

```

1 #include<bits/stdc++.h>
2 using namespace std;
3 using Int = long long;
4 //BEGIN CUT HERE
5
6 #define EPS (1e-10)
7 #define equals(a,b) (fabs((a)-(b)) < EPS)
8 #define PI 3.141592653589793238
9 struct Point3D{
10     double x,y,z;
11     Point3D(){}
12     Point3D(double x,double y,double z):x(x),y(y),z(z){}
13     Point3D operator+(Point3D p) {return Point3D(x+p.x,y+p.y,z+p.z);}
14     Point3D operator-(Point3D p) {return Point3D(x-p.x,y-p.y,z-p.z);}
15     Point3D operator*(double k){return Point3D(x*k,y*k,z*k);}
16     Point3D operator/(double k){return Point3D(x/k,y/k,z/k);}
17     Point3D operator*(Point3D p){
18         return Point3D(y*p.z-z*p.y,z*p.x-x*p.z,x*p.y-y*p.x);
19     }
20     double operator^(Point3D p){
21         return x*p.x+y*p.y+z*p.z;
22     }
23     double norm(){return x*x+y*y+z*z;}
24     double abs(){return sqrt(norm());}
25     bool operator < (const Point3D &p) const{
26         if(x!=p.x) return x<p.x;
27         if(y!=p.y) return y<p.y;
28         return z<p.z;
29     }
30     bool operator == (const Point3D &p) const{
31         return fabs(x-p.x)<EPS && fabs(y-p.y)<EPS && fabs(z-p.z)<EPS;
32     }
33 };
34 istream &operator >> (istream &is,Point3D &p){
35     is>>p.x>>p.y>>p.z;
36     return is;
37 }
38 ostream &operator << (ostream &os,Point3D p){
39     os<<fixed<<setprecision(12)<<p.x<<" "<<p.y<<" "<<p.z;
40     return os;
41 }
42
43 typedef Point3D Vector3D;
44 typedef vector<Point3D> Polygon3D;
45
46 struct Segment3D{
47     Point3D p1,p2;
48     Segment3D(){}
49     Segment3D(Point3D p1, Point3D p2):p1(p1),p2(p2){}
50 };
51 typedef Segment3D Line3D;
52
53 istream &operator >> (istream &is,Segment3D &s){
54     is>>s.p1>>s.p2;
55     return is;
56 }
57
58 struct Sphere{
59     Point3D c;
60     double r;

```

```

61   Sphere(){}
62   Sphere(Point3D c,double r):c(c),r(r){}
63 };
64
65 istream &operator >> (istream &is,Sphere &c){
66     is>>c.c>>c.r;
67     return is;
68 }
69
70 double norm(Vector3D a){
71     return a.x*a.x+a.y*a.y+a.z*a.z;
72 }
73 double abs(Vector3D a){
74     return sqrt(norm(a));
75 }
76 double dot(Vector3D a,Vector3D b){
77     return a.x*b.x+a.y*b.y+a.z*b.z;
78 }
79 Vector3D cross(Vector3D a,Vector3D b){
80     return Vector3D(a.y*b.z-a.z*b.y,a.z*b.x-a.x*b.z,a.x*b.y-a.y*b.x);
81 }
82
83 Point3D project(Line3D l,Point3D p){
84     Point3D b=l.p2-l.p1;
85     double t=dot(p-l.p1,b)/norm(b);
86     return l.p1+b*t;
87 }
88
89 Point3D reflect(Line3D l,Point3D p){
90     return p+(project(l,p)-p)*2.0;
91 }
92
93 double getDistanceLP(Line3D l,Point3D p){
94     return abs(cross(l.p2-l.p1,p-l.p1)/abs(l.p2-l.p1));
95 }
96
97 double getDistanceSP(Segment3D s,Point3D p){
98     if(dot(s.p2-s.p1,p-s.p1) < 0.0 ) return abs(p-s.p1);
99     if(dot(s.p1-s.p2,p-s.p2) < 0.0 ) return abs(p-s.p2);
100    return getDistanceLP(s,p);
101 }
102
103 bool intersectSC(Segment3D s,Sphere c){
104     double d=getDistanceSP(s,c.c);
105     if(d>c.r) return 0;
106     return !((abs(s.p1-c.c)<=c.r)&&(abs(s.p2-c.c)<=c.r));
107 }
108
109 struct ConvexHull3D{
110     struct face{
111         Int a,b,c;
112         bool ok;
113         face(){}
114         face(Int a,Int b,Int c,bool ok):a(a),b(b),c(c),ok(ok){}
115     };
116     Int n,num;
117     vector<Point3D> p;
118     vector<face> f;
119     vector<vector<Int> > g;
120

```

```

121 ConvexHull3D(Int n):n(n),p(n),f(n*8),g(n,vector<Int>(n)){}
122
123 void input(){
124     for(Int i=0;i<n;i++) cin>>p[i];
125 }
126
127 double dblcmp(Point3D q,face f){
128     Point3D m=p[f.b]-p[f.a];
129     Point3D n=p[f.c]-p[f.a];
130     Point3D t=q-p[f.a];
131     return (m*n)^t;
132 }
133
134 void deal(Int q,Int a,Int b){
135     Int idx=g[a][b];
136     face add;
137     if(f[idx].ok){
138         if(dblcmp(p[q],f[idx])>EPS) dfs(q,idx);
139     }
140     else{
141         add=face(b,a,q,1);
142         g[q][b]=g[a][q]=g[b][a]=num;
143         f[num++]=add;
144     }
145 }
146
147 void dfs(Int q,Int now){
148     f[now].ok=0;
149     deal(q,f[now].b,f[now].a);
150     deal(q,f[now].c,f[now].b);
151     deal(q,f[now].a,f[now].c);
152 }
153
154 void build(){
155     num=0;
156     if(n<4) return;
157     bool flg=1;
158     for(Int i=1;i<n;i++){
159         if(abs(p[0]-p[i])>EPS){
160             swap(p[1],p[i]);
161             flg=0;
162             break;
163         }
164     }
165     if(flg) return;
166     flg=1;
167     for(Int i=2;i<n;i++){
168         if(abs((p[0]-p[1])*(p[1]-p[i]))>EPS){
169             swap(p[2],p[i]);
170             flg=0;
171             break;
172         }
173     }
174     if(flg) return;
175     flg=1;
176     for(Int i=3;i<n;i++){
177         if(abs(((p[0]-p[1])*(p[1]-p[2]))^(p[0]-p[i]))>EPS){
178             swap(p[3],p[i]);
179             flg=0;
180             break;

```

```

181     }
182 }
183 if(flag) return;
184 face add;
185 for(Int i=0;i<4;i++){
186     add=face((i+1)%4,(i+2)%4,(i+3)%4,1);
187     if(dblcmp(p[i],add)>0) swap(add.b,add.c);
188     g[add.a][add.b]=g[add.b][add.c]=g[add.c][add.a]=num;
189     f[num++]=add;
190 }
191 for(Int i=4;i<n;i++){
192     for(Int j=0;j<num;j++){
193         if(f[j].ok&&dblcmp(p[i],f[j])>EPS){
194             dfs(i,j);
195             break;
196         }
197     }
198 }
199 Int tmp=num;
200 num=0;
201 for(Int i=0;i<tmp;i++){
202     if(f[i].ok) f[num++]=f[i];
203 }
204
205 double volume(Point3D a,Point3D b,Point3D c,Point3D d){
206     return ((b-a)*(c-a))^(d-a);
207 }
208
209 bool same(Int s,Int t){
210     Point3D &a=p[f[s].a];
211     Point3D &b=p[f[s].b];
212     Point3D &c=p[f[s].c];
213     return (abs(volume(a,b,c,p[f[t].a]))<EPS)
214         && (abs(volume(a,b,c,p[f[t].b]))<EPS)
215         && (abs(volume(a,b,c,p[f[t].c]))<EPS);
216 }
217
218 Int polygon(){
219     Int res=0;
220     for(Int i=0;i<num;i++){
221         Int flg=1;
222         for(Int j=0;j<i;j++){
223             flg&=!same(i,j);
224         }
225         res+=flg;
226     }
227     return res;
228 }
229
230 Int triangle(){
231     return num;
232 }
233
234 double area(Point3D a,Point3D b,Point3D c){
235     return abs((b-a)*(c-a));
236 }
237
238 Point3D cross(Point3D a,Point3D b,Point3D c){
239     return Point3D((b.y-a.y)*(c.z-a.z)-(b.z-a.z)*(c.y-a.y),
240         (b.z-a.z)*(c.x-a.x)-(b.x-a.x)*(c.z-a.z),
241         (b.x-a.x)*(c.y-a.y)-(b.y-a.y)*(c.x-a.x));

```

```
241 }
242
243 double area(){
244     double res=0;
245     if(n==3){
246         Point3D q=cross(p[0],p[1],p[2]);
247         res=abs(q)/2.0;
248         return res;
249     }
250     return res;
251     for(Int i=0;i<num;i++)
252         res+=area(p[f[i].a],p[f[i].b],p[f[i].c]);
253     return res/2.0;
254 }
255 };
256
257 //END CUT HERE
258
259 signed main(){
260     Int n;
261     while(cin>>n){
262         ConvexHull3D ch(n);
263         ch.input();
264         ch.build();
265         cout<<ch.polygon()<<endl;
266     }
267     return 0;
268 }
269
270 /*
271     verified on 2017/12/31
272     http://rhodon.u-aizu.ac.jp:8080/arena/room.jsp?id=3794
273 */
```