Competitive

Programming

Reference

First, solve the problem. Then, write the code.

John Johnson

Ву

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Coding Resources

C++

Competitive Programming Template

```
/*****************
https://searleser97.gitlab.io/algorithms/template.cpp
************************************
#include <bits/stdc++.h>
using namespace std;
#define\ endl\ '\n'
#define forr(_, x, n) for (int _ = x; ~_; _--)
#define fos(_, x, n, s) for(int _ = x; _ < n; _ += s)
#define forn(\_, x, n) fos (\_, x, n, 1)
#define rep(_, n) forn(_, 0, n)
#define fi first
#define se second
#define pb push_back
#define pairii pair<int, int>
// typedef __int128_t lli;
typedef long long int li;
typedef long double ld;
void _main(int tc) {
int main() {
 ios_base::sync_with_stdio(0);
 cin.tie(0), cout.tie(0);
 _main(0); return 0;
 int tc;
 cin >> tc;
 rep(i, tc) _main(i + 1);
```

Decimal Precision

```
// rounds up the decimal number
cout << setprecision(N) << n << endl;
// specify N fixed number of decimals
cout << fixed << setprecision(N) << n << endl;</pre>
```

Include All Libraries

```
#include <bits/stdc++.h>
using namespace std;
```

IO Optimization

```
int main() {
  ios_base::sync_with_stdio(0);
  cin.tie(0);
}
```

Map Value To Int

```
// val = value
typedef string Val;
unordered_map<Val, int> intForVal;
unordered_map<int, Val> valForInt;
int mapId = 0;
int Map(Val val) {
   if (intForVal.count(val)) return intForVal[val];
   valForInt[mapId] = val;
   return intForVal[val] = mapId++;
}

Val IMap(int n) { return valForInt[n]; }

void initMapping() {
   mapId = 0;
   intForVal.clear();
   valForInt.clear();
}
```

Number To String

```
#include <bits/stdc++.h>
using namespace std;

int main() {
    // to_string method converts any type of number
    // (int, double, long long int, ...) to string
    string str = "str+" + to_string(123 + 1);
    cout << str << endl; // output: str+124
    return 0;
}</pre>
```

Permutations

```
typedef vector<int> T; // typedef string T;

vector<T> permutations(T v) {
  vector<vector<int>> ans;
  sort(v.begin(), v.end());
  do
    ans.push_back(v);
  while (next_permutation(v.begin(), v.end()));
  return ans;
}
```

Print Vector

```
void printv(vector<int> v) {
  if (v.size() == 0) {
    cout << "[]" << endl;
    return;
  }
  cout << "[" << v[0];
  for (int i = 1; i < v.size(); i++)
    cout << ", " << v[i];
  cout << "]" << endl;
}</pre>
```

Priority Queue Of Object

Random

Read Line

```
// when reading lines, don't mix 'cin' with
// 'getline' just use getline and split
string input() {
   string ans;
   cin >> ws;
   cin.ignore(numeric_limits<streamsize>::max(), '\n');
   getline(cin, ans);
   return ans;
}
```

Set of Object

```
struct Object {
   char first;
   int second;
};

int main() {
   auto cmp = [](const Object& a, const Object& b) {
    return a.second > b.second;
   };
   set<Object, decltype(cmp)> pq(cmp);
}
```

Sort Vector Of Object

```
struct Object {
  char first;
  int second;
};

bool cmp(const Object& a, const Object& b) {
  return a.second > b.second;
}

int main() {
  vector<Object> v = {{'c', 3}, {'a', 1}, {'b', 2}};
  sort(v.begin(), v.end(), cmp);
}
```

Sort Vector of Pairs

```
vector<pair<int, int>> pairs;
// sorts array on the basis of the first element
sort(pairs.begin(), pairs.end());
```

Split String

```
vector<string> split(string str, char token) {
   stringstream ss(str);
   vector<string> v;
   while (getline(ss, str, token)) v.push_back(str);
   return v;
}
```

String To Int

```
#include <bits/stdc++.h>
using namespace std;

int main() {
   int n = stoi("123") + 1;
   cout << n << endl; // output: 124
   // stoll for long long int
   // stoull for unsigned long int
   // stod for double
   // stold for long double
}</pre>
```

Typedef

```
typedef TYPE ALIAS;
// example:
typedef int T;
```

Unordered Map with pair as key

Python

Combinations

```
import itertools
# from arr choose k = > combinations(arr, k)
print(list(itertools.combinations([1, 2, 3], 3)))
```

Fast IO

```
from sys import stdin, stdout

N = 10
# Reads N chars from stdin(it counts '\n' as char)
stdin.read(N)
# Reads until '\n' or EOF
line = stdin.readline()
# Reads all lines in stdin until EOF
lines = stdin.readlines()
# Writes a string to stdout, it doesn't add '\n'
stdout.write(line)
# Writes a list of strings to stdout
stdout.writelines(lines)
# Reads numbers separated by space in a line
numbers = list(map(int, stdin.readline().split()))
```

Permutations

```
import itertools
print(list(itertools.permutations([1, 2, 3])))
```

Random

```
import random
# Initialize the random number generator.
random.seed(None)
# Returns a random integer N such that a <= N <= b.
random.randint(a, b)
# Returns a random integer N such that 0 <= N < b
random.randrange(b)
# Returns a random integer N such that a <= N < b.
random.randrange(a, b)
# Returns and integer with k random bits.
random.getrandbits(k)
# shuffles a list
random.shuffle(li)</pre>
```

Sort List

```
li = ['a', 'c', 'b']
# sorts inplace in descending order
li.sort(reverse=True)
# returns sorted list ascending order
ol = sorted(li)
```

Sort List Of Object

```
class MyObject :
    def __init__(self, first, second, third):
        self.first = first
        self.second = second
        self.third = third
```

```
li = [MyObject('b', 3, 1), MyObject('a', 3, 2),

→ MyObject('b', 3, 3)]
# returns list sorted by first then by second then by

→ third in increasing order

ol = sorted(li, key = lambda x: (x.first, x.second,

→ x.third), reverse=False)
# sorts inplace by first then by second then by third

→ in increasing order
li.sort(key = lambda x: (x.first, x.second, x.third),

→ reverse=False)
```

BITs Manipulation

Bit Count

```
int bitCount(int n) {
  return sizeof(n) * 8 - __builtin_clz(n);
}
int bitCount(int n) {
  int c = 0;
  while (n) c++, n >>= 1;
  return c;
}
```

Bits To Int

```
typedef __int128_t lli

lli bitsToInt(string bits, bool isneg) {
    lli ans = 0;
    for (int i = bits.size() - 1, j = 0; ~i; i--, j++) {
        if (isneg) bits[i] = bits[i] == '0' ? '1' : '0';
        ans |= (lli)(bits[i] - '0') << j;
    }
    return isneg ? -(++ans) : ans;
}</pre>
```

Count Leading Zeroes

```
int clz(int n) {
  return __builtin_clz(n);
  // return __builtin_clzl(n); for long
  // return __builtin_clzll(n); for long long
}
int clz(int n) {
  // return sizeof(n) * 8 - bitCount(n);
  int c = 0;
  while (n) c++, n >>= 1;
  return sizeof(n) * 8 - c;
}
```

Count Set Bits

```
int popCount(int n) {
   return __builtin_popcount(n);
   // return __builtin_popcountl(n); for long
   // return __builtin_popcountll(n); for long long
}

int popCount(int n) {
   int c = 0;
   while (n) c++, n &= n - 1;
   return c;
}
```

Count Trailing Zeroes

```
int ctz(int n) {
  return __builtin_ctz(n);
  // return __builtin_ctzl(n); for long
  // return __builtin_ctzll(n); for long long
}

int ctz(int n) {
  int c = 0;
  n = ~n;
  while(n & 1) c++, n >>= 1;
  return c;
}
```

Divide By 2

```
int divideBy2(int n) { return n >> 1; }
```

Is Even

```
bool isEven(int n) { return ~n & 1; }
```

Is i-th Bit Set

```
bool isIthBitSet(int n, int i) {
  return n & (1 << i);
}</pre>
```

Is Odd

```
bool isOdd(int n) { return n & 1; }
```

Is Power Of 2

```
bool isPowerOf2(int n) { return n && !(n & (n - 1)); }
```

Least Significant Set Bit

```
int lsb(int n) { return n & -n; }
```

Log2

```
int Log2(int n) {
   return sizeof(n) * 8 - __builtin_clz(n) - 1;
}
int Log2(int n) {
   int lg2 = 0;
   while (n >>= 1) lg2++;
   return lg2;
}
```

Most Significant Set Bit

```
int msb(int n) {
  return 1 << (sizeof(n) * 8 - __builtin_clz(n) - 1);
}</pre>
```

Multiply By 2

```
int multiplyBy2(int n) { return n << 1; }</pre>
```

One's Complement

```
int onesComplement(int n) { return ~n; }
```

Parity Check

```
bool parityCheck(int n) {
  return !__builtin_parity(n);
  // return !__builtin_parityl(n); for long
  // return !__builtin_parityll(n); for long long
}

bool parityCheck(int n) {
  return isEven(popCount(n));
}
```

Print Bits

```
void printBits(int n) {
  for (int i = sizeof(n) * 8 - 1; ~i; i--)
    cout << ((n >> i) & 1);
  cout << endl;
}</pre>
```

Set i-th Bit

```
int setIthBit(int n, int i) { return n | (1 << i); }</pre>
```

Swap Integer Variables

```
void swap(int &a, int &b) {
   a ^= b;
   b ^= a;
   a ^= b;
}
```

To Lower Case

```
char lowerCase(char c) {
  return c | ' ';
}
```

To Upper Case

```
char upperCase(char c) {
  return c & '_';
}
```

Toggle Case

```
char toggleCase(char c) {
  return c ^ ' ';
}
```

Toggle i-th Bit

```
int toggleIthBit(int n, int i) {
  return n ^ (1 << i);
}</pre>
```

Two's Complement

```
int twosComplement(int n) { return ~n + 1; }
```

Unset i-th Bit

```
int unsetIthBit(int n, int i) {
  return n & (~(1 << i));
}</pre>
```

// c = center, r = radius;

#include "Point.cpp"

Data Structures

Geometry

Circle

```
struct Circle {
 Point c;
 ld r;
 Circle(Point c, ld r) : c(c), r(r) {}
Point
typedef long double ld;
const ld pi = acos(-1);
struct Point {
 ld x, y;
 Point(): x(0), y(0) {}
 Point(ld x, ld y) : x(x), y(y) {}
 Point operator+(const Point &p) {
   return Point(x + p.x, y + p.y);
 Point operator-(const Point &p) {
   return Point(x - p.x, y - p.y);
 Point operator*(const ld &k) {
   return Point(x * k, y * k);
 Point operator/(const ld &k) {
   return Point(x / k, y / k);
 ld dot(const Point &p) {
   return x * p.x + y * p.y;
 ld cross(const Point &p) {
   return x * p.y - y * p.x;
 }
 ld norm() const { return sqrt(x * x + y * y); }
 Point perpendicularLeft() { return Point(-y, x); }
 Point perpendicularRight() { return Point(y, -x); }
```

Graphs

Union Find

```
struct UnionFind {
  int n:
  vector<int> dad, size;
  UnionFind(int N) : n(N), dad(N), size(N, 1) {
    while (N--) dad[N] = N;
  // O(lq*(N))
  int root(int u) {
    if (dad[u] == u) return u;
   return dad[u] = root(dad[u]);
  }
  // 0(1)
  void join(int u, int v) {
    int Ru = root(u), Rv = root(v);
    if (Ru == Rv) return;
   if (size[Ru] > size[Rv]) swap(Ru, Rv);
    --n, dad[Ru] = Rv;
   size[Rv] += size[Ru];
  }
  // O(lg*(N))
  bool areConnected(int u, int v) {
    return root(u) == root(v);
  int getSize(int u) { return size[root(u)]; }
  int numberOfSets() { return n; }
};
```

Union Find (Partially Persistent)

```
// jTime = join time, t = time
struct UnionFind {
  int Time = 0;
  vector<int> dad, size, jTime;

UnionFind(int N) : dad(N), size(N, 1), jTime(N) {
    while (N--) dad[N] = N;
}

// O(lg(N))
int root(int u, int t) {
  while (jTime[u] <= t && u != dad[u]) u = dad[u];
  return u;
}</pre>
```

```
// 0(1)
  void join(int u, int v, bool newTime = 1) {
    int Ru = root(u, Time), Rv = root(v, Time);
    if (newTime) Time++;
    if (Ru == Rv) return;
    if (size[Ru] > size[Rv]) swap(Ru, Rv);
    jTime[Ru] = Time;
   dad[Ru] = Rv;
   size[Rv] += size[Ru];
  // O(lg(N))
 bool areConnected(int u, int v, int t) {
   return root(u, t) == root(v, t);
  // O(lg(N))
  int getLastVersionSize(int u) {
   return size[root(u, Time)];
  // O(lg(Time) * lg(N))
  int joinTime(int u, int v) {
   int l = 0, r = Time, ans = -1;
   while (1 <= r) {
      int mid = (1 + r) >> 1;
      if (areConnected(u, v, mid))
        ans = mid, r = mid - 1;
      else
        l = mid + 1;
   }
   return ans;
 }
};
```

Ranges

BIT

```
template <class T>
struct BIT {
   T neutro = 0;
   vector<T> bit;

BIT(int n) { bit.assign(++n, neutro); }

inline T F(T a, T b) {
   return a + b;
   // return a * b;
}

// Inverse of F
inline T I(T a, T b) {
   return a - b;
   // return a / b;
}
```

```
// O(N)
  void build() {
    for (int i = 1; i < bit.size(); i++) {</pre>
      int j = i + (i & -i);
      if (j < bit.size()) bit[j] = F(bit[j], bit[i]);</pre>
  }
  // O(lq(N))
  void update(int i, T val) {
    for (i++; i < bit.size(); i += i & -i)</pre>
      bit[i] = F(bit[i], val);
  // O(lq(N))
  T query(int i) {
    T ans = neutro;
    for (i++; i; i -= i & -i) ans = F(ans, bit[i]);
    return ans;
  // O(lg(N)), [l, r]
  T query(int 1, int r) {
    return I(query(r), query(--1));
  T& operator[](int i) { return bit[++i]; }
};
BIT Range Update
typedef long long int T;
T neutro = 0;
vector<T> bit1, bit2;
void initVars(int n) {
  bit1.assign(++n, neutro);
  bit2 = bit1;
}
// O(lg(N))
void update(vector<T> &bit, int i, T val) {
  for (i++; i < bit.size(); i += i & -i)</pre>
    bit[i] += val;
}
// O(lq(N)), [l, r]
void update(int 1, int r, T val) {
  update(bit1, 1, val);
  update(bit1, r + 1, -val);
  update(bit2, r + 1, val * r);
  update(bit2, 1, -val * (l - 1));
// O(lq(N))
T query(vector<T> &bit, int i) {
  T ans = neutro;
  for (i++; i; i -= i & -i) ans += bit[i];
  return ans;
}
```

```
// O(lq(N))
T query(int i) {
 return query(bit1, i) * i + query(bit2, i);
// O(lg(N)), [l, r]
T query(int 1, int r) {
 return query(r) - query(l - 1);
```

```
Segment Tree
// st = segment tree. st[1] = root;
// neutro = operation neutral value
// e.g. for sum is 0, for multiplication
// is 1, for gcd is 0, for min is INF, etc.
template <class T>
struct SegmentTree {
 T neutro = 0;
  int N:
  vector<T> st;
 SegmentTree(int n) : st(2 * n, neutro), N(n) {}
  inline T F(T a, T b) {
   return a + b;
   // return __gcd(a, b);
   // return a * b;
    // return min(a, b);
  // O(2N)
  void build() {
   for (int i = N - 1; i > 0; i--)
      st[i] = F(st[i << 1], st[i << 1 | 1]);
  // O(lq(2N)), works like replacing arr[i] with val
 void update(int i, T val) {
   for (st[i += N] = val; i > 1; i >>= 1)
      st[i >> 1] = F(st[i], st[i ^ 1]);
  }
  // O(3N), [l, r]
  void update(int 1, int r, T val) {
   if (1 == r)
      update(1, val);
      for (1 += N, r += N; 1 <= r; 1++) st[1] = val;
      build();
   }
  }
  // O(lg(2N)), [l, r]
  T query(int 1, int r) {
   T ans = neutro;
   for (1 += N, r += N; 1 <= r; 1 >>= 1, r >>= 1) {
      if (1 \& 1) ans = F(ans, st[1++]);
      if (r \& 1) ans = F(ans, st[r--]);
   }
   return ans;
```

```
T& operator[](int i) { return st[i + N]; }
};
```

```
Segment Tree Lazy Propagation
// st = segment tree, st[1] = root, H = height of d
// u = updates, d = delayed updates
// neutro = operation neutral val
// e.g. for sum is 0, for multiplication
// is 1, for gcd is 0, for min is INF, etc.
template <class T>
struct SegmentTree {
  T neutro = 0;
  int N, H;
  vector<T> st, d;
  vector<bool> u;
  SegmentTree(int n, T val)
     : st(2 * n, val), d(n), u(n) {
   H = sizeof(int) * 8 - __builtin_clz(N = n);
  inline T kTimesF(T a, T k) {
   return a * k;
    // return pow(a, k);
    // return a;
  inline T F(T a, T b) {
   return a + b;
    // return a * b;
    // return __gcd(a, b);
    // return min(a, b);
  inline T UF(T a, T b) {
   return b; // replace update
    // return F(a, b); // apply F to current value
  void apply(int i, T val, int k) {
    st[i] = UF(st[i], kTimesF(val, k));
    if (i < N) d[i] = UF(d[i], val), u[i] = 1;</pre>
  }
  void calc(int i) {
   if (!u[i]) st[i] = F(st[i << 1], st[i << 1 | 1]);</pre>
  }
  // O(2N)
  void build() {
    for (int i = N - 1; i > 0; i--) calc(i);
  // O(lg(N))
  void build(int p) {
   while (p > 1) p >>= 1, calc(p);
```

```
// O(lq(N))
  void push(int p) {
    for (int s = H, k = 1 << (H - 1); s > 0;
         s--, k >>= 1) {
      int i = p >> s;
      if (u[i]) {
        apply(i \ll 1, d[i], k);
        apply(i << 1 | 1, d[i], k);
        u[i] = 0, d[i] = neutro;
      }
   }
  }
  // O(lg(N)), [l, r]
  void update(int 1, int r, T val) {
   push(1 += N);
   push(r += N);
   int ll = 1, rr = r, k = 1;
   for (; 1 <= r; 1 >>= 1, r >>= 1, k <<= 1) {
      if (1 & 1) apply(1++, val, k);
      if (~r & 1) apply(r--, val, k);
   }
   build(11);
   build(rr);
  // O(lg(2N)), [l, r]
  T query(int 1, int r) {
   push(1 += N);
   push(r += N);
   T ans = neutro;
   for (; 1 <= r; 1 >>= 1, r >>= 1) {
      if (1 & 1) ans = F(ans, st[1++]);
      if (-r \& 1) ans = F(ans, st[r--]);
   }
   return ans;
 T& operator[](int i) { return st[i + N]; }
};
```

Sparse Table

```
// st = sparse table, Arith = Arithmetic
typedef int T;
int neutro = 0;
vector<vector<T>>> st;

T F(T a, T b) {
    // return min(a, b);
    return __gcd(a, b);
    // return a + b; // Arith
    // return a * b; // Arith
}
```

```
// O(Nlq(N))
void build(vector<T> &arr) {
  st.assign(log2(arr.size()), vector<T>(arr.size()));
  st[0] = arr;
  for (int i = 1; (1 << i) <= arr.size(); i++)
    for (int j = 0; j + (1 << i) <= arr.size(); <math>j++)
      st[i][j] = F(st[i - 1][j],
                   st[i - 1][j + (1 << (i - 1))]);
}
// O(1), [l, r]
T query(int 1, int r) {
  int i = log2(r - 1 + 1);
  return F(st[i][l], st[i][r + 1 - (1 << i)]);
}
// O(lg(N)), [l, r]
T queryArith(int 1, int r) {
 T ans = neutro;
  while (true) {
    int k = log2(r - 1 + 1);
    ans = F(ans, st[k][1]);
    1 += 1 << k;
    if (1 > r) break;
  return ans;
}
```

Wavelet Tree

```
// pref = prefix sum
// lte = less than or equal, 1-indexed
// A = max element(from, to)
// lcount = left children count
struct WaveletTree {
  WaveletTree *1, *r;
  int lo, hi;
  vector<int> lcount, pref;
  // O(N*lq(A))
  WaveletTree(vector<int>::iterator from,
              vector<int>::iterator to, int lo,
              int hi) {
    this->lo = lo, this->hi = hi;
    if (lo == hi or from >= to) return;
    int mid = (lo + hi) >> 1;
    auto f = [mid](int x) { return x <= mid; };</pre>
    lcount.reserve(to - from + 1);
   pref.reserve(to - from + 1);
   lcount.push_back(0);
   pref.push_back(0);
    for (auto it = from; it != to; it++)
      lcount.push_back(lcount.back() + f(*it)),
          pref.push_back(pref.back() + *it);
    auto pivot = stable_partition(from, to, f);
    1 = new WaveletTree(from, pivot, lo, mid);
    r = new WaveletTree(pivot, to, mid + 1, hi);
```

```
// O(lg(A)) frequency of k in [a, b]
  int freq(int a, int b, int k) {
   if (a > b or k < lo or k > hi) return 0;
    if (lo == hi) return b - a + 1;
    int lc = lcount[a - 1], rc = lcount[b];
   if (k > ((lo + hi) >> 1))
      return r->freq(a - lc, b - rc, k);
   return l->freq(lc + 1, rc, k);
  // O(lg(A)) kth-Smallest element in [a, b]
  int kth(int a, int b, int k) {
    if (a > b) return 0;
   if (lo == hi) return lo;
    int lc = lcount[a - 1], rc = lcount[b],
        inleft = rc - lc;
   if (k > inleft)
     return r->kth(a - lc, b - rc, k - inleft);
   return l->kth(lc + 1, rc, k);
  }
  // O(lg(A)) count of elements <= to k in [a, b]
  int lte(int a, int b, int k) {
   if (a > b or k < lo) return 0;
   if (hi <= k) return b - a + 1;
   int lc = lcount[a - 1], rc = lcount[b];
   return l->lte(lc + 1, rc, k) +
           r->lte(a - lc, b - rc, k);
  // O(lq(A)) sum of numbers <= to k in [a, b]
  int sumlte(int a, int b, int k) {
   if (a > b or k < lo) return 0;
   if (hi <= k) return pref[b] - pref[a - 1];</pre>
    int lc = lcount[a - 1], rc = lcount[b];
   return l->sumlte(lc + 1, rc, k) +
           r->sumlte(a - lc, b - rc, k);
 }
};
```

Wavelet Tree Compressed

```
// lte = less than or equal, c = compressed
// o = original, O-indexed
#include "../../Techniques/Binary Search.cpp"
#include "Wavelet Tree.cpp"

template <class T>
struct WaveletTreeCompressed {
  unordered_map<int, T> imap;
  unordered_map<T, int> Map;
  WaveletTree* wt;
  vector<T> o;
```

```
// O(N*lq(N))
  WaveletTreeCompressed(vector<T>& v) {
    int inf = 1 << 30, n = 0, lo = inf, hi = -inf;
    set<T> s(v.begin(), v.end());
   vector<int> c(v.size());
   for (auto& e : s) Map[e] = n++;
    for (int i = 0; i < v.size(); i++)</pre>
      c[i] = Map[v[i]], imap[Map[v[i]]] = v[i];
    for (auto& e : c)
      lo = min(lo, e), hi = max(hi, e);
    wt = new WaveletTree(c.begin(), c.end(), lo, hi);
  // O(lg(N)) frequency of k in [a, b]
  int freq(int 1, int r, T k) {
   return wt->freq(++1, ++r, Map[k]);
  }
  // O(lg(N)) kth-Smallest element in [l, r]
  T kth(int 1, int r, int k) {
    return imap[wt->kth(++1, ++r, k)];
  // O(lg(N)) count of numbers <= to k in [l, r]
  T lte(int 1, int r, T k) {
    int kk = Map[bSearch < T > (o, k, l, r)[1]];
   return imap[wt->lte(++1, ++r, kk)];
  // O(lg(N)) sum of numbers <= to k in [l, r]
  T sumlte(int 1, int r, T k) {
    int kk = Map[bSearch<T>(o, k, l, r)[1]];
    return imap[wt->sumlte(++1, ++r, kk)];
  }
};
```

Strings

Suffix Automaton

```
// link[u]: links to the longest suffix which is
           not in the same endpos-equivalence class
//
// len[u]: length of the longest suffix that
//
           corresponds to u's endpos-equivalence class
struct SuffixAutomaton {
  vector<int> len, link, isClone, first;
  vector<map<char, int>> next;
  int size, last;
  void init(int n) {
    first = isClone = len = link = vector<int>(2 * n);
   next.resize(2 * n);
   len[0] = 0, link[0] = -1, size = 1, last = 0;
  }
  // O(N)
  SuffixAutomaton(const string& s) {
   init(s.size());
    for (const auto& c : s) add(c);
  }
```

```
// 0(1)
  void add(const char& c) {
    int p = last, u = size++;
    len[u] = len[p] + 1, first[u] = len[p];
    while (p != -1 \&\& !next[p].count(c))
      next[p][c] = u, p = link[p];
    if (p == -1) link[u] = 0;
    else {
      int q = next[p][c];
      if (len[p] + 1 == len[q]) link[u] = q;
      else {
        int clone = size++;
        first[clone] = first[q];
        len[clone] = len[p] + 1, isClone[clone] = 1;
        link[clone] = link[q], next[clone] = next[q];
        while (p != -1 \&\& next[p][c] == q)
          next[p][c] = clone, p = link[p];
        link[q] = link[u] = clone;
      }
    }
    last = u;
  }
  // O(N)
 unordered_set<int> getTerminals() {
    unordered_set<int> terminals;
    for (int p = last; p; p = link[p])
      terminals.insert(p);
    return terminals;
 }
};
Trie
// wpt = number of words passing through
// w = number of words ending in the node
// c = character
struct Trie {
  struct Node {
    // for lexicographical order use 'map'
    // map<char, Node *> ch;
    unordered_map<char, Node *> ch;
    int w = 0, wpt = 0;
 };
 Node *root = new Node();
  // O(STR.SIZE)
  void insert(string str) {
    Node *curr = root;
    for (auto &c : str) {
      if (!curr->ch.count(c))
        curr->ch[c] = new Node();
      curr->wpt++, curr = curr->ch[c];
    }
    curr->wpt++, curr->w++;
```

```
// O(STR.SIZE)
Node *find(string &str) {
 Node *curr = root;
  for (auto &c : str) {
    if (!curr->ch.count(c)) return nullptr;
    curr = curr->ch[c];
 return curr;
// O(STR.SIZE) number of words with given prefix
int prefixCount(string prefix) {
 Node *node = find(prefix);
 return node ? node->wpt : 0;
// O(STR.SIZE) number of words matching str
int strCount(string str) {
  Node *node = find(str);
  return node ? node->w : 0;
}
// O(N)
void getWords(Node *curr, vector<string> &words,
              string &word) {
  if (!curr) return;
 if (curr->w) words.push_back(word);
  for (auto &c : curr->ch) {
    getWords(c.second, words, word += c.first);
    word.pop_back();
 }
}
// O(N)
vector<string> getWords() {
 vector<string> words;
  string word = "";
  getWords(root, words, word);
 return words;
}
// O(N)
vector<string> getWordsByPrefix(string prefix) {
  vector<string> words;
  getWords(find(prefix), words, prefix);
}
// O(STR.SIZE)
bool remove(Node *curr, string &str, int &i) {
  if (i == str.size()) {
    curr->wpt--;
   return curr->w ? !(curr->w = 0) : 0;
  }
 int c = str[i];
  if (!curr->ch.count(c)) return false;
 if (remove(curr->ch[c], str, ++i)) {
    if (!curr->ch[c]->wpt)
      curr->wpt--, curr->ch.erase(c);
   return true;
  return false;
```

```
// O(STR.SIZE)
int remove(string str) {
  int i = 0;
  return remove(root, str, i);
}
};
```

Trees And Heaps

Red Black Tree

```
template <class K, class V>
struct RedBlackTree {
  struct Node {
    K key;
    V val;
    Node *1, *r; // left, right
    bool isRed;
    Node(K k, V v, bool isRed)
         : key(k), val(v), isRed(isRed) {}
 };
 Node *root = nullptr;
  int compare(K a, K b) {
    if (a < b) return -1;
    if (a > b) return 1;
    return 0;
  // O(lg(N))
  V at(K key) {
    Node *x = root;
    while (x) {
      int cmp = compare(key, x->key);
      if (!cmp) return x->val;
      if (cmp < 0) x = x->1;
      if (cmp > 0) x = x->r;
    }
    throw runtime_error("Key doesn't exist");
  }
 Node *rotateLeft(Node *h) {
    Node *x = h->r;
    h->r = x->1;
    x->1 = h;
    x\rightarrow isRed = h\rightarrow isRed;
    h\rightarrowisRed = 1;
    return x;
  Node *rotateRight(Node *h) {
    Node *x = h->1;
    h\rightarrow 1 = x\rightarrow r;
    x->r = h;
    x\rightarrow isRed = h\rightarrow isRed;
    h\rightarrow isRed = 1;
    return x;
  }
```

```
void flipColors(Node *h) {
                  h\rightarrow isRed = 1;
                  h\rightarrow 1\rightarrow isRed = 0;
                  h\rightarrow r\rightarrow isRed = 0;
          // O(lg(N))
          Node *insert(Node *h, K key, V val) {
                   if (!h) return new Node(key, val, 1);
                   int cmp = compare(key, h->key);
                   if (!cmp) h->val = val;
                    if (cmp < 0) h\rightarrow l = insert(h\rightarrow l, key, val);
                   if (cmp > 0) h\rightarrow r = insert(h\rightarrow r, key, val);
                   if (h->r && h->r->isRed && !(h->l && h->l->isRed))
                            h = rotateLeft(h);
                   if (h->1 & h->1->isRed & h->1->1 &
                                     h\rightarrow l\rightarrow l\rightarrow isRed
                            h = rotateRight(h);
                    if (h->1 && h->1->isRed && h->r && h->r->isRed)
                            flipColors(h);
                   return h;
          }
          // O(lq(N))
          void insert(K key, V val) {
                  root = insert(root, key, val);
};
```

Geometry

Max Interval Overlap

```
typedef long long int T;
typedef pair<T, T> Interval;
vector<Interval> maxIntervals;
```

```
// O(N * lg(N))
int maxOverlap(vector<Interval> &arr) {
 maxIntervals.clear();
 map<T, int> m;
 int maxI = 0, curr = 0, isFirst = 1;
 T l = -1LL, r = -1LL;
 for (auto &i : arr) m[i.first]++, m[i.second + 1]--;
 for (auto &p : m) {
   curr += p.second;
   if (curr > maxI) maxI = curr, l = p.first;
    if (curr == maxI) r = p.first;
 curr = 0;
 for (auto &p : m) {
   curr += p.second;
   if (curr == maxI && isFirst)
      l = p.first, isFirst = 0;
   if (curr < maxI && !isFirst)</pre>
      maxIntervals.push_back({1, p.first - 1}),
          isFirst = 1;
 }
 return maxI;
// O(MaxPoint) maxPoint < vector::max_size
int maxOverlap(vector<Interval> &arr) {
 maxIntervals.clear();
 T \text{ maxPoint} = 0;
 for (auto &i : arr)
    if (i.second > maxPoint) maxPoint = i.second;
 vector<int> x(maxPoint + 2);
 for (auto &i : arr) x[i.first]++, x[i.second + 1]--;
 int maxI = 0, curr = 0, isFirst = 1;
 T l = -1LL, r = -1LL;
 for (int i = 0; i < x.size(); i++) {</pre>
   curr += x[i];
    if (curr > maxI) maxI = curr;
 curr = 0;
 for (int i = 0; i < x.size(); i++) {</pre>
   curr += x[i];
    if (curr == maxI && isFirst) l = i, isFirst = 0;
   if (curr < maxI && !isFirst)</pre>
      maxIntervals.push_back({1, i - 1}), isFirst = 1;
 return maxI;
```

Graphs

Articulation Points And Bridges

```
// APB = articulation points and bridges
// Ap = Articulation Point
// br = bridges, p = parent
// disc = discovery time
// low = lowTime, ch = children
// nup = number of edges from u to p
typedef pair<int, int> Edge;
int Time;
vector<vector<int>> adj;
vector<int> disc, low, isAp;
vector<Edge> br;
void init(int N) { adj.assign(N, vector<int>()); }
void addEdge(int u, int v) {
  adj[u].push_back(v);
  adj[v].push_back(u);
int dfsAPB(int u, int p) {
  int ch = 0, nup = 0;
  low[u] = disc[u] = ++Time;
  for (int &v : adj[u]) {
    if (v == p && !nup++) continue;
    if (!disc[v]) {
      ch++, dfsAPB(v, u);
      if (disc[u] <= low[v]) isAp[u]++;</pre>
      if (disc[u] < low[v]) br.push_back({u, v});</pre>
      low[u] = min(low[u], low[v]);
      low[u] = min(low[u], disc[v]);
  }
  return ch;
}
// O(N)
void APB() {
  br.clear();
  isAp = low = disc = vector<int>(adj.size());
  for (int u = 0; u < adj.size(); u++)</pre>
    if (!disc[u]) isAp[u] = dfsAPB(u, u) > 1;
}
```

Connected Components

```
// comp = component
int compId;
vector<vector<int>> adj;
vector<int> getComp;
```

```
void init(int N) {
  adj.assign(N, vector<int>());
  getComp.assign(N, -1);
  compId = 0;
void addEdge(int u, int v) {
  adj[u].push back(v);
  adj[v].push_back(u);
void dfsCC(int u, vector<int> &comp) {
  if (getComp[u] > -1) return;
  getComp[u] = compId;
  comp.push_back(u);
  for (auto &v : adj[u]) dfsCC(v, comp);
// O(N)
vector<vector<int>>> connectedComponents() {
  vector<vector<int>> comps;
  for (int u = 0; u < adj.size(); u++) {
   vector<int> comp;
   dfsCC(u, comp);
   if (!comp.empty())
      comps.push_back(comp), compId++;
 }
 return comps;
```

Flood Fill

```
int n, m, oldColor = 0, color = 1;
vector<vector<int>> mat;
vector<vector<int>> movs = {
    \{1, 0\}, \{0, 1\}, \{-1, 0\}, \{0, -1\}\};
void floodFill(int i, int j) {
  if (i >= mat.size() || i < 0 ||</pre>
      j >= mat[i].size() || j < 0 ||</pre>
      mat[i][j] != oldColor)
    return;
 mat[i][j] = color;
  for (auto move : movs)
    floodFill(i + move[1], j + move[0]);
void floodFill() {
  for (int i = 0; i < n; i++)
    for (int j = 0; j < m; j++)
      if (mat[i][j] == oldColor) floodFill(i, j);
}
```

Heavy Light Decomposition

```
// p = parent;
#include "../Data Structures/Ranges/Segment Tree.cpp"
typedef int T;
vector<vector<int>> adj;
vector<int> p, heavy, depth, root, stPos, vals;
SegmentTree<T> st(0);
```

```
void init(int n) {
  adj.assign(n, vector<int>());
  heavy.assign(n, -1);
  vals.assign(n, 0);
  p = root = stPos = depth = heavy;
  st = SegmentTree<T>(n);
}
void addEdge(int u, int v, T val) {
  adj[u].push_back(v);
  p[v] = u, vals[v] = val;
T F(T a, T b) { return a + b; }
// O(N)
int dfs(int u) {
  int size = 1, maxSubtree = 0;
  for (int &v : adj[u]) {
    depth[v] = depth[u] + 1;
    int subtree = dfs(v);
    if (subtree > maxSubtree)
      heavy[u] = v, maxSubtree = subtree;
    size += subtree;
  }
  return size;
}
// O(N)
void initHeavyLight() {
  for (int i = 0; i < adj.size(); i++)</pre>
    if (p[i] < 0) dfs(i);</pre>
  for (int i = 0, pos = 0; i < adj.size(); i++)
    if (p[i] < 0 || heavy[p[i]] != i)</pre>
      for (int j = i; ~j; j = heavy[j]) {
        st.setValAt(vals[j], stPos[j] = pos++);
        root[j] = i;
      }
  st.build();
// O(lg^2 (N))
template <class Op>
void processPath(int u, int v, Op op) {
  for (; root[u] != root[v]; v = p[root[v]]) {
    if (depth[root[u]] > depth[root[v]]) swap(u, v);
    op(stPos[root[v]], stPos[v]);
  if (depth[u] > depth[v]) swap(u, v);
  // for values on edges
  if (u != v) op(stPos[u] + 1, stPos[v]);
  // for values on nodes
  // op(stPos[u], stPos[v]);
// O(lg^2 (N))
void update(int u, int v, T val) {
  processPath(u, v, [&val](int 1, int r) {
    st.update(1, r, val);
  });
}
```

T F(T a, T b) { return a.first < b.first ? a : b; }</pre>

```
// O(lg^2 (N))
                                                           void build() {
T query(int u, int v) {
                                                             st.assign(log2(tour.size()),
 T \text{ ans} = T();
                                                                        vector<T>(tour.size()));
  processPath(u, v, [&ans](int 1, int r) {
                                                             st[0] = tour;
                                                             for (int i = 1; (1 << i) <= tour.size(); i++)</pre>
    ans = F(ans, st.query(1, r));
  });
                                                               for (int j = 0; j + (1 << i) <= tour.size(); j++)
 return ans;
                                                                  st[i][j] = F(st[i - 1][j],
                                                                               st[i - 1][j + (1 << (i - 1))]);
                                                           }
                                                           void eulerTour(int u, int p, int h) {
Is Bipartite
                                                             first[u] = tour.size();
                                                             tour.push_back({h, u});
vector<vector<int>> adj;
                                                             for (int v : adj[u])
                                                               if (v != p) {
void init(int N) { adj.assign(N, vector<int>()); }
                                                                 eulerTour(v, u, h + 1);
void addEdge(int u, int v) {
                                                                 tour.push_back({h, u});
  adj[u].push_back(v);
  adj[v].push_back(u);
                                                           }
                                                           // O(N * lg(N))
// O(N)
                                                           void preprocess() {
bool isBipartite() {
                                                             tour.clear();
  vector<int> color(adj.size(), -1);
                                                             first.assign(adj.size(), -1);
  for (int s = 0; s < adj.size(); s++) {</pre>
                                                             vector<int> roots = {0};
    if (color[s] > -1) continue;
                                                             for (auto &root : roots) eulerTour(root, -1, 0);
    color[s] = 0;
                                                             build();
    queue<int> q;
                                                           }
    q.push(s);
    while (!q.empty()) {
                                                           // 0(1)
      int u = q.front();
                                                           int lca(int u, int v) {
      q.pop();
                                                             int l = min(first[u], first[v]);
      for (int &v : adj[u]) {
                                                             int r = max(first[u], first[v]);
        if (color[v] < 0)</pre>
                                                             int i = log2(r - 1 + 1);
          q.push(v), color[v] = !color[u];
                                                             return F(st[i][1], st[i][r + 1 - (1 << i)]).second;</pre>
        if (color[v] == color[u]) return false;
      }
    }
  }
                                                           MST Kruskal
  return true;
                                                           // N = number of nodes, Wedge = Weighted Edge
                                                           #include "../Data Structures/Graphs/UnionFind.cpp"
                                                           typedef int T;
LCA
                                                           typedef pair<int, int> Edge;
                                                           typedef pair<T, Edge> Wedge;
// st = sparse table, p = parent
                                                           vector<Wedge> Wedges;
typedef pair<int, int> T;
                                                           vector<Wedge> mst;
int neutro = 0;
                                                           UnionFind uf(0);
vector<vector<T>> st;
vector<int> first;
                                                           void init(int N) {
vector<T> tour;
                                                             mst.clear();
vector<vector<int>> adj;
                                                             Wedges.clear();
                                                             uf = UnionFind(N);
void init(int N) { adj.assign(N, vector<int>()); }
                                                           }
void addEdge(int u, int v) {
                                                           void addEdge(int u, int v, T w) {
  adj[u].push_back(v);
                                                             Wedges.push_back({w, {u, v}});
  adj[v].push_back(u);
                                                           }
```

```
T kruskal() {
  T cost = 0;
  sort(Wedges.begin(), Wedges.end());
  // reverse(Wedges.begin(), Wedges.end());
  for (Wedge &wedge : Wedges) {
    int u = wedge.second.first,
        v = wedge.second.second;
    if (!uf.areConnected(u, v))
        uf.join(u, v), mst.push_back(wedge),
            cost += wedge.first;
  }
  return cost;
}
```

MST Prim

```
// st = spanning tree, p = parent
// vis = visited, dist = distance
typedef int T;
typedef pair<int, int> Edge;
typedef pair<T, Edge> Wedge;
typedef pair<T, int> DistNode;
long long int inf = (111 << 62) - 1;
vector<vector<int>> adj;
unordered_map<int, unordered_map<int, T>> weight;
vector<int> p, vis;
vector<T> dist;
vector<vector<Wedge>> msts;
void init(int N) {
  adj.assign(N, vector<int>());
  p.assign(N, 0);
 vis.assign(N, 0);
 dist.assign(N, inf);
 weight.clear();
 msts.clear();
void addEdge(int u, int v, T w) {
  adj[u].push_back(v);
  weight[u][v] = w;
  adj[v].push_back(u);
  weight[v][u] = w;
```

```
// \sim O(E * log(V))
T prim(int s) {
  vector<Wedge> mst;
  vector<T> dist(adj.size(), inf);
  priority queue<DistNode> q;
  T cost = dist[s] = 0;
  q.push({0, s});
  while (q.size()) {
    pair<int, int> aux = q.top();
    int u = aux.second;
    q.pop();
    if (dist[u] < -aux.first) continue;</pre>
    vis[u] = 1, cost += dist[u];
    mst.push_back({dist[u], {p[u], u}});
    for (int &v : adj[u]) {
      T w = weight[u][v];
      if (!vis[v] && w < dist[v])</pre>
        q.push({-(dist[v] = w), v});
    }
  }
  msts.push_back(
      vector<Wedge>(mst.begin() + 1, mst.end()));
  return cost;
// O(V + E * log(V))
T prim() {
  T cost = 0;
  map<int, T> q;
  for (int i = 0; i < adj.size(); i++)</pre>
    if (!vis[i]) cost += prim(i);
  return cost;
}
```

Strongly Connected Components

```
// tv = top value from stack
// sccs = strongly connected components
// scc = strongly connected component
// disc = discovery time, low = low time
// s = stack, top = top index of the stack
int Time, top;
vector<vector<int>> adj, sccs;
vector<int> disc, low, s;

void init(int N) { adj.assign(N, vector<int>()); }

void addEdge(int u, int v) { adj[u].push_back(v); }
```

```
void dfsSCCS(int u) {
  if (disc[u]) return;
  low[u] = disc[u] = ++Time;
  s[++top] = u;
  for (int &v : adj[u])
    dfsSCCS(v), low[u] = min(low[u], low[v]);
  if (disc[u] == low[u]) {
    vector<int> scc;
    while (true) {
      int tv = s[top--];
      scc.push_back(tv);
      low[tv] = adj.size();
      if (tv == u) break;
    }
    sccs.push_back(scc);
}
// O(N)
void SCCS() {
  s = low = disc = vector<int>(adj.size());
 Time = 0, top = -1, sccs.clear();
 for (int u = 0; u < adj.size(); u++) dfsSCCS(u);</pre>
}
```

Topological Sort

```
// vis = visited
vector<vector<int>> adj;
vector<int> vis, toposorted;
void init(int N) {
  adj.assign(N, vector<int>());
  vis.assign(N, 0);
  toposorted.clear();
void addEdge(int u, int v) { adj[u].push_back(v); }
// returns false if there is a cycle
// O(N)
bool toposort(int u) {
  vis[u] = 1;
  for (auto &v : adj[u])
    if (v != u && vis[v] != 2 &&
        (vis[v] || !toposort(v)))
      return false;
  vis[u] = 2;
  toposorted.push_back(u);
  return true;
}
// O(N)
bool toposort() {
  for (int u = 0; u < adj.size(); u++)</pre>
    if (!vis[u] && !toposort(u)) return false;
  return true;
```

Topological Sort (All possible sorts)

```
// indeg0 = indegree 0
vector<int> vis, indegree, path;
vector<vector<int>> adj, toposorts;
deque<int> indeg0;
void init(int n) {
  adj.assign(n, vector<int>());
  vis.assign(n, 0);
  indegree = vis;
}
void addEdge(int u, int v) {
  adj[u].push_back(v);
  indegree[v]++;
}
// O(V!)
void dfs() {
  for (int i = 0; i < indeg0.size(); i++) {</pre>
    int u = indeg0.front();
    indeg0.pop_front();
    path.push_back(u);
    for (auto &v : adj[u])
      if (!--indegree[v]) indeg0.push_back(v);
    if (!indeg0.size()) toposorts.push_back(path);
    dfs();
    for (int v = adj[u].size() - 1; ~v; v--) {
      indegree[adj[u][v]]++;
      if (indeg0.back() == adj[u][v])
        indeg0.pop_back();
    indeg0.push_back(u);
    path.pop_back();
}
// O(V + V!)
void allToposorts() {
  for (int u = 0; u < adj.size(); u++)</pre>
    if (!indegree[u]) indeg0.push_back(u);
  dfs();
}
```

Topological Sort (lowest lexicographically)

Cycles

Get Some Cycles

```
// at least detects one cycle per component
vector<vector<int>> adj, cycles;
vector<int> vis, cycle;
bool flag = false, isDirected = false;
int root = -1;
```

```
void init(int N) {
  adj.assign(N, vector<int>());
 vis.assign(N, 0);
  cycles.clear();
 root = -1, flag = false;
void addEdge(int u, int v) {
  adj[u].push_back(v);
  if (!isDirected) adj[v].push_back(u);
// O(N)
bool hasCycle(int u, int prev) {
  vis[u] = 1;
  for (auto &v : adj[u]) {
    if (v == u || vis[v] == 2 ||
        (!isDirected && v == prev))
      continue;
    if (flag) {
      if (!vis[v]) hasCycle(v, u);
      continue;
    }
    if (vis[v] || hasCycle(v, u)) {
      if (root == -1) root = v, flag = true;
      cycle.push_back(u);
      if (root == u)
        flag = false, root = -1,
        cycles.push_back(cycle), cycle.clear();
    }
  }
  vis[u] = 2;
  return flag;
// O(N)
bool hasCycle() {
  for (int u = 0; u < adj.size(); u++)</pre>
    if (!vis[u]) cycle.clear(), hasCycle(u, -1);
  return cycles.size() > 0;
Has Cycle
vector<vector<int>> adj;
vector<int> vis;
bool isDirected = false;
```

```
vector<vector<int>> adj;
vector<int> vis;
bool isDirected = false;

void init(int N) {
   adj.assign(N, vector<int>());
   vis.assign(N, 0);
}

void addEdge(int u, int v) {
   adj[u].push_back(v);
   if (!isDirected) adj[v].push_back(u);
}
```

Flow

Max Flow Min Cut Dinic

```
// cap[a][b] = Capacity from a to b
// flow[a][b] = flow occupied from a to b
// level[a] = level in graph of node a
// iflow = initial flow, icap = initial capacity
// pathMinCap = capacity bottleneck for a path (s->t)
typedef int T;
vector<int> level;
vector<vector<int>> adj;
unordered_map<int, unordered_map<int, T>> cap, flow;
long long int inf = (111 << 62) - 1;
void init(int N) {
  adj.assign(N, vector<int>());
  cap.clear();
  flow.clear();
}
void addEdge(int u, int v, T icap, T iflow = 0) {
  cap[u][v] = icap;
  flow[u][v] += iflow;
  flow[v][u] -= iflow;
  adj[u].push_back(v);
  adj[v].push_back(u);
}
```

```
bool levelGraph(int s, int t) {
  level.assign(adj.size(), 0);
  level[s] = 1;
  queue<int> q;
  q.push(s);
  while (!q.empty()) {
    int u = q.front();
    q.pop();
    for (int &v : adj[u]) {
      if (!level[v] && flow[u][v] < cap[u][v]) {</pre>
        q.push(v);
        level[v] = level[u] + 1;
      }
    }
 }
 return level[t];
T blockingFlow(int u, int t, T pathMinCap) {
  if (u == t) return pathMinCap;
  for (int v : adj[u]) {
    T capLeft = cap[u][v] - flow[u][v];
    if (level[v] == (level[u] + 1) && capLeft > 0)
      if (T pathMaxFlow = blockingFlow(
          v, t, min(pathMinCap, capLeft))) {
        flow[u][v] += pathMaxFlow;
        flow[v][u] -= pathMaxFlow;
        return pathMaxFlow;
      }
 }
 return 0;
}
// O(E * V^2)
T maxFlowMinCut(int s, int t) {
  if (s == t) return inf;
 T \max Flow = 0;
  while (levelGraph(s, t))
    while (T flow = blockingFlow(s, t, inf))
      maxFlow += flow;
 return maxFlow;
}
```

Maximum Bipartite Matching

```
// mbm = maximum bipartite matching
#include "Max Flow Min Cut Dinic.cpp"

void addEdgeMBM(int u, int v) {
   addEdge(u += 2, v += 2, 1);
   addEdge(0, u, 1);
   addEdge(v, 1, 1);
}

// O(E * V^2)
T mbm() { return maxFlowMinCut(0, 1); }
```

ShortestPaths

0 - 1 BFS

```
// s = source
typedef int T;
long long int inf = (111 << 62) - 1;
vector<vector<int>> adj;
unordered_map<int, unordered_map<int, T>> weight;
void init(int N) {
  adj.assign(N, vector<int>());
  weight.clear();
}
void addEdge(int u, int v, T w, bool isDirected = 0) {
  adj[u].push_back(v);
  weight[u][v] = w;
  if (isDirected) return;
  adj[v].push_back(u);
  weight[v][u] = w;
}
// O(E)
vector<T> bfs(int s) {
  vector<T> dist(adj.size(), inf);
  dist[s] = 0;
  deque<int> q;
  q.push_front(s);
  while (q.size()) {
    int u = q.front();
    for (auto& v : adj[u]) {
      T d = dist[u] + weight[u][v];
      if (d < dist[v])</pre>
        weight[u][v] ? q.push_back(v)
                     : q.push_front(v);
    }
  }
  return dist;
}
```

Bellman Ford

```
// s = source
// returns {} if there is a negative weight cycle
typedef int T;
long long int inf = (111 << 62) - 1;
vector<vector<int>> adj;
unordered_map<int, unordered_map<int, T>> weight;
void init(int N) {
  adj.assign(N, vector<int>());
  weight.clear();
void addEdge(int u, int v, T w, bool isDirected = 0) {
  adj[u].push_back(v);
  weight[u][v] = w;
  if (isDirected) return;
  adj[v].push_back(u);
  weight[v][u] = w;
}
```

```
// O(V * E)
vector<T> bellmanFord(int s) {
  vector<T> dist(adj.size(), inf);
  dist[s] = 0;
  for (int i = 1; i <= adj.size(); i++)
     for (int u = 0; u < adj.size(); u++)
     for (auto &v : adj[u]) {
        T d = dist[u] + weight[u][v];
        if (dist[u] != inf && d < dist[v]) {
            if (i == adj.size()) return {};
                  dist[v] = d;
                  }
        }
     return dist;
}</pre>
```

Bellman Ford Fast

```
// s = source, its = iterations of node u
// returns {} if there is a negative weight cycle
typedef int T;
long long int inf = (111 << 62) - 1;
vector<vector<int>> adj;
unordered_map<int, unordered_map<int, T>> weight;
void init(int N) {
  adj.assign(N, vector<int>());
  weight.clear();
void addEdge(int u, int v, T w, bool isDirected = 0) {
  adj[u].push_back(v);
  weight[u][v] = w;
  if (isDirected) return;
  adj[v].push_back(u);
  weight[v][u] = w;
// O(V * E)
vector<T> bellmanFordFast(int s) {
  vector<T> dist(adj.size(), inf);
  vector<int> its(adj.size()), inqueue(adj.size());
  queue<int> q;
  q.push(s), dist[s] = 0, its[s] = 1;
  while (!q.empty()) {
    int u = q.front();
    q.pop(), inqueue[u] = 0;
    for (auto &v : adj[u]) {
      T d = dist[u] + weight[u][v];
      if (d < dist[v]) {</pre>
        dist[v] = d;
        if (!inqueue[v]++) q.push(v), its[v]++;
        if (its[v] == adj.size()) return {};
      }
    }
  }
 return dist;
```

Dijkstra

```
// s = source
typedef int T;
typedef pair<T, int> DistNode;
long long int inf = (111 << 62) - 1;
vector<vector<int>> adj;
unordered_map<int, unordered_map<int, T>> weight;
void init(int N) {
  adj.assign(N, vector<int>());
  weight.clear();
void addEdge(int u, int v, T w, bool isDirected = 0) {
  adj[u].push_back(v);
  weight[u][v] = w;
  if (isDirected) return;
  adj[v].push_back(u);
  weight[v][u] = w;
}
// \sim O(E * lq(V))
vector<T> dijkstra(int s) {
  vector<T> dist(adj.size(), inf);
  priority_queue<DistNode> q;
  q.push({0, s}), dist[s] = 0;
  while (q.size()) {
    DistNode top = q.top();
    q.pop();
    int u = top.second;
    if (dist[u] < -top.first) continue;</pre>
    for (int &v : adj[u]) {
      T d = dist[u] + weight[u][v];
      if (d < dist[v]) q.push({-(dist[v] = d), v});
  }
 return dist;
}
```

Floyd Warshall

```
// d = distance
typedef int T;
long long int inf = (111 << 62) - 1;
vector<vector<T>> d;

void init(int n) {
   d.assign(n, vector<T>(n, inf));
   for (int i = 0; i < n; i++) d[i][i] = 0;
}

void addEdge(int u, int v, T w, bool isDirected = 0) {
   d[u][v] = w;
   if (isDirected) return;
   d[v][u] = w;
}</pre>
```

```
// O(V^3)
void floydwarshall() {
  for (int k = 0; k < d.size(); k++)
    for (int u = 0; u < d.size(); u++)
      for (int v = 0; v < d.size(); v++)
        d[u][v] = min(d[u][v], d[u][k] + d[k][v]);
}</pre>
```

Shortest Path in Directed Acyclic Graph

```
// s = source
#include "../Topological Sort.cpp"
typedef int T;
long long int inf = (111 << 62) - 1;
unordered map<int, unordered map<int, T>> weight;
void init(int N) {
  adj.assign(N, vector<int>());
  vis.assign(N, 0);
  toposorted.clear();
  weight.clear();
void addEdge(int u, int v, int w) {
  adj[u].push_back(v);
  weight[u][v] = w;
// O(N)
vector<T> dagsssp(int s) {
  vector<T> dist(adj.size(), inf);
  dist[s] = 0;
 toposort(s);
  while (toposorted.size()) {
    int u = toposorted.back();
    toposorted.pop_back();
    for (auto &v : adj[u]) {
      T d = dist[u] + weight[u][v];
      if (d < dist[v]) dist[v] = d;</pre>
    }
 }
 return dist;
```

Maths

Matrix Operations

Addition

```
typedef int T;
typedef vector<vector<T>>> Matrix;

// O(N * M)

Matrix add(Matrix a, Matrix b) {
   Matrix ans(a.size(), vector<T>(a[0].size()));
   for (int i = 0; i < a.size(); i++)
      for (int j = 0; j < a[i].size(); j++)
        ans[i][j] = a[i][j] + b[i][j];
   return ans;
}</pre>
```

Multiplication

```
typedef int T;
typedef vector<vector<T>>> Matrix;

// O(N^3)

Matrix multiply(Matrix a, Matrix b) {
   if (a[0].size() != b.size()) return {};
   Matrix ans(a.size(), vector<T>(b[0].size()));
   for (int i = 0; i < a.size(); i++)
      for (int j = 0; j < b[i].size(); j++)
      for (int k = 0; k < b.size(); k++)
        ans[i][j] += a[i][k] * b[k][j];
   return ans;
}</pre>
```

Number Theory

Binary Exponentiation

```
typedef __int128_t lli;

lli binPow(lli a, lli p) {
    lli ans = 1LL;
    while (p) {
        if (p & 1LL) ans *= a;
        a *= a, p >>= 1LL;
    }
    return ans;
}
```

Divisibility Criterion

```
def divisorCriteria(n, lim):
   results = []
    tenElevated = 1
    for i in range(lim):
        \# remainder = pow(10, i, n)
        remainder = tenElevated % n
        negremainder = remainder - n
        if(remainder <= abs(negremainder)):</pre>
            results.append(remainder)
        else:
            results.append(negremainder)
        tenElevated *= 10
    return results
def testDivisibility(dividend, divisor,

→ divisor_criteria):
    dividend = str(dividend)
    addition = 0
    dividendSize = len(dividend)
    i = dividendSize - 1
    j = 0
    while j < dividendSize:</pre>
        addition += int(dividend[i]) *

    divisor_criteria[j]

        i -= 1
        j += 1
    return addition % divisor == 0
if __name__ == '__main__':
    dividend, divisor = map(int, input().split())
    divisor_criteria = divisorCriteria(divisor,
    → len(str(dividend)))
    print(divisor_criteria)
    print(testDivisibility(dividend, divisor,

→ divisor_criteria))
```

Divisors

```
// divs = divisors

typedef long long int li;
typedef vectorV;

// O(sqrt(N))

V getDivisors(li n) {
   V divs;
   for (li i = 1; i * i <= n; i++)
        if (!(n % i)) {
            divs.push_back(i);
            if (i * i != n) divs.push_back(n / i);
        }
   return divs;
}</pre>
```

Divisors Pollard Rho

```
// pf = primeFactors, divs = divisors
#include "../Primes/Prime Factorization Pollard
→ Rho.cpp"
typedef vectorV;
void divisors(Map &pf, V &divs, li ans, li p) {
  auto next = ++pf.find(p);
  int power = pf[p];
  for (li k = 0; k \le power; k++, ans *= p) {
    if (next == pf.end()) divs.push_back(ans);
    else divisors(pf, divs, ans, next->first);
}
// O(number of pf)
V getDivisors(li n) {
  Map pf = getPrimeFactors(n);
  V divs;
  divisors(pf, divs, 1, pf.begin()->first);
  return divs;
}
```

Euler's Phi

```
#include "../Primes/Prime Factorization Pollard

And Rho.cpp"

// #include "../Primes/Prime Factorization.cpp"

// counts the number of integers (Xi) between 1 and n

// which are coprime (gcd(Xi, n) = 1) to n

lli phi(lli n) {

if (isPrime(n)) return n - 1;

Map pf = getPrimeFactors(n);

for (auto &p : pf) n -= n / p.first;

return n;
}
```

Extended Euclidean

```
// r = remainder
typedef __int128_t lli;
// \gcd(a, b) = ax + by
vector<lli> extendedGCD(lli a, lli b) {
  if (a > 0 \&\& b == 0) return \{a, 1, 0\};
  lli x = 1, y, prevx, prevy = 1, q, r;
 while (true) {
   q = a / b, r = a - b * q;
   if (!r) break;
   a = b, b = r;
   x -= prevx * q;
   swap(x, prevx);
   y -= prevy * q;
   swap(y, prevy);
  // gcd = b, x = prevx, y = prevy
 return {b, prevx, prevy};
GCD
typedef __int128_t lli;
lli gcd(lli a, lli b) {
 return !b ? a : gcd(b, a % b);
// Iterative version
lli gcdI(lli a, lli b) {
 while (b) a \%= b, swap(a, b);
 return a;
```

LCM

```
#include "GCD.cpp"
int lcm(lli a, lli b) {
  int c = gcd(a, b);
  return c ? a / c * b : 0;
}
```

Modular Exponentiation

```
#include "./Modular Multiplication.cpp"

// O(lg(p))

lli pow(lli a, lli p, lli m) {
   a %= m;
   lli ans = 1;
   while (p) {
      if (p & 1LL) ans = multiply(ans, a, m);
      a = multiply(a, a, m), p >>= 1;
   }
   return ans;
}
```

Modular Multiplication

```
typedef __int128_t lli;

// O(lg(b))

lli multiply(lli a, lli b, lli m) {
    a %= m;
    lli ans = 0;
    while (b) {
        if (b & 1)
            ans += a, ans = (ans >= m ? ans - m : ans);
        b >>= 1, a <<= 1;
        a = (a >= m ? a - m : a);
    }
    return ans;
}
```

Modulo with negative numbers

```
typedef int T;

T mod(T a, T b) {
  if (a < 0 && b >= 0) return a % b + b;
  if (a >= 0 && b < 0) return -(a % b + b);
  return a % b;
}</pre>
```

Primes

Is Prime Miller Rabin

```
#include ".../Number Theory/Modular Exponentiation.cpp"
bool isPrime(lli p, int k = 20) {
  if (p == 2 || p == 3) return 1;
  if ((~p & 1) || p == 1) return 0;
  lli d = p - 1, phi = d, r = 0;
  while (^d \& 1) d >>= 1, r++;
  while (k--) {
    // set seed with: int main() { srand(time(0)); }
    lli a = 2 + \text{rand}() \% (p - 3); // [2, p - 2]
    lli e = pow(a, d, p), r2 = r;
    if (e == 1 || e == phi) continue;
    bool flag = 1;
    while (--r2) {
      e = multiply(e, e, p);
      if (e == 1) return 0;
     if (e == phi) {
       flag = 0;
        break;
    if (flag) return 0;
 return 1;
```

Prime Factorization

```
typedef long long int li;
// if li == __int128_t: use map<li, int> Map;
typedef unordered_map<li, int> Map;
// \sim O(sqrt(N) * lq(N))
Map getPrimeFactors(li n) {
 Map pf;
  while (~n & 1) pf[2]++, n >>= 1;
  for (li i = 3; i * i <= n; i += 2)
    while (!(n % i)) pf[i]++, n /= i;
  if (n > 1) pf[n]++;
 return pf;
```

Prime Factorization Pollard Rho

```
// pf = prime factors
#include "../Number Theory/GCD.cpp"
#include "./Is Prime Miller Rabin.cpp"
typedef long long int li;
// if li == __int128_t: use map<li, int> Map;
typedef unordered_map<li, int> Map;
li _abs(li a) { return a < 0 ? -a : a; }
li getRandomDivisor(li n) {
  if (~n & 1) return 2;
  li c = 1 + rand() % (n - 1), a = 2, b = 2, d = 1;
  auto f = [&](li x) {
   return (multiply(x, x, n) + c) % n;
  };
  while (d == 1)
    a = f(a), b = f(f(b)), d = gcd(abs(a - b), n);
  return d;
}
void getpf(li n, Map &pf) {
  if (n == 1LL) return;
  if (isPrime(n)) {
   pf[n]++;
   return;
  li divisor = getRandomDivisor(n);
  getpf(divisor, pf);
  getpf(n / divisor, pf);
}
// ~O(N^{(1/4)})
Map getPrimeFactors(li n) {
 Map pf;
  getpf(n, pf);
  return pf;
}
Prime Sieve
vector<int> sieve, primes;
// \sim O(N * lg(lg(N)))
void primeSieve(int n) {
  sieve.assign(n + 1, 0);
  primes = {};
  for (int i = 3; i * i <= n; i += 2)
    if (!sieve[i])
      for (int j = i * i; j \le n; j += 2 * i)
        if (!sieve[j]) sieve[j] = i;
  primes.push_back(2);
  for (int i = 3; i < n; i++)
    if (!sieve[i] && (i & 1)) primes.push_back(i);
}
```

Strings

Distinct Substring Count

```
#include "../Data Structures/Strings/Suffix
→ Automaton.cpp"
// O(N)
int distinctSubstrCount(const string& s) {
  SuffixAutomaton sa(s);
  vector<int> dp(sa.size);
 function \langle int(int) \rangle dfs = [&] (int u) {
    if (dp[u]) return dp[u];
    for (auto& v : sa.next[u]) dp[u] += dfs(v.second);
    return ++dp[u];
 };
 return dfs(0) - 1;
KMP
// p = pattern, t = text
// f = error function, cf = create error function
// pos = positions where pattern is found in text
int MAXN = 1000000;
vector<int> f(MAXN + 1);
vector<int> kmp(string &p, string &t, int cf) {
  vector<int> pos;
  if (cf) f[0] = -1;
  for (int i = cf, j = 0; j < t.size();) {</pre>
    while (i > -1 && p[i] != t[j]) i = f[i];
    i++, j++;
    if (cf) f[j] = i;
    if (!cf && i == p.size())
      pos.push_back(j - i), i = f[i];
 return pos;
vector<int> search(string &p, string &t) {
                    // create error function
 kmp(p, p, -1);
  return kmp(p, t, 0); // search in text
```

Lexicographically K-th Substring

```
#include "../Data Structures/Strings/Suffix
  Automaton.cpp"
// O(N * ks.size)
vector<string> kthSubstr(string& s, vector<int>& ks) {
  SuffixAutomaton sa(s);
  vector<int> dp(sa.size);
  function<int(int)> dfs = [&](int u) {
    if (dp[u]) return dp[u];
    for (auto& v : sa.next[u]) dp[u] += dfs(v.second);
    return ++dp[u];
  };
  dfs(0);
  vector<string> ans;
  for (auto k : ks) {
    int u = 0;
    string ss;
    while (k)
      for (auto& v : sa.next[u])
        if (k <= dp[v.second]) {</pre>
          ss += v.first, u = v.second, k--;
        } else
          k -= dp[v.second];
    ans.push_back(ss);
  return ans;
}
```

Lexicographically Smallest Cyclic Shift

```
#include "../Data Structures/Strings/Suffix
    Automaton.cpp"

// O(N)
string smallestCyclicShift(const string& s) {
    SuffixAutomaton sa(s + s);
    int k = s.size(), u = 0;
    string ans;
    while (k)
    for (auto& v : sa.next[u]) {
        ans += v.first, u = v.second, k--;
        break;
    }
    return ans;
}
```

Number of Ocurrences

```
// O(T * Lg(T) + p.size() * ps.size())
vector<int> nOcurrences(string& t,
                        vector<string>& ps) {
 SuffixAutomaton sa(t);
 vector<int> cnt(sa.size), aux(sa.size), ans;
 for (int u = 0; u < sa.size; aux[u] = u, u++)
    if (!sa.isClone[u]) cnt[u] = 1;
 sort(aux.begin(), aux.end(), [&](int& a, int& b) {
    return sa.len[b] < sa.len[a];</pre>
 });
 for (auto& u : aux)
    if (u) cnt[sa.link[u]] += cnt[u];
 for (auto& p : ps)
   for (int u = 0, i = 0; i < p.size(); i++) {
      if (!sa.next[u].count(p[i])) {
        ans.push_back(0);
        break;
     }
     u = sa.next[u][p[i]];
      if (i + 1 == p.size()) ans.push_back(cnt[u]);
 return ans;
```

Ocurrences Positions

```
// invLink = inverse suffix-link
#include "../Data Structures/Strings/Suffix
→ Automaton.cpp"
// O(T + OCURRENCES(ps[i]) * ps.size())
vector<vector<int>>> ocurrencesPos(
   string& t, vector<string>& ps) {
 SuffixAutomaton sa(t);
 vector<vector<int>> ans, invLink(sa.size);
 for (int u = 1; u < sa.size; u++)</pre>
   invLink[sa.link[u]].push_back(u);
 function<void(int, int, vector<int>&)> dfs =
      [&](int u, int pLen, vector<int>& oc) {
        if (!sa.isClone[u])
          oc.push_back(sa.first[u] - pLen + 1);
       for (auto& v : invLink[u]) dfs(v, pLen, oc);
      };
 for (auto& p : ps)
   for (int u = 0, i = 0; i < p.size(); i++) {
      if (!sa.next[u].count(p[i])) {
       ans.push_back({});
       break;
     u = sa.next[u][p[i]];
      if (i + 1 == p.size()) {
       vector<int> oc;
        dfs(u, p.size(), oc), ans.push_back(oc);
   }
 return ans;
```

Rabin Karp

```
class RollingHash {
 public:
  vector<unsigned long long int> pow;
  vector<unsigned long long int> hash;
  unsigned long long int B;
  RollingHash(const string &text) : B(257) {
    int N = text.size();
    pow.resize(N + 1);
   hash.resize(N + 1);
    pow[0] = 1;
   hash[0] = 0;
    for (int i = 1; i <= N; ++i) {
      // in c++ an unsigned long long int is
      // automatically modulated by 2^64
      pow[i] = pow[i - 1] * B;
      hash[i] = hash[i - 1] * B + text[i - 1];
   }
  }
  unsigned long long int getWordHash() {
    return hash[hash.size() - 1];
  unsigned long long int getSubstrHash(int begin,
    return hash[end] -
           hash[begin - 1] * pow[end - begin + 1];
  }
  int size() { return hash.size(); }
};
vector<int> rabinKarp(RollingHash &rhStr,
                      string &pattern) {
  vector<int> positions;
  RollingHash rhPattern(pattern);
  unsigned long long int patternHash =
      rhPattern.getWordHash();
  int windowSize = pattern.size(), end = windowSize;
  for (int i = 1; end < rhStr.size(); i++) {</pre>
    if (patternHash == rhStr.getSubstrHash(i, end))
      positions.push_back(i);
    end = i + windowSize;
  return positions;
}
```

Techniques

Binary Search

```
/* if e in v and lower = false (upper_bound):
 r = position of e in v
  l = r + 1
if e in v and lower = true (lower bound):
  l = position of e in v
  r = l - 1
if e not in v and inv = false it means that:
  v[r] < e < v[l]
if e not in v and inv = true it means that:
  v[r] > e > v[l] */
// O(lg(r - l)) [l, r]
template <class T>
vector<T> bSearch(vector<T> &v, T e, int l, int r,
                  bool lower = 0, bool inv = 0) {
  while (1 <= r) {
    int mid = 1 + (r - 1) / 2;
    if (e < v[mid])</pre>
      inv ? l = mid + 1 : r = mid - 1;
    else if (e > v[mid])
      inv ? r = mid - 1 : l = mid + 1;
   else
      lower ? r = mid - 1 : l = mid + 1;
  } // bSearch[0] tells if the element was found
 return {lower ? v[1] == e : v[r] == e, r, 1};
} // be aware that r can be < given l and l > given r
```

Bitonic Search

```
/* assumes that the bitonic point is the greastest
 * value in v*/
#include "Binary Search.cpp"
template <class T>
vector<vector<int>> bitonicSearch(vector<T> &v, T e) {
  int l = 0, r = v.size() - 1, mid;
  while (1 <= r) {
    mid = 1 + (r - 1) / 2;
    if (!mid || (mid >= v.size() - 1)) break;
    if (v[mid - 1] <= v[mid] && v[mid] > v[mid + 1])
      break:
    if (v[mid - 1] \leftarrow v[mid] & v[mid] \leftarrow v[mid + 1])
      l = mid + 1;
    if (v[mid - 1] > v[mid] && v[mid] > v[mid + 1])
      r = mid - 1;
  } // at the end of the loop mid = bitonic point
  return {
      bSearch<T>(v, e, 0, mid),
      bSearch<T>(v, e, mid, v.size() - 1, false,

    true)};
}
```

Multiple Queries

Mo

```
// q = query
// qs = queries
struct Query {
  int 1, r;
};
int blksize;
vector<Query> qs;
vector<int> arr;
void initVars(int N, int M) {
  arr = vector<int>(N);
  qs = vector<Query>(M);
}
bool cmp(Query &a, Query &b) {
  if (a.1 == b.1) return a.r < b.r;</pre>
  return a.l / blksize < b.l / blksize;</pre>
}
void getResults() {
  blksize = (int)sqrt(arr.size());
  sort(qs.begin(), qs.end(), cmp);
  int prevL = 0, prevR = -1;
  int sum = 0;
  for (auto &q : qs) {
    int L = q.1, R = q.r;
    while (prevL < L) {</pre>
      sum -= arr[prevL]; // problem specific
      prevL++;
    while (prevL > L) {
      prevL--;
      sum += arr[prevL]; // problem specific
    while (prevR < R) {</pre>
      prevR++;
      sum += arr[prevR]; // problem specific
    while (prevR > R) {
      sum -= arr[prevR]; // problem specific
      prevR--;
    cout << "sum[" << L << ", " << R << "] = " << sum
         << endl;</pre>
}
int main() {
  initVars(9, 2);
  arr = \{1, 1, 2, 1, 3, 4, 5, 2, 8\};
  qs = \{\{0, 8\}, \{3, 5\}\};
  getResults();
}
```

SQRT Decomposition

```
// sum of elements in range
int neutro = 0;
vector<int> arr;
vector<int> blks;
void initVars(int n) {
  arr.assign(n, neutro);
  blks.assign(sqrt(n), neutro);
void preprocess() {
  for (int i = 0, j = 0; i < arr.size(); i++) {
    if (i == blks.size() * j) j++;
    blks[j - 1] += arr[i]; // problem specific
  }
}
// problem specific
void update(int i, int val) {
 blks[i / blks.size()] += val - arr[i];
  arr[i] = val;
}
int query(int 1, int r) {
  int sum = 0;
  int lblk = 1 / blks.size();
  if (l != blks.size() * lblk++)
    while (1 < r && 1 != lblk * blks.size()) {</pre>
      sum += arr[1]; // problem specific
      1++;
    }
  while (l + blks.size() <= r) {</pre>
    sum += blks[l / blks.size()]; // problem specific
    l += blks.size();
  while (1 <= r) {
    sum += arr[1]; // problem specific
    1++;
  }
 return sum;
int main() {
  initVars(10);
  arr = \{1, 5, 2, 4, 6, 1, 3, 5, 7, 10\};
  preprocess();
  for (int i = 0; i < blks.size() + 1; i++)</pre>
    cout << blks[i] << " ";
  // output: 8 11 15 10
  cout << endl;</pre>
  cout << query(3, 8) << " ";</pre>
  cout << query(1, 6) << " ";
  update(8, 0);
  cout << query(8, 8) << endl;</pre>
  // output: 26 21 0
 return 0;
```

Problems Solved

Maths

N as Sum of different numbers from 1 to M

```
int main() {
  int t;
  scanf("%d", &t);
  for (int j = 1; j \le t; j++) {
    lli x;
    scanf("%lld", &x);
    lli count = 0;
    V divisors = getDivisors(2LL * x);
    for (auto &div : divisors) {
      double d =
          ((double)x / div) + ((1.00 - div) / 2.00);
      if (d > 0 && div > 1 && d == floor(d) &&
          div < x &&
          (2 * d * div + (div - 1) * div == 2 * x)) {
   }
   printf("case %d: %lld\n", j, count);
}
```

Extras

C++

Automatic Type Conversions

When performing operations with different primitive data types in C++, the operand with smaller rank gets converted to the data type of the operand with the greater rank.

Data Type Ranks			
Rank	Data Type		
1	bool		
2	char, signed char, unsigned char		
3	short int, unsigned short int		
4	int, unsigned int		
5	long int, unsigned long int		
6	long long int, unsigned long long int		
7	int128_t		
8	float		
9	double		
10	long double		

 $Source: \ https://en.cppreference.com/w/c/language/conversion$

Integer Types Properties

Properties			
Width in bits	Data Type		
8	bool		
At least 8	char, signed char, unsigned char		
At least 16	short int, unsigned short int		
At least 16	int, unsigned int		
At least 32	long int, unsigned long int		
At least 64	long long int, unsigned long long int		
128	int128_t		

Sources:

https://en.cppreference.com/w/cpp/language/types

https://www.geeksforgeeks.org/c-data-types/

https://stackoverflow.com/questions/2064550/c-why-bool-is-8-bits-long

Data Structures

Strings

Suffix Automaton

ullet Each node u corresponds to an endpos-equivalence class for which its longest suffix corresponds to the path from root to u.

Maths

Common Sums

$\sum_{k=0}^{n} k = \frac{n(n+1)}{2}$	$\sum_{k=0}^{n} k^2 = \frac{n(n+1)(2n+1)}{6}$	$\sum_{k=0}^{n} k^3 = \frac{n^2(n+1)^2}{4}$
$\sum_{k=0}^{n} k^4 = \frac{n}{30}(n+1)(n+1)(n+1)(n+1)(n+1)(n+1)(n+1)(n+1)$	$\sum_{k=0}^{n} a^k = \frac{1 - a^{n+1}}{1 - a}$	
$\sum_{k=0}^{n} ka^{k} = \frac{a[1 - (n+1)a^{n} + na^{n+1}]}{(1-a)^{2}}$	$\sum_{k=0}^{n} k^2 a^k = \frac{a[(1+a)-(n+1)^2 a^n + (2n^2+2n-1)a^{n+1} - n^2 a^{n+2}]}{(1-a)^3}$	
$\sum_{k=0}^{\infty} a^k = \frac{1}{1-a}, a < 1$	$\sum_{k=0}^{\infty} k a^k = \frac{a}{(1-a)^2}, a < 1$	$\sum_{k=0}^{\infty} k^2 a^k = \frac{a^2 + a}{(1-a)^3}, a < 1$
$\sum_{k=0}^{\infty} \frac{1}{a^k} = \frac{a}{a-1}, a > 1$	$\sum_{k=0}^{\infty} \frac{k}{a^k} = \frac{a}{(a-1)^2}, a > 1$	$\sum_{k=0}^{\infty} \frac{k^2}{a^k} = \frac{a^2 + a}{(a-1)^3}, a > 1$
$\sum_{k=0}^{\infty} \frac{a^k}{k!} = e^a$	$\sum_{k=0}^{n} \binom{n}{k} = 2^n$	$\sum_{k=0}^{n} \binom{k}{m} = \binom{n+1}{m+1}$

Logarithm Rules

$\log_b(b^k) = k$	$\log_b(1) = 0$	$\log_b(X) = \frac{\log_c(X)}{\log_c(b)}$
$\log_b(X \cdot Y) = \log_b(X) + \log_b(Y)$	$\log_b(\frac{X}{Y}) = \log_b(X) - \log_b(Y)$	$\log_b(X^k) = k \cdot \log_b(X)$