

Week 6, Day 2

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Continuing on with Uncertainty

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Potential measures and ways to visualize uncertainty:

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- ▶ Visually we are likely to encounter error bars, highlighted confidence intervals, or some other sort of visual differentiation between a given estimate and the surrounding potential range of values.

Confidence Intervals

- ▶ We will encounter confidence intervals here (CIs for short). I'd like for us to know how to interpret this correctly, especially related to our confidence levels.
- ▶ Confidence intervals specify a potential range of values for a potential measurement of interest, given an associated confidence level.

$$CI = \text{Measurement} \pm MoE = [\text{Upper Bound}, \text{Lower Bound}]$$

- ▶ Where the **Margin of Error (MoE)** is the standard error ($\frac{\sigma}{\sqrt{n}}$) multiplied by the Z-or t-score relative to the chosen confidence level (typically 95%, but also 90% and 99% possible).

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- ▶ *Standard deviation* is an estimated statistical parameter about the spread of our data. Basically the expected amount of variation from observation to observation in the sample, and consequentially inferred about the population.
- ▶ *Standard error* is a measure of precision relative to the sample and its associated standard deviation.

Formulae

Sample Standard Deviation of Mean s :

$$s = \sqrt{\frac{\sum_{i=1}^N (x_i - \bar{x})^2}{n - 1}}$$

where the numerator is the squared sum of differences between each observation x_i of the variable of interest and the variable's mean (\bar{x}). The denominator is the number of observations n minus 1. Easily done in R by `sd(var, na.rm = T)`.

Sample Standard Deviation of Proportion s :

$$s = \sqrt{\hat{\pi}(1 - \hat{\pi})}$$

Where $\hat{\pi}$ is the sample proportion.

Formulae

Standard Error (SE):

If based on a mean:

$$SE = \frac{s}{\sqrt{n}}$$

Where s is the sample standard deviation.

If based on proportion:

$$SE = \frac{s}{\sqrt{n}} = \sqrt{\frac{\hat{\pi}(1 - \hat{\pi})}{n}}$$

Margin of Error

Confidence Level	z
0.70	1.04
0.75	1.15
0.80	1.28
0.85	1.44
0.90	1.645
0.92	1.75
0.95	1.96
0.96	2.05
0.98	2.33
0.99	2.58

Point Estimates and Uncertainty

- ▶ But the concept instead is to provide the exact measurement available with the data, then show the range of potential values
- ▶ Could be mean, median, or the entire distribution that we can place a potential interval around.