



**Invertible NN**

momentum scaling

force scaling

translation

$v$   
update:  
( $d = +$ )

$$v_k'' = \Gamma^+(v_k; \zeta_{v_k}) \equiv v_k \odot \exp \left( \frac{\varepsilon_v^k}{2} s_v^k(\zeta_{v_k}) \right) - \frac{\varepsilon_v^k}{2} \left[ \partial_x S(x_k) \odot \exp \left( \varepsilon_v^k q_v^k(\zeta_{v_k}) \right) + t_v^k(\zeta_{v_k}) \right]$$

$$\zeta_{v_k} = [x_k, \partial_x S(x_k)]$$

$x$   
update:  
( $d = +$ )

$$x_k'' = \Lambda^+(x_k; \zeta_{v_k}) \equiv x_k \odot \exp \left( \varepsilon_x^k s_x^k(\zeta_{x_k}) \right) + \varepsilon_x^k \left[ v_k' \odot \exp \left( \varepsilon_x^k q_x^k(\zeta_{x_k}) \right) + t_x^k(\zeta_{x_k}) \right]$$

$$\zeta_{x_k} = [\bar{m}^k \odot x_k, v_k]$$

$$\text{(input)} \quad \xi_0 \rightarrow \xi_1 \rightarrow \cdots \rightarrow \xi_k \rightarrow \xi_{k+1} \rightarrow \cdots \rightarrow \xi_{N_{\text{LF}}} \equiv \xi'' \quad \text{(proposal)}$$