

# One-way ANOVA

MAM5120 - Statistical Concepts, Methods and Tools

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# Content

## 1 Introduction

## 2 Hypothesis

## 3 ANOVA Table

## 4 Example

- Analysing Data
- Calculations
- R: ANOVA Table

## 5 Conclusions



# Introduction to ANOVA

## One-way ANOVA

- to compare three or more means
- to determine whether groups are significantly different
- useful to test differences between medicines, populations, etc.

## Assumptions

- samples are independent
- response is normally distributed



# Hypothesis

## NULL HYPOTHESIS

$$H_0: \mu_1 = \mu_2 = \mu_3 = \dots = \mu_k$$

## ALTERNATIVE HYPOTHESIS

$H_A$ : "at least two means are different"

## Significance

if p-value is significant at 95% ( $p < 0.05$ ) then we reject the NULL Hypothesis



## Table

Source	SS	df	MS	F	p(>F)
Treatment	$SS_{treat}$	k-1	$SS_{treat} / (k - 1)$	$MS_{treat} / MS_{resid}$	p
Residual	$SS_{resid}$	N-k	$SS_{resid} / (N - k)$		
Total	$SS_{treat} + SS_{resid}$	N-1			

## Annotating

- SS = Sum of Squares
- df = Degrees of Freedom
- MS = Mean of Squares
- F = f-statistic



## Example

A Marine Research Centre want to observe sightings of Maui's Dolphins off the coast of New Zealand for 3 random days



Figure: Maui dolphin. Image Source: Daily Mail<sup>1</sup>

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<sup>1</sup> <http://www.dailymail.co.uk/sciencetech/article-2118304/Worlds-smallest-dolphin-threat-nets-species-reduced-just-55-survivors.html?ito=feeds-newsxml>



# Data

Sightings				
Random Day	Morning	Afternoon	Evening	Night
1	6	3	10	8
2	4	7	9	7
3	3	8	8	5
<b>6.5</b>	4.3333...	6	9	6.6666...

## Assuming

- Sightings/Days are independent
- Counts/Numbers are normally distributed



# Identifying Calculations

$k = 4$ ;  $N = 12$ ; at 95%

Source	SS	df	MS	F
Treatment	33.6667	3	11.2222	3.54386
Residual	25.3333	8	3.1667	
Total	59	11		

## Annotating

- $SS_{treat}: 3(4.3333... - 6.5)^2 + 3(6 - 6.5)^2 + ... = 33.6667$
- $SS_{resid}: ((6 - 4.3) + (4 - 4.3) + (3 - 4.3)) + ((3 - 6) + (7 - 6) + ...) + ... = 25.3333$
- $df_t = k - 1 = 4 - 1 = 3$
- $df_r = N - k = 12 - 4 = 8$
- $MS_{treat} : SS_{treat} / df_t = 33.6667 / 3 = 11.2222$
- $MS_{resid} : SS_{resid} / df_r = 25.3333 / 8 = 3.1667$
- $F : MS_{treat} / MS_{resid} = 11.2222 / 3.1667 = 3.54386$





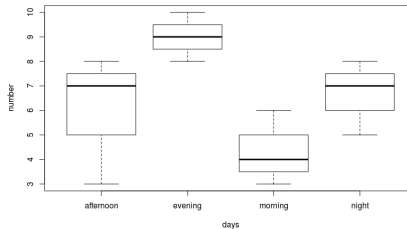
# Example in R

```
> summary(aov(number ~ days, data=sightings))
```

	Df	Sum Sq	Mean Sq	F value	Pr(>F)	
days	3	33.67	11.222	3.544	0.0677	.
Residuals	8	25.33	3.167			

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Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1



## Remember

if p-value is significant at 95% ( $p < 0.05$ ) then we reject the NULL Hypothesis



# Results

- p-value = 0.0677
- $p > 0.05$
- not significant at 95%
- insufficient evidence to reject  $H_0$  in favour of  $H_A$
- observations from different times of day come from distributions that have the same mean

