



ifis

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Multimedia Databases

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- Multiresolution Analysis
- Shape-based Features
 - Thresholding
 - Edge detection
 - Morphological Operators





5 Shape-based Features

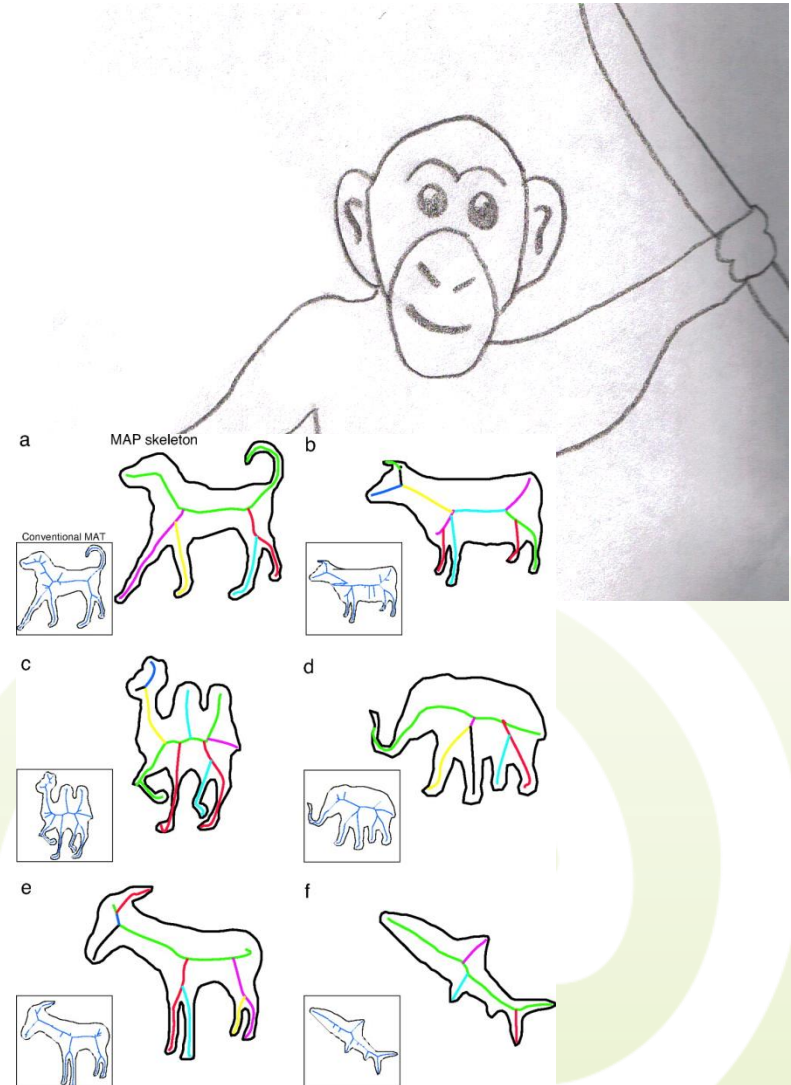
5 Shape-based Features

5.1 Chain Codes

5.2 Area-based Retrieval

5.3 Moment Invariants

5.4 Query by Example





5.1 Shape Representation

- Segmentation provides multiple different possibilities for the **representation** of individual objects or of the entire image
 - **Individual objects**
 - Description of the contours by characteristics of a closed curve
 - Description of the area that is enclosed by the curve
 - Hybrid representation (curve and surface)
 - **Entire image**
 - Description of the dominant edges in the image (e.g., edge histograms)



5.1 Shape Representation

- Shape based image similarity allows for **different** interpretations:
 - Images with **similar shaped objects**
 - Images with **similar dominant shapes**
- Both are reasonable ideas and a “meaningful” definition is highly dependent on the particular application



5.1 Contour-based Comparison

- By comparing the contours we can determine which images contain **similarly shaped objects**
- The outline is usually viewed as **closed contour**
- This is more or less provided through segmentation
- The **semantics** of the objects here is better described than e.g., global edge images



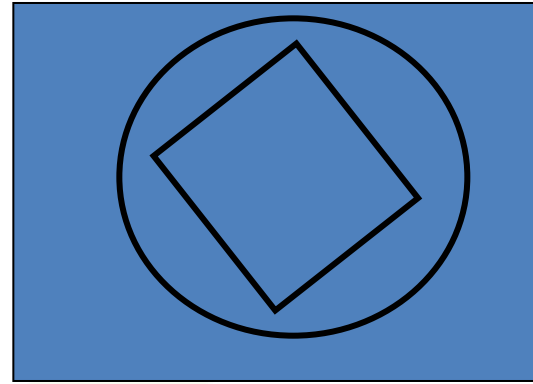
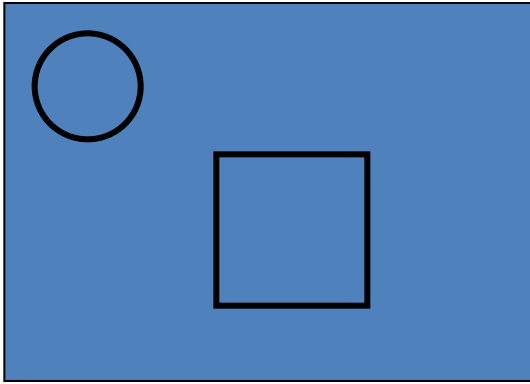
5.1 Contour-based Comparison

- Shape matching requires **complex similarity measures**
- Requirements for the comparative measure:
 - Invariant regarding **shifts** (translation invariance)
 - Invariant regarding **scaling**
 - Invariant regarding **rotations** (rotational invariance)





5.1 Contour-based Comparison



- Visual impression of the two images is different, but the shapes are identical



5.1 Low Level Features

- Simple indicators of forms, which are characterized by their contour:
 - Number of vertices
 - Area
 - Enclosed area (holes are not included)
 - Eccentricity
 - ...



5.1 Low Level Features

- These numbers only give an **absolute sense** of the shape
 - Scale invariance is not provided
 - The shape is not reconstructable
 - The similarity of shapes due to such numbers (e.g., shape area) is doubtful
- In shape description, low level features are **only helpful** in combination with other features



5.1 Chain Codes

- **Chain codes** (also known as Freeman codes)
 - Are very simple pixel-based descriptions of a form (Freeman, 1961)
- The contour is traversed either clockwise/inverse
- Changes of the edges direction are logged
- Each pixel receives a code depending on its predecessor

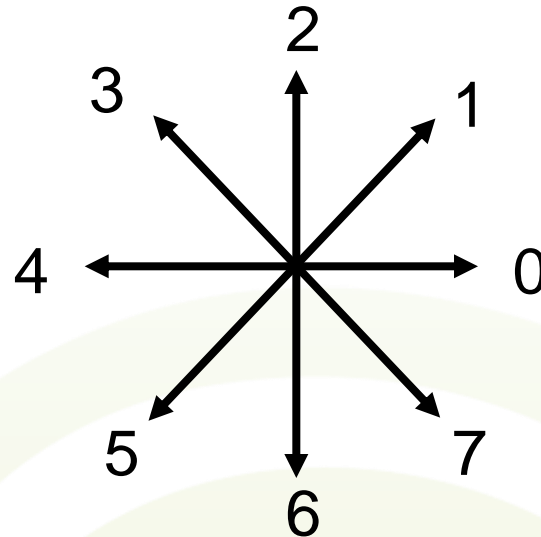




5.1 Chain Codes

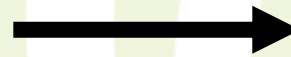
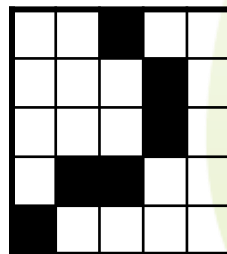
- **Direction codes**

3	2	1
4	X	0
5	6	7



- Translation invariance is clear in this way

- E.g.:



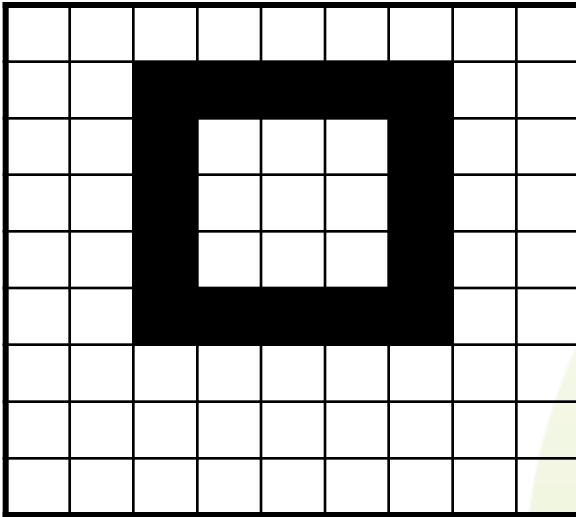
... x 1 0 1 2 3 ...

(Chain Code of the image)

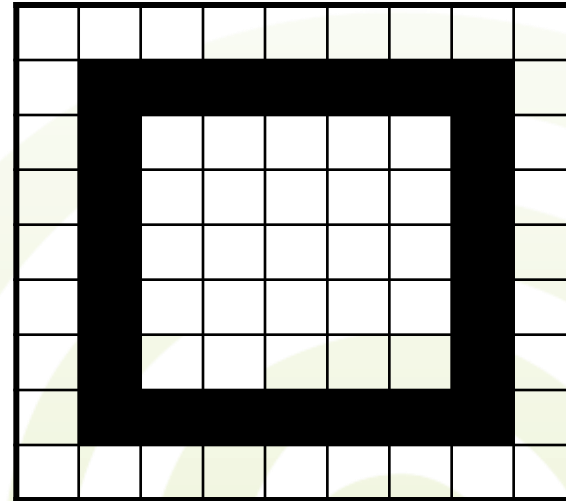


5.1 Chain Codes

- **For scale invariance:**
 - Remove equal consecutive numbers (works poorly with complex shapes)



00000666664444422222 → 0642



00000006666666444444222222 → 0642

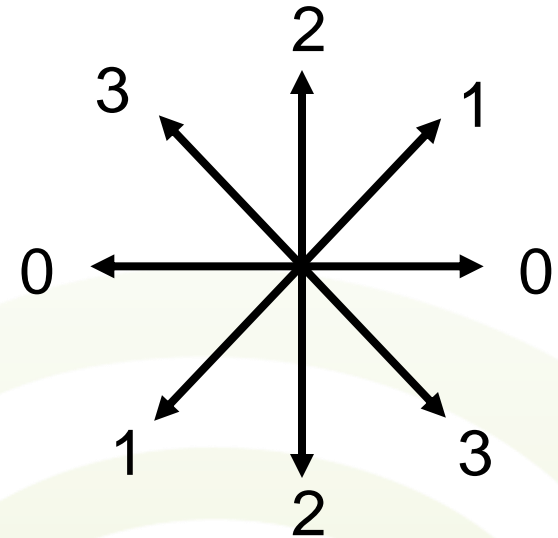
- Rectangles have the same code as squares



5.1 Chain Codes

- **Reduced Chain code**

3	2	1
0	X	0
1	2	3



- Opposite directions receive the same encoding



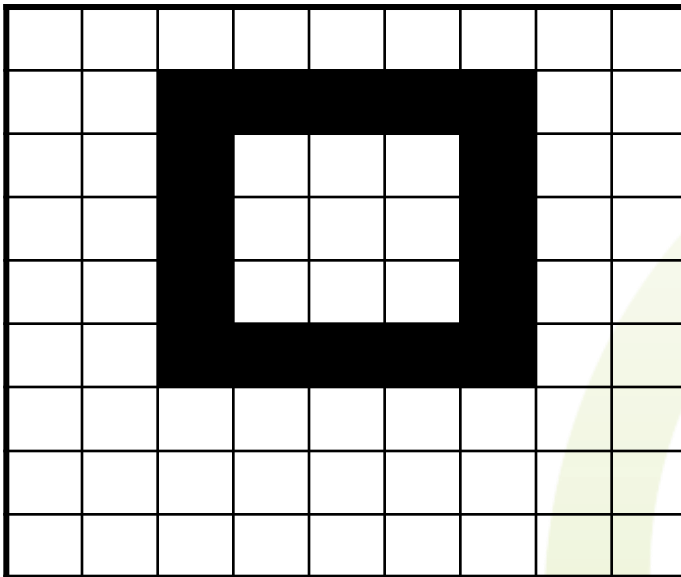
5.1 Chain Codes

- **Reduced Difference Chain Code (RDC)**
(Freeman, 1961)
 - Each two consecutive points are summarized by their difference
 - Advantage: compression
 - (0 0 0 0 2 2 2 2 0 0 0 0 2 2 2 2)
 - (0 0 0 0 -2 0 0 0 2 0 0 0 0 -2 0 0 0 2)
 - (0 -2 0 2 0 -2 0 2)



5.1 Chain Codes

- Reduced Difference Chain Code bring a conditional **rotational invariance**



Chain Code:

00000666664444422222

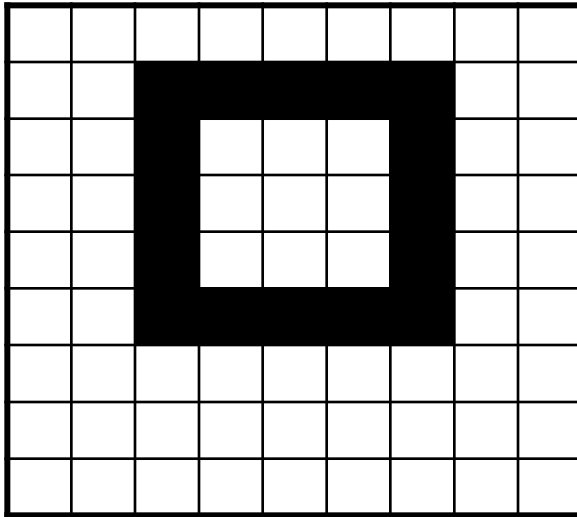
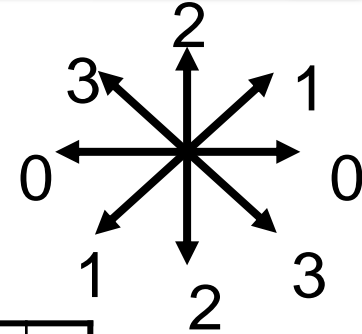
Reduced Chain Code:

00000222220000022222

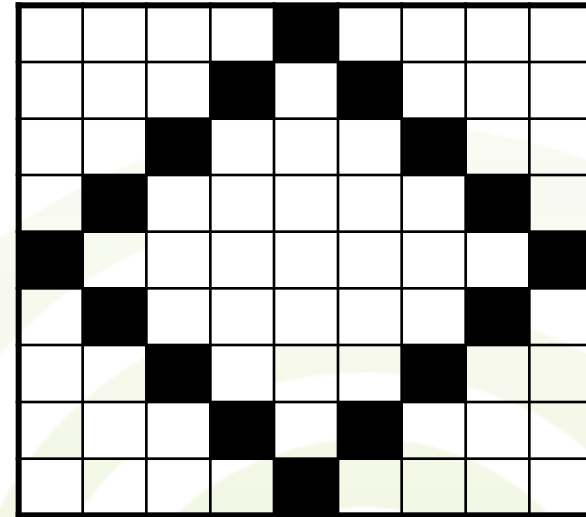


5.1 Chain Codes

- Example: rotational invariance



00000222220000022222
→ 0 -2 0 2 0 -2 0 2

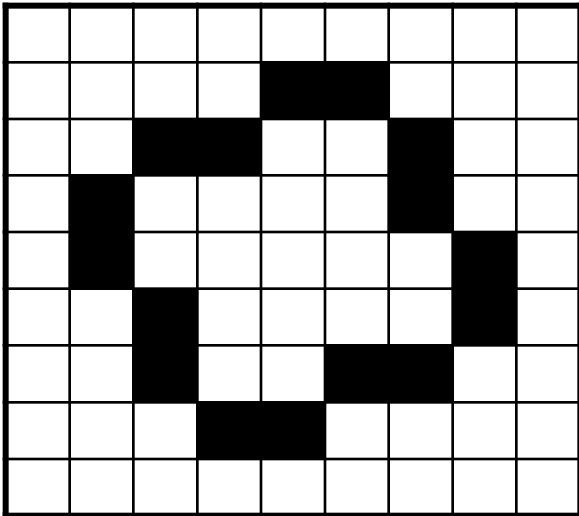


11111333331111133333
→ 0 -2 0 2 0 -2 0 2



5.1 Chain Codes

- Works only with rotations by multiples of 45°



0 1 0 1 2 3 2 3 0 1 0 1 2 3 2 3 0

→ -1 1 -1 -1 -1 1 -1 3

-1 1 -1 -1 -1 1 -1 3

→ -1 1 -1 1 -1 3

-1 1 -1 1 -1 3

- Sequence of numbers in the code is not unique



5.1 Chain Codes

- Alternative coding describes this behavior with edges (Shape numbers) (Bribiesca / Guzman, 1978)
- convex corner
Code 1
- edge
Code 2
- concave corner
Code 3





5.1 Chain Codes

- **Shape numbers**
 - Generate all **cyclic permutations** of the chain code
 - Sort the list of these permutations **lexicographically**
 - Select as encoding of the shape **first permutation** of this list



5.1 Chain Codes

- Matching of two chain codes by comparing the two generated strings

$$A = (a_1, \dots, a_m) \text{ and } B = (b_1, \dots, b_n)$$

- Often is **edit distance** used for comparison:
 - Levensthein-distance
 - Advanced Levensthein-distance
 - ...



5.1 Chain Codes

- **Weighted Levenstein distance**
 - Idea: string A can be converted through a sequence of
 - Substitutions of single characters ($a \rightarrow b$),
 - Insertions ($\epsilon \rightarrow a$) and
 - Deletions ($a \rightarrow \epsilon$)into string B
 - Each of these operations have associated costs (natural numbers)
 - Find a sequence of operations, which converts A to B , with **minimal cost**
 - These costs are the **distance** between A and B



5.1 Chain Codes

- **Advanced Levensthein-distance**
 - Generalization of Levensthein-distance
 - Additional, operations:
 - $aab \rightarrow abb$
 - $abb \rightarrow aab$
 - $a \rightarrow aa$
 - $aa \rightarrow a$
 - This will also be assigned cost values
 - Distance is again the minimum total value of all the transformations from A to B



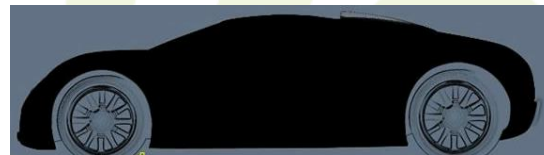
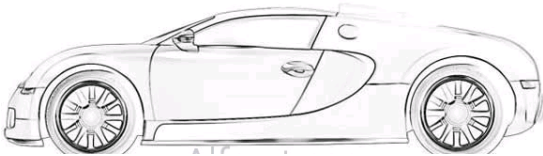
5.1 Chain Codes

- **Advantages:**
 - Relatively easy to calculate
- **Disadvantages:**
 - Scaling and rotation invariance are not always given
 - Much information is reduced or lost



5.2 Area-based Retrieval

- Representation
 - Area based description doesn't only use the contour, but also the **interior of a shape**
 - Representations are divided into
 - Information-preserving representations (Image transformations, etc.)
 - Non-information-preserving representations (Low-Level Features, descriptive moments, ...)





5.2 Representation

- **Transformation**
 - Hough, Walsh, Wavelet transforms
- **Structural representation**
 - Primitive shapes which cover an area (rectangles, circles, ...)
- **Geometric representation**
 - Shape area, number of holes, compactness, symmetry, moments, moment invariants, ...



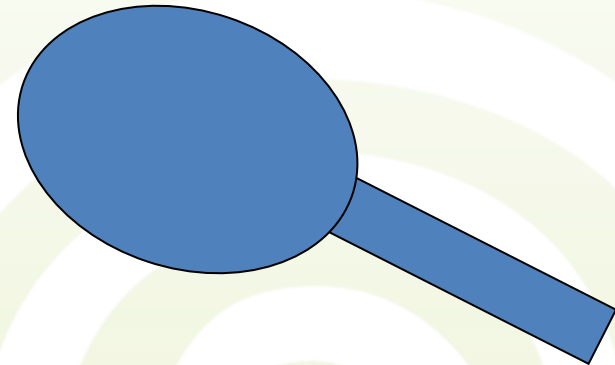
5.2 Low Level Features

- **Shape area**
 - Number of set pixels
- **Roundness**
 - $\text{Perimeter}^2 / \text{surface area}$
(minimum) for circles
- **Euler number**
 - Difference:
 - Number of connected components
 - Number of holes in the components



5.2 Structural Representation

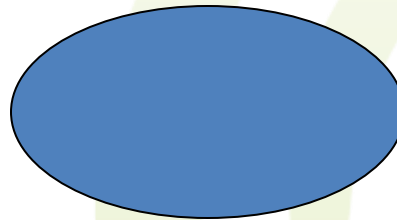
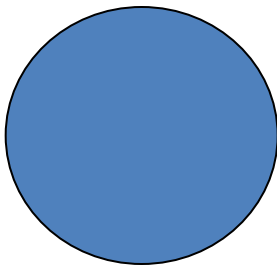
- How well can shapes be covered with a minimal number of **primitive shapes**?





5.2 Structural Representation

- Primitive shapes are e.g., **Superquadrics** (Barr, 1981)
 - Distortion of circles (spheres), e.g., ellipsoids, hyperboloids, etc.
 - Distortions are twists, bends, ...





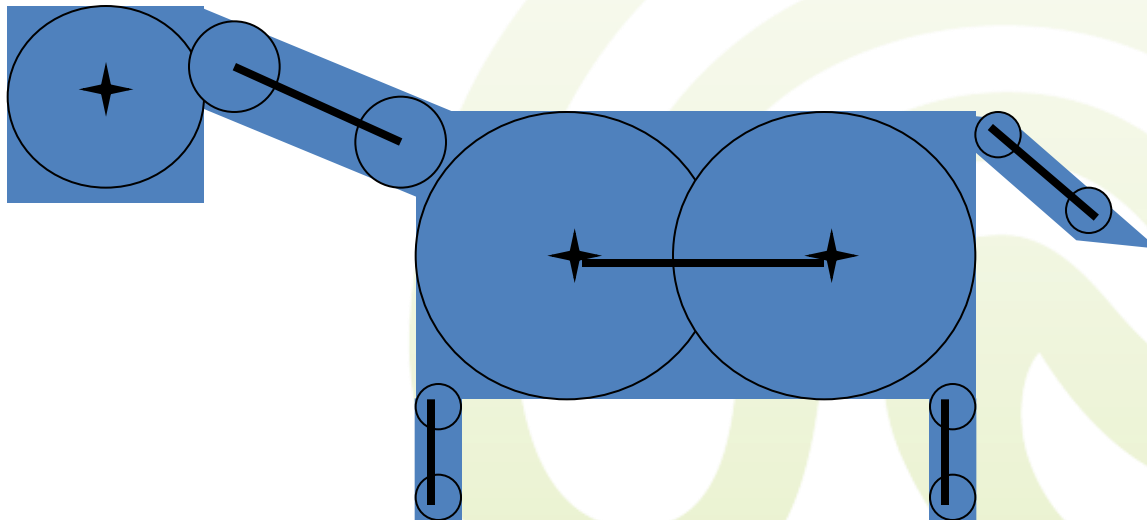
5.2 Structural Representation

- We aim at obtaining a minimal **coverage**
- What does **minimal** mean?
 - The encoding of each shape requires a certain length (depending on complexity)
 - If only primitive shapes are used, then, representation is susceptible to flaws
 - If more shapes are used...
 - Then the **total length** of the coding is higher
 - But the **error** is smaller
 - **Therefore:** Minimize a weighted sum consisting of length and coding errors



5.2 Skeleton

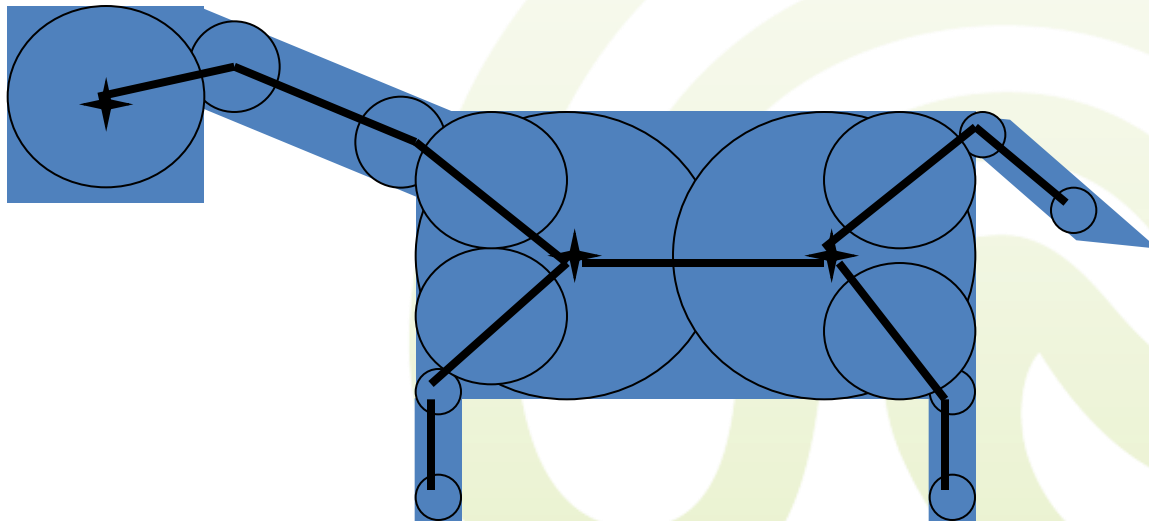
- Shapes can also be described by their **skeleton** (Blum, 1973)
 - **Central axis:** the number of centers of all circles with maximum area, inscribed in the shape





5.2 Skeleton

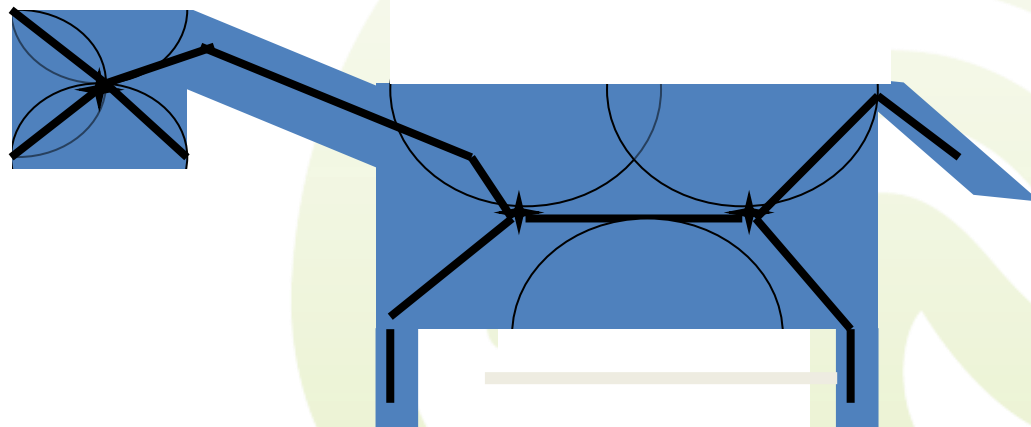
- **Symmetric boundary points**
 - Set of centers of all inscribed, bitangent circles (bitangent = 2 points of contact)
 - Slightly more accurate than the central axis, but very sensitive to small changes in the shape





5.2 Skeleton

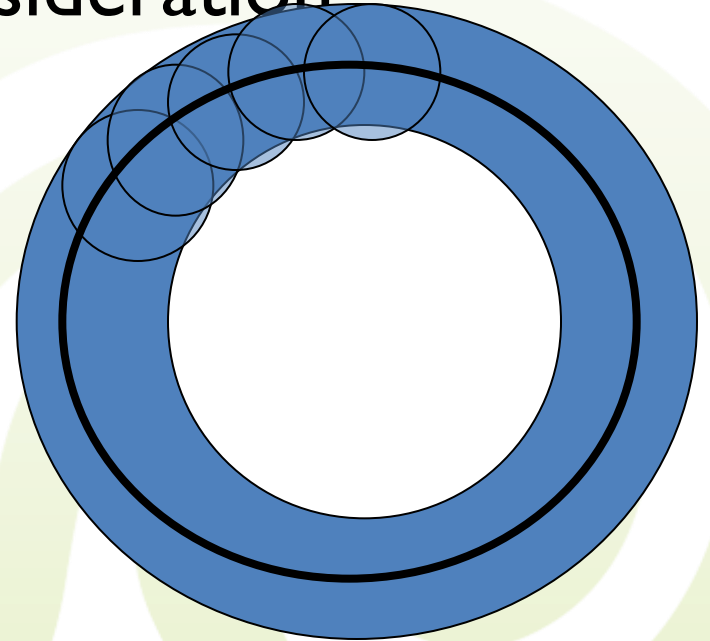
- The **shock set** approach
 - Also results in a skeleton
 - Wave fronts start from the edges with the same speed. The skeleton is provided by the points where the wave fronts meet (like wildfire)





5.2 Skeleton

- The **graph of the skeleton** is stored and used for comparison
- Skeletons are indeed calculated from boundary points, but also take into consideration shapes, e.g., holes





5.2 Skeleton

- Example: (Sebastian and Kimia, 2005)





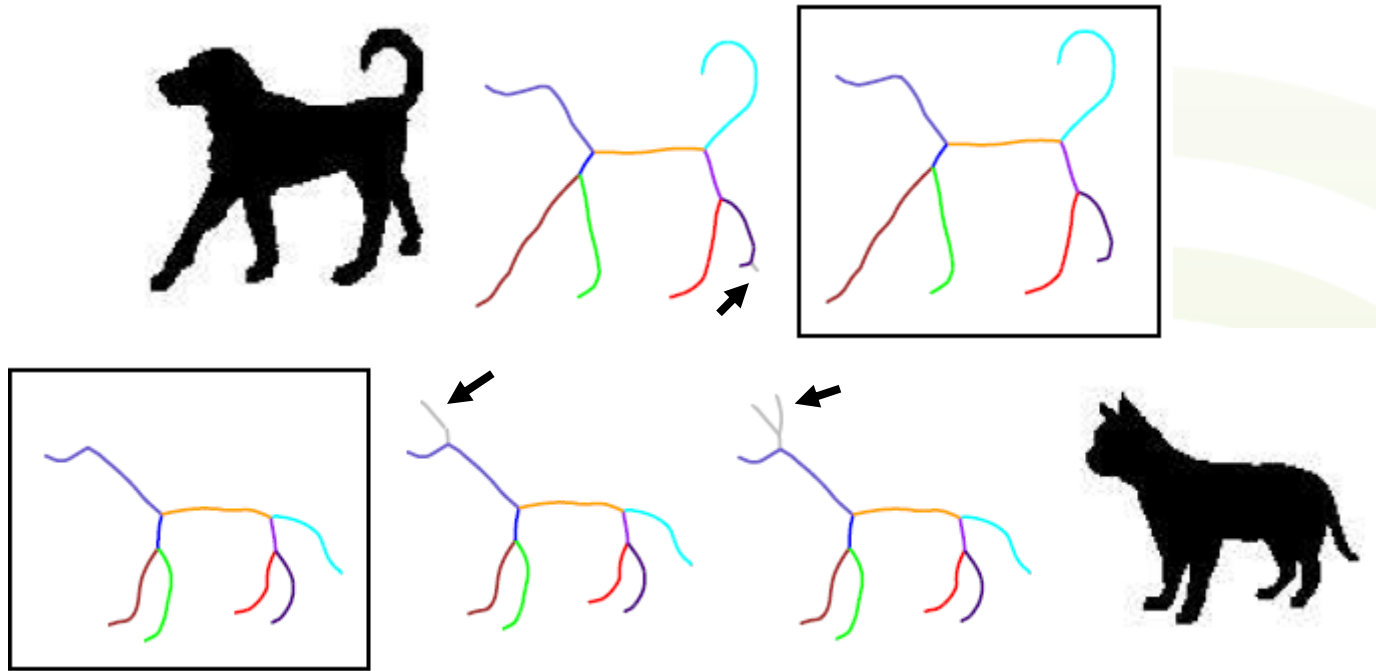
5.2 Skeleton

- The matching of different skeletons is usually done by using the editing distance with different editing costs
- Four basic editing operations:
 - **Splice** removes a skeleton branch
 - **Contract** represents n branches at a node with $n-1$ branches
 - **Merge** removes a node between exactly two skeleton branches
 - **Deform** deforms a branch



5.2 Skeleton

- Example: skeletons have the same topology after some splice operations





5.3 Moments

- A special type of shape features based on the **image moments**
- The **intensity function** $I(x, y)$ of the gray values of an image (after appropriate normalization) can be in addition interpreted as a **probability distribution** on the pixels of the image
 - If we take a random pixel of the image, considering this distribution, there is a high probability that the pixel is dark and a low probability that is bright
- The **statistical properties** of I can be used as shape features



5.3 A little Stochastics

- Let f be a **discrete probability distribution** on a finite set A of real numbers
- Then:
 - $f(x) \geq 0$ for all $x \in A$,
 - $\sum_{x \in A} f(x) = 1$
- If X is a **random variable with distribution f** , then $f(x)$ is the probability that X takes the value x





5.3 A little Stochastics

- The **i-th moment** of X is

$$m_i := \sum_{x \in A} x^i \cdot f(x)$$

- Already known from the stochastic:
The **first moment** of X is the **expected value**



5.3 Uniqueness Theorem

- Each distribution function can be uniquely described by its moments
- **Uniqueness Theorem:**
 - f can uniquely be reconstructed from the sequence of moments m_0, m_1, m_2, \dots
 - The only condition: all elements must exist, that is, be finite





5.3 A little Stochastics

- The **i-th central moment** of X is

$$\mu_i := \sum_{x \in A} (x - \bar{x})^i \cdot f(x)$$

where \bar{x} denotes the expected value of X

- The second central moment of X is the **variance**
- The first central moment is always 0
- Important property: central moments are **invariant to shifts**



5.3 2-D Moments

- Now let f be a **two-dimensional** discrete distribution function, e.g.:
 - $f : A \times B \rightarrow [0, 1]$
 - $f(x, y) \geq 0$ for all $(x, y) \in A \times B$
 - $\sum_{(x,y) \in A \times B} f(x, y) = 1$
- Where (X, Y) is a **random vector** with distribution f



5.3 2-D Moments

- The **(i, j)-th moment** of (X, Y)

$$m_{i,j} := \sum_{(x,y) \in A \times B} x^i \cdot y^j \cdot f(x, y)$$

- The **(i, j)-th central moment** of (X, Y) is

$$\mu_{i,j} := \sum_{(x,y) \in A \times B} (x - m_{1,0})^i \cdot (y - m_{0,1})^j \cdot f(x, y)$$

- Known: $\mu_{1,1}$, is the **covariance** of X and Y
- The **uniqueness theorem** applies also here, as before



5.3 Image as Distribution

- Example: an image of width b and height h with pixel intensities $I(x, y)$:



$$b = 10$$

$$h = 6$$

$$I(0, 0) = 0, \quad I(2, 0) = 1, \quad I(1, 1) = 1, \quad \dots$$

- By normalizing I , we obtain a two-dimensional **discrete probability distribution** f :

$$f(x, y) := \frac{I(x, y)}{\sum_{(u, v) \in A \times B} I(u, v)}$$

$$A := \{0, 1, \dots, b - 1\}$$

$$B := \{0, 1, \dots, h - 1\}$$



5.3 Image Moments as Features

- Considering the uniqueness theorem, the moments of f (the **image moments**) represent a complete description of the image
- Therefore: use the (first k) image moments as shape features
- By using the central moments we have features that are **invariant towards shifts!**
- But: how do we obtain invariance against scaling and rotation?



5.3 Scaling Invariant Moments

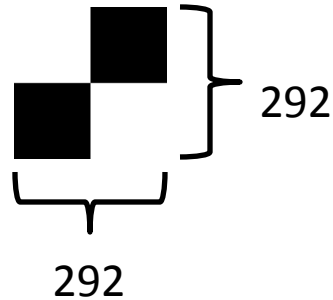
- From the central moments, we can calculate the **normalized central moments**:

$$\eta_{i,j} := \frac{\mu_{i,j}}{\left(\sum_{(x,y) \in A \times B} I(x,y) \right)^{(i+j)/2}}$$

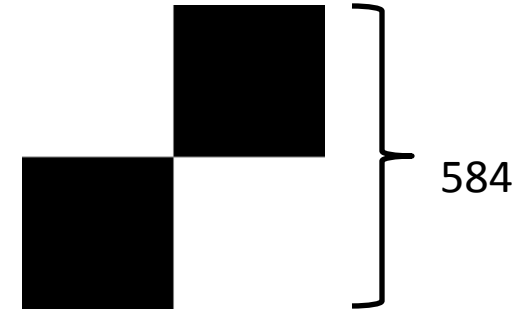
- It can be shown that:
 - The normalized central moments $\eta_{i,j}$ are **invariant towards scaling**



5.3 Example (Scaling Invariant)



- $m_{0,1} = 146$
- $m_{1,0} = 146$
- $m_{0,2} = 28349$
- $m_{1,1} = 16060$
- $m_{2,0} = 28349$
- $\mu_{0,1} = 0$
- $\mu_{1,0} = 0$
- $\mu_{0,2} = 7032$
- $\mu_{1,1} = -5256$
- $\mu_{2,0} = 7032$



- $m_{0,1} = 291,5$
- $m_{1,0} = 291,5$
- $m_{0,2} = 113100$
- $m_{1,1} = 63947$
- $m_{2,0} = 113100$
- $\mu_{0,1} = 0$
- $\mu_{1,0} = 0$
- $\mu_{0,2} = 28131$
- $\mu_{1,1} = -21025$
- $\mu_{2,0} = 28131$

- $\eta_{0,1} = 0$
- $\eta_{1,0} = 0$
- $\eta_{0,2} = 0,165$
- $\eta_{1,1} = -0,1233$
- $\eta_{2,0} = 0,165$



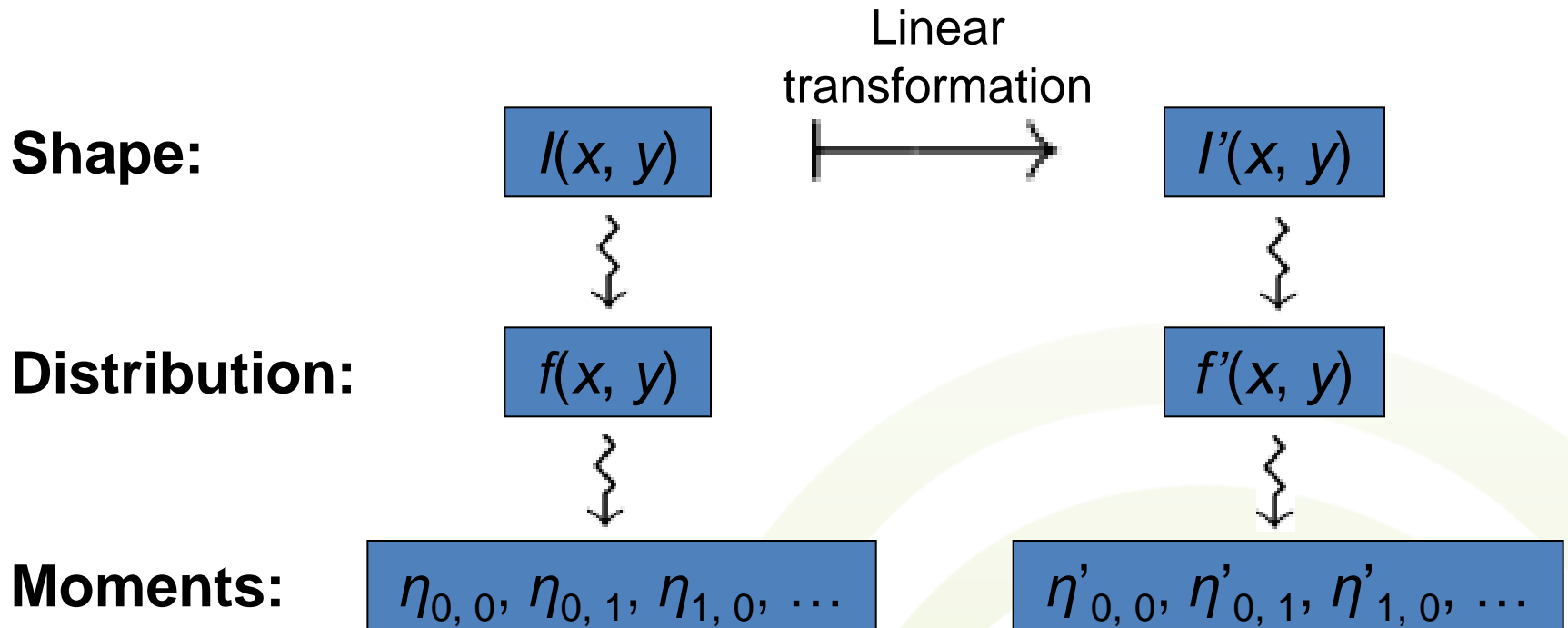
5.3 Linear Transformation

- We still lack the **rotational invariance**
- Rotations (and scaling) in the \mathbb{R}^2 can be described through **linear transformations**
 - These are functions $t: \mathbb{R}^2 \rightarrow \mathbb{R}$, described by a (2×2) matrix A , thus $t(x, y) = A \cdot (x, y)$
- Rotation with angle α (followed by scaling with factor s):

$$A = s \cdot \begin{pmatrix} \cos(\alpha) & -\sin(\alpha) \\ \sin(\alpha) & \cos(\alpha) \end{pmatrix}$$



5.3 Moment Invariants



- **Goal: invariant functions g with**

$$g(\eta_{0,0}, \eta_{0,1}, \eta_{1,0}, \dots) = g(\eta'_{0,0}, \eta'_{0,1}, \eta'_{1,0}, \dots)$$



5.3 Moment Invariants

- We are looking for functions g , which transform the normalized central moments to **new characteristic values**, so that ...
 - Rotations of the original shape do not change these metrics
- These metrics describe the form, **regardless of their location and size**
- Such functions are called **moment invariants** (Hu, 1962)



5.3 Algebraic Invariants

- How do we find moment invariants?
 - Algebra: **algebraic invariants**
 - A function $g: \mathbb{R}^n \rightarrow \mathbb{R}$ is called **relative invariant** with weight $w \in \mathbb{R}$, if for all $(n \times n)$ matrices with full rank and all $x \in \mathbb{R}^n$ we have:
 - $g(A \cdot x) = [\det(A)]^w \cdot g(x)$
 - Thus invariant under linear transformation expressed by A
- For $w = 0$, g is called **absolute invariant**



5.3 Algebraic Invariants

- **Important property**
 - If g_1 and g_2 (independent of one another) are **relative invariants** with weights w_1 and w_2 , then

$$h(x) := \frac{(g_1(x))^{w_2}}{(g_2(x))^{w_1}}$$

is an **absolute invariant**

- **Proof:**

$$h(A \cdot x) = \frac{(g_1(A \cdot x))^{w_2}}{(g_2(A \cdot x))^{w_1}} = \frac{(\det(A))^{w_1 \cdot w_2} \cdot (g_1(x))^{w_2}}{(\det(A))^{w_1 \cdot w_2} \cdot (g_2(x))^{w_1}} = h(x)$$



5.3 Algebraic Invariants

- There are known methods in the **linear algebra** that can be used to find relative algebraic invariants for our special case
- A set of seven (absolute) moment invariants for moments of degree 2 and 3 is presented in (Hu, 1962)



$$- g_1 (...) = \eta_{2,0} + \eta_{0,2}(...)$$

$$- g_2 (...) = (\eta_{2,0} - \eta_{0,2})^2 + 4 \eta_{1,1}^2$$

$$- g_3 (...) = (\eta_{3,0} - \eta_{0,3})^2 + (\eta_{2,1} - \eta_{1,2})^2$$

$$- g_4 (...) = (\eta_{3,0} - \eta_{1,2})^2 + (3 \eta_{2,1} + \eta_{0,3})^2$$



5.3 Algebraic Invariants

Stress Reduction Kit

**Bang
Head
Here**

Directions:



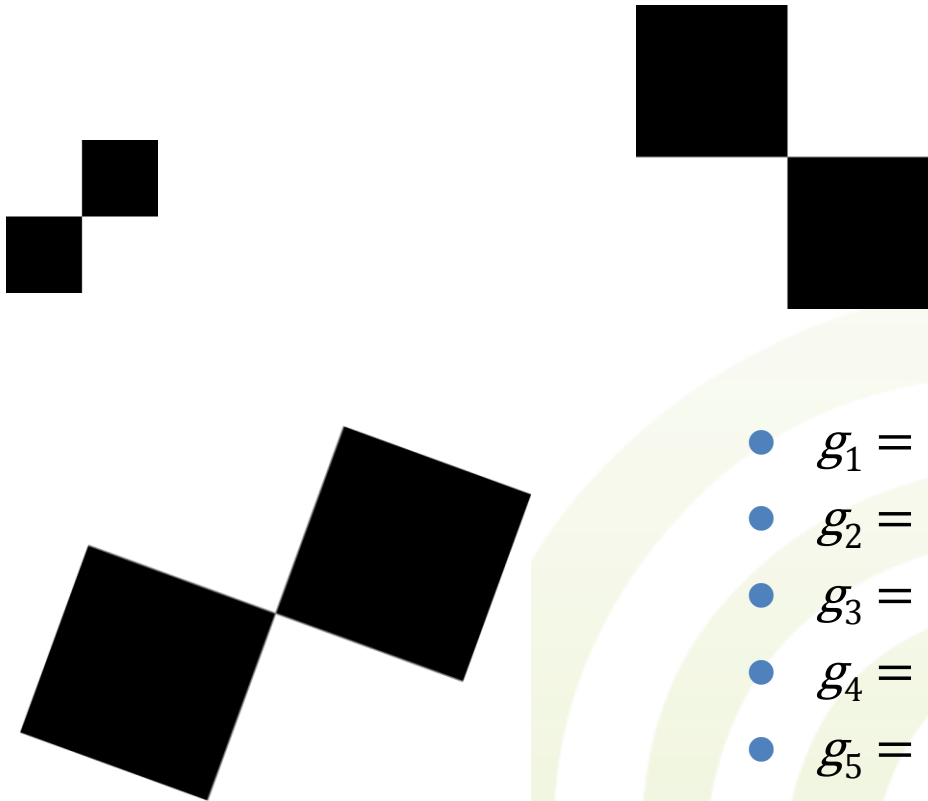
$$\begin{aligned} -g_5(\dots) &= (\eta_{3,0} - 3\eta_{1,2})(\eta_{3,0} + \eta_{1,2}) \\ &\quad [(\eta_{3,0} + \eta_{1,2})^2 - 3(\eta_{2,1} + \eta_{0,3})^2] \\ &\quad + (3\eta_{2,1} - \eta_{0,3})(\eta_{2,1} + \eta_{0,3}) \\ &\quad [3(\eta_{3,0} + \eta_{1,2})^2 - (\eta_{2,1} + \eta_{0,3})^2] \end{aligned}$$

$$\begin{aligned} -g_6(\dots) &= (\eta_{2,0} - \eta_{0,2}) [(\eta_{3,0} + \eta_{1,2})^2 \\ &\quad - (\eta_{2,1} + \eta_{0,3})^2] \\ &\quad + 4\eta_{1,1}(\eta_{3,0} + \eta_{1,2})(\eta_{2,1} + \eta_{0,3}) \end{aligned}$$

$$\begin{aligned} -g_7(\dots) &= (3\eta_{2,1} - \eta_{0,3})(\eta_{3,0} + \eta_{1,2}) \\ &\quad [(\eta_{3,0} + \eta_{1,2})^2 - 3(\eta_{2,1} - \eta_{3,0})^2] \\ &\quad + (3\eta_{1,2} - \eta_{3,0})(\eta_{2,1} + \eta_{0,3}) \\ &\quad [3(\eta_{3,0} + \eta_{1,2})^2 - (\eta_{2,1} + \eta_{0,3})^2] \end{aligned}$$



5.3 Example



- $g_1 = 0,3299$
- $g_2 = 0,1697$
- $g_3 = 0$
- $g_4 = 0$
- $g_5 = 0$
- $g_6 = 0$
- $g_7 = 0$



5.3 Moment Invariants

- If we found suitable moment invariants, we can characterize shapes by the vector of related characteristic values
- The comparison of shapes is then performed by measuring the distance of real vectors
- How many moment invariants do we need?



5.3 Separability Property

- Separability:
 - Two different shapes in the database must differentiate in at least one element of the feature vector
- This requirement determines how many different moment invariants are necessary



5.3 Moment Invariants

- The quality of the representation of shapes by moment invariants can be increased, by using other types of moments
- Examples:
 - Zernike moments
 - Tschebyschew moments
 - Fourier moments



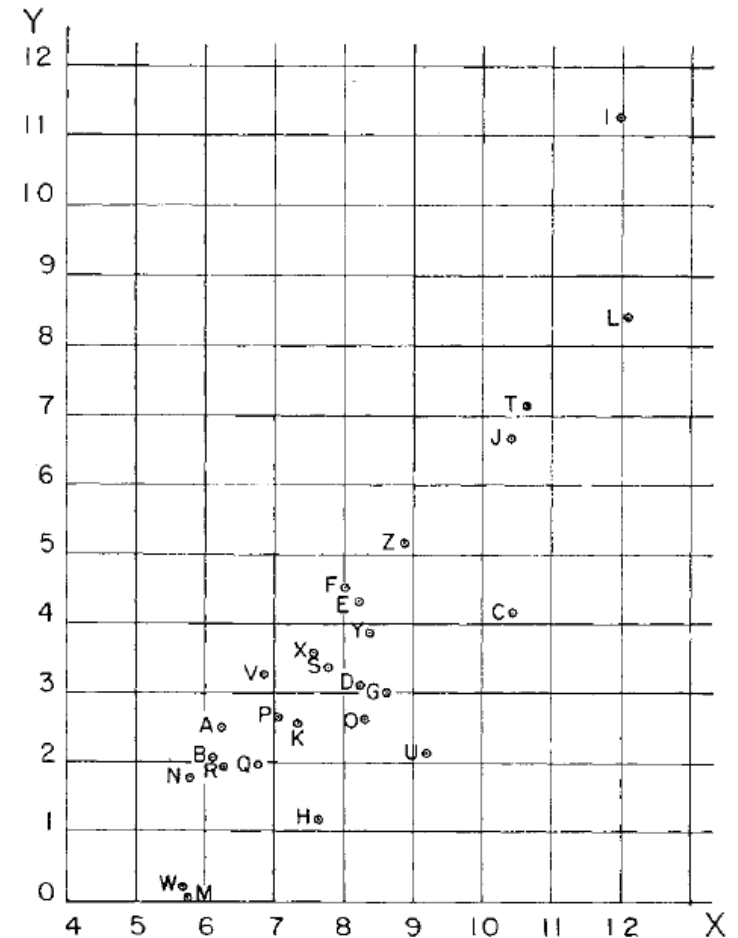
5.3 Moment Invariants

- The calculation of feature vectors can be simplified if the contour of the shapes have a special form
- Examples:
 - Splines (based) on polynomial functions
 - Polygons
 - Curves in parametric representation



5.3 Moment Invariants

- **Example (Hu, 1962):**
 - The shapes of the characters in the alphabet are represented each with a two-dimensional vector





5.3 Moment Invariants

- Experiments: Retrieval System (STAR Mehtre and others, 1995)
 - Test collection: company logos
 - **Moment invariants** show an average retrieval efficiency of 85-88%
 - **Combined feature vectors:**
In combination with other features even 89-94% is obtained
 - “Retrieval Effectiveness” is here a mix of precision and recall



5.4 Whole Image Description

Detour

- No description of individual shapes, but of the **overall impression created by** the shapes in the picture
- Images are considered perceptually similar if shapes occur in **similar correlations**
- Simple queries:
 - **Query by visual example**
 - **Query by sketch**

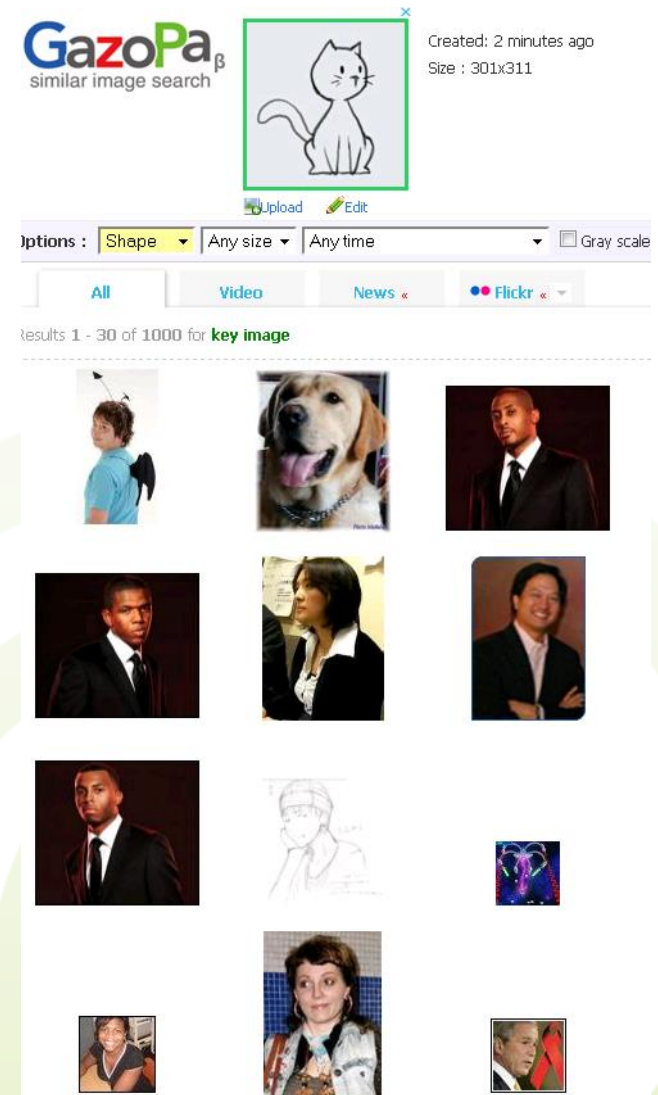
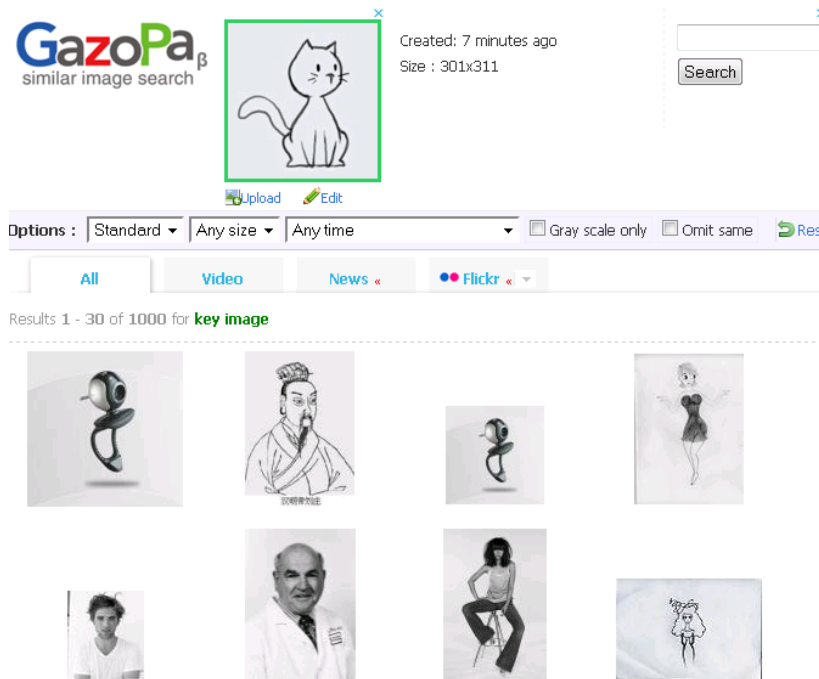




5.4 Whole Image Description

Detour

- Query by visual example
 - GazoPa shape similarity
 - Doesn't work that great





5.4 Query by Visual Example

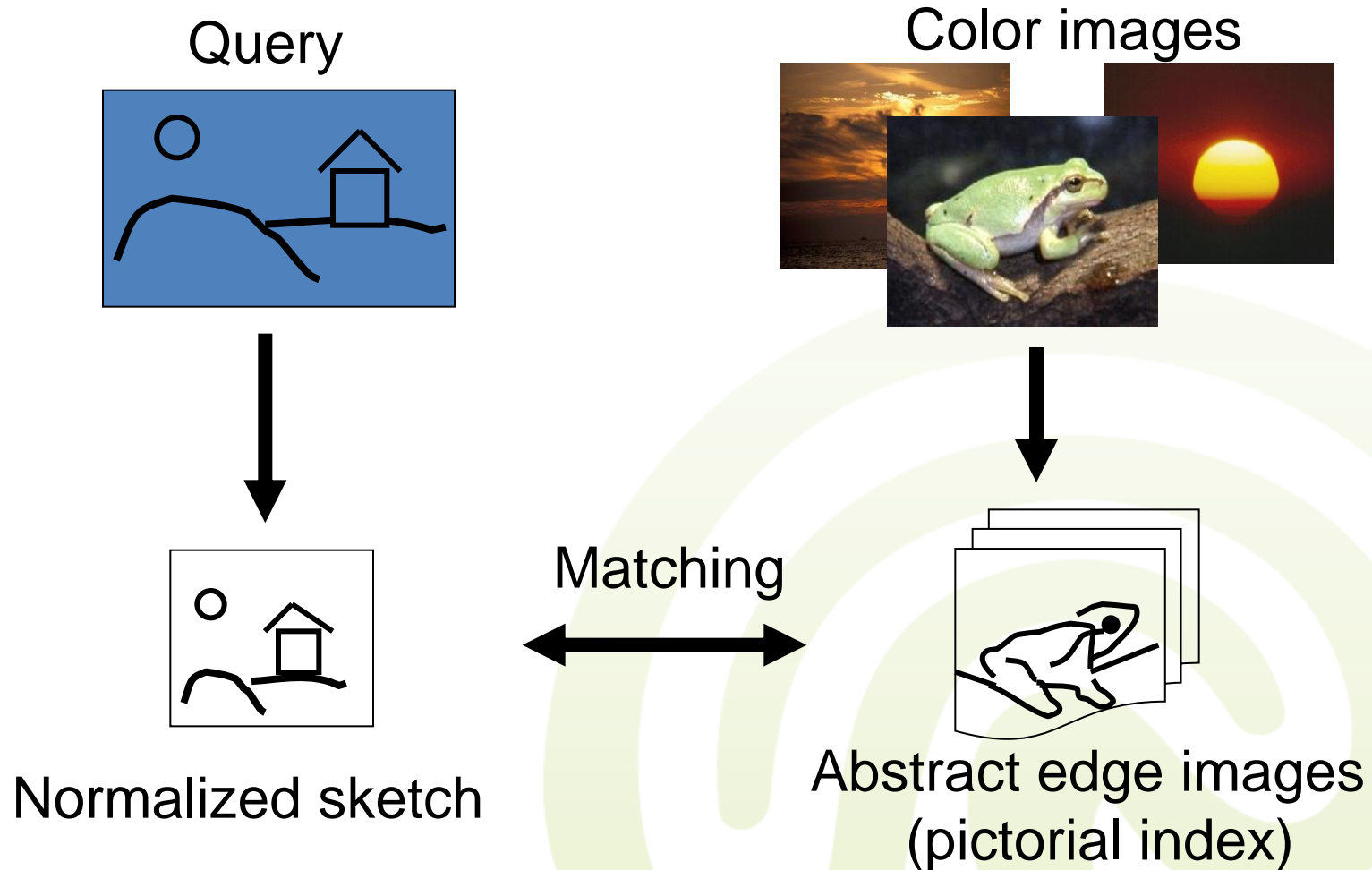
Detour

- Procedure (Hirata and Kato, 1992)
 - Pre-process the images in the database
 - Segment the images from the database and extract the edges (resulting in a binary image)
 - For each image from the database, save a normalized representation of the **dominant shapes (Pictorial Index)**
 - Users provide a **rough drawing** (binary)
 - Compare the drawing with the Pictorial Index



5.4 Query by Visual Example

Detour





5.4 Query by Visual Example

Detour

- **Image abstraction** for the pictorial index
 - **Reduce the image size** to, e.g., 64×64 pixels
 - **Gradient calculation** in four directions using the brightness values of each pixel
 - Calculate the **edges**:
 - All points with gradient greater than the average gradient plus standard deviation



5.4 Query by Visual Example

Detour

- Compute edges with **strong local significance**:
 - All points p belonging to global edges, which also have been recognized as global edges in a 7×7 **resolution sample** around p
- Remove all global edges, which are not local
- Thinning provides the final edge image



5.4 Query by Visual Example

Detour

- **Matching** can not simply compare at pixel level
 - White spots in the sketch may mean that **nothing should be there, or it's not important**, what is at the point
 - Sketches could be simplified, deformed and/or moved
 - Therefore, calculate the **local correlation** between the edge image and the sketch



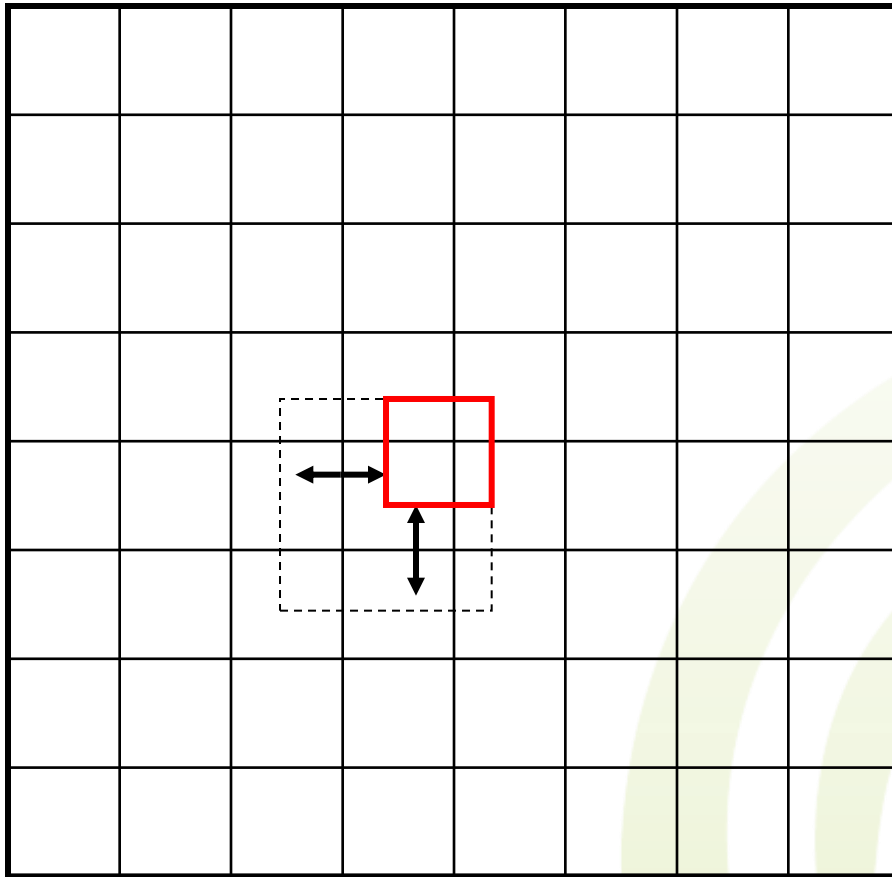


- Calculating the **local correlation**:
 - Divide the edge image and the sketch in 8×8 blocks, and compare any two blocks at the same coordinates
 - Move the sketch-block over the edge image (original image), in the x and y directions (-4 to +4 pixels) and sum over the number of each matching pixel values
 - The maximum of these sums is the **local correlation**
 - The aim of this step is to compensate **local inaccuracies** in the drawing and the pictorial index



5.4 Query by Visual Example

Detour



Edge image 8×8 Blocks

Move the equivalent block of the sketches against the edge image and count intensity matching pixels

Shifting -4 to 4 pixels in both directions results in 64 shifts



5.4 Query by Visual Example

Detour

- Calculation of the **global correlation**
 - The global correlation is simply the **sum of all local correlations**
 - After calculating the global correlation for each image in the database, sort the database by correlation size



5.4 Query by Visual Example

Detour

- **Advantages**

- Good retrieval results with respect to the overall visual impression
- Imprecision in the sketch is adjusted in matching



- **Disadvantages**

- The calculation of similarities is **very expensive** and **can not be calculated in advance**

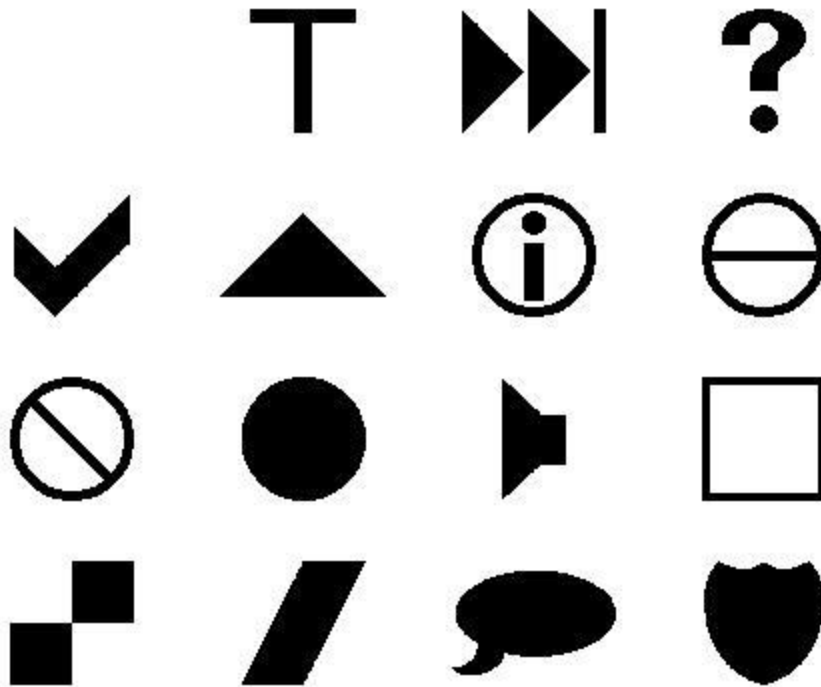


5.4 Query by Visual Example

Detour

- Matlab example

Image database



Query image

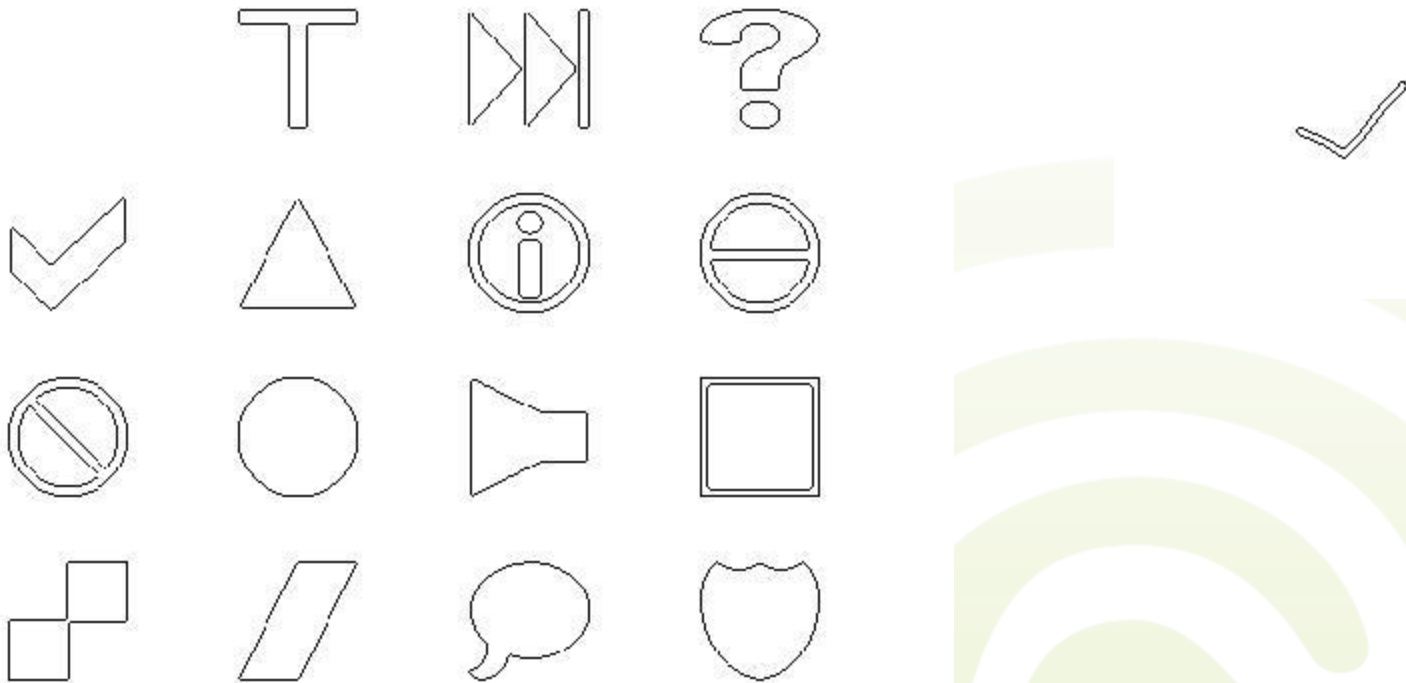




5.4 Query by Visual Example

Detour

- Extract edges

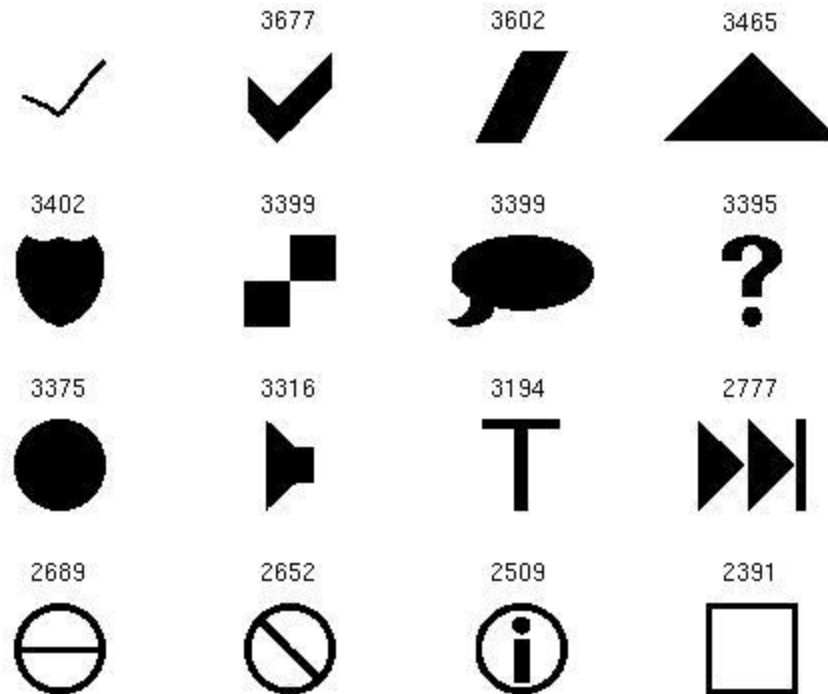




5.4 Query by Visual Example

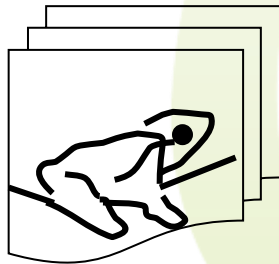
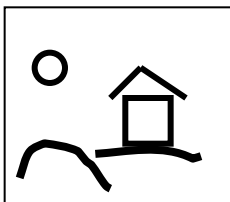
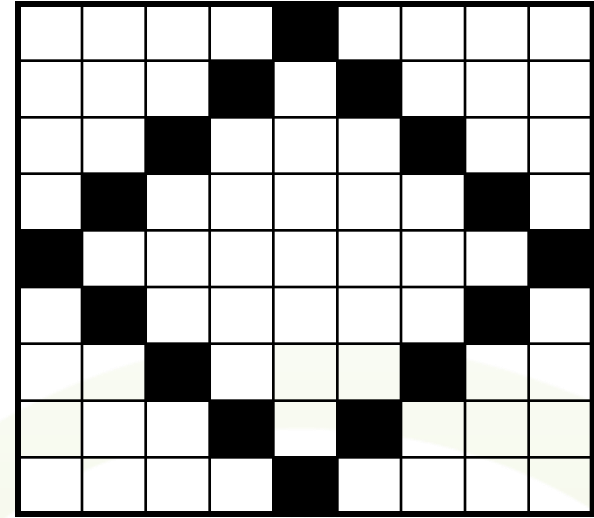
Detour

- Result





- Shape-based Features
 - Chain Codes
 - Area-based Retrieval
 - Moment Invariants
 - Query by Example





Next lecture

- Introduction to Audio Retrieval
 - Basics of audio
 - Audio information in databases
 - Basics of audio retrieval

