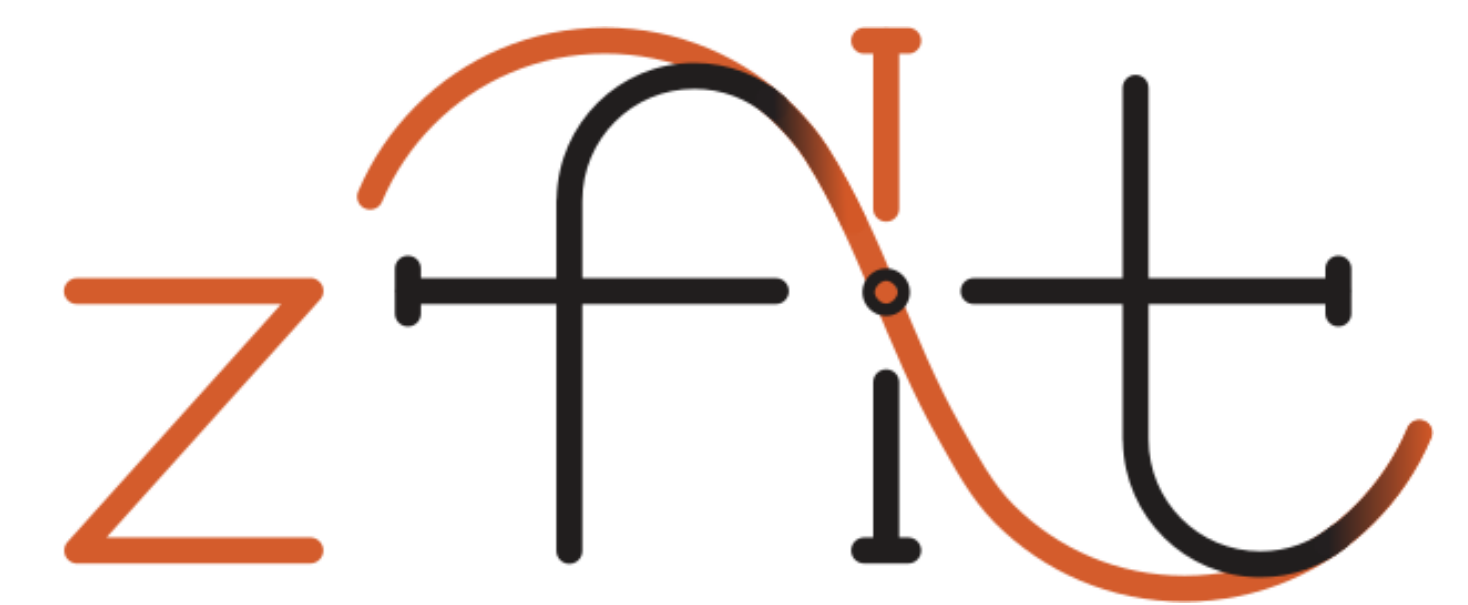


# scalable pythonic likelihood fitting

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## General likelihood fitting

Fitting something more complicated than a normal distribution or a fit is too slow?  
zfit allows to build multidimensional, composed models of arbitrary shaped PDFs.  
The backend uses speedup-techniques from TensorFlow to speedup and run on GPUs

Used in High Energy Physics with large data & complicated PDFs



Model

Data

Loss

Minimize

Errors

## Workflow

```
obs = zfit.Space("x", limits=(-2, 3))

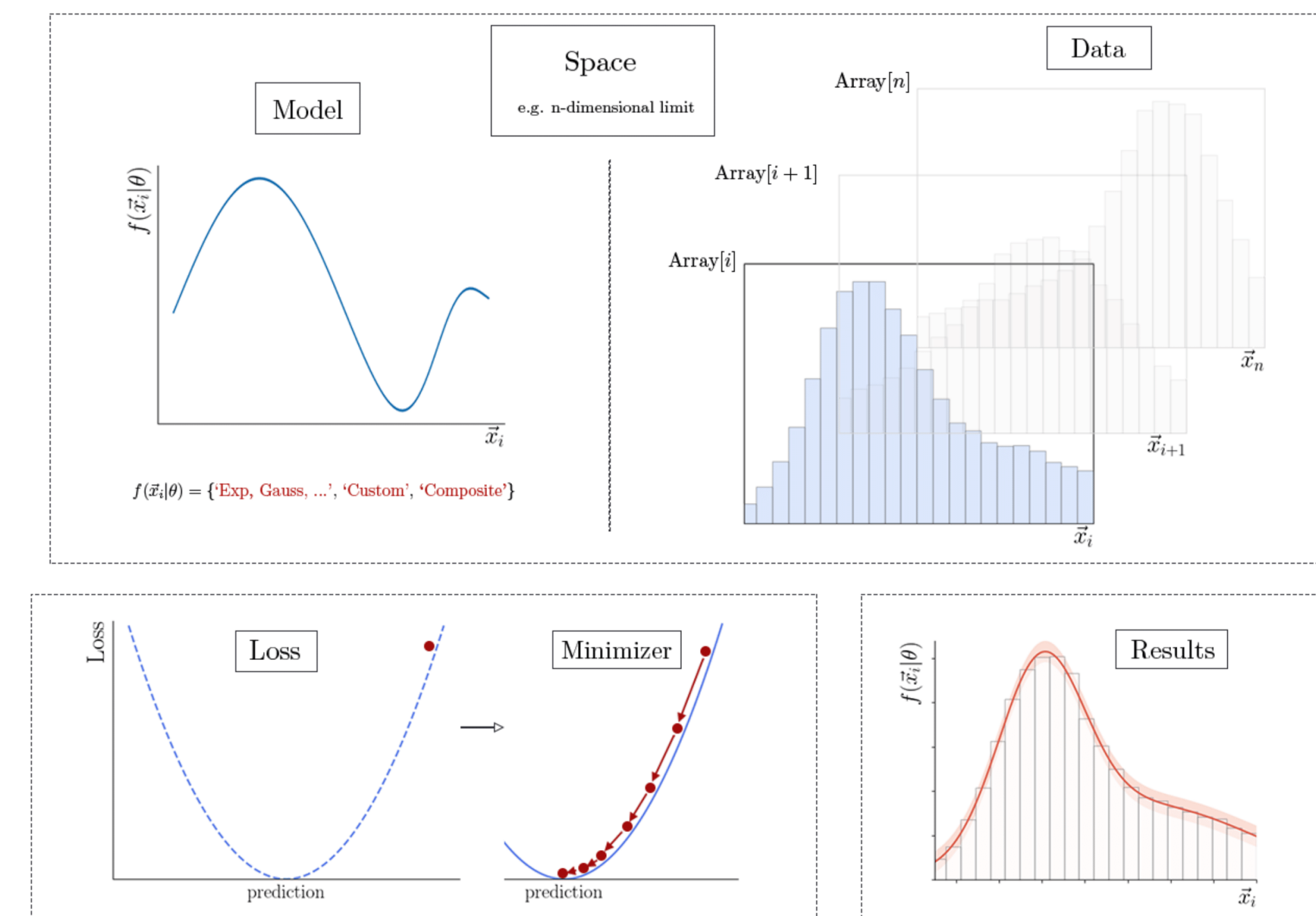
mu = zfit.Parameter("mu", 1.2, -4, 6)
sigma = zfit.Parameter("sigma", 1.3, 0.1, 10)
gauss = zfit.pdf.Gauss(mu=mu, sigma=sigma, obs=obs)

data = zfit.Data.from_numpy(obs=obs, array=normal_np)

nll = zfit.loss.UnbinnedNLL(model=gauss, data=data)

minimizer = zfit.minimize.Minuit()
result = minimizer.minimize(nll)

param_errors = result.error()
```



## Parameter

Build arbitrary compositions

```
free_param = zfit.Parameter("free", 5, 0, 15)
param_shift = zfit.ComposedParameter("comp",
    lambda x: x + 5, free_param)
```

## Data

- Multiple formats supported
  - Full capability of Pandas DataFrames
- ```
data_raw = zfit.Data.from_root(...)
df = data_raw.to_pandas()
# preprocess in pandas
data = zfit.Data.from_pandas(df)
```

## Loss

Simultaneous

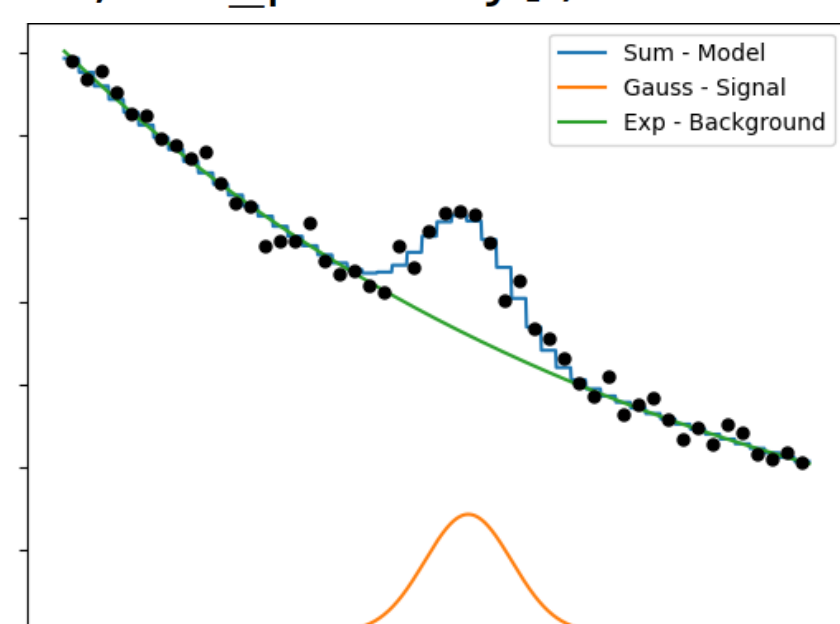
```
nll1 = zfit.loss.UnbinnedNLL(model=gauss1, data=data1)
nll2 = zfit.loss.UnbinnedNLL(model=gauss2, data=data2)
nll_simultaneous = nll1 + nll2
```

Constraints

```
constr = zfit.constraint.GaussianConstraint(...)
mu_penalty = tf.square(mu - 1.3)
nll.add_constraints([constr, mu_penalty])
```

Variety of losses

Binned, unbinned,  
chi2, extended



## Model building

Custom model

```
class CustomPDF(zfit.pdf.ZPDF):
    _PARAMS = ['alpha']

    def _unnormalized_pdf(self, x):
        data = x.unstack_x()
        alpha = self.params['alpha']
        return tf.exp(alpha * data)

obs = zfit.Space("y", (-4, 4))
custom_pdf = CustomPDF(obs=obs, alpha=0.2)

integral = custom_pdf.integrate(limits=(-1, 2))
sample = custom_pdf.sample(n=1000)
prob = custom_pdf.pdf(sample)
```

Composition

```
frac = zfit.Parameter('fraction', 0.5, 0, 1)
sum_pdf = zfit.pdf.SumPDF([gauss, exponential], frac)
```

Product 2-D

(dims defined by observables)

```
#['y', 'x'] <- obs 'y' * 'x'
product_2d = custom_pdf * sum_pdf
```

## Minimization

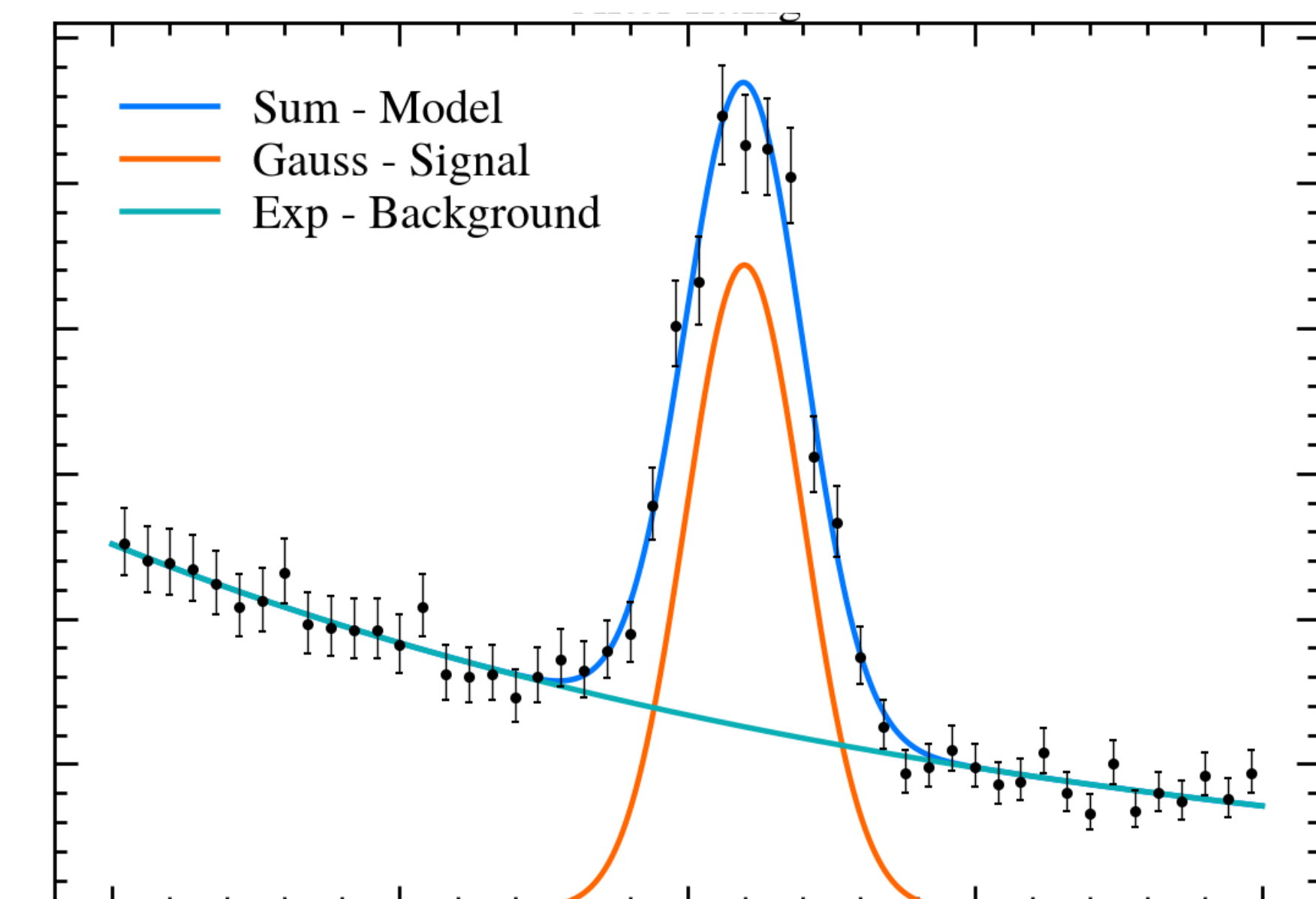
- Wraps minimizer libraries
  - Minuit, Scipy, Ipyopt, NLOpt
- ```
minimizer = zfit.minimize.Adam(...)
result = minimizer.minimize(loss)
```
- Convenient BaseClass available
  - Common convergence criterion
  - Automatic gradient available

## Fit result

- Access results
- ```
successful = result.converged
mu_result = result.params[mu]
```
- Calculate errors
- ```
hesse_error = result.hesse()
minos_error = result.error()
```
- Store results
- ```
res_dilled = zfit.dill.dumps(result)
res_loaded = zfit.dill.loads(res_dilled)
```

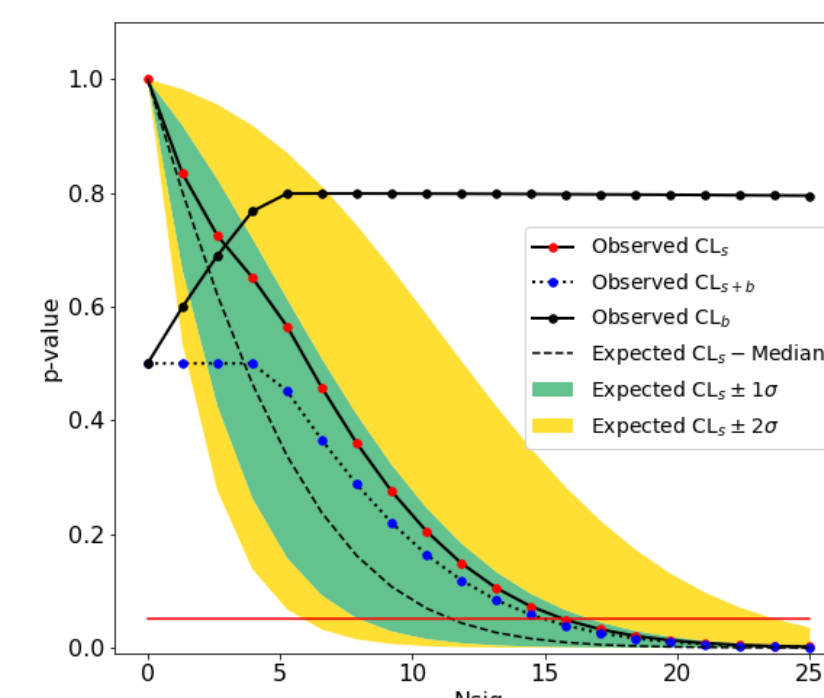
## Compositions

Mixture (plot), Convolutions, Products



## Inference

hepstats library  
Confidence Interval,  
limits, sWeights,...



## Conclusion

Fast likelihood model fitting in pure Python for complicated distributions.  
*It allows to connect with many other libraries for a seamless workflow.*