

Implementing an SVM: A Shot in the Dark

Daniel Hanson, Sam Kreter, Brendan Marsh, and Christina R.S. Mosnick

Abstract—The abstract goes here.

I. INTRODUCTION

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II. IMPLEMENTATION

Our SVM implementation first uses a parser class to transform the input data. The parser is able to load and write numpy arrays of the testing and label data. To transform the label sets for training individual class dividers, the parser sets all labels that are of the current class being trained to 1, and to -1 for the rest of the classes. Additionally, we created a set of kernel functions to be passed into the svm instance dynamically, depending on the particular kernel needed. We packaged the training and prediction functionalities into instances of svm classes, which additionally store trained variables such as the support vectors and the bias. This allows us to train and store multiple svms.

The SVM class is instantiated with the pre-processed samples (feature vectors), their corresponding labels (1 or -1), the appropriate kernel function, and its necessary parameters (such as σ for an RBF function). In the training function, the support vectors are computed by finding the Gram Matrix, which stores all possible combinations of data points being passed into the kernel. We then solve for the dual form using lagrangian optimization (below), using cvxopt for our quadratic programming solver.

A. Dual Representation (from Eqn. 7.2 [1])

$$\mathbf{L} = \sum_N a_n - \frac{1}{2} \sum_n \sum_m a_n a_m t_n t_m \mathbf{K} \quad (1)$$

In order to use the CVXOPT solver we need to convert the Dual Representation into the standard quadratic programming form shown in equation 2.

B. Quadratic Programming Problem [3]

$$\min_{\mathbf{x}} \frac{1}{2} \mathbf{x}^T \mathbf{P} \mathbf{x} - \mathbf{Q}^T \mathbf{x} \quad (2)$$

C. Parameters for Quadratic Programming

By transforming the dual representation we derived the parameters shown in equations 3 and 4.

$$\mathbf{P} = \sum_n \sum_m t_n t_m \mathbf{K} \quad (3)$$

$$\mathbf{Q} = \begin{pmatrix} -1 & -1 & -1 \\ -1 & -1 & -1 \\ -1 & -1 & -1 \end{pmatrix} \quad (4)$$

- Where Q's dimensions are determined by number of samples

D. Constraints

Next we changed the constraints into a form that is necessary for the quadratic programming solver as shown in equations 5, 6.

$$\mathbf{G} \mathbf{x} \leq \mathbf{h} \quad (5)$$

$$\mathbf{A} \mathbf{x} \leq \mathbf{b} \quad (6)$$

Equation 7 is referencing the transformation for the standard constraints.

$$a_n \geq 0 \rightarrow -a_n \leq 0 \quad (7)$$

$$\text{std} \mathbf{G} \begin{pmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \quad (8)$$

$$\text{std} \mathbf{H} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad (9)$$

Equation 10 is referencing the transformation for the slack constraints.

$$a_n \leq \mathbf{C} \quad (10)$$

$$\text{slack} \mathbf{G} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \quad (11)$$

$$\text{slack} \mathbf{H} \begin{pmatrix} \mathbf{C} & \mathbf{C} & \mathbf{C} \\ \mathbf{C} & \mathbf{C} & \mathbf{C} \\ \mathbf{C} & \mathbf{C} & \mathbf{C} \end{pmatrix} \quad (12)$$

Equation 13 is referencing the transformation for the equality constraints.

$$\sum_{n=1}^N a_n t_n = 0 \quad (13)$$

$$\mathbf{A} = \mathbf{y} \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix} \quad (14)$$

$$\mathbf{B} = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad (15)$$

E. Bias

Solving for a gives us the indices for the support vectors. These, along with the passed in data, give us the vectors, labels, and weights of the support vectors. We can use all of this information to find the bias and start computing predictions on the functions. The bias is simply computed from the form in equation 16:

$$b = \frac{1}{N_M} \sum_{n \in M} (t_n - \sum_{m \in S} a_m t_m k(\mathbf{x}_n, \mathbf{x}_m)) \quad (16)$$

F. Prediction

We now have everything we need to implement the prediction function from equation 17:

$$y(\mathbf{x}) = \sum_{n=1}^N a_n t_n k(\mathbf{x}, \mathbf{x}_n) + b \quad (17)$$

We also use equation 17 to find the bias since it is the same equation when b is zero.

After calling the training function with the data set, labels, and kernel function, we can now call the predict function by passing in a test point. It will return some value between 1 and -1 which we can use to classify the point.

Next, we tackled the problem of classifying many classes with an SVM that only supports two class classification. To do this we used two different methods for comparison. In both cases we use a 1 vs the rest model in a bootstrapping method. We train a matrix of SVMs in which the columns denote SVMs trained on different classes and the rows denote SVMs of the same class but different subsets of the training data (bootstrap samples). In the first case, we take the arithmetic mean of each set of SVMs for a particular class. The class with the highest overall mean (above a set certainty threshold) will be used for the final label class, as long as it achieves a minimum threshold. The certainty threshold ensures that if all committee results are low, the point should be determined unclassified.

The second bootstrapping testing method classifies points based on the mean of the committee votes, weighted by their standard deviations. To do this, we find the standard deviation of the results, and subtract a standard deviation from the arithmetic mean. This helps to lower confidence intervals in situations where a committees individual results for a point

vary more, and increase confidence when variance is low for a given point. The class with the highest value is once again chosen, given it is below the certainty threshold.

Finally we have implemented a pickling function to write and load the trained SVMs to a file in order to persist the state of the trained SVMs instead of having to train the SVMs on the same training data over and over again. This can be very beneficial for using larger bootstrapping samples or having more classes where it would take a large amount of time to train.

III. EXPERIMENTS

After the SVMs were all trained using the bootstrapping method, we used a committee-waterfall approach to determine the best class for each test point. In order to do this, the SVMs are grouped by classifier, with 7 independently trained SVMs per each of the 8 classifiers. Each test point is run through each of the 7*8=56 SVMs.

IV. CONCLUSION

Conclusion paragraph text goes here.

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