Competitive

Programming

Reference

First, solve the problem. Then, write the code.

John Johnson

Ву

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1 Coding Resources

1.1 C++

1.1.1 Decimal Precision

```
// rounds up the decimal number
cout << setprecision(N) << n << endl;
// specify N fixed number of decimals
cout << fixed << setprecision(N) << n << endl;</pre>
```

1.1.2 IO Optimization

```
int main() {
  ios_base::sync_with_stdio(0);
  cin.tie(0);
}
```

1.1.3 Int To Binary

```
#include <bits/stdc++.h>
using namespace std;
typedef long long int lli;
lli bitsInInt(lli n) { // clz = count leading zeroes
  return sizeof(n) * 8 - __builtin_clzll(n);
vector<bool> intToBitsArray(lli n) {
  n = abs(n);
  if (!n) return {};
  int length = bitsInInt(n), lastPos = length - 1;
  vector<bool> v(length);
  for (lli i = lastPos, j = 0; i > -1LL; i--, j++)
  \rightarrow v[j] = (n >> i) & 1LL;
  return v;
}
int main() {
  vector<bool> ans = intToBitsArray(8LL);
  for (auto a : ans) cout << a << " ";</pre>
  cout << endl;</pre>
 return 0;
```

1.1.4 Map Value To Int

}

```
return valForInt[val];
}
void initMapping() {
  mapId = 0;
  intForVal.clear();
  valForInt.clear();
}
1.1.5 Permutations
typedef vector<int> T;// typedef string T;
vector<T> permutations(T v) {
  vector<vector<int>> ans;
  sort(v.begin(), v.end());
    ans.push_back(v);
  while (next_permutation(v.begin(), v.end()));
  return ans;
}
1.1.6 Print Vector
void printv(vector<int> v) {
  if (v.size() == 0) {
    cout << "[]" << endl;
    return;
  }
  cout << "[" << v[0];
  for (int i = 1; i < v.size(); i++) {
    cout << ", " << v[i];
  cout << "]" << endl;</pre>
}
1.1.7 Priority Queue Of Object
struct Object {
  char first;
  int second;
};
int main() {
  auto cmp = [](const Object& a,
                const Object& b) {
    return a.second > b.second;
  priority_queue<Object, vector<Object>,
                 decltype(cmp)>
      pq(cmp);
  vector<Object> v = {
      {'c', 3}, {'a', 1}, {'b', 2}};
  sort(v.begin(), v.end(), cmp);
  return 0;
}
1.1.8 Random
int random(int min, int max) {
  return min + rand() % (max - min + 1);
```

```
int main() {
  srand(time(0));
  // code
1.1.9 Read Line
// when reading lines, don't mix 'cin' with
// 'getline' just use getline and split
string input() {
  string ans;
  // cin >> ws; // eats all whitespaces.
 getline(cin, ans);
 return ans;
1.1.10 Sort Pair
pair<int, int> p;
sort(p.begin(), p.end());
// sorts array on the basis of the first element
1.1.11 Sort Vector Of Object
struct Object {
  char first;
  int second;
}:
bool cmp(const Object& a, const Object& b) {
 return a.second > b.second;
int main() {
  vector<Object> v = {
      {'c', 3}, {'a', 1}, {'b', 2}};
  sort(v.begin(), v.end(), cmp);
  printv(v);
 return 0;
1.1.12 Split String
vector<string> split(string str, char token) {
  stringstream test(str);
  string seg;
  vector<string> seglist;
  while (getline(test, seg, token))
    seglist.push_back(seg);
  return seglist;
1.1.13 Typedef
typedef TYPE ALIAS
// e.g.
typedef int T;
```

```
1.2 Python
1.2.1 Combinations
import itertools
#from arr choose k = > combinations(arr, k)
print(list(itertools.combinations([1, 2, 3], 3)))
1.2.2 Fast IO
from sys import stdin, stdout
N = 10
#Reads N chars from stdin(it counts '\n' as char)
stdin.read(N)
#Reads until '\n' or EOF
line = stdin.readline()
#Reads all lines in stdin until EOF
lines = stdin.readlines()
#Writes a string to stdout, it doesn't add '\n'
stdout.write(line)
#Writes a list of strings to stdout
stdout.writelines(lines)
#Reads numbers separated by space in a line
numbers = list(map(int, stdin.readline().split()))
1.2.3 Permutations
import itertools
print(list(itertools.permutations([1, 2, 3])))
1.2.4 Random
import random
# Initialize the random number generator.
random.seed(None)
# Returns a random integer N such that a \leq N \leq b.
random.randint(a, b)
```

```
import random
# Initialize the random number generator.
random.seed(None)
# Returns a random integer N such that a <= N <= b
random.randint(a, b)
# Returns a random integer N such that 0 <= N < b
random.randrange(b)
# Returns a random integer N such that a <= N < b.
random.randrange(a, b)
# Returns and integer with k random bits.
random.getrandbits(k)
# shuffles a list
random.shuffle(li)</pre>
```

1.2.5 Sort List

```
li = ['a', 'c', 'b']
# sorts inplace in descending order
li.sort(reverse=True)
# returns sorted list ascending order
ol = sorted(li)
```

1.2.6 Sort List Of Object

2 Data Structures

2.1 Graphs

2.1.1 UnionFind

```
struct UnionFind {
 vector<int> dad, size;
  int n:
 UnionFind(int N=0) : n(N), dad(N), size(N, 1) {
   while (N--) dad[N] = N;
 }
  int root(int u) {
   if (dad[u] == u) return u;
   return dad[u] = root(dad[u]);
  }
 bool areConnected(int u, int v) {
   return root(u) == root(v);
  }
  void join(int u, int v) {
   int Ru = root(u), Rv = root(v);
   if (Ru == Rv) return;
   --n, dad[Ru] = Rv;
    size[Rv] += size[Ru];
  }
  int getSize(int u) {
   return size[root(u)];
  int numberOfSets() {
   return n;
  }
};
```

2.2 Ranges

2.2.1 BIT

2.2.2 Interval Tree

2.2.3 Segment Tree

```
// st = segment tree. st[1] = root;
// neutro = operation neutral value
// e.g. for sum is 0, for multiplication
// is 1, for gcd is 0, for min is INF, etc.
typedef int T;
T neutro = 0;
int N;
vector<T> st;
void initVars(int n) {
  st.assign(2 * (N = n), neutro);
TF(Ta, Tb) {
 return a + b;
  // return __gcd(a, b);
  // return a * b;
  // return min(a, b);
// 0(2N)
void build() {
  for (int i = N - 1; i > 0; i--) st[i] = F(st[i <<
  → 1], st[i << 1 | 1]);</pre>
}
// O(lq(2N))
void updateNode(int i, T val) {
  for (st[i += N] = val; i > 1; i >>= 1) st[i >> 1] =
  → F(st[i], st[i ^ 1]);
}
// O(3N), [l, r]
void updateRange(int 1, int r, T val) {
  for (1 += N, r += N; 1 <= r; 1++) st[1] = val;
  build();
}
// O(lg(2N)), [l, r]
T query(int 1, int r) {
  T ans = neutro;
  for (1 += N, r += N; 1 <= r; 1 >>= 1, r >>= 1) {
    if (l \& 1) ans = F(ans, st[l++]);
    if (r \& 1) ans = F(ans, st[r--]);
  return ans;
}
```

```
st[pos + N] = val;
T getValAt(int pos) {
 return st[pos + N];
2.2.4 Segment Tree Lazy Propagation
// st = segment tree, st[1] = root, H = height of d
// u = updates, d = delayed updates
// neutro = operation neutral val
// e.g. for sum is 0, for multiplication
// is 1, for gcd is 0, for min is INF, etc.
typedef int T;
T neutro = 0;
int N, H;
vector<T> st, d;
vector<bool> u;
void initVars(T n) {
  u.assign(N = n, 0);
  d.assign(n, neutro);
  st.assign(2 * n, neutro);
 H = sizeof(int) * 8 - __builtin_clz(n);
T F(T a, T b) {
 return a + b;
  // return __gcd(a, b);
  // return a * b;
  // return min(a, b);
T kTimesF(T a, T k) {
  return a * k; // sum
  // return a; // min, max, qcd
  // return pow(a, k); // multiplication
void apply(int i, T val, int k) {
  st[i] = kTimesF(val, k);
  if (i < N) d[i] = val, u[i] = 1;</pre>
void calc(int i) {
  if (!u[i]) st[i] = F(st[i << 1], st[i << 1 | 1]);</pre>
}
// O(2N)
void build() {
  for (int i = N - 1; i > 0; i--) calc(i);
void build(int p) {
  while (p > 1) p >>= 1, calc(p);
```

void setValAt(T val, int pos) {

```
void push(int p) {
  for (int s = H, k = 1 \ll (H - 1); s > 0; s--, k >>=
  → 1) {
    int i = p \gg s;
    if (u[i]) {
      apply(i \ll 1, d[i], k);
      apply(i \ll 1 \mid 1, d[i], k);
      u[i] = 0, d[i] = neutro;
  }
}
// [l, r] O(lg(2N))
void modify(int 1, int r, T val) {
  push(1 += N);
  push(r += N);
  int ll = 1, rr = r, k = 1;
  for (; 1 \le r; 1 >>= 1, r >>= 1, k <<= 1) {
    if (1 & 1) apply(1++, val, k);
    if (~r & 1) apply(r--, val, k);
  build(11);
  build(rr);
}
// [l, r] O(lg(2N))
T query(int 1, int r) {
  push(1 += N);
  push(r += N);
  T ans = neutro;
  for (; l <= r; l >>= 1, r >>= 1) {
    if (1 & 1) ans = F(ans, st[1++]);
    if (r \& 1) ans = F(ans, st[r--]);
  return ans;
void setValAt(T val, int pos) {
  st[pos + N] = val;
}
T getValAt(int pos) {
  return st[pos + N];
2.2.5 Sparse Table
// st = sparse table, Arith = Arithmetic
typedef int T;
int neutro = 0;
vector<vector<T>>> st;
T F(T a, T b) {
  // return min(a, b);
  return __gcd(a, b);
  // return a + b; // Arith
  // return a * b; // Arith
}
```

```
// O(NlqN)
void build(vector<T> &arr) {
  st.assign(ceil(log2(arr.size())),

    vector<T>(arr.size()));
  st[0] = arr;
  for (int i = 1; (1 << i) <= arr.size(); i++)
    for (int j = 0; j + (1 << i) <= arr.size(); j++)
    \rightarrow st[i][j] = F(st[i - 1][j], st[i - 1][j + (1 <<

    (i - 1))]);
}
// 0(1)
T query(int L, int R) {
  int i = log2(R - L + 1);
 return F(st[i][L], st[i][R + 1 - (1 << i)]);</pre>
// O(lqN)
T queryArith(int L, int R) {
  T ans = neutro;
  while (true) {
    int k = log2(R - L + 1);
    ans = F(ans, st[k][L]);
    L += 1 << k;
    if (L > R) break;
 }
 return ans;
2.3 Strings
2.3.1 Trie
// wpt = number of words passing through
// w = number of words ending in the node
// c = character
struct Trie {
  struct Node {
    // for lexicographical order use 'map'
    // map<char, Node *> ch;
    unordered_map<char, Node *> ch;
    int w = 0, wpt = 0;
 };
 Node *root = new Node();
  // O(STR.SIZE)
  void insert(string str) {
    Node *curr = root;
    for (auto &c : str) {
      curr->wpt++;
      if (!curr->ch.count(c)) curr->ch[c] = new
      → Node();
      curr = curr->ch[c];
    }
    curr->wpt++;
    curr->w++;
  }
 Node *find(string &str) {
```

```
Node *curr = root;
  for (auto &c : str) {
    if (!curr->ch.count(c)) return nullptr;
    curr = curr->ch[c];
 }
 return curr;
// number of words with given prefix O(N)
int prefixCount(string prefix) {
  Node *node = find(prefix);
  return node ? node->wpt : 0;
// number of words matching str O(N)
int strCount(string str) {
  Node *node = find(str);
  return node ? node->w : 0;
}
void getWords(Node *curr, vector<string> &words,

    string &word) {

 if (!curr) return;
 if (curr->w) words.push_back(word);
  for (auto &c : curr->ch) {
    getWords(c.second, words, word += c.first);
    word.pop_back();
 }
// O(N)
vector<string> getWords() {
  vector<string> words;
  string word = "";
  getWords(root, words, word);
  return words;
// O(N)
vector<string> getWordsByPrefix(string prefix) {
  vector<string> words;
  getWords(find(prefix), words, prefix);
}
bool remove(Node *curr, string &str, int &i) {
  if (i == str.size()) {
    curr->wpt--;
    return curr->w ? !(curr->w = 0) : 0;
 int c = str[i];
 if (!curr->ch.count(c)) return false;
 if (remove(curr->ch[c], str, ++i)) {
    if (!curr->ch[c]->wpt) curr->wpt--,

    curr→ch.erase(c);

   return true;
 return false;
```

```
// O(STR.SIZE)
int remove(string str) {
  int i = 0;
  return remove(root, str, i);
};
```

2.4 Trees

2.4.1 Treap

3 Graphs

3.1 Articulation Points And Bridges

```
// APB = articulation points and bridges
// ap = Articulation Point
// br = bridges
// p = parent
// disc = discovery time
// low = lowTime
// ch = children
typedef pair<int, int> Edge;
int MAXN = 101, Time;
vector<vector<int>> ady;
vector<int> disc, low, ap;
vector<Edge> br;
void initVars(int N) {
 ady.assign(N, vector<int>());
int dfsAPB(int u, int p) {
  int ch = 0;
  low[u] = disc[u] = ++Time;
  for (int &v : ady[u]) {
    if (v == p) continue;
    if (!disc[v]) {
      ch++;
      dfsAPB(v, u);
      if (disc[u] <= low[v]) ap[u]++;</pre>
      if (disc[u] < low[v]) br.push_back({u, v});</pre>
      low[u] = min(low[u], low[v]);
    } else
      low[u] = min(low[u], disc[v]);
  }
 return ch;
}
// O(N)
void APB() {
  br.clear();
  ap = low = disc = vector<int>(ady.size());
 Time = 0;
  for (int u = 0; u < N; u++)
    if (!disc[u]) ap[u] = dfsAPB(u, u) > 1;
```

```
void addEdge(int u, int v) {
  ady[u].push_back(v);
  ady[v].push_back(u);
}
```

3.2 Connected Components

```
// comp = component
int MAXN = 26, N, compId = 0;
vector<vector<int>> ady;
vector<int> getComp;
void initVars(int N) {
  ady.assign(N, vector<int>());
  getComp.assign(N, -1);
  compId = 0;
void dfsCC(int u, vector<int> &comp) {
  if (getComp[u] > -1) return;
  getComp[u] = compId;
  comp.push_back(u);
  for (auto &v : ady[u]) dfsCC(v, comp);
}
// O(N)
vector<vector<int>> connectedComponents() {
  vector<vector<int>> comps;
  for (int u = 0; u < ady.size(); u++) {</pre>
    vector<int> comp;
    dfsCC(u, comp);
    if (!comp.empty()) comps.push_back(comp),

→ compId++;

  }
  return comps;
}
void addEdge(int u, int v) {
  ady[u].push_back(v);
  ady[v].push_back(u);
}
```

3.3 Flood Fill

```
for (auto move : movs)
    floodFill(i + move[1], j + move[0]);
                                                               }
                                                             }
                                                             return 0;
                                                           }
void floodFill() {
 for (int i = 0; i < n; i++)
    for (int j = 0; j < m; j++)
                                                           // O(E * V^2)
      if (mat[i][j] == oldColor) floodFill(i, j);
                                                           Num dinicMaxFlow(int s, int t) {
                                                             if (s == t) return -1;
                                                             Num maxFlow = 0;
                                                             while (levelGraph(s, t))
3.4 Flow
                                                               while (Num flow = blockingFlow(s, t, 1 << 30))</pre>
3.4.1 Max Flow Dinic

→ maxFlow += flow;

                                                             return maxFlow;
// cap[a][b] = Capacity from a to b
// flow[a][b] = flow occupied from a to b
// level[a] = level in graph of node a
                                                           void addEdge(int u, int v, Num capacity) {
// Num = number
                                                             cap[u][v] = capacity;
typedef int Num;
                                                             ady[u].push_back(v);
int N, MAXN = 101;
                                                           }
vector<int> level;
vector<vector<int>> ady;
unordered_map<int, unordered_map<int, Num>> cap, flow;
                                                           3.4.2 Maximum Bipartite Matching
void initVars(int N) {
                                                           #include "Max Flow Dinic.cpp"
  ady.assign(N, vector<int>());
                                                           void addEdge(int u, int v) {
  cap.clear();
                                                             cap[u][v] = 1;
 flow.clear();
                                                             ady[u].push_back(v);
                                                           }
bool levelGraph(int s, int t) {
                                                           int main() {
 level = vector<int>(ady.size());
                                                             int n, s = 0, t = 1;
  level[s] = 1;
                                                             cin >> n;
  queue<int> q;
                                                             initVars(n);
  q.push(s);
                                                             while (n--) {
  while (!q.empty()) {
                                                               int u, v;
    int u = q.front();
                                                               cin >> u >> v;
                                                               addEdge(u += 2, v += 2);
    q.pop();
    for (int &v : ady[u]) {
                                                               addEdge(s, u);
      if (!level[v] && flow[u][v] < cap[u][v]) {</pre>
                                                               addEdge(v, t);
                                                             }
        q.push(v);
        level[v] = level[u] + 1;
                                                             cout << dinicMaxFlow(s, t) << endl;</pre>
                                                             return 0;
    }
                                                           }
  }
  return level[t];
                                                           3.5
                                                                Has Cycle
Num blockingFlow(int u, int t, Num currPathMaxFlow) {
                                                           vector<vector<int>>> ady, cycles;
  if (u == t) return currPathMaxFlow;
                                                           vector<int> vis, cycle;
  for (int v : ady[u]) {
                                                           bool flag = false, isDirected = false;
    Num capleft = cap[u][v] - flow[u][v];
                                                           int root = -1;
    if ((level[v] == (level[u] + 1)) && (capleft > 0))
                                                           void initVars(int N) {
      Num pathMaxFlow = blockingFlow(v, t,
                                                             ady.assign(N, vector<int>());

→ min(currPathMaxFlow, capleft));
                                                             vis.assign(N, 0);
      if (pathMaxFlow > 0) {
                                                             cycles.clear();
        flow[u][v] += pathMaxFlow;
                                                             root = -1, flag = false;
                                                           }
        flow[v][u] -= pathMaxFlow;
        return pathMaxFlow;
```

```
}
bool hasCycle(int u, int prev) {
  vis[u] = 1;
  for (auto &v : ady[u]) {
                                                           3.7 LCA
    if (v == u || vis[v] == 2 || (!isDirected && v ==
    → prev)) continue;
                                                           // st = sparse table
    if (flag) {
                                                           typedef pair<int, int> T;
      if (!vis[v]) hasCycle(v, u);
                                                           int neutro = 0;
      continue;
                                                           vector<vector<T>> st;
    }
    if (vis[v] || hasCycle(v, u)) {
                                                           vector<int> first;
      if (root == -1) root = v, flag = true;
                                                           vector<T> tour;
      cycle.push_back(u);
                                                           vector<vector<int>> ady;
      if (root == u) flag = false, root = -1,

    cycles.push_back(cycle), cycle.clear();

                                                           T F(T a, T b) {
                                                             return a.first < b.first ? a : b;</pre>
  }
                                                           }
 vis[u] = 2;
  return flag;
                                                           void build() {
                                                             st.assign(ceil(log2(tour.size())),

    vector<T>(tour.size()));
// O(N)
                                                             st[0] = tour;
bool hasCycle() {
                                                             for (int i = 1; (1 << i) <= tour.size(); i++)</pre>
  for (int u = 0; u < ady.size(); u++)</pre>
                                                                for (int j = 0; j + (1 << i) <= tour.size(); j++)
    if (!vis[u]) cycle.clear(), hasCycle(u, -1);
                                                                \rightarrow st[i][j] = F(st[i - 1][j], st[i - 1][j + (1 <<
 return cycles.size() > 0;
                                                                \rightarrow (i - 1))]);
                                                           }
void addEdge(int u, int v) {
                                                           T query(int 1, int r) {
  ady[u].push_back(v);
                                                             int i = log2(r - 1 + 1);
  if (!isDirected) ady[v].push_back(u);
                                                             return F(st[i][l], st[i][r + 1 - (1 << i)]);
3.6 Is Bipartite
                                                           void initVars(int N) {
                                                             ady.assign(N, vector<int>());
vector<vector<int>> ady;
void initVars(int N) {
                                                           void eulerTour(int u, int p, int h) {
  ady.assign(N, vector<int>());
                                                             first[u] = tour.size();
                                                             tour.push_back({h, u});
                                                             for (int v : ady[u])
// O(N)
                                                               if (v != p) {
bool isBipartite() {
                                                                  eulerTour(v, u, h + 1);
  vector<int> color(ady.size(), -1);
                                                                  tour.push_back({h, u});
  for (int s = 0; s < ady.size(); s++) {</pre>
                                                           }
    if (color[s] > -1) continue;
    color[s] = 0;
                                                           void preprocess() {
    queue<int> q;
    q.push(s);
                                                             tour.clear();
    while (!q.empty()) {
                                                             first.assign(ady.size(), -1);
      int u = q.front();
                                                             eulerTour(0, 0, 0);
                                                             build();
      q.pop();
      for (int &v : ady[u]) {
                                                           }
        if (color[v] < 0) q.push(v), color[v] =</pre>
                                                           int lca(int u, int v) {
         if (color[v] == color[u]) return false;
                                                             int l = min(first[u], first[v]);
      }
                                                             int r = max(first[u], first[v]);
    }
                                                             return query(1, r).second;
  }
                                                           }
```

return true;

```
void addEdge(int u, int v) {
                                                            weight.clear();
  ady[u].push_back(v);
                                                            msts.clear();
                                                          }
  ady[v].push_back(u);
                                                          Num prim(int s) {
                                                            vector<Wedge> mst;
    MST Kruskal
3.8
//N = number of nodes
                                                            set<Edge> q;
#include "../Data Structures/Graphs/UnionFind.cpp"
typedef int Num;
                                                            q.insert(\{0, s\});
typedef pair<int, int> Edge;
                                                            while (q.size()) {
typedef pair<Num, Edge> Wedge;
vector<Wedge> Wedges; // gets filled from input;
                                                              q.erase(q.begin());
vector<Wedge> mst;
UnionFind uf(0);
void initVars(int N) {
  mst.clear();
 Wedges.clear();
  uf = UnionFind(N);
                                                                }
                                                              }
Num kruskal() {
                                                            }
 Num cost = 0;
  sort(Wedges.begin(), Wedges.end());

→ mst.end()));
  // reverse(Wedges.begin(), Wedges.end());
                                                            return cost;
 for (Wedge &wedge : Wedges) {
                                                          }
   int u = wedge.second.first, v =

→ wedge.second.second;

                                                          Num primLazy(int s) {
   if (!uf.areConnected(u, v)) uf.join(u, v),
                                                            vector<Wedge> mst;

→ mst.push_back(wedge), cost += wedge.first;

  }
  return cost;
void addEdge(int u, int v, Num w) {
                                                            q.push(\{0, s\});
 Wedges.push_back({w, {u, v}});
                                                            while (q.size()) {
                                                              int u = aux.second;
3.9 MST Prim
                                                              q.pop();
// st = spanning tree, p = parent
// vis = visited, dist = distance
typedef int Num;
typedef pair<int, int> Edge;
typedef pair<Num, Edge> Wedge;
typedef pair<Num, int> DistNode;

    v});
int MAXN = 20001, INF = 1 << 30;
                                                              }
vector<vector<int>> ady;
                                                            }
unordered_map<int, unordered_map<int, Num>> weight;
vector<int> p, vis;

→ mst.end());
vector<Num> dist;
                                                            return cost;
vector<vector<Wedge>> msts;
                                                          }
void initVars(int N) {
                                                          // O(V + E * log(V))
  ady.assign(N, vector<int>());
```

p.assign(N, 0);

vis.assign(N, 0);

dist.assign(N, INF);

```
vector<set<Edge>::iterator> pos(ady.size());
  vector<Num> dist(ady.size(), INF);
  Num cost = dist[s] = 0;
    int u = q.begin()->second;
    vis[u] = 1, cost += dist[u];
    mst.push_back({dist[u], {p[u], u}});
    for (int &v : ady[u]) {
      Num w = weight[u][v];
      if (!vis[v] && w < dist[v]) {</pre>
        if (dist[v] != INF) q.erase(pos[v]);
        pos[v] = q.insert({dist[v] = w, v}).first;
  msts.push_back(vector<Wedge>(mst.begin() + 1,
  vector<set<Edge>::iterator> pos(ady.size());
  vector<Num> dist(ady.size(), INF);
  priority_queue<DistNode, vector<DistNode>,

    greater<DistNode>> q;

  Num cost = dist[s] = 0;
    pair<int, int> aux = q.top();
    if (dist[u] < aux.first) continue;</pre>
    vis[u] = 1, cost += dist[u];
    mst.push_back({dist[u], {p[u], u}});
    for (int &v : ady[u]) {
      Num w = weight[u][v];
      if (!vis[v] && w < dist[v]) q.push({dist[v] = w,</pre>
  msts.push_back(vector<Wedge>(mst.begin() + 1,
Num prim() {
  Num cost = 0;
  map<int, Num> q;
```

```
for (int i = 0; i < ady.size(); i++)
    if (!vis[i]) cost += prim(i);
                                                            void initVars(int N) {
                                                              ady.assign(N, vector<int>());
  return cost;
                                                              weight.clear();
void addEdge(int u, int v, Num w) {
  ady[u].push_back(v);
                                                            // O(E * log(V))
  weight[u][v] = w;
                                                            vector<int> dijkstra(int s) {
  ady[v].push_back(u);
                                                              vector<set<DistNode>::iterator> pos(ady.size());
  weight[v][u] = w;
                                                              vector<Num> dist(ady.size(), INF);
                                                              set<DistNode> q;
                                                              q.insert(\{0, s\}), dist[s] = 0;
                                                              while (q.size()) {
3.10
       ShortestPaths
                                                                int u = q.begin()->second;
3.10.1 Bellman Ford
                                                                q.erase(q.begin());
                                                                for (int &v : ady[u]) {
//N = number of nodes
                                                                  Num w = weight[u][v];
// returns {} if there is a negative weight cycle
                                                                  if (dist[u] + w < dist[v]) {</pre>
                                                                    if (dist[v] != INF) q.erase(pos[v]);
typedef int Num;
                                                                    pos[v] = q.insert({dist[v] = dist[u] + w,
int MAXN = 20001, N, INF = 1 << 30, isDirected = true;</pre>

    v}).first;
vector<vector<int>> ady;
                                                                  }
unordered_map<int, unordered_map<int, Num>> weight;
                                                                }
                                                              }
void initVars(int N) {
                                                              return dist;
  ady.assign(N, vector<int>());
                                                            }
  weight.clear();
}
                                                            vector<int> dijkstraLazy(int s) {
                                                              vector<int> dist(ady.size(), INF);
// O(V * E)
                                                              priority_queue<DistNode, vector<DistNode>,
vector<Num> bellmanFord(int s) {

    greater<DistNode>> q;

  vector<Num> dist(ady.size(), INF);
                                                              q.push({0, s}), dist[s] = 0;
  dist[s] = 0;
                                                              while (q.size()) {
  for (int i = 1; i <= ady.size(); i++)</pre>
                                                                DistNode top = q.top(); q.pop();
    for (int u = 0; u < ady.size(); u++)</pre>
                                                                int u = top.second;
      for (auto &v : ady[u]) {
                                                                if (dist[u] < top.first) continue;</pre>
        Num w = weight[u][v];
                                                                for (int &v : ady[u]) {
        if (dist[u] != INF && dist[u] + w < dist[v]) {</pre>
                                                                  Num w = weight[u][v];
          if (i == ady.size()) return {};
                                                                  if (dist[u] + w < dist[v]) q.push({dist[v] =</pre>
          dist[v] = dist[u] + w;
                                                                   \rightarrow dist[u] + w, v});
        }
                                                                }
      }
                                                              }
  return dist;
                                                              return dist;
}
                                                            }
void addEdge(int u, int v, Num w) {
                                                            void addEdge(int u, int v, Num w) {
  ady[u].push_back(v);
                                                              ady[u].push_back(v);
  weight[u][v] = w;
                                                              weight[u][v] = w;
  if (isDirected) return;
                                                              if (isDirected) return;
  ady[v].push_back(u);
                                                              ady[v].push_back(u);
  weight[v][u] = w;
                                                              weight[v][u] = w;
                                                            }
3.10.2 Dijkstra
                                                                   Strongly Connected Components
                                                            3.11
typedef int Num;
typedef pair<Num, int> DistNode;
int MAXN = 20001, INF = 1 << 30, isDirected = false;</pre>
                                                            // tv = top value from stack
                                                            // sccs = strongly connected components
vector<vector<int>> ady;
                                                            // scc = strongly connected component
unordered_map<int, unordered_map<int, Num>> weight;
```

```
// disc = discovery time
// low = low time
// s = stack
// top = top index of the stack
int MAXN = 101, Time, top;
vector<vector<int>> ady, sccs;
vector<int> disc, low, s;
void initVars(int N) {
  ady.assign(N, vector<int>());
void dfsSCCS(int u) {
  if (disc[u]) return;
  low[u] = disc[u] = ++Time;
  s[++top] = u;
  for (int &v : ady[u]) dfsSCCS(v), low[u] =

    min(low[u], low[v]);
  if (disc[u] == low[u]) {
    vector<int> scc;
    while (true) {
      int tv = s[top--];
      scc.push_back(tv);
      low[tv] = ady.size();
      if (tv == u) break;
    sccs.push_back(scc);
}
// O(N)
void SCCS() {
  s = low = disc = vector<int>(ady.size());
  Time = 0, top = -1, sccs.clear();
  for (int u = 0; u < ady.size(); u++) dfsSCCS(u);</pre>
void addEdge(int u, int v) {
 ady[u].push_back(v);
3.12
      Topological Sort
// vis = visited
vector<vector<int>> ady;
vector<int> vis, toposorted;
```

```
// vis = visited
vector<vector<int>> ady;
vector<int>> vis, toposorted;

void initVars(int N) {
   ady.assign(N, vector<int>());
   vis.assign(N, 0);
   toposorted.clear();
}

// returns false if there is a cycle
bool toposort(int u) {
   vis[u] = 1;
   for (auto &v : ady[u]) {
      if (v == u || vis[v] == 2) continue;
      if (vis[v] == 1 || !toposort(v)) return false;
```

```
}
vis[u] = 2;
toposorted.push_back(u);
return true;
}

// O(N)
bool toposort() {
  vis.clear();
  for (int u = 0; u < ady.size(); u++)
    if (!vis[u])
      if (!toposort(u)) return false;
  return true;
}</pre>
```

4 Maths

4.1 Number Theory

4.1.1 Divisibility Criterion

```
def divisorCriteria(n, lim):
    results = []
    tenElevated = 1
    for i in range(lim):
        \# remainder = pow(10, i, n)
        remainder = tenElevated % n
        negremainder = remainder - n
        if(remainder <= abs(negremainder)):</pre>
            results.append(remainder)
        else:
            results.append(negremainder)
        tenElevated *= 10
    return results
def testDivisibility(dividend, divisor,

    divisor_criteria):

    dividend = str(dividend)
    addition = 0
    dividendSize = len(dividend)
    i = dividendSize - 1
    j = 0
    while j < dividendSize:</pre>
        addition += int(dividend[i]) *

    divisor_criteria[j]

        i -= 1
        j += 1
    return addition % divisor == 0
if __name__ == '__main__':
    dividend, divisor = map(int, input().split())
    divisor_criteria = divisorCriteria(divisor,
    → len(str(dividend)))
    print(divisor_criteria)
    print(testDivisibility(dividend, divisor,

→ divisor_criteria))
```

```
4.1.2 Extended Euclidean
// \gcd(a, b) = ax + by
vector<long long int> extendedGCD(
    long long int a, long long int b) {
  if (a > OLL && b == OLL) {
   return {a, 1LL, 0LL};
  long long int x = 1LL, y = 0LL, prevx = 0LL,
                prevy = 1LL, q, remainder;
  while (true) {
   q = a / b;
   remainder = a - b * q;
   if (remainder == OLL) break;
   a = b;
   b = remainder;
   x = x - prevx * q;
   swap(x, prevx);
   y = y - prevy * q;
   swap(y, prevy);
  }
  // gcd = b, x = prevx, y = prevy
 return {b, prevx, prevy};
4.1.3 GCD
int gcd(int a, int b) {
 return !b ? a : gcd(b, a % b);
int gcdI(int a, int b) {
 while (b) {
   a %= b;
   swap(a, b);
 }
 return a;
4.1.4 LCM
```

```
int lcm(int a, int b) {
 int c = gcd(a, b);
 return c ? a / c * b : 0;
```

4.1.5 Prime Check Miller Rabin

```
from random import randrange
def is_prime(p):
   k = 100
    if p == 2 or p == 3:
       return True
    if (p \& 1) == 0 or p == 1:
        return False
    phi = p - 1
    d = phi
    r = 0
```

```
while (d \& 1) == 0:
    d = int(d >> 1)
    r += 1
for i in range(k):
    a = randrange(2, p - 2)
    exp = pow(a, d, p)
    if exp == 1 or exp == p - 1:
        continue
    flag = False
    for j in range(r - 1):
        exp = pow(exp, 2, p)
        if exp == 1:
            return False
        if exp == p - 1:
            flag = True
            break
    if flag:
        continue
    else:
        return False
return True
```

4.1.6 Prime Sieve

```
vector<int> primeSieve(int n) {
  vector<int> sieve(n + 1);
  for (int i = 4; i \le n; i += 2) sieve[i] = 2;
  for (int i = 3; i * i <= n; i += 2)
    if (!sieve[i])
      for (int j = i * i; j \le n; j += 2 * i)
        if (!sieve[j]) sieve[j] = i;
  return sieve;
}
```

Strings

5.1 KMP

```
// f = error function
// cf = create error function
// p = pattern
// t = text
// pos = positions where pattern is found in text
int MAXN = 1000000;
vector<int> f(MAXN + 1);
vector<int> kmp(string &p, string &t, int cf) {
  vector<int> pos;
  if (cf) f[0] = -1;
  for (int i = cf, j = 0; j < t.size();) {</pre>
    while (i > -1 \&\& p[i] != t[j]) i = f[i];
    i++, j++;
    if (cf) f[j] = i;
    if (!cf && i == p.size()) pos.push_back(j - i), i
  }
 return pos;
```

```
vector<int> search(string &p, string &t) {
  kmp(p, p, -1);  // create error function
  return kmp(p, t, 0);  // search in text
}
```

5.2 Rabin Karp

class RollingHash {

```
public:
  vector<unsigned long long int> pow;
  vector<unsigned long long int> hash;
  unsigned long long int B;
  RollingHash(const string &text) : B(257) {
    int N = text.size();
   pow.resize(N + 1);
   hash.resize(N + 1);
    pow[0] = 1;
   hash[0] = 0;
    for (int i = 1; i <= N; ++i) {
      // in c++ an unsigned long long int is
      // automatically modulated by 2^64
      pow[i] = pow[i - 1] * B;
      hash[i] = hash[i - 1] * B + text[i - 1];
   }
  }
  unsigned long long int getWordHash() {
   return hash[hash.size() - 1];
  unsigned long long int getSubstrHash(int begin, int
  \rightarrow end) {
   return hash[end] - hash[begin - 1] * pow[end -
    \rightarrow begin + 1];
  int size() {
   return hash.size();
  }
};
vector<int> rabinKarp(RollingHash &rhStr, string
vector<int> positions;
 RollingHash rhPattern(pattern);
 unsigned long long int patternHash =

¬ rhPattern.getWordHash();
  int windowSize = pattern.size(), end = windowSize;
  for (int i = 1; end < rhStr.size(); i++) {</pre>
   if (patternHash == rhStr.getSubstrHash(i, end))
    → positions.push_back(i);
    end = i + windowSize;
  }
  return positions;
```

6 Techniques

6.1 Binary Search

6.2 Multiple Queries

6.2.1 Mo

```
#include <bits/stdc++.h>
using namespace std;
// q = query
// qs = queries
struct Query {
  int 1, r;
};
int N, M, blksize;
vector<Query> qs;
vector<int> arr;
void initVars() {
  qs = vector<Query>(M);
  arr = vector<int>(N);
}
bool cmp(Query &a, Query &b) {
  if (a.1 == b.1) return a.r < b.r;</pre>
  return a.l / blksize < b.l / blksize;</pre>
}
void getResults() {
  blksize = (int)sqrt(N);
  sort(qs.begin(), qs.end(), cmp);
  int prevL = 0, prevR = -1;
  int sum = 0;
  for (auto &q : qs) {
    int L = q.1, R = q.r;
    while (prevL < L) {</pre>
      sum -= arr[prevL]; // problem specific
      prevL++;
    while (prevL > L) {
      prevL--;
      sum += arr[prevL]; // problem specific
    while (prevR < R) {</pre>
      prevR++;
      sum += arr[prevR]; // problem specific
    while (prevR > R) {
      sum -= arr[prevR]; // problem specific
      prevR--;
    }
    cout << "sum[" << L << ", " << R
```

```
<< "] = " << sum << endl;
int main() {
 arr = \{1, 1, 2, 1, 3, 4, 5, 2, 8\};
 N = arr.size();
 qs = \{\{0, 8\}, \{3, 5\}\};
 M = qs.size();
 getResults();
6.2.2 SQRT Decomposition
// sum of elements in range
#include <bits/stdc++.h>
using namespace std;
int N, blksize;
int MAXN = 100, MAXSQR = (int)sqrt(MAXN);
vector<int> arr(MAXN);
vector<int> blks(MAXSQR + 1);
void preprocess() {
 blksize = sqrt(N);
  for (int i = 0, j = 0; i < N; i++) {
    if (i == blksize * j) j++;
    blks[j - 1] += arr[i]; // problem specific
 }
}
// problem specific
void update(int i, int val) {
 blks[i / blksize] += val - arr[i];
  arr[i] = val;
}
int query(int 1, int r) {
  int sum = 0;
  int lblk = 1 / blksize;
  if (l != blksize * lblk++)
    while (l < r && l != lblk * blksize) {</pre>
      sum += arr[1]; // problem specific
      1++;
    }
  while (l + blksize <= r) {</pre>
    sum += blks[l / blksize]; // problem specific
    1 += blksize;
  while (1 <= r) {
    sum += arr[1]; // problem specific
    1++;
 return sum;
```

```
int main() {
  N = 10;
  arr = \{1, 5, 2, 4, 6, 1, 3, 5, 7, 10\};
  preprocess();
  for (int i = 0; i < blksize + 1; i++)</pre>
    cout << blks[i] << " ";
  // 8 11 15 10
  cout << endl;</pre>
  cout << query(3, 8) << " ";</pre>
  cout << query(1, 6) << " ";</pre>
  update(8, 0);
  cout << query(8, 8) << endl;</pre>
  // 26 21 0
  return 0;
}
```