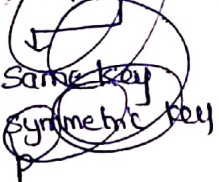


Network Security

1

Cryptography



→ Sym - DES & modes, AES
→ Asym

* For a group of n individuals num of keys reqd in
Private key cryptography - $\frac{n(n-1)}{2}$
Public key cryptography - $2n$

DES :

DES - 56 bit key
2-DES - 112 bits
3-DES - 168 bits

Plaintext { 64 bit
Cipher text { 64 bit

AES 10 Rounds - 128 bit
12 Rounds - 192 bits
14 Rounds - 256 bits

Stages : 19

16

key dependant
and iterative

3

key independent

Proof : Feistel

Attack : Leslie

Monalphabetic substitution.

Modes of DES

- Electronic code book.
- cipher block chaining
- cipher block feedback
- output feedback
- Stream mode
- Counter mode

* 3 DES can be implemented with two keys
E: K_1, K_2, K_1
D: K_1, K_2, K_1

* Property of Good candidate key is N and $\frac{N-1}{2}$ should be primes

RSA Algorithm :

$$P, Q > 10^{100}$$

$$n = P * Q$$

$$\phi(n) = (P-1) * (Q-1)$$

$$\text{GCD}(d, \phi(n)) = 1$$

$$ed \equiv 1 \pmod{\phi(n)}$$

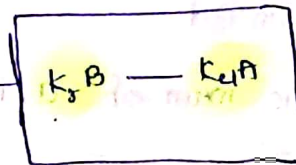
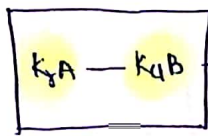
d → private key

(e, n) → public key

$$C \equiv M^e \pmod{n} \rightarrow \text{Encryption}$$

$$M \equiv C^d \pmod{n} \rightarrow \text{Decryption}$$

Digital signature :



sign is big
↓ sol

Message digest



Hash

Algo

E_{K_A}

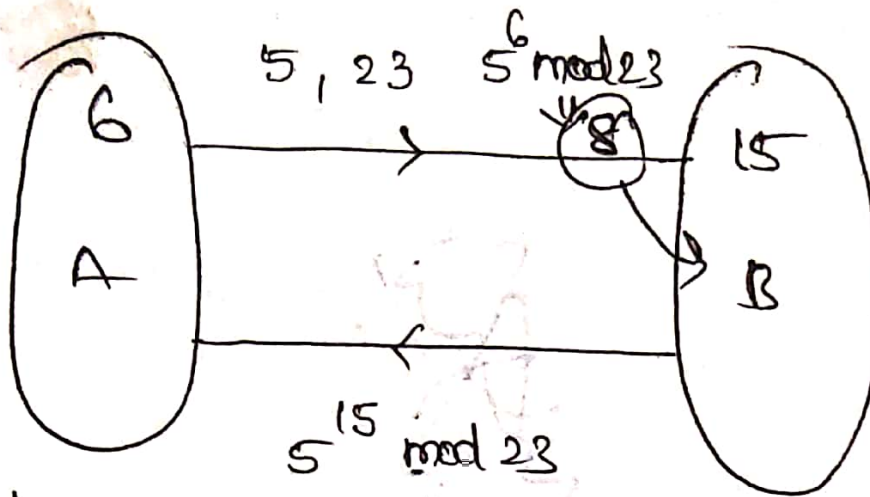
sign

- MD5 - 128 bit
- SHA-1 - 160 bits
- SHA-512 - 512 bit
- SHA-1024 - 1024 bits.

Arbitrary len

11

DH Key Exchange $g=5 \pmod{23}$



$$5^6 \pmod{23} = 8$$

$$5^{15} \pmod{23} = 2$$

$$8^{15} \pmod{23} = 2$$

2	8
8	2

Modular Arithmetic

*) $a \equiv b \pmod{n}$: a and b leave same remainder when you divide them by 'n'.

*) $a \equiv b \pmod{n}$: if n divides $a-b$.

*) if $a \equiv b \pmod{n}$ and $c \equiv d \pmod{n}$ then $a+c \equiv (b+d) \pmod{n}$

$$a-c \equiv (b-d) \pmod{n}$$

$$a*c \equiv (b*d) \pmod{n}$$

Imp *) if $a \equiv (b*c) \pmod{n}$ then $a \equiv (b \pmod{n} * c \pmod{n}) \pmod{n}$.

$$a \equiv (b+c) \pmod{n} \text{ then } a \equiv (b \pmod{n} + c \pmod{n}) \pmod{n}$$

Euler's totient function

Num of +ve integers which are less than 'n', Coprime to n.

*) when n is prime num $\phi(n) = n-1$

*) when m and n are Coprime then $\phi(m*n) = \phi(m) * \phi(n)$
 $= (m-1) * (n-1)$

*) if the prime factorization of n is given by

$$n = p_1^{e_1} * p_2^{e_2} * \dots * p_n^{e_n} \text{ then}$$

$$\phi(n) = n \left(1 - \frac{1}{p_1}\right) \left(1 - \frac{1}{p_2}\right) \dots \left(1 - \frac{1}{p_n}\right)$$

Multiplicative Inverse

For each $a \not\equiv 0 \pmod{p}$ [p is a prime num] there is 'b' such that
 $ab \equiv 1 \pmod{p}$ then b is multiplicative inverse of a.

$$\text{ie } ab \equiv 1 \pmod{p}$$

$$b \equiv a^{-1} \pmod{p}$$

GCD=1

if p is not prime.

if a and n have no common factors then a has a multiplicative inverse mod n.

$$\boxed{\text{GCD}(a, n) = 1}$$

Ex:- ① $2 \not\equiv 0 \pmod{7}$ prime.

$$2 * x \equiv 1 \pmod{7}$$

$$4 \equiv 2^{-1} \pmod{7}$$

4 is multiplicative inverse of 2 mod 7

② $5 \not\equiv 0 \pmod{9}$

$5 * x \equiv 1 \pmod{9}$ not prime but $\text{GCD}(5, 9) = 1$
Coprime.

$$2 \equiv 5^{-1} \pmod{9}$$

Euler's theorem :

If n is a +ve integer and a, n are Coprime then

$$\boxed{a^{\phi(n)} \equiv 1 \pmod{n}}$$

Ex:- $a = 8$ $n = 165$

$$\text{GCD}(8, 165) = 1 \checkmark$$

Now,

$$\phi(165) = 3 * 55 \Rightarrow 3 * 5 * 11$$

$$\Rightarrow 165 \left(1 - \frac{1}{3}\right) \left(1 - \frac{1}{5}\right) \left(1 - \frac{1}{11}\right)$$

$$\Rightarrow 165 * \frac{2}{3} * \frac{4}{5} * \frac{10}{11} \Rightarrow 80$$

$$\therefore \boxed{8^{80} \equiv 1 \pmod{165}}$$

Fermat's theorem :

Special case of Euler's theorem

For any prime number n and $a \not\equiv 0 \pmod{n}$ then

$$\boxed{a^{n-1} \equiv 1 \pmod{n}}$$

* If n is a +ve integer and a, n are Co-prime then (2)

$$a^{\phi(n)+1} \equiv a \pmod{n}$$

(or)

$$a^{\phi(n) \cdot t + 1} \equiv a \pmod{n}$$

Ex:- $a=9$ $n=13$ $\phi(n)=12$.

$$9^{12} \equiv 1 \pmod{13}$$

$$9^{13} \equiv 9 \pmod{13}$$

$$9^{25} \equiv 9 \pmod{13}$$

* If n is a +ve integer, (a, n) are Coprimes and $b \equiv 1 \pmod{\phi(n)}$ then

$$a^b \equiv a \pmod{n}$$

Primitive root:

The number b in $a \equiv b \pmod{n}$ is called residue of $a \pmod{n}$.

Residue:

Ex:- $7 \equiv 85 \pmod{13}$

85 is residue of $7 \pmod{13}$

Residue class:

Residue classes of $f(x) \pmod{n}$ are all possible values of $f(x) \pmod{n}$.

Ex:- RC of $x^2 \pmod{6}$ are $\{0, 1, 3, 4\}$

$$0^2 \pmod{6} \Rightarrow 0$$

$$1^2 \pmod{6} \Rightarrow 1$$

$$2^2 \pmod{6} \Rightarrow 4$$

$$3^2 \pmod{6} \Rightarrow 3$$

$$4^2 \pmod{6} \Rightarrow 4$$

$$5^2 \pmod{6} \Rightarrow 1$$

$$\vdots$$

Ex:- $a=2$ $p=11$ $b=9$

(3)

$a^x \equiv b \pmod{p}$

Primitive root:

Let p be a prime then b is a primitive root for p if powers of b

b^0, b^1, b^2, \dots includes all residue classes of \pmod{p} .

~~Ex:- $p=7$~~

Note: If p is a prime,

The powers of b form a repeating cycle and the cycle can't be larger than $(p-1)$ then b is primitive root of p .

Ex:- $p=7$ $b=3$

$$\begin{aligned} 3^0 &\equiv 1 \pmod{7} \\ 3^1 &\equiv 3 \pmod{7} \\ 3^2 &\equiv 2 \pmod{7} \\ 3^3 &\equiv 6 \pmod{7} \\ 3^4 &\equiv 4 \pmod{7} \\ 3^5 &\equiv 5 \pmod{7} \\ 3^6 &\equiv 1 \pmod{7} \end{aligned}$$

$\therefore 3$ is primitive root

* Excluding 1, 2, 4 the numbers with primitive roots are of shape $p^k, 2p^k$ where p is odd prime number

Ex:- 3, 5, 6, 7, 10, 14, $2 \cdot 7^2, \dots$

* 'm' is primitive root modulo n iff multiplicative order of m is $\phi(n)$
ie $m^{\phi(n)} \equiv 1 \pmod{n}$.

Discrete logarithm:

The problem of finding x such that $a^x \equiv b \pmod{p}$ [p is prime, a, b are non zero integers] is called discrete logarithm problem.

→ It is a Np hard problem

→ It is one way function

↓
if $f(x)$ is easy to compute, but y is computationally infeasible to find x such that $y = f(x)$.

Ex:- $a = 2$ $p = 11$ $b = 9$

$a \equiv b \pmod{p}$

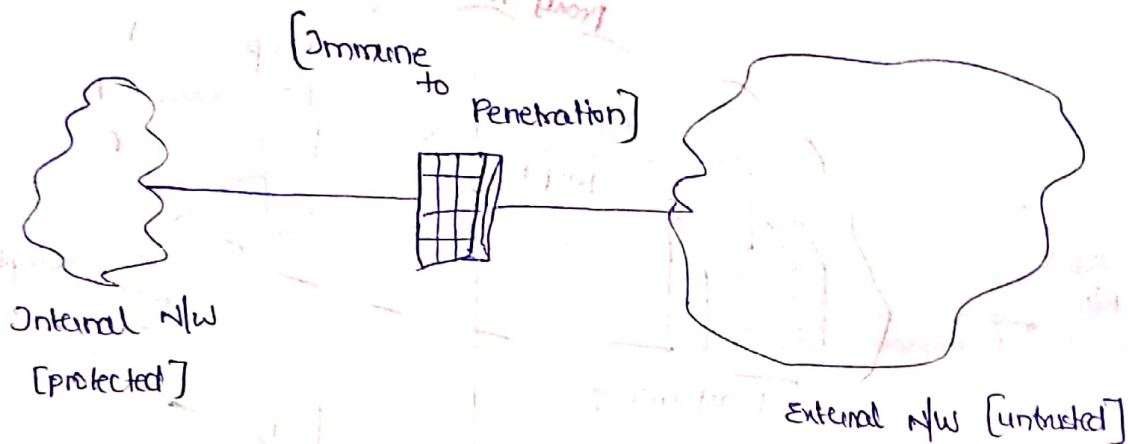
$2^x \equiv 9 \pmod{p}$

At $(x=6) \rightarrow$ Hard to find

Fire walls : (software)

\rightarrow A Firewall forms a barrier through which the traffic going in each direction must pass through it

\rightarrow A Firewall security policy dictates which traffic is authorized to pass in each direction



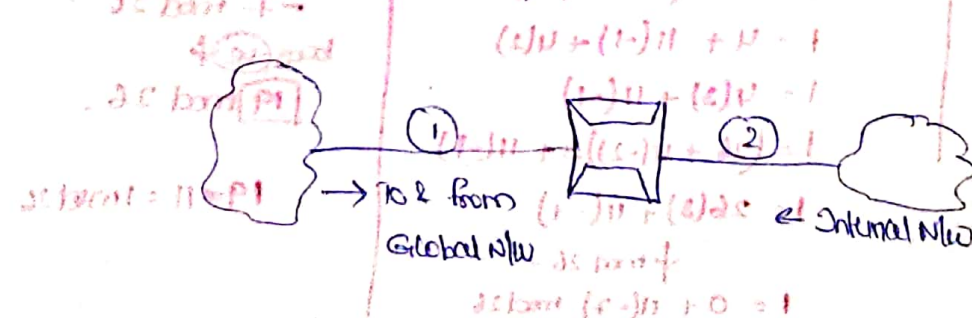
\Rightarrow A Firewall may be designed to operate as a filter at the level of Ip packets or may operate at higher layer protocols.

\rightarrow ~~A Firewall defines a single choke point~~

Types of Firewalls :

① packet filtering Firewall :

A packet filtering firewall applies a set of rules to each incoming and outgoing Ip packet and then forwards or discards the packet based on information present in Tcp and Ip headers.

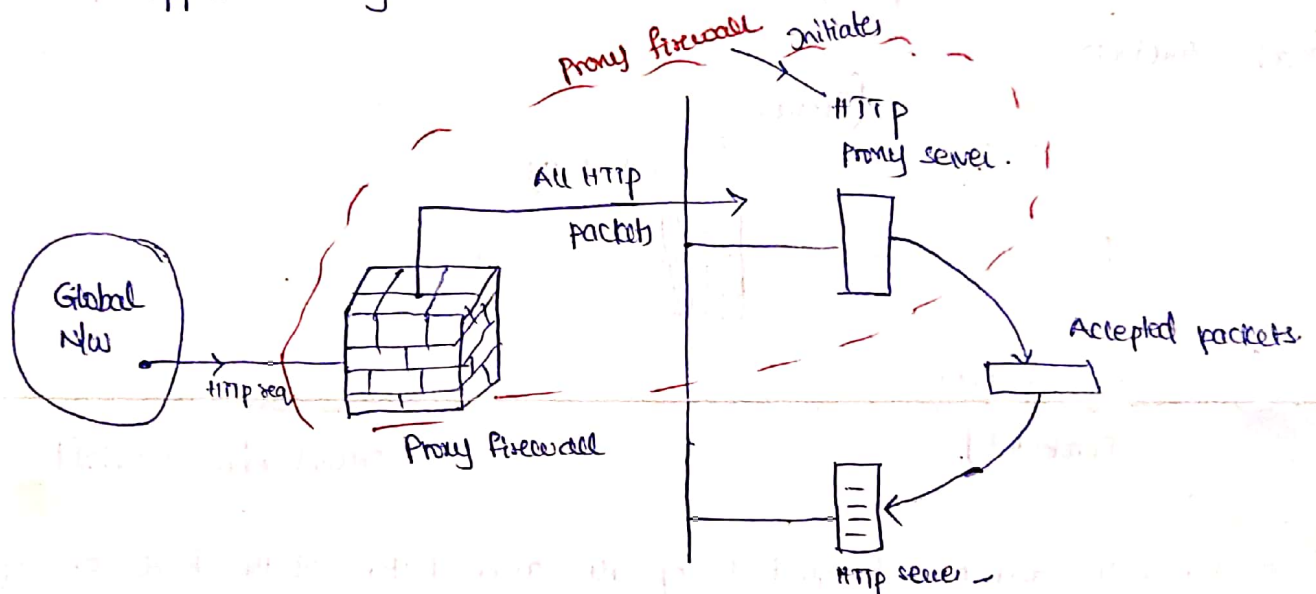


then

Interface	Source Ip	Source port	Destination Ip	Destination port	
1	131.34.0.0	*	*	*	Block a N/w entering into Internal N/w
*	*	*	*	23	Block Telnet service from both sides
1	*	*	194.78.0.8	*	Block accessing particular Ip addr
2	*	80	*	*	Block HTTP is accessed within Internal N/w

② proxy firewall :

- Filters the message based on contents of the message
- works at application layer



- When user client process sends a message, the proxy firewall sends a server process to receive the request
- The server opens the packet at the application level and finds out if the request is legitimate.

Finding modulo inverse : ($11^{-1} \bmod 26$)

Using Extended Euclidean Algo

$$26 = 11(2) + 4$$

$$11 = 4(2) + 3$$

$$4 = 3(1) + 1 \rightarrow \text{can be applied}$$

$$3 = 1(3) + 0$$

$$\therefore 1 = 4 + 3(-1)$$

$$1 = 4 + (11 + 4(-2))(-1)$$

$$1 = 4 + 11(-1) + 4(2)$$

$$1 = 4(3) + 11(-1)$$

$$1 = (26 + 11(-2))3 + 11(-1)$$

$$1 = 26(3) + 11(-7)$$

$$\downarrow \bmod 26$$

$$1 = 0 + 11(-7) \bmod 26$$

$$1 = 11(-7) \bmod 26$$

$$-7 \bmod 26 =$$

$$\text{bec } (-ve) \rightarrow 19 \bmod 26$$

$$19 * 11 = 1 \bmod 26$$