



Invertible NN

v
update:
($d = +$)

$$v_k'' = \Gamma^+(v_k; \zeta_{v_k}) \equiv v_k \odot \exp\left(\frac{\epsilon_v^k}{2} s_v^k(\zeta_{v_k})\right) - \frac{\epsilon_v^k}{2} \left[\partial_x S(x_k) \odot \exp\left(\epsilon_v^k q_v^k(\zeta_{v_k})\right) + t_v^k(\zeta_{v_k}) \right]$$

momentum scaling

force scaling

translation

$$\zeta_{v_k} = [x_k, \partial_x S(x_k)]$$

x
update:
($d = +$)

$$x_k'' = \Lambda^+(x_k; \zeta_{v_k}) \equiv x_k \odot \exp\left(\epsilon_x^k s_x^k(\zeta_{x_k})\right) + \epsilon_x^k \left[v_k' \odot \exp\left(\epsilon_x^k q_x^k(\zeta_{x_k})\right) + t_x^k(\zeta_{x_k}) \right]$$

$$\zeta_{x_k} = [\bar{m}^k \odot x_k, v_k]$$

(input) $\xi_0 \rightarrow \xi_1 \rightarrow \cdots \rightarrow \xi_k \rightarrow \xi_{k+1} \rightarrow \cdots \rightarrow \xi_{N_{\text{LF}}} \equiv \xi''$ (proposal)