

Difference between Q_{Kappa} and Q_p :

Dahlen and Tromp 1998, page 350

$$C_p = \sqrt{\frac{K + \frac{4}{3}\mu}{\rho}} = \sqrt{\frac{\lambda + 2\mu}{\rho}}$$

$$\Rightarrow K = \lambda + 2\mu - \frac{4}{3}\mu = \lambda + \frac{2}{3}\mu \quad \text{in 3D}$$

Carcione 1993 generalizes this to 2D and 3D by writing: (see also Carcione et al 1988 equation (A9))
 $K = \lambda + \frac{2}{n}\mu$ with n the spatial dimension ($n=2$ or $n=3$)

Q_μ is always equal to Q_s , but

Q_{Kappa} is not equal to Q_p in general.

The formula to convert one to the other is given in Dahlen and Tromp (1998) eq (9.59):

$$Q_p = \frac{1}{\frac{1 - \frac{4}{3}\left(\frac{C_s}{C_p}\right)^2}{Q_{\text{Kappa}}} + \frac{\frac{4}{3}\left(\frac{C_s}{C_p}\right)^2}{Q_{\text{mu}}}}$$

This formula is wrong in 2D plane strain, see next page.

$\lambda(f)$ and $C_p = C_p(f)$ are given by at which one wants to conversion (for a ^{really} constant Q , λ does not matter); however representation of a constant Q it

does vary a little bit, because $\frac{C_s}{C_p}$ will slightly vary with f because they scale as $\sqrt{\frac{1}{N} \sum \frac{\tau_{E1}}{C_{G1}}}$ and $\sqrt{\frac{1}{N} \sum \frac{\tau_{E2}}{C_{G2}}}$.

In 2D plane strain, one spatial dimension is much greater than the others (see for example: <http://www.engineering.ucsb.edu/~hpscicom/projects/stress/introge.pdf>) and thus $\kappa = \lambda + \mu$ in 2D plane strain (instead of $\kappa = \lambda + \frac{2}{3}\mu$ in 3D).

See for example equation 6 in <http://cherrypit.princeton.edu/papers/paper-99.pdf>. In 2D axisymmetric I think the $\frac{2}{3}$ coefficient is OK, but it would be worth doublechecking.