

Tables and Figures

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## [1] "multinom_hcsb_1000_count"
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1 Power

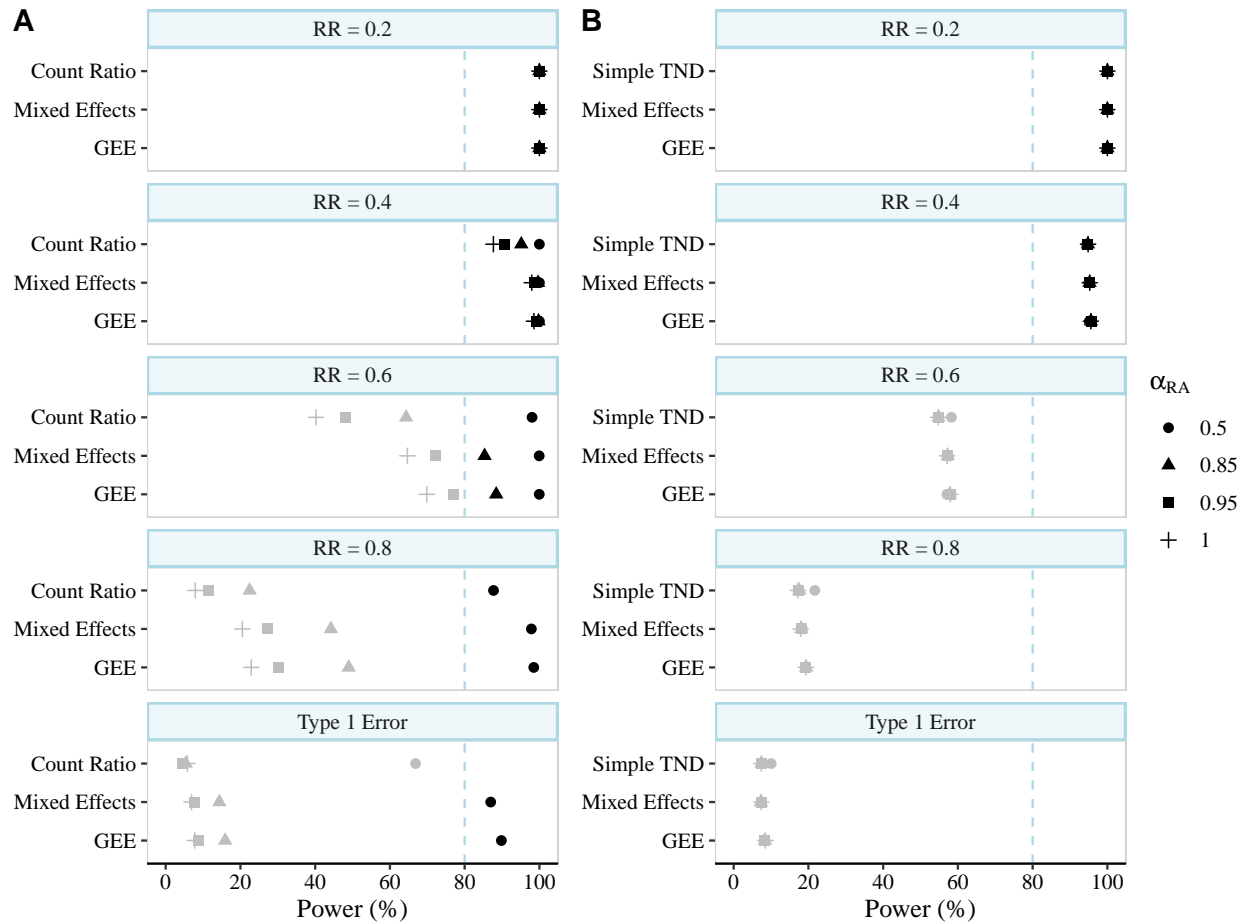


Table 1: The power, and Type I error rates, in testing departure from the null of no intervention effect based on estimation methods with and without debiasing by negative control counts for a range of Relative Risks (λ), over 10,000 intervention allocations applied to each of 9 historical time periods with 1,000 cases and 4,000 negative controls (when applicable). Differential ascertainment (α_{RA}) is allowed to increase in severity.

| λ | α_{RA} | Count Only Methods* | | | Negative Control Debaised Methods† | | |
|-------------------|---------------|---------------------|---------------|-------------|------------------------------------|---------------|------------|
| | | GEE | Mixed Effects | Count Ratio | GEE | Mixed Effects | Simple TND |
| Type 1 Error: 1.0 | 1.00 | 0.078 | 0.069 | 0.058 | 0.085 | 0.074 | 0.074 |
| | 0.95 | 0.086 | 0.078 | 0.045 | 0.084 | 0.073 | 0.073 |
| | 0.85 | 0.159 | 0.144 | 0.054 | 0.084 | 0.073 | 0.074 |
| | 0.50 | 0.898 | 0.870 | 0.669 | 0.084 | 0.074 | 0.100 |
| 0.8 | 1.00 | 0.229 | 0.205 | 0.079 | 0.193 | 0.179 | 0.172 |
| | 0.95 | 0.302 | 0.271 | 0.113 | 0.193 | 0.181 | 0.172 |
| | 0.85 | 0.490 | 0.442 | 0.224 | 0.194 | 0.181 | 0.176 |
| | 0.50 | 0.985 | 0.979 | 0.877 | 0.193 | 0.184 | 0.217 |
| 0.6 | 1.00 | 0.699 | 0.647 | 0.402 | 0.580 | 0.571 | 0.547 |
| | 0.95 | 0.769 | 0.722 | 0.481 | 0.580 | 0.573 | 0.549 |
| | 0.85 | 0.884 | 0.853 | 0.643 | 0.578 | 0.573 | 0.548 |
| | 0.50 | 1.000 | 0.999 | 0.980 | 0.571 | 0.574 | 0.583 |
| 0.5 | 1.00 | 0.900 | 0.871 | 0.668 | 0.813 | 0.808 | 0.791 |
| | 0.95 | 0.931 | 0.909 | 0.731 | 0.813 | 0.806 | 0.790 |
| | 0.85 | 0.973 | 0.964 | 0.835 | 0.812 | 0.807 | 0.791 |
| | 0.50 | 1.000 | 1.000 | 0.997 | 0.804 | 0.808 | 0.797 |
| 0.4 | 1.00 | 0.985 | 0.979 | 0.877 | 0.956 | 0.953 | 0.948 |
| | 0.95 | 0.991 | 0.988 | 0.907 | 0.956 | 0.953 | 0.948 |
| | 0.85 | 0.998 | 0.996 | 0.951 | 0.956 | 0.952 | 0.948 |
| | 0.50 | 1.000 | 1.000 | 1.000 | 0.952 | 0.951 | 0.945 |
| 0.3 | 1.00 | 1.000 | 0.999 | 0.980 | 0.997 | 0.997 | 0.997 |
| | 0.95 | 1.000 | 1.000 | 0.987 | 0.997 | 0.997 | 0.996 |
| | 0.85 | 1.000 | 1.000 | 0.996 | 0.997 | 0.997 | 0.996 |
| | 0.50 | 1.000 | 1.000 | 1.000 | 0.996 | 0.996 | 0.996 |
| 0.2 | 1.00 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| | 0.95 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| | 0.85 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |
| | 0.50 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 |

* GEE and mixed effects count only models assume Poisson distributed counts and use the canonical log link.

† GEE and mixed effects negative control de-biased models assume binomially distributed counts and use the canonical logit link.

2 Bias

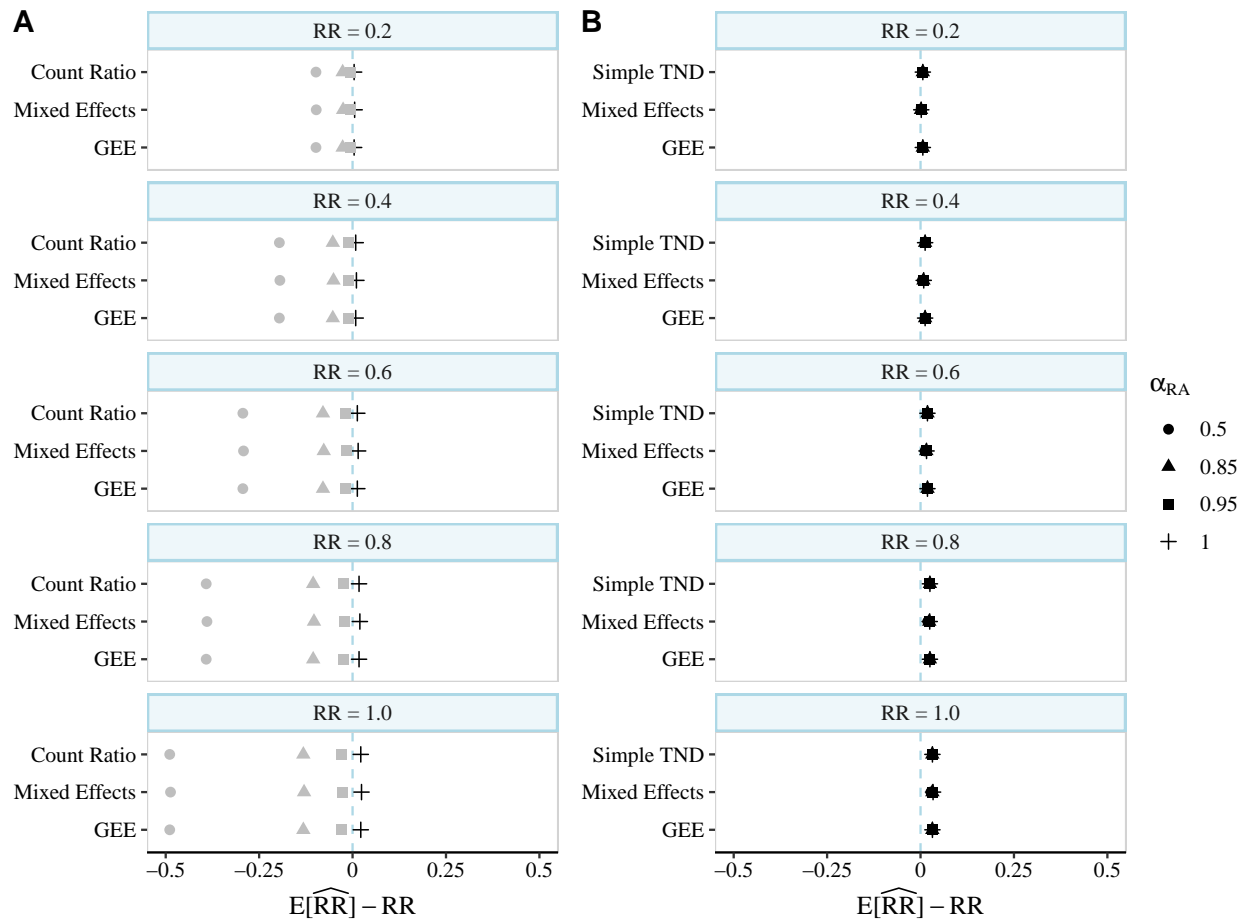


Table 2: Bias in estimation of the intervention Relative Risk for estimation methods with and without debiasing by negative control counts for a range of Relative Risks (λ), over 10,000 intervention allocations applied to each of 9 historical time periods with 1,000 cases and 4,000 controls (when applicable). Differential ascertainment(α_{RA}) is allowed to increase in severity.

| λ | α_{RA} | Count Only Methods* | | | Negative Control De-Biased Methods† | | |
|-----------|---------------|---------------------|---------------|-------------|-------------------------------------|---------------|------------|
| | | GEE | Mixed Effects | Count Ratio | GEE | Mixed Effects | Simple TND |
| 1.0 | 1.00 | 0.022 | 0.024 | 0.022 | 0.032 | 0.033 | 0.032 |
| | 0.95 | -0.030 | -0.027 | -0.030 | 0.031 | 0.032 | 0.031 |
| | 0.85 | -0.132 | -0.130 | -0.132 | 0.031 | 0.032 | 0.031 |
| | 0.50 | -0.489 | -0.487 | -0.489 | 0.032 | 0.028 | 0.032 |
| 0.8 | 1.00 | 0.017 | 0.020 | 0.017 | 0.025 | 0.025 | 0.025 |
| | 0.95 | -0.024 | -0.021 | -0.024 | 0.025 | 0.024 | 0.025 |
| | 0.85 | -0.105 | -0.103 | -0.105 | 0.025 | 0.023 | 0.025 |
| | 0.50 | -0.392 | -0.390 | -0.392 | 0.025 | 0.019 | 0.025 |
| 0.6 | 1.00 | 0.013 | 0.015 | 0.013 | 0.018 | 0.016 | 0.018 |
| | 0.95 | -0.018 | -0.016 | -0.018 | 0.019 | 0.016 | 0.019 |
| | 0.85 | -0.079 | -0.077 | -0.079 | 0.019 | 0.015 | 0.019 |
| | 0.50 | -0.294 | -0.292 | -0.294 | 0.019 | 0.012 | 0.019 |
| 0.5 | 1.00 | 0.010 | 0.013 | 0.010 | 0.015 | 0.012 | 0.015 |
| | 0.95 | -0.015 | -0.013 | -0.015 | 0.015 | 0.012 | 0.015 |
| | 0.85 | -0.066 | -0.064 | -0.066 | 0.015 | 0.011 | 0.015 |
| | 0.50 | -0.245 | -0.243 | -0.245 | 0.015 | 0.008 | 0.015 |
| 0.4 | 1.00 | 0.008 | 0.010 | 0.008 | 0.012 | 0.009 | 0.012 |
| | 0.95 | -0.012 | -0.010 | -0.012 | 0.012 | 0.008 | 0.012 |
| | 0.85 | -0.053 | -0.051 | -0.053 | 0.012 | 0.008 | 0.012 |
| | 0.50 | -0.196 | -0.195 | -0.196 | 0.012 | 0.005 | 0.012 |
| 0.3 | 1.00 | 0.006 | 0.008 | 0.006 | 0.009 | 0.005 | 0.009 |
| | 0.95 | -0.009 | -0.007 | -0.009 | 0.009 | 0.005 | 0.009 |
| | 0.85 | -0.040 | -0.038 | -0.040 | 0.009 | 0.005 | 0.009 |
| | 0.50 | -0.147 | -0.146 | -0.147 | 0.009 | 0.002 | 0.009 |
| 0.2 | 1.00 | 0.004 | 0.006 | 0.004 | 0.006 | 0.002 | 0.006 |
| | 0.95 | -0.006 | -0.005 | -0.006 | 0.006 | 0.002 | 0.006 |
| | 0.85 | -0.026 | -0.025 | -0.026 | 0.006 | 0.001 | 0.006 |
| | 0.50 | -0.098 | -0.097 | -0.098 | 0.006 | -0.001 | 0.006 |

* GEE and mixed effects count only models assume Poisson distributed counts and use the canonical log link.

† GEE and mixed effects negative control de-biased models assume binomially distributed counts and use the canonical logit link.

3 Coverage

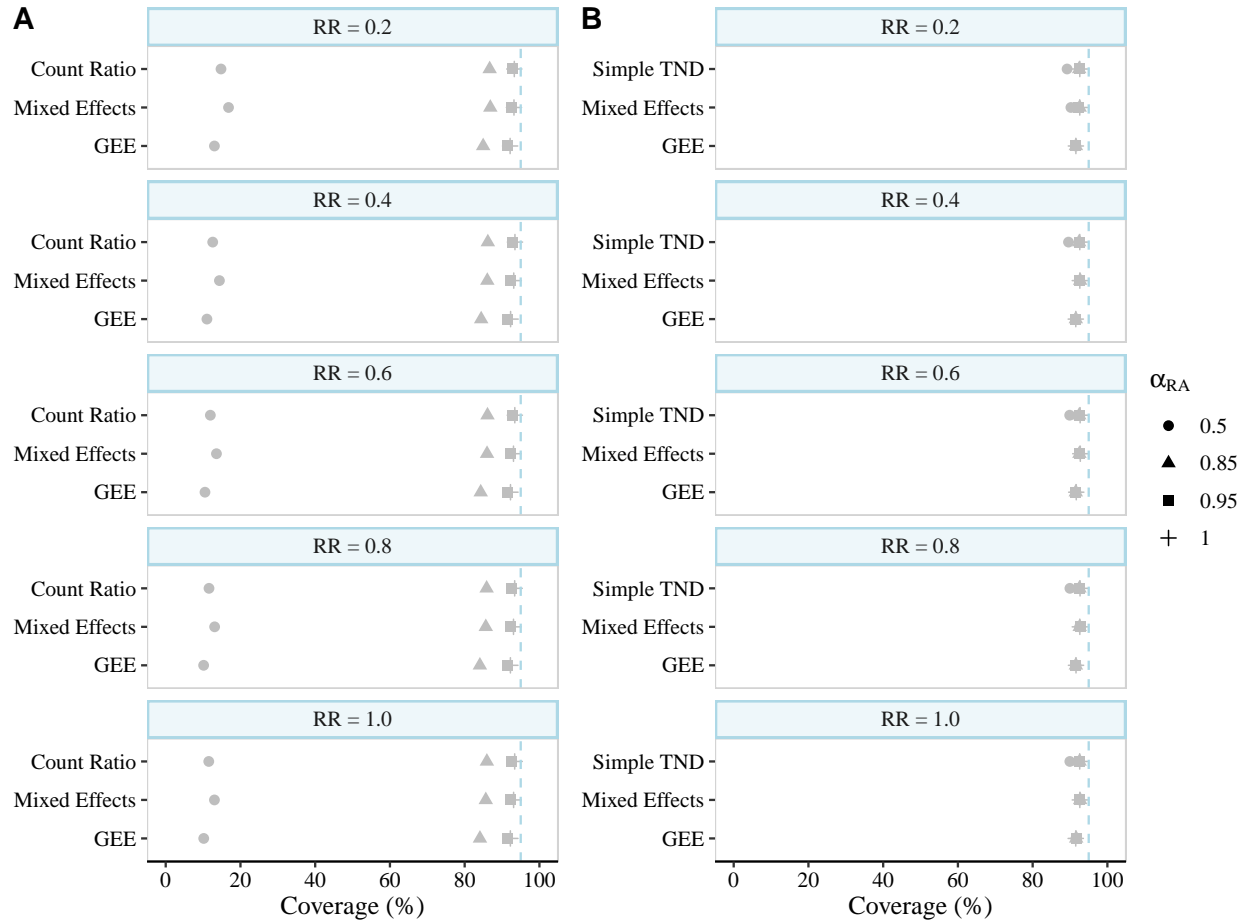


Table 3: 95% confidence interval coverage based on estimation of the intervention Relative Risk for estimation methods with and without debiasing by negative control counts for a range of Relative Risks (λ), over 10,000 intervention allocations applied to each of 9 historical time periods with 1,000 cases and 4,000 negative controls (when applicable). Differential ascertainment (α_{RA}) is allowed to increase in severity.

| λ | α_{RA} | Count Only Methods* | | | Negative Control De-Biased Methods† | | |
|-----------|---------------|---------------------|---------------|-------------|-------------------------------------|---------------|------------|
| | | GEE | Mixed Effects | Count Ratio | GEE | Mixed Effects | Simple TND |
| 1.0 | 1.00 | 0.922 | 0.931 | 0.934 | 0.915 | 0.926 | 0.926 |
| | 0.95 | 0.914 | 0.922 | 0.926 | 0.916 | 0.927 | 0.927 |
| | 0.85 | 0.841 | 0.856 | 0.859 | 0.916 | 0.927 | 0.926 |
| | 0.50 | 0.102 | 0.130 | 0.115 | 0.916 | 0.926 | 0.900 |
| 0.8 | 1.00 | 0.922 | 0.931 | 0.934 | 0.916 | 0.926 | 0.927 |
| | 0.95 | 0.914 | 0.923 | 0.926 | 0.915 | 0.927 | 0.926 |
| | 0.85 | 0.841 | 0.856 | 0.859 | 0.916 | 0.926 | 0.925 |
| | 0.50 | 0.101 | 0.131 | 0.116 | 0.916 | 0.926 | 0.900 |
| 0.6 | 1.00 | 0.923 | 0.931 | 0.934 | 0.917 | 0.928 | 0.927 |
| | 0.95 | 0.915 | 0.923 | 0.927 | 0.915 | 0.926 | 0.925 |
| | 0.85 | 0.843 | 0.860 | 0.861 | 0.915 | 0.925 | 0.925 |
| | 0.50 | 0.105 | 0.136 | 0.119 | 0.916 | 0.926 | 0.899 |
| 0.5 | 1.00 | 0.922 | 0.931 | 0.934 | 0.916 | 0.926 | 0.926 |
| | 0.95 | 0.913 | 0.922 | 0.925 | 0.915 | 0.926 | 0.925 |
| | 0.85 | 0.843 | 0.859 | 0.860 | 0.917 | 0.926 | 0.926 |
| | 0.50 | 0.106 | 0.137 | 0.121 | 0.916 | 0.925 | 0.898 |
| 0.4 | 1.00 | 0.923 | 0.931 | 0.935 | 0.915 | 0.926 | 0.926 |
| | 0.95 | 0.916 | 0.923 | 0.927 | 0.916 | 0.925 | 0.926 |
| | 0.85 | 0.844 | 0.861 | 0.862 | 0.916 | 0.927 | 0.924 |
| | 0.50 | 0.110 | 0.144 | 0.126 | 0.915 | 0.925 | 0.896 |
| 0.3 | 1.00 | 0.922 | 0.931 | 0.934 | 0.917 | 0.927 | 0.927 |
| | 0.95 | 0.914 | 0.925 | 0.926 | 0.916 | 0.926 | 0.927 |
| | 0.85 | 0.846 | 0.864 | 0.864 | 0.916 | 0.927 | 0.925 |
| | 0.50 | 0.117 | 0.152 | 0.134 | 0.916 | 0.924 | 0.895 |
| 0.2 | 1.00 | 0.922 | 0.932 | 0.933 | 0.916 | 0.926 | 0.926 |
| | 0.95 | 0.915 | 0.926 | 0.927 | 0.915 | 0.924 | 0.926 |
| | 0.85 | 0.849 | 0.869 | 0.867 | 0.916 | 0.926 | 0.924 |
| | 0.50 | 0.130 | 0.168 | 0.148 | 0.916 | 0.902 | 0.892 |

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† GEE and mixed effects negative control de-biased models assume binomially distributed counts and use the canonical logit link.