies the correlation between x and y. The choice of likelihood function is again done by setting type="vn" or type="p" in the <expmu> tag.

To ensure backwards compatibility, type="n" however still requires the tags <a>, , <c> to give the inverse of the covariance matrix instead of <uncertainty> and <correlation>, see [1].

¹The values in the <uncertainty> tag can be given with or without a sign.

Multi-dimensional data

```
For correlated signal strengths in more than 2 dimensions, a new format is introduced.
118
    We here illustrate it by means of the CMS result [3], which has signal strengths for 24
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   production and decay mode combinations plus a 24 \times 24 correlation matrix. First, we set
120
   dim="24" and label the various signal strengths as axes d1, d2, d3, ... d24:2
121
    <expmu dim="24" type="vn">
122
      <eff axis="d1" prod="ggH" decay="gammagamma">1.0</eff>
123
      <eff axis="d2" prod="ggH" decay="ZZ">1.0</eff>
124
      <eff axis="d3" prod="ggH" decay="WW">1.0</eff>
125
126
      <eff axis="d24" prod="ttH" decay="tautau">1.0</eff>
127
   The best-fit values for each axis are specified as
128
      <bestfit>
129
        <d1>1.16</d1>
130
        <d2>1.22</d2>
131
        <d3>1.35</d3>
132
133
        <d24>0.23</d24>
134
      </bestfit>
135
    The  tag then contains the uncertainties and correlations in the form
136
      <param>
137
        <uncertainty axis="d1" side="left">-0.18</uncertainty>
138
        <uncertainty axis="d1" side="right">+0.21</uncertainty>
139
        <uncertainty axis="d2" side="left">-0.21</uncertainty>
        <uncertainty axis="d2" side="right">+0.23</uncertainty>
141
        . . .
142
        <uncertainty axis="d24" side="left">-0.88</uncertainty>
143
        <uncertainty axis="d24" side="right">+1.03</uncertainty>
144
145
        <correlation entry="d1d2">0.12</correlation>
146
        <correlation entry="d1d3">0.16</correlation>
        <correlation entry="d1d4">0.08</correlation>
148
149
        <correlation entry="d23d24">0</correlation>
150
      </param>
151
   </expmu>
   This will also work for type="n".
```

²The <experiment>, <source>, <sqrts>, etc. tags are omitted for brevity.

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154 Likelihood calculation

For the variable Gaussian, the computation of the likelihood in computelikelihood.py follows Section 3.6 "Variable Gaussian (2)" of [4]. The Poisson distribution is implemented according to Section 3.4 "Generalised Poisson", eq. (10a), of [4].

159 give explicit equations and explain implementation i the code

60 ATLAS and CMS results included in the database update

161 ATLAS Run 2 results for 36 fb⁻¹

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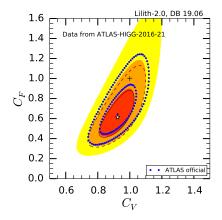
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The ATLAS Run 2 results included in this release are summarised in Table 1 and explained in more detail below.

mode	$\gamma\gamma$	ZZ^*	WW^*	au au	$b \overline{b}$	inv.
ggH	[5]	[6]	[7]	[8]	_	
VBF	[5]	[6]	[7]	[8]	[9]	_
WH	[5]	[6]	_	_	[10]	_
ZH	[၁]	[O]	_	_	[10]	[11]
$\mathrm{tt}\mathrm{H}$	[5, 12]	[6, 12]	[12]	[12]	[12, 13]	_

Table 1: Overview of ATLAS Run 2 results included in this release.

 $H \to \gamma \gamma$ (HIGG-2016-21): The ATLAS analysis [5] provides in Fig. 12 $H \to \gamma \gamma$ signal strengths separated into ggH, VBF, VH and "top" (ttH+tH) production modes. Since no correlations are given for the signal strengths, we use instead the correlations for the stage-0 simplified template cross sections (STXS) provided in Fig. 40a of the ATLAS paper, which should be a close enough match. It turns out that these data do not allow to reproduce very well the ATLAS coupling fits for (C_V, C_F) or (C_γ, C_g) . The reason seems to be that the μ values rounded to one decimal are not precise enough. We have therefore extracted the best-fit points and uncertainties from fits to the 1D profile likelihoods, which are provided as Auxiliary Figures 23a–d on the analysis webpage. and used these together with the STXS correlations in the Lilith XML file. This gives a better coupling fit, as shown in the validation plots in Fig. 1.



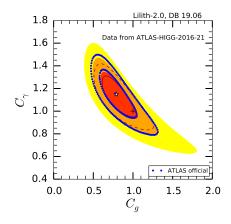


Figure 1: Fit of C_F vs. C_V (left) and C_γ vs. C_g (right) for data from the ATLAS $H \to \gamma \gamma$ analysis [3]. The red, orange and yellow filled areas show the 68%, 95% and 99.7% CL regions obtained with Lilith using best-fit values and uncertainties for the signal strengths as extracted from Aux. Figs. 23a-d of the ATLAS analysis together with the correlation matrix for the stage-0 STXS. This can be compared to the 68%, 95% CL contours obtained using the rounded values from Fig. 12 of [3] (solid and dashed dark red lines) and to the official 68%, 95% CL contours from ATLAS (blue dots).

We note that the same fit quality is obtained when using only the correlation between ggH and VBF production modes (as 2D data) and treating VH and ttH as independent (as 1D data). The relevant XML files are all included in the database, so the user can choose

the preferred combination. This is relevant to avoid double counting when combining this with other measurements, concretely with the data from [12].

 $H \to ZZ^* \to 4l$ (HIGG-2016-22): A similar issue as discussed for $H \to \gamma \gamma$ above arises when using the signal strengths given in Table 9 of [6] together with the correlation matrix given in Aux. Fig. 4a. We therefore use $\mu(\text{ggH}, ZZ^*)$ and $\mu(\text{VBF}, ZZ^*)$ extracted from the 1D profile likelihoods Aux. Figs. 7a and 7b with a correlation $\rho = -0.41$ according to Aux. Fig. 4c. For the VH and ttH production modes, we convert the given 95% CL limits into $\mu(\text{VH}, ZZ^*) = 0^{+1.85}_{-0.0}$ and $\mu(\text{ttH}, ZZ^*) = 0^{+3.75}_{-0.0}$. For validation, we compare to the C_F vs. C_V fit from ATLAS, see Fig. 2.

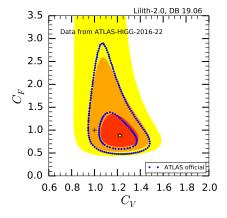


Figure 2: Fit of C_F vs. C_V for data from the ATLAS $H \to ZZ^*$ analysis [6]. The 68%, 95% and 99.7% CL regions obtained with Lilith are shown as red, orange and yellow areas, and compared to the 68%, 95% CL contours from ATLAS (in blue).

```
H 	o WW^* 	o 2l2
u 	ext{ (HIGG-2016-07):}
H 	o 	au	au 	ext{ (HIGG-2017-07):}
H 	o t	au 	ext{ (HIGG-2016-29 and HIGG-2016-30):}
```

 $H \to \text{invisible (HIGG-2016-28)}$: Results from the search for invisibly decaying Higgs bosons produced in association with a Z boson are presented in [11]. Assuming the Standard Model ZH production cross-section, an observed (expected) upper limit of 67% (39%) at the 95% confidence level is set on $BR(H \to inv)$ for $m_H = 125$ GeV. We use 1 – CLs as function $BR(H \to inv)$ extracted from auxiliary Figure 1c on the analysis' webpage.

CMS Run 2 results for 36 fb^{-1}

The CMS Run 2 results included in this release are summarised in Table 2 and explained in more detail below.

mode	$\gamma\gamma$	ZZ^*	WW^*	au au	$b \overline{b}$	$\mu\mu$	inv.
ggH	[3]	[3]	[3]	[3]	[3]	[3]	[14]
VBF	[3]	[3]	[3]	[3]	_	[3]	[14]
WH	[3]	[3]	[3]	[15]	[3]	_	[14]
ZH	[3]	[3]	[3]	[15]	[3]	_	[14]
ttH	[3]	[3]	[3]	[3]	[3]	_	_

Table 2: Overview of CMS Run 2 results included in this release. Note that we use the full 24×24 correlation matrix for the signal strengths for each production and decay mode combination provided in [3].

Combined measurements (HIG-17-031): CMS presented in [3] a combination of the individual measurements for the $H \to \gamma\gamma$ [16], ZZ [17], WW [18], $\tau\tau$ [19], $b\bar{b}$ [20, 21] and $\mu\mu$ [22] decay modes as well as the $t\bar{t}H$ analyses [23–25]. We use the best fit values and uncertainties for the signal strengths for each production and decay mode combination presented in Table 3 of [3] together with the 24 × 24 correlation matrix provided as "Additional Figure 1" on the analysis webpage. As shown in Fig. 3, this allows to reproduce well the coupling fits of the CMS paper.

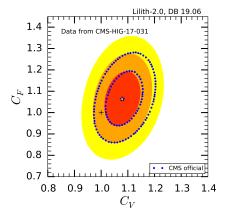


Figure 3: Fit of C_F vs. C_V using best-fit values and uncertainties for the signal strengths for each production (ggH, VBF, WH, ZH, ttH) and decay ($\gamma\gamma$, ZZ, WW, $\tau\tau$, $b\bar{b}$, $\mu\mu$) mode combination together with the 24×24 correlation matrix from the CMS combination paper [3]. The 1σ , 2σ and 3σ regions obtained with Lilith are shown as red, orange and yellow areas, and compared to the 1σ and 2σ contours from CMS (blue dots).

VH, $H \to \tau\tau$ (HIG-18-007): The above data from [3] is supplemented by the results for the $\tau\tau$ decay mode from the WH and ZH targeted analysis [15]. These are implemented in the form of 1D intervals for $\mu(ZH, H \to \tau\tau)$ and $\mu(WH, H \to \tau\tau)$ taken from Fig. 6 of [15].

 $H \to \text{invisible (HIG-17-023)}$: In [14], CMS performed a search for invisible decays of a Higgs boson produced through vector boson fusion. We use the profile likelihood ratios for the qqH-tag, Z(ll)H-, V(qq')H- and ggH-tag categories extracted from their Fig. 8b

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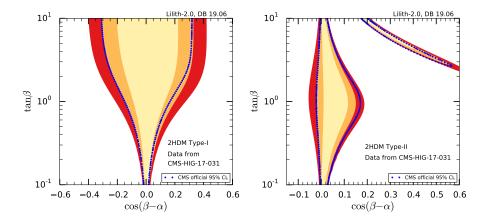


Figure 4: Fit of $\tan \beta$ vs. $\cos(\beta - \alpha)$ for the Two-Higgs-Doublet models of Type I (left) and Type II (right) using the data from the combined CMS measurement [3]. The beige, orange and red filled areas show the 68%, 95% and 99.7% CL regions obtained with Lilith, while the blue dots mark the 95% CL contours from CMS.

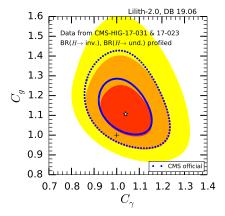


Figure 5: Fit of C_g vs. C_{γ} using the data from the combined CMS measurement [3] and the search for invisible decays of a Higgs boson [14]. The branching ratios of invisible and undetected decays are treated as free parameters in the fit. The 1σ , 2σ and 3σ regions obtained with Lilith are shown as red, orange and yellow areas, and compared to the 1σ and 2σ contours from CMS (in blue).

together with the relative contributions from the different Higgs production mechanisms given in Table 6 of that paper. This assumes that the relative signal contributions stay roughly the same as for SM production cross sections. For validation, we reproduce in Fig. 5 the C_g vs. C_{γ} fit of [3], where the branching ratios of invisible and undetected decays are treated as free parameters.³

³The profiling in Fig. 5 was done with Minuit. Since Minuit does not allow conditional limits, in this case $BR(H \to inv.) + BR(H \to undetected) < 1$, we demanded that both $BR(H \to inv.)$ and $BR(H \to undetected)$ be less than 50%.

225 Status of Higgs coupling fits

26 Conclusion

227 must include a conclusion.

228 Acknowledgements

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Overview of XML data files

Implementation of 2D Poisson likelihood with correlation

Log-likelihood for Poisson distribution with continuous variable

The probability mass function of Poisson distribution, with parameter $\lambda > 0$, and variable k = 0, 1, 2, 3, ...

$$f(k;\lambda) = \frac{e^{-\lambda}\lambda^k}{k!}. (1)$$

239 The log-likelihood function for Poisson distribution:

$$l(\lambda; k) = \log[f(k; \lambda)] = -\lambda + k \log \lambda - \log k!. \tag{2}$$

Here, since k is a discrete variable, we would redefine a log-likelihood function of parameter λ that fix continuous variable, denoted as " ν ". We re-define the parameter as $\lambda \equiv \rho(\lambda - 242 c) + \tau$, with $\eta = \tau/\rho$, and c is the expected value at which the log-likelihood function reaches extrema. The new log-likelihood function reads:

$$l(\lambda; \nu) = -\rho(\lambda - c + \eta) + \nu \log \rho(\lambda - c + \eta) + \text{const.}$$
(3)

Here we want to set the extrema at $\lambda = c$. Since the Poisson distribution has expected value equal it parameter, we set $\nu = \rho \eta$ so that the log-likelihood function reaches extrema at f(c). For Poisson distribution, the extrema of log-likelihood function is not equal 0, we will consider its Δ log-likelihood function:

$$\Delta l(\lambda; \nu) = l(\lambda; \nu) - l(c; \nu) = -\rho(\lambda - c) + \nu \ln \left[1 + \frac{\rho}{\nu} (\lambda - c) \right]. \tag{4}$$

 $\Delta l(\sigma_-; \nu)$ and $\Delta l(\sigma_+; \nu)$ yields -1/2, dividing their r.h.s terms of by ν followed by taking the exponentials, we get the relation:

$$\frac{1 - \gamma \sigma_{-}}{1 - \gamma \sigma_{+}} = e^{-\gamma(\sigma_{-} + \sigma_{+})}.$$
 (5)

From $\Delta l(\sigma_+; \nu) = -1/2$, we could derive ν :

$$\nu = \frac{1}{2(\gamma \sigma_+ - \ln(1 + \gamma \sigma_+))}.\tag{6}$$

A model for bivariate Poisson distribution with negative correlation

252 For references, see: Berkhout, Plug's.

The probability mass function (pmf) of Poisson distribution, with parameter $\lambda > 0$, and variable k = 0, 1, 2, 3, ...:

$$f(k;\lambda) = \frac{e^{-\lambda}\lambda^k}{k!}. (7)$$

We would like to apply a model of bivariate Poisson distribution which allows negative correlation. We define marginal and dependent pmf respectively as:

$$g_1(k_1; \lambda_1) = \frac{e^{-\lambda_1} \lambda_1^{k_1}}{k_1!},\tag{8}$$

$$g_2(k_2|k_1;\lambda_2) = \frac{e^{-\lambda_2}\lambda_2^{k_2}}{k_2!}. (9)$$

257 By convention, the parameters read:

$$\lambda_1 = e^{x'\beta_1},\tag{10}$$

$$\lambda_2 = e^{x'\beta_2 + \alpha k_1}. (11)$$

The parameter α is added as a small correction that correspondent for the correlation of k_1, k_2 . The joint pmf:

$$f(k_1, k_2; \lambda_1, \lambda_2) = g_2(k_2 | k_1; \lambda_2) g_1(k_1; \lambda_1). \tag{12}$$

The marginal pmf remains the form of Poisson distribution, its expected value and variance reads:

$$E(k_1) = \operatorname{Var}(k_1) = \lambda_1. \tag{13}$$

262 The (r, s)th factorial moment of the joint distribution is derived as:

$$E[k_1(k_1-1)...(k_1-r+1)k_2(k_2-1)...(k_2-s+1)]$$
(14)

$$= \sum_{k_1=r}^{\infty} \sum_{k_2=s}^{\infty} \frac{e^{k_1(x'\beta_1) - \exp(x'\beta_1) + k_2(x'\beta_2 + \alpha k_1) - \exp(x'\beta_2 + \alpha k_1)}}{(k_1 - r)!(k_2 - s)!}$$
(15)

$$=\lambda_1^r e^{\lambda_1[\exp(s\alpha)-1]+sx'\beta_2+rs\alpha}. (16)$$

The expected value, variance of k_2 and expected value of k_1k_2 is derived from the factorial moment 16 as:

$$E(k_2) = e^{x'\beta_2 + (\exp(\alpha) - 1)\lambda_1}, \tag{17}$$

$$Var(k_2) = E(k_2) + [E(k_2)]^2 \{ e^{\lambda_1 [\exp(\alpha) - 1]} \},$$
(18)

$$E(k_1k_2) = \lambda_1 E(k_2) \exp(\alpha). \tag{19}$$

The covariance of k_1 and k_2 reads:

$$Cov(k_1, k_2) = E(k_1 k_2) - E(k_1)E(k_2) = \lambda_1 E(k_2)[\exp(\alpha) - 1].$$
(20)

The correlation reads:

$$Corr(k_1, k_2) = \frac{\lambda_1 E(k_2)[\exp(\alpha) - 1]}{\sqrt{\lambda_1 E(k_2)\{1 + E(k_2)\{e^{\lambda_1 [\exp(\alpha) - 1]^2} - 1\}\}}}.$$
 (21)

For later convenience, we derive the relation between λ_2 and $E(k_2)$:

$$\lambda_2 = E(k_2)e^{\alpha k_1 - [\exp(\alpha) - 1]\lambda_1} = E(k_2)e^{\alpha k_1 - [\exp(\alpha) - 1]E(k_1)}.$$
(22)

Log-likelihood for bivariate Poisson distribution with continuous variable and negative correlation

We derive a log-likelihood function that fixes continuous variables for the bivariate Poisson distribution which allows negative correlation. Now for the marginal pmf:

$$g_1(k_1; \lambda_1) = \frac{e^{-\lambda_1} \lambda_1^{k_1}}{k_1!}.$$
 (23)

It remains the form of ordinary Poisson distribution. We apply 4 to derive the Δ loglikelihood function:

$$\Delta l_1(\lambda_1; \nu_1) = -\rho_1(\lambda_1 - c_1) + \nu_1 \log \left[1 + \frac{\rho_1}{\nu_1} (\lambda_1 - c_1) \right]. \tag{24}$$

274 Considering the dependent pmf:

$$g_2(k_2|k_1;\lambda_2) = \frac{e^{-\lambda_2}\lambda_2^{k_2}}{k_2!}. (25)$$

Its log-likelihood function fixing discrete variable k_2 :

$$l_2(\lambda_2; k_2) = \log[g_2(k_2|k_1; \lambda_2)] = -\lambda_2 + k_2 \log \lambda_2 - \log k_2!, \tag{26}$$

with the parameter λ_2 reads:

$$\lambda_2 = E(k_2)e^{\alpha k_1 - [\exp(\alpha) - 1]E(k_1)}. (27)$$

For fixing continuous variable ν_2 , we redefine the parameter λ_2 as:

$$\lambda_2 \equiv \rho_2(\lambda_2 - c_2 + \eta_2)e^{\alpha\nu_1 - [\exp(\alpha) - 1]\rho_1(\lambda_1 - c_1 + \eta_1)}.$$
 (28)

The log-likelihood function l_2 now become a function of two parameters λ_1, λ_2 fixing two variables ν_1, ν_2 :

$$l_2(\lambda_1, \lambda_2; \nu_1, \nu_2) = -\lambda_2 + \nu_2 \log \lambda_2 + \text{const.}$$
(29)

Its Δ log-likelihood function reads:

$$\Delta l_2(\lambda_1, \lambda_2; \nu_1, \nu_2) = l_2(\lambda_1, \lambda_2; \nu_1, \nu_2) - l_2(c_1, c_2; \nu_1, \nu_2). \tag{30}$$

The correlation in 21 becomes:

$$Corr(\nu_1, \nu_2) = \frac{\nu_1 \nu_2 [\exp(\alpha) - 1]}{\sqrt{\nu_1 \nu_2 \{1 + \nu_2 \{e^{\nu_1 [\exp(\alpha) - 1]^2} - 1\}\}}}.$$
 (31)

Finally, the Δ log-likelihood for joint pmf:

$$\Delta l_{\text{join}}(\lambda_1, \lambda_2; \nu_1, \nu_2) = \Delta l_1(\lambda_1; \nu_1) + \Delta l_2(\lambda_1, \lambda_2; \nu_1, \nu_2). \tag{32}$$

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References

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