# ACM-ICPC-REFERENCE

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### 1 Strings

#### 1.1 trie

```
#include<bits/stdc++.h>
using namespace std;
class Trie {
private:
    class TrieNode {
    public:
        unordered_map<char, TrieNode*> children;
        // map<char, TrieNode*> children;
        bool endOfWord:
        int numberOfWords:
        TrieNode() {
            this->numberOfWords = 0;
            this->endOfWord = false;
        }
        ~TrieNode() {
            unordered_map<char, TrieNode*> thisNodeChildren =
            unordered_map<char, TrieNode*>::iterator i =

    thisNodeChildren.begin();

            // map<char, TrieNode*> thisNodeChildren = this->children;
            // map<char, TrieNode*>::iterator i =

    thisNodeChildren.begin();

            while (i != thisNodeChildren.end()) {
                delete i->second;
                i++;
            }
            thisNodeChildren.clear();
        }
    };
private:
    TrieNode* root = nullptr;
public:
    Trie() {
        root = new TrieNode();
    ~Trie() {
        delete root;
    void insert(string &word) {
        TrieNode *current = this->root;
```

```
current->numberOfWords++;
        for (int i = 0; i < word.size(); i++) {</pre>
            char symbol = word[i];
            if (current->children.count(symbol) == 0)
                current->children[symbol] = new TrieNode();
            current = current->children[symbol];
            current->numberOfWords++;
        current->endOfWord = true;
    bool find(string &word) {
        TrieNode *current = this->root;
        for (int i = 0; i < word.size(); i++) {</pre>
            char symbol = word[i];
            if (current->children.count(symbol) == 0)
                return false;
            current = current->children[symbol];
        return current->endOfWord;
    }
private:
    bool deleteWord(TrieNode *current, string &word, int &index) {
        if (index == word.size()) {
            if (!current->endOfWord)
                return false;
            current->endOfWord = false;
            return current->children.size() == 0;
        char symbol = word[index];
        if (current->children.count(symbol) == 0)
            return false;
        bool shouldDeleteChild = deleteWord(current->children[symbol],
        \rightarrow word, index += 1);
        if (shouldDeleteChild) {
            current->children.erase(symbol);
            return current->children.size() == 0;
        return false;
    }
    void getWords(TrieNode* node, vector<string> &words, string &word) {
        if (node->endOfWord)
            words.push_back(word);
```

```
for (auto i : node->children) {
            getWords(i.second, words, word += i.first);
            word.pop_back();
        }
public:
    void deleteWord(string &word) {
        int index = 0;
        deleteWord(this->root, word, index);
    vector<string> getWords() {
        vector<string> words;
        string word = "";
        getWords(this->root, words, word);
        return words;
    vector<string> getWords(string &prefix) {
        vector<string> words;
        TrieNode *current = this->root;
        for (int i = 0; i < prefix.size(); i++) {</pre>
            if (current->children.count(prefix[i]) == 0)
                return words:
            current = current->children[prefix[i]];
        bool prevState = current->endOfWord;
        current->endOfWord = false;
        getWords(current, words, prefix);
        current->endOfWord = prevState;
        return words;
};
void printv(vector<string> v) {
    if (v.size() == 0) {
        cout << "[]" << endl;
        return;
    cout << "[" << v[0]:
    for (int i = 1; i < v.size(); i++) {</pre>
        cout << ", " << v[i];
    cout << "]" << endl;
```

```
int main() {
    std::ios_base::sync_with_stdio(0);
    int n, k;
    Trie *tr = new Trie();
    cin >> n:
    for (int i = 0; i < n; i++) {</pre>
        string aux;
        cin >> aux;
        tr->insert(aux);
    }
    cin >> k;
    for (int j = 0; j < k; j++) {
        string str;
        cin >> str;
        cout << "Case #" << j + 1 << ":" << '\n';
        printv(tr->getWords(str));
    }
    cin >> k;
    for (int j = 0; j < k; j++) {
        string str;
        cin >> str;
        tr->deleteWord(str);
        printv(tr->getWords());
    }
    delete tr;
    return 0;
}
1.2 kmp
#include <bits/stdc++.h>
using namespace std;
vector<int> prefixArray(string& pattern) {
    vector<int> prefixArr(pattern.size());
    for (int i = 0, j = 1; j < pattern.size();)</pre>
        if (pattern[i] == pattern[j])
        {
```

```
i++;
            prefixArr[j] = i;
            j++;
        } else {
            if (i != 0)
                i = prefixArr[i - 1];
            else {
                prefixArr[j] = 0;
                j++;
            }
        }
    return prefixArr;
vector<int> kmp(string& str, string& pattern) {
    vector<int> positions;
    if (pattern.size() == 0)
        return positions;
    vector<int> prefixArr = prefixArray(pattern);
    for (int i = 0, j = 0; j < str.size();) {</pre>
        if (pattern[i] == str[j]) {
            j++;
            i++;
        } else {
            if (i != 0) {
                i = prefixArr[i - 1];
            } else {
                j++;
            }
        }
        if (i == pattern.size()) {
            positions.push_back(j + 1 - pattern.size());
            i = prefixArr[i - 1];
        }
    return positions;
}
int main() {
    int t;
    cin >> t:
    for (int i = 0; i < t; i++) {</pre>
        string str, pattern;
        cin >> str >> pattern;
        vector<int> positions = kmp(str, pattern);
```

```
if (positions.size() == 0) {
             cout << "Not Found" << "\n\n";</pre>
             continue;
        cout << positions.size() << '\n';</pre>
        for (int j = 0; j < positions.size(); j++) {</pre>
             cout << positions[j] << " ";</pre>
        cout << "\n\n";
    return 0;
1.3 rabinKarp
#include <iostream>
#include <stdio.h>
#include <vector>
using namespace std;
class RollingHash {
public:
    vector <unsigned long long int> pow;
    vector <unsigned long long int> hash;
    unsigned long long int B;
    RollingHash(const string &str) : B(257) {
        int N = str.size();
        pow.resize(N + 1);
        hash.resize(N + 1);
        pow[0] = 1;
        hash[0] = 0;
        for (int i = 1; i <= N; ++i) {</pre>
            // in c++ an unsigned long long int is automatically modulated
             \rightarrow by 2<sup>64</sup>
            pow[i] = pow[i - 1] * B;
            hash[i] = hash[i - 1] * B + str[i - 1];
    }
    unsigned long long int getWordHash() {
        return hash[hash.size() - 1];
    }
```

```
unsigned long long int getSubstrHash(int begin, int end) {
        return hash[end] - hash[begin - 1] * pow[end - begin + 1];
    int size() {
        return hash.size();
};
vector<int> rabinKarp(RollingHash &rhStr, string &pattern) {
    vector<int> positions;
    RollingHash rhPattern(pattern);
    unsigned long long int patternHash = rhPattern.getWordHash();
    int windowSize = pattern.size(), end = windowSize;
    for (int i = 1; end < rhStr.size(); i++) {</pre>
        if (patternHash == rhStr.getSubstrHash(i, end))
            positions.push_back(i);
        end = i + windowSize;
    return positions;
}
int main() {
    int t;
    cin >> t:
    for (int i = 0; i < t; i++) {</pre>
        string str, pattern;
        cin >> str;
        RollingHash rhStr(str);
        int k;
        cin >> k;
        for (int 1 = 0; 1 < k; ++1)
            cin >> pattern;
            vector<int> positions = rabinKarp(rhStr, pattern);
             if (positions.size() == 0) {
                cout << "Not Found" << "\n\n";</pre>
                continue;
            cout << positions.size() << '\n';</pre>
            for (int j = 0; j < positions.size(); j++) {</pre>
                cout << positions[j] << " ";</pre>
            }
             cout << "\n\n";
        }
```

```
}
return 0;
}
```

## 2 Graphs

#### 2.1 GraphAPI

```
#include <bits/stdc++.h>
using namespace std;
double INF = 1 << 30;
template <class T> class Edge {
public:
   T v, w;
    double weight;
    Edge(T v, T w, double weight = 0) {
        this->v = v;
        this->w = w;
        this->weight = weight;
   }
};
template <class T> class Graph {
public:
    //node -> value , neighbors -> value, weight
    unordered_map<T, unordered_map<T, double> > nodes;
    bool isDirectedGraph;
    vector<Edge<T>> edges;
    // 0 -> undirected, 1 -> directed
    Graph(bool isDirectedGraph = false) {
        this->isDirectedGraph = isDirectedGraph;
    }
    unordered_map<T, unordered_map<T, double> > getNodes() {
        return this->nodes;
    }
    bool hasNode(T node) {
        return this->nodes.count(node);
    }
```

```
#include "indexedPriorityQueue.h"
    void addNode(T newNode) {
                                                                               using namespace std;
        if (!hasNode(newNode))
            this->nodes[newNode];
                                                                               typedef int T;
    }
                                                                               void dijkstra(Graph<T> &g, unordered_map<T, double> &distances,
    T nextNode() {

    unordered_map<T, T> &parents, T source) {

        return this->nodes.begin()->first;
                                                                                    indexedPriorityQueue<T> ipq;
                                                                                    for (auto node : g.nodes) {
                                                                                        ipq.push(node.first, INF);
    vector<Edge<T>> getEdges() {
        return this->edges;
                                                                                    ipq.update(source, 0);
                                                                                    distances[source] = 0;
                                                                                    parents[source] = source;
    bool hasEdge(T v, T w) {
                                                                                    while (!ipq.empty()) {
        return this->nodes.count(v) ? this->nodes[v].count(w) : false;
                                                                                        auto current = ipq.pop();
                                                                                        distances[current.first] = current.second;
    }
                                                                                        for (auto neighbor : g.nodes[current.first]) {
                                                                                            if (!ipq.containsKey(neighbor.first))
    double getEdgeWeight(T v, T w) {
        if (hasEdge(v, w))
                                                                                                continue;
                                                                                            double newDistance = distances[current.first] +
            return this->nodes[v][w];
                                                                                            → neighbor.second;
        return INF:
    }
                                                                                            if (ipq.getWeight(neighbor.first) > newDistance) {
                                                                                                ipq.update(neighbor.first, newDistance);
    void addOrUpdateEdge(T v, T w, double cost = 0) {
                                                                                                parents[neighbor.first] = current.first;
        if (!hasNode(v)) addNode(v);
                                                                                        }
        if (!hasNode(w)) addNode(w);
                                                                                   }
        this->nodes[v][w] = cost;
                                                                               }
        this->edges.push_back(Edge<T>(v, w, cost));
        if (isDirectedGraph)
                                                                               int main() {
            return:
        this->nodes[w][v] = cost;
                                                                                    int Te;
        this->edges.push_back(Edge<T>(w, v, cost));
                                                                                    cin >> Te;
                                                                                    for (int 1 = 1; 1 <= Te; 1++) {
                                                                                        int n, m, s, t, a, b;
    void printEdges() {
                                                                                        double w;
        for (auto edge : this->edges)
                                                                                        cin >> n >> m >> s >> t;
            cout << edge.v << " " << edge.w << " " << edge.weight << endl;</pre>
                                                                                        Graph < T > g(0);
    }
                                                                                        while (m--) {
                                                                                            cin >> a >> b >> w:
                                                                                            g.addOrUpdateEdge(a, b, w < g.getEdgeWeight(a, b) ? w :</pre>

    g.getEdgeWeight(a, b));

     dijkstra
                                                                                        cout << "Case #" << 1 << ": ";
// uva 10986 - Sending email
                                                                                        unordered_map<T, double> distances;
#include <bits/stdc++.h>
```

};

#include "graphAPI.h"

```
unordered_map<T, T> parents;
                                                                                      vector<T> component;
       dijkstra(g, distances, parents, s);
                                                                                      dfsCC(g, component, nodeComponentIds, visited, node.first,
       if (!distances.count(t)) {

→ componentId);

           cout << "unreachable" << endl;</pre>
                                                                                      connectedComponents.push_back(component);
           continue;
                                                                                      componentId++;
       }
                                                                              return {connectedComponents, nodeComponentIds};
                                                                          }
       if (distances[t] == INF) {
           cout << "unreachable" << endl;</pre>
                                                                          string input() {
           continue:
       }
                                                                              string str;
                                                                              getline(cin, str);
       cout << distances[t] << endl;</pre>
                                                                              return str;
                                                                          }
   return 0;
                                                                          int main() {
                                                                              int t;
                                                                              t = stoi(input());
    connectedComponents
                                                                              input();
                                                                              while (t--) {
// uva 459 - graph connectivity
                                                                                  Graph<T> g;
#include <bits/stdc++.h>
                                                                                  string highest;
#include "graphAPI.h"
                                                                                  highest = input();
using namespace std;
                                                                                  for (T i = highest[0]; i >= 'A'; i--)
                                                                                      g.addNode(i);
typedef char T;
                                                                                  while (true) {
                                                                                      string edge = input();
void dfsCC(Graph<T> &g, vector<T> &component, unordered_map<T, int>
                                                                                      if (edge == "")
break;
g.addOrUpdateEdge(edge[0], edge[1]);
   visited.insert(actualNodeId);
   nodeComponentIds[actualNodeId] = componentId;
                                                                                  pair<vector<T>>, unordered_map<T, int>> connectedComponents
   component.push_back(actualNodeId);
                                                                                  for (auto neighbor : g.nodes[actualNodeId])
                                                                                  cout << connectedComponents.first.size() << endl;</pre>
       if (!visited.count(neighbor.first))
                                                                                  if (t != 0)
           dfsCC(g, component, nodeComponentIds, visited, neighbor.first,
                                                                                      cout << endl;</pre>

    componentId);
                                                                              }
                                                                              return 0;
                                                                          }
pair<vector<T>>, unordered_map<T, int>>

    getConnectedComponents(Graph<T> &g) {
   unordered_map<T, int> nodeComponentIds;
                                                                          2.4 cycleInUndirectedGraph
   vector<vector<T>> connectedComponents;
   unordered_set<T> visited;
                                                                          #include <bits/stdc++.h>
                                                                          #include "graphAPI.h"
   int componentId = 1;
   for (auto node : g.nodes)
                                                                          using namespace std;
       if (!visited.count(node.first)) {
```

```
typedef int T;
                                                                               #include "graphAPI.h"
                                                                               using namespace std;
bool hasUndirectedCycle(Graph<T> &g, T node, T prevNode, unordered_set<T>
typedef int T;
    visited.insert(node);
    for (auto neighbor : g.nodes[node]) {
                                                                               bool bellmanFord(Graph<T> &g, unordered_map<T, double> &distances,
        T v = neighbor.first;

    unordered_map<T, T> &parents, T source) {

        if (v == node || v == prevNode)
                                                                                   queue<T> q;
            continue;
                                                                                   unordered_set<T> in_queue;
        if (visited.count(v))
                                                                                   unordered_map<T, int> ocurrenceOfNodeInQueue;
                                                                                   for (auto node : g.nodes) {
            return true;
        if (hasUndirectedCycle(g, v, node, visited))
                                                                                       distances[node.first] = INF;
                                                                                       parents[node.first] = node.first;
            return true;
                                                                                   distances[source] = 0;
    return false;
}
                                                                                   q.push(source);
                                                                                   int limit = g.nodes.size() - 1;
bool hasUndirectedCycle(Graph<T> &g) {
                                                                                   in_queue.insert(source);
                                                                                   ocurrenceOfNodeInQueue[source] += 1;
    unordered_set<T> visited;
                                                                                   while (!q.empty()) {
    for (auto node : g.nodes) {
        T u = node.first:
                                                                                       T u = q.front(); q.pop(); in_queue.erase(u);
        if (!visited.count(u))
                                                                                       for (auto neighbor : g.nodes[u]) {
            if (hasUndirectedCycle(g, u, u, visited))
                                                                                           T v = neighbor.first;
                                                                                           double newDistance = distances[u] + neighbor.second;
                return true:
    }
                                                                                           if (newDistance < distances[v]) {</pre>
                                                                                               distances[v] = newDistance:
    return false;
}
                                                                                               parents[v] = u;
                                                                                               if (!in_queue.count(v)) {
int main() {
                                                                                                   q.push(v);
    Graph<int> g(0);
                                                                                                   ocurrenceOfNodeInQueue[v] += 1;
                                                                                                   if (ocurrenceOfNodeInQueue[v] > limit)
    int n, m, u , v;
    cin >> n >> m;
                                                                                                        return false;
                                                                                               }
    while (n--)
        g.addOrUpdateEdge(n + 1, n + 1);
                                                                                           }
                                                                                       }
    while (m--) {
                                                                                   }
        cin >> u >> v;
        g.addOrUpdateEdge(u, v);
                                                                                   return true;
                                                                               }
    cout << (hasUndirectedCycle(g) ? "cycle" : "no cycle") << endl;</pre>
    return 0:
                                                                               int main() {
}
                                                                                   int T:
                                                                                   cin >> T;
                                                                                   while (T--) {
     bellmanFord
                                                                                       unordered_map<int, double> distances;
                                                                                       unordered_map<int, int> parents;
// uva 558 - Wormholes
#include <bits/stdc++.h>
```

```
Graph<int> g(1);
                                                                                             if (visitedTime[node] <= lowTime[v])</pre>
                                                                                                 isArticulationPoint = true:
        int n, m, x, y, t;
        cin >> n >> m;
                                                                                             else
        while (m--) {
                                                                                                 lowTime[node] = min(lowTime[node], lowTime[v]);
            cin >> x >> y >> t;
                                                                                         } else
            g.addOrUpdateEdge(x, y, t);
                                                                                             lowTime[node] = min(lowTime[node], visitedTime[v]);
        }
                                                                                    }
        if (!bellmanFord(g, distances, parents, 0))
                                                                                     bool isRootNode = parent[node] == node;
            cout << "possible" << endl;</pre>
                                                                                     if ((isRootNode && childCount > 1) || (!isRootNode &&
                                                                                     → isArticulationPoint))
        else
            cout << "not possible" << endl;</pre>
                                                                                         articulationPoints.push_back(node);
    }
                                                                                }
                                                                                vector<T> getArticulationPoints(Graph<T> &g) {
    return 0;
                                                                                     unordered_set<T> visited;
                                                                                     vector<T> articulationPoints;
                                                                                     unordered_map<T, int> visitedTime, lowTime;
     articulation Points
                                                                                     unordered_map<T, T> parent;
                                                                                    T startNode = g.nodes.begin()->first;
// uva 315 - Network
                                                                                     parent[startNode] = startNode;
#include <bits/stdc++.h>
                                                                                     int time = 0;
#include "graphAPI.h"
                                                                                     dfsArticulationPoints(g, startNode, time, visitedTime, lowTime,
using namespace std;

→ articulationPoints, parent, visited);
                                                                                    return articulationPoints;
typedef int T;
                                                                                }
void dfsArticulationPoints(Graph<T> &g, T &node, int &time,
                                                                                vector<string> split(string str, char token) {
                            unordered_map<T, int> &visitedTime,
                                                                                     stringstream test(str);

    unordered_map<T, int> &lowTime,

                                                                                     string segment;
                            vector<T> &articulationPoints, unordered_map<T,</pre>
                                                                                     vector<std::string> seglist;
                            \rightarrow T> &parent,
                            unordered set<T> &visited) {
                                                                                     while (std::getline(test, segment, token))
    visited.insert(node):
                                                                                         seglist.push_back(segment);
    visitedTime[node] = time;
                                                                                    return seglist;
    lowTime[node] = time;
                                                                                }
    time++;
    int childCount = 0;
                                                                                string input() {
    bool isArticulationPoint = false;
                                                                                     string ans;
    for (const auto &neighbor : g.nodes[node]) {
                                                                                     cin >> ws;
        T v = neighbor.first;
                                                                                     getline(cin, ans);
        if (v == parent[node])
                                                                                    return ans;
            continue;
                                                                                }
        if (!visited.count(v)) {
            parent[v] = node;
                                                                                int main() {
            childCount++;
                                                                                     int N;
            dfsArticulationPoints(g, v, time, visitedTime, lowTime,
            → articulationPoints, parent, visited);
```

```
while (true) {
        N = stoi(input());
        if (!N)
                                                                                    return minCost;
                                                                                }
            return 0;
        Graph < T > g(0);
        string line;
                                                                                void printv(vector<Edge<T>> v) {
        while (true) {
                                                                                     if (v.size() == 0) {
            line = input();
                                                                                         cout << "" << endl;
            if (line == "0")
                                                                                         return:
                break:
            vector<string> nodes = split(line, ' ');
                                                                                     for (int i = 0; i < v.size(); i++) {</pre>
                                                                                         cout << v[i].v << " " << v[i].w << " " << v[i].weight << endl;</pre>
            T u = stoi(nodes[0]);
            for (int i = 1; i < nodes.size(); i++)</pre>
                                                                                }
                g.addOrUpdateEdge(u, stoi(nodes[i]));
        }
                                                                                int main() {
        cout << getArticulationPoints(g).size() << endl;</pre>
                                                                                     int i;
                                                                                     int t = 0;
    return 0;
}
                                                                                     while (cin >> i) {
                                                                                         if (t != 0)
                                                                                             cout << endl;</pre>
     kruskalMST
2.7
                                                                                         Graph < T > g(0);
                                                                                         int a, b, cost;
// uva 908 - Re-connecting computer sites
                                                                                         i--;
#include <bits/stdc++.h>
                                                                                         while (i--) {
#include "graphAPI.h"
                                                                                             cin >> a >> b >> cost:
#include "unionFind.cpp"
                                                                                             g.addOrUpdateEdge(a, b, cost);
using namespace std;
                                                                                         vector<Edge<T>> mst1;
typedef int T;
                                                                                         cout << kruskalMST(g, mst1) << endl;</pre>
                                                                                         Graph<T> g2(0);
double kruskalMST(Graph<T> &g, vector<Edge<T>> &mst) {
                                                                                         cin >> i;
    //mst = minimum spanning tree
                                                                                         while (i--) {
    double minCost = 0;
                                                                                             cin >> a >> b >> cost;
    // change '<' to '>' if maximum spanning tree is needed
                                                                                             g2.addOrUpdateEdge(a, b, cost);
    auto cmp = [] (const Edge<T> & a, const Edge<T> & b) {return a.weight
    cin >> i;
    sort(g.edges.begin(), g.edges.end(), cmp);
                                                                                         while (i--) {
    UnionFind<T> uf;
                                                                                             cin >> a >> b >> cost;
    int limit = g.nodes.size() - 1;
                                                                                             g2.addOrUpdateEdge(a, b, cost);
    for (int i = 0; (i < g.edges.size()) && (mst.size() < limit); i++) {</pre>
                                                                                         }
        Edge<T> e = g.edges[i];
                                                                                         vector<Edge<T>> mst2;
        T v = e.v, w = e.w;
                                                                                         cout << kruskalMST(g2, mst2) << endl;</pre>
        if (!uf.areNodesConnected(v, w)) {
                                                                                         t++;
            uf.addEdge(v, w);
                                                                                     }
            mst.push_back(e);
            minCost += e.weight;
```

```
return 0;
                                                                                      int n, m;
                                                                                      T a, b;
                                                                                      Graph < T > g(1);
                                                                                      cin >> n >> m;
    topologicalSort
2.8
                                                                                      if (n == 0 \&\& m == 0)
                                                                                          break;
// uva 10305 Ordering Tasks
                                                                                      while (n) {
#include <bits/stdc++.h>
                                                                                          g.addOrUpdateEdge(n, n);
#include "graphAPI.h"
using namespace std;
                                                                                      }
                                                                                      while (m) {
typedef int T;
                                                                                          cin >> a >> b;
                                                                                          g.addOrUpdateEdge(a, b);
void dfsTopologicalSort(Graph<T> &g, T current, int &index,
→ unordered_set<T> &visited, vector<T> &topologicalSortedNodes) {
                                                                                      }
    visited.insert(current);
                                                                                      printv(topologicalSort(g));
    for (auto neighbor : g.nodes[current])
                                                                                  }
        if (!visited.count(neighbor.first))
                                                                                  return 0;
            dfsTopologicalSort(g, neighbor.first, index, visited,
                                                                              }

→ topologicalSortedNodes);
    topologicalSortedNodes[index--] = current;
}
                                                                                   maxFlow
                                                                              2.9
vector<T> topologicalSort(Graph<T> &g) {
                                                                              // uva 820 - Internet Bandwidth
    unordered_set<T> visited;
                                                                              #include <bits/stdc++.h>
                                                                              #include "graphAPI.h"
    int index = g.nodes.size() - 1;
    vector<T> topologicalSortedNodes(g.nodes.size());
                                                                              using namespace std;
    for (auto node : g.nodes)
        if (!visited.count(node.first))
                                                                              typedef int T;
            dfsTopologicalSort(g, node.first, index, visited,

→ topologicalSortedNodes);
                                                                              bool hasAugmentedPath(Graph<T> &residualGraph, unordered_map<T, T>
    return topologicalSortedNodes;
                                                                              }
                                                                                  queue<T> q;
                                                                                  q.push(source);
void printv(vector<T> v) {
                                                                                  unordered_set<T> visited;
    if (v.size() == 0) {
                                                                                  visited.insert(source);
        cout << "" << endl;
                                                                                  while (!q.empty()) {
                                                                                      T current = q.front(); q.pop();
        return;
                                                                                      for (auto neighbor : residualGraph.nodes[current]) {
    cout << "" << v[0];
                                                                                          T v = neighbor.first;
    for (int i = 1; i < v.size(); i++)</pre>
                                                                                          if (!visited.count(v) && neighbor.second > 0) {
        cout << " " << v[i];
                                                                                              q.push(v);
    cout << "" << endl;
                                                                                              visited.insert(v);
}
                                                                                              parent[v] = current;
                                                                                              if (v == target)
int main() {
                                                                                                  return true;
    while (true) {
                                                                                         }
```

```
}
                                                                                             break;
                                                                                        cin >> s >> t >> c:
                                                                                        while (c--) {
    return false;
}
                                                                                             cin >> u >> v >> w;
                                                                                             if (g.hasEdge(u, v))
double maxFlow(Graph<T> &g, vector<vector<T>> &paths, T source, T target)
                                                                                                 g.addOrUpdateEdge(u, v, g.getEdgeWeight(u, v) + w);
                                                                                             else
    Graph<T> residualGraph(1);
                                                                                                 g.addOrUpdateEdge(u, v, w);
    residualGraph.nodes = g.nodes;
    double max_flow = 0;
                                                                                        vector<vector<int>> parents;
                                                                                        cout << "Network " << i << endl;</pre>
    unordered_map<T, T> parent;
                                                                                        cout << "The bandwidth is " << maxFlow(g, parents, s, t) << "." <<</pre>
    while (hasAugmentedPath(residualGraph, parent, source, target)) {
        vector<T> path;
                                                                                         \rightarrow endl;
        double flow = INF;
                                                                                         cout << endl;</pre>
        T v = target;
                                                                                        i++;
        while (v != source) {
                                                                                    }
            T u = parent[v];
                                                                                    return 0;
            if (flow > residualGraph.getEdgeWeight(u, v))
                                                                                }
                flow = residualGraph.getEdgeWeight(u, v);
            path.push_back(v);
            v = u;
                                                                                2.10 indexedPriorityQueue
        path.push_back(source);
                                                                                #include <bits/stdc++.h>
        reverse(path.begin(), path.end());
        paths.push_back(path);
                                                                                using namespace std;
        max_flow += flow;
        v = target;
                                                                                template <typename T> class indexedPriorityQueue {
        while (v != source) {
                                                                                private:
            T u = parent[v];
                                                                                    class Node {
            residualGraph.addOrUpdateEdge(u, v,
                                                                                    public:

→ residualGraph.getEdgeWeight(u, v) - flow);

                                                                                        double weight;
            residualGraph.addOrUpdateEdge(v, u,
                                                                                        T key;

→ residualGraph.getEdgeWeight(v, u) + flow);

                                                                                    };
            v = u;
                                                                                    vector<Node> pq;
        }
                                                                                    unordered_map<T, int> nodePosition;
    return max_flow;
                                                                                private:
}
                                                                                    void updatePositionInMap(T key1, T key2, int pos1, int pos2) {
                                                                                        this->nodePosition[key1] = pos1;
int main() {
                                                                                        this->nodePosition[key2] = pos2;
    int i = 1, n, s, t, c, u, v;
                                                                                    }
    double w;
                                                                                public:
    while (true) {
                                                                                    bool containsKey(T key) {
        Graph<int> g(0);
                                                                                        return this->nodePosition.count(key);
        cin >> n;
                                                                                    }
        if (!n)
```

```
T top() {
   return this->pq[0].key;
}
bool empty() {
   return this->pq.size() == 0;
}
void push(T key, int weight) {
   Node node;
   node.weight = weight;
   node.key = key;
    this->pq.push_back(node);
    int current = this->pq.size() - 1;
    int parentIndex = (current - 1) / 2;
    this->nodePosition[node.key] = current;
    while (parentIndex > -1) {
        Node parentNode = this->pq[parentIndex];
        Node currentNode = this->pq[current];
        // use '>' for minHeap, use '<' for maxheap</pre>
        if (parentNode.weight > currentNode.weight) {
            swap(this->pq[parentIndex], this->pq[current]);
            updatePositionInMap(this->pg[parentIndex].key,
            this->pq[current].key, parentIndex, current);
            current = parentIndex;
            parentIndex = (current - 1) / 2;
        } else
            break:
   }
}
void update(T key, int newWeight) {
   if (!this->nodePosition.count(key))
        return;
    int pos = this->nodePosition[key];
    this->pq[pos].weight = newWeight;
    int parent = (pos - 1) / 2;
    while (parent > - 1) {
        // use '>' for minHeap, use '<' for maxheap</pre>
        if (this->pq[parent].weight > this->pq[pos].weight) {
            swap(this->pq[parent], this->pq[pos]);
            updatePositionInMap(this->pq[parent].key,

→ this->pq[pos].key, parent, pos);
            pos = parent;
            parent = (pos - 1) / 2;
        } else
```

```
break;
    }
}
double getWeight(T key) {
    if (!this->nodePosition.count(key))
        return -1:
    return this->pq[this->nodePosition[key]].weight;
pair<T, double> pop() {
    int lastPos = this->pq.size() - 1;
    Node topNode = this->pq[0];
    this->pq[0] = this->pq[lastPos];
    this->nodePosition.erase(topNode.key);
    this->nodePosition[this->pq[0].key] = 0;
    this->pq.erase(pq.begin() + lastPos);
    int currentPos = 0;
    lastPos--;
    while (true) {
        int left = 2 * currentPos + 1:
        int right = left + 1;
        if (left > lastPos)
            break;
        if (right > lastPos)
            right = left;
        // in case of using maxheap, smallerPos will haver the

→ biggerPos value

        // use '>' for minHeap, use '<' for maxheap</pre>
        int smallerPos = this->pq[right].weight >
        → this->pq[left].weight ? left : right;
        // use '>' for minHeap, use '<' for maxheap
        if (this->pq[currentPos].weight > this->pq[smallerPos].weight)
            swap(this->pq[currentPos], this->pq[smallerPos]);
            updatePositionInMap(this->pq[currentPos].key,

    this->pq[smallerPos].key, currentPos, smallerPos);

            currentPos = smallerPos;
        } else
            break:
    return {topNode.key, topNode.weight};
}
void printPositionInMap () {
```

```
cout << "{ ";
                                                                                }
        for (auto i : this->nodePosition)
            cout << i.first << "=" << i.second << ",";</pre>
                                                                                int main() {
        cout << " }" << endl;
                                                                                    Graph<int> g(1);
                                                                                    g.addOrUpdateEdge(1, 2);
                                                                                    g.addOrUpdateEdge(1, 3);
    void printHeap () {
                                                                                    g.addOrUpdateEdge(2, 3);
        for (Node n : this->pq)
                                                                                    g.addOrUpdateEdge(4, 1);
            cout << n.key << " " << n.weight << endl;</pre>
                                                                                    g.addOrUpdateEdge(4, 5);
                                                                                    g.addOrUpdateEdge(5, 6);
                                                                                    g.addOrUpdateEdge(6, 4);
};
                                                                                    cout << hasDirectedCycle(g) << endl;</pre>
                                                                                    return 0;
                                                                                }
2.11 cycleInDirectedGraph
#include <bits/stdc++.h>
                                                                                2.12 unionFind
#include "graphAPI.h"
using namespace std;
                                                                                #include <bits/stdc++.h>
                                                                                using namespace std;
typedef int T;
                                                                                template <class T> class UnionFind {
bool hasDirectedCycle(Graph<T> &g, T node, T prevNode, unordered_map<T,
                                                                                public:

    int> &visited) {

                                                                                    // stores the parent of each node
    visited[node] = 1;
                                                                                    unordered_map<T, T> tree;
    for (auto neighbor : g.nodes[node]) {
                                                                                    // stores the size of each sub-tree
        T v = neighbor.first;
                                                                                    unordered_map<T, int> treeSize;
        if (v == node || visited[v] == 2)
                                                                                    int numberOfSets = 0;
            continue;
        if (visited[v] == 1)
                                                                                    bool hasNode(T node) {
                                                                                        return this->tree.count(node);
            return true;
        if (hasDirectedCycle(g, v, node, visited))
                                                                                    }
            return true;
                                                                                    void addNode(T newNode) {
    visited[node] = 2:
                                                                                        if (!hasNode(newNode)) {
    return false;
                                                                                            this->tree[newNode] = newNode:
}
                                                                                            this->treeSize[newNode] = 1;
                                                                                            this->numberOfSets++;
bool hasDirectedCycle(Graph<T> &g) {
                                                                                        }
    unordered_map<T, int> visited;
                                                                                    }
    for (auto node : g.nodes) {
        T u = node.first;
                                                                                    void addEdge(T v, T w) {
        if (!visited[u])
                                                                                        addNode(v);
            if (hasDirectedCycle(g, u, u, visited))
                                                                                        addNode(w);
                                                                                        T i = setGetRoot(v);
                return true;
                                                                                        T j = setGetRoot(w);
                                                                                        if (i == j)
    return false;
```

```
return;
        this->numberOfSets--;
        if (treeSize[i] < treeSize[j]) {</pre>
            this->tree[i] = j;
            this->treeSize[j] += this->treeSize[i];
        } else {
            this->tree[j] = i;
            this->treeSize[i] += this->treeSize[j];
        }
    bool areNodesConnected(T v, T w) {
        if (!this->tree.count(v) || !this->tree.count(w))
            return false;
        return setGetRoot(v) == setGetRoot(w);
    int getNumberOfSets() {
        return this->numberOfSets;
private:
    T setGetRoot(T v) {
        while (v != this->tree[v])
            v = this->tree[v] = this->tree[this->tree[v]];
        return v;
};
string input() {
    string ans;
    getline(cin, ans);
    return ans;
}
vector<string> split(string str, char token) {
    stringstream test(str);
    string segment;
    vector<std::string> seglist;
    while (std::getline(test, segment, token))
        seglist.push_back(segment);
    return seglist;
}
```

```
/*int main() {
    string str;
   int t;
   t = stoi(input());
    str = input();
    while (t--) {
        auto g = new UnionFind<int>();
        int ac = 0, wa = 0;
        int n;
        n = stoi(input());
        while (n--) {
            g \rightarrow addEdge(n + 1, n + 1);
        while (true) {
            vector<string> vals = split(input(), ' ');
            if (vals.size() == 0)
                break:
            if (vals[0] == "c") {
                g->addEdge(stoi(vals[1]), stoi(vals[2]));
            if (vals[0] == "q") {
                if (g->areNodesConnected(stoi(vals[1]), stoi(vals[2]))) {
                }
                else {
                    wa++;
                }
            }
        cout << ac << "," << wa << "\n";
        if (t != 0)
            cout << "\n";
        delete g;
   }
    return 0;
}*/
2.13 stronglyConnectedComponents
```

```
// uva 247 - Calling Circles
#include <bits/stdc++.h>
#include "graphAPI.h"
using namespace std;
typedef string T;
```

```
void dfsStronglyConnectedComponents(Graph<T> &g, T node, int &time,
                                   unordered_map<T, int> &visitedTime,

    unordered_map<T, int> &lowTime,

                                    vector<vector<T>>

    stack<T> &Stack,

                                    unordered_set<T> &inStack,

    unordered_set<T> &visited) {
    visited.insert(node);
    visitedTime[node] = time;
    lowTime[node] = time;
    time++;
    Stack.push(node);
    inStack.insert(node);
    for (const auto &neighbor : g.nodes[node]) {
       T v = neighbor.first;
        if (!visited.count(v)) {
            dfsStronglyConnectedComponents(g, v, time, visitedTime,
            → lowTime, stronglyConnectedComponents, Stack, inStack,
            → visited):
            lowTime[node] = min(lowTime[node], lowTime[v]);
       } else if (inStack.count(v))
            lowTime[node] = min(lowTime[node], visitedTime[v]);
    if (visitedTime[node] == lowTime[node]) {
        vector<T> stronglyConnectedComponent;
       Tu;
        while (true) {
            u = Stack.top(); Stack.pop();
            inStack.erase(u);
            stronglyConnectedComponent.push_back(u);
            if (u == node)
               break;
       }
        stronglyConnectedComponents.push_back(stronglyConnectedComponent);
}
vector<vector<T>> getStronglyConnectedComponents(Graph<T> &g) {
    unordered set<T> visited:
    vector<vector<T>> stronglyConnectedComponents;
    unordered_map<T, int> visitedTime, lowTime;
    unordered_set<T> inStack;
    stack<T> Stack;
    int time = 0;
```

```
for (const auto &node : g.nodes)
        if (!visited.count(node.first))
             dfsStronglyConnectedComponents(g, node.first, time,

→ visitedTime, lowTime, stronglyConnectedComponents, Stack,

→ inStack, visited);
    return stronglyConnectedComponents;
}
int main() {
    int n, m, nT = 1;
    while (true) {
        cin >> n >> m;
        if (!n && !m)
             return 0:
        if (nT != 1)
             cout << endl;</pre>
        Graph < T > g(1);
        string from, to;
        while (m--) {
             cin >> from >> to;
             g.addOrUpdateEdge(from, to);
        }
        vector<vector<T>> scc = getStronglyConnectedComponents(g);
        cout << "Calling circles for data set " << nT << ":" << endl;</pre>
        for (int i = 0; i < scc.size(); i++) {</pre>
             cout << scc[i][0];
            for (int j = 1; j < scc[i].size(); j++)</pre>
                 cout << ", " << scc[i][j];</pre>
             cout << endl;</pre>
        }
        nT++;
    }
    return 0;
```

## 3 NumberTheory

#### 3.1 extendedEuclidean

```
#include <bits/stdc++.h>
using namespace std;
```

```
void printv(vector<long long int> v) {
    if (v.size() == 0) {
        cout << "[]" << endl:
        return;
    cout << "[" << v[0];
    for (int i = 1; i < v.size(); i++) {</pre>
        cout << ", " << v[i];
    cout << "]" << endl;
// \gcd(a, b) = ax + by
vector<long long int> extendedGCD(long long int a, long long int b) {
    if (a > OLL && b == OLL) {
        return {a, 1LL, 0LL};
    long long int x = 1LL, y = 0LL, prevx = 0LL, prevy = 1LL, q,
    → remainder;
    while (true) {
        q = a / b;
        remainder = a - b * q;
        if (remainder == OLL)
            break;
        a = b;
        b = remainder;
        x = x - prevx * q;
        swap(x, prevx);
        y = y - prevy * q;
        swap(y, prevy);
    // gcd = b, x = prevx, y = prevy
    return {b, prevx, prevy};
int main() {
    long long int a, b;
    cin >> a >> b;
    printv(extendedGCD(a, b));
    printv(extendedGCD(b, a));
    return 0;
}
```

#### 3.2 divisibilityCriterion

```
def divisorCriteria(n, lim):
    results = []
    tenElevated = 1
    for i in range(lim):
        # remainder = pow(10, i, n)
        remainder = tenElevated % n
        negremainder = remainder - n
        if(remainder <= abs(negremainder)):</pre>
            results.append(remainder)
        else:
            results.append(negremainder)
        tenElevated *= 10
    return results
def testDivisibility(dividend, divisor, divisor_criteria):
    dividend = str(dividend)
    addition = 0
    dividendSize = len(dividend)
    i = dividendSize - 1
    j = 0
    while j < dividendSize:</pre>
        addition += int(dividend[i]) * divisor_criteria[j]
        i -= 1
        i += 1
    return addition % divisor == 0
if __name__ == '__main__':
    dividend, divisor = map(int, input().split())
    divisor_criteria = divisorCriteria(divisor, len(str(dividend)))
    print(divisor_criteria)
    print(testDivisibility(dividend, divisor, divisor_criteria))
3.3 gcd
#include <bits/stdc++.h>
using namespace std;
int gcd(int a, int b) {
    return b == 0 ? a : gcd(b, a % b);
}
int gcdI(int a, int b) {
```

```
while (b) {
    a %= b;
    swap(a, b);
}
return a;
}
int main() {
    int a, b;
    cin >> a >> b;
    cout << gcd(a, b) << "\n";
    cout << gcdI(a, b) << "\n";
}</pre>
```

#### 4 Primes

#### 4.1 myPrimesSieve

```
# sieve of primes, use dict if you want to save memory
# however using it will make this slower
def mySieve(N=10000000):
   n = N + 1
    dic = [0] * (n)
    # dic = \{0: 0, 1: 1\}
    primes = []
    if N == 2:
        primes = [2]
    if N > 2:
        primes = [2, 3]
    dic[0] = -1
    dic[1] = 1
   for i in range(4, n, 2):
        dic[i] = 2
   for i in range(9, n, 6):
        dic[i] = 3
    i = 5
    w = 2
   k = i * i
    while k < n:
        # if i not in dic:
        if dic[i] == 0:
            primes.append(i)
            # skip multiples of 2
            jump = 2 * i
            for j in range(k, n, jump):
                dic[j] = i
```

```
i += w
    w = 6 - w
    k = i * i

# if you need primes bigger than the root of N
while i < n:
    if dic[i] == 0:
        primes.append(i)
    i += w
    w = 6 - w
return dic, primes

if __name__ == '__main__':
    print(mySieve(int(input()))[1])</pre>
```

#### 4.2 primeFactorization

```
def mySieve(N=10000000):
    n = N + 1
    dic = [0] * (n)
    # dic = \{0: 0, 1: 1\}
    primes = []
    if N == 2:
        primes = [2]
    if N > 2:
        primes = [2, 3]
    dic[0] = -1
    dic[1] = 1
    for i in range(4, n, 2):
        dic[i] = 2
    for i in range(9, n, 6):
        dic[i] = 3
    i = 5
    w = 2
    k = i * i
    while k < n:
        # if i not in dic:
        if dic[i] == 0:
            primes.append(i)
            # skip multiples of 2
            jump = 2 * i
            for j in range(k, n, jump):
                dic[j] = i
        i += w
        w = 6 - w
```

```
k = i * i
    \# if you need primes bigger than the root of N
    while i < n:
        if dic[i] == 0:
            primes.append(i)
        i += w
        w = 6 - w
    return dic, primes
def getPrimeFactors(N, sieveToMaxN):
    n = N
    primeFactors = []
    while n != 1:
        if sieveToMaxN[n] == 0:
            primeFactors.append(n)
            break
        primeFactors.append(sieveToMaxN[n])
        n /= sieveToMaxN[n]
    return primeFactors
if __name__ == '__main__':
   n = int(input())
    sieve = mySieve(n)[0]
    print(sieve)
    print(getPrimeFactors(n, sieve))
4.3 isPrimeSieve
#include <bits/stdc++.h>
using namespace std;
pair<vector<int>, vector<int> > mySieve(int N) {
    int n = N + 1;
    vector<int> dic(n);
    vector<int> primes;
    if (N == 2)
        primes = \{2\};
    if (N > 2)
        primes = \{2, 3\};
    dic[0] = -1;
    dic[1] = 1;
    for (int i = 4; i < n; i += 2)
        dic[i] = 2;
```

```
for (int i = 9; i < n; i += 6)
        dic[i] = 3:
   int i = 5, w = 2, k = i * i;
    while (k < n) {
        if (dic[i] == 0) {
            primes.push_back(i);
            // skip multiples of 2
            int jump = 2 * i;
            for (long long int j = k; j < n; j += jump)
                dic[i] = i;
        i += w;
        w = 6 - w;
        k = i * i;
   }
    // if you need primes bigger than the root of N
    while (i < n) {
        if (dic[i] == 0)
            primes.push_back(i);
        i += w;
        w = 6 - w;
   return {dic, primes};
}
bool isPrime(int N, vector<int> &sieve, vector<int> &primes) {
    if (N < sieve.size())</pre>
        return sieve[N] == 0 ? true : false;
   for (int prime : primes) {
        if (prime * prime > N)
            break;
        if (N % prime == 0)
            return false;
   }
    return true;
int main() {
    pair<vector<int>, vector<int> > sieve = mySieve(10000000);
    long long int n;
    cin >> n:
    cout << isPrime(n, sieve.first, sieve.second) << '\n';</pre>
   return 0;
}
```

#### 4.4 isPrimeMillerRabin

```
from random import randrange
def is_prime(p):
   k = 100
    if p == 2 or p == 3:
        return True
    if (p & 1) == 0 or p == 1:
        return False
    phi = p - 1
    d = phi
    r = 0
    while (d & 1) == 0:
        d = int(d >> 1)
        r += 1
   for i in range(k):
        a = randrange(2, p - 2)
        exp = pow(a, d, p)
        if exp == 1 or exp == p - 1:
            continue
        flag = False
        for j in range(r - 1):
            exp = pow(exp, 2, p)
            if exp == 1:
                return False
            if exp == p - 1:
                flag = True
                break
        if flag:
            continue
        else:
            return False
    return True
if __name__ == '__main__':
    while True:
        try:
            n = int(input())
            print(n, is_prime(n))
        except EOFError:
            break
```

#### 4.5 primesSievesComparison

```
from math import sqrt
import timeit
# sieve of primes, use dict if you want to save memory
# however using it will make this slower
def sieve(N=100000000):
    n = N + 1
    dic = [0] * (n)
    # dic = \{0: 0, 1: 1\}
    dic[0] = -1
    dic[1] = 1
   for i in range(4, n, 2):
        dic[i] = 2
   for i in range(9, n, 6):
        dic[i] = 3
    i = 5
    w = 2
   k = i * i
    while k < n:
        # if i not in dic:
        if dic[i] == 0:
            # skip multiples of 2
            jump = 2 * i
            for j in range(k, n, jump):
                dic[j] = i
        i += w
        w = 6 - w
        k = i * i
   return dic
def clasicSieve(N=100000000):
    criba = [0] * (N + 1)
   raiz = int(sqrt(N))
    criba[0] = -1
    criba[1] = 1
    for i in range(4, N + 1, 2):
        criba[i] = 2
   for i in range(3, raiz + 1, 2):
        if (criba[i] == 0):
            for j in range(i * i, N + 1, i):
                if (criba[j] == 0):
                    criba[j] = i
```

```
if __name__ == '__main__':
    print(timeit.timeit(clasicSieve, number=1))
    print(timeit.timeit(sieve, number=1))
4.6 primesSievesComparison
#include <bits/stdc++.h>
using namespace std;
vector<int> sieve(int N) {
    int n = N + 1:
    vector<int> dic(n);
    dic[0] = -1;
    dic[1] = 1;
    for (int i = 4; i < n; i += 2)
        dic[i] = 2;
    for (int i = 9; i < n; i += 6)
        dic[i] = 3:
    int i = 5, w = 2, k = i * i;
    while (k < n) {
        if (dic[i] == 0) {
            int jump = 2 * i;
           for (int j = k; j < n; j += jump)
                dic[j] = i;
        }
       i += w;
        w = 6 - w;
       k = i * i;
    return dic;
// Criba de Eratostenes de 1 a n.
vector<int> clasicSieve(int n) {
    vector<int> criba(n + 1);
    for (int i = 4; i <= n; i += 2)
        criba[i] = 2;
    for (int i = 3; i * i <= n; i += 2)
        if (!criba[i])
            for (int j = i * i; j <= n; j += i)
                if (!criba[j]) criba[j] = i;
```

return criba

```
return criba;
int main() {
    int n = 10000000;
    cin >> n:
    clock_t start, stop;
    for (int i = 0; i < 4; i++) {
        start = clock();
        clasicSieve(n);
        stop = clock();
        cout << (double)(stop - start) / CLOCKS_PER_SEC << " seconds." <<</pre>
         \rightarrow endl;
        start = clock();
        sieve(n);
        stop = clock();
        cout << (double)(stop - start) / CLOCKS_PER_SEC << " seconds." <<</pre>

    endl;

    }
    return 0;
}
4.7 primeFactorization
#include <bits/stdc++.h>
using namespace std;
// sieve of primes, use unordered_map if you want to save memory
// however using it will make this slower
pair<vector<int>, vector<int> > mySieve(int N) {
    int n = N + 1:
    vector<int> dic(n):
    vector<int> primes;
    if (N == 2)
        primes = \{2\};
    if (N > 2)
        primes = \{2, 3\};
    dic[0] = -1;
    dic[1] = 1;
    for (int i = 4; i < n; i += 2)
        dic[i] = 2;
    for (int i = 9; i < n; i += 6)
        dic[i] = 3;
```

```
int i = 5, w = 2, k = i * i;
                                                                                       cout << ", " << v[i];
                                                                                   }
    while (k < n) {
        if (dic[i] == 0) {
                                                                                   cout << "]" << endl;
            primes.push_back(i);
                                                                               }
           // skip multiples of 2
           int jump = 2 * i;
            for (long long int j = k; j < n; j += jump)
                                                                               int main() {
                dic[i] = i;
                                                                                   int n;
                                                                                   cin >> n;
        i += w;
                                                                                   vector<int> sieve = mySieve(n).first;
        w = 6 - w;
                                                                                   printv(sieve);
        k = i * i;
                                                                                   printv(getPrimeFactors(n, sieve));
                                                                               }
    // if you need primes bigger than the root of N
    while (i < n) {
        if (dic[i] == 0)
                                                                               4.8 myPrimesSieve
            primes.push_back(i);
        i += w;
                                                                               #include <bits/stdc++.h>
        w = 6 - w;
                                                                               using namespace std;
    return {dic, primes};
}
                                                                               // sieve of primes, use unordered_map if you want to save memory
                                                                               // however using it will make this slower
                                                                               pair<vector<int>, vector<int> > mySieve(int N) {
vector<int> getPrimeFactors(long long int N, vector<int> &sieveToMaxN) {
                                                                                   int n = N + 1;
    long long int n = N;
                                                                                   vector<int> dic(n);
    vector<int> primeFactors;
                                                                                   vector<int> primes;
    while (n != 1LL) {
                                                                                   if (N == 2)
        if (sieveToMaxN[n] == 0) {
                                                                                       primes = \{2\};
            primeFactors.push_back(n);
                                                                                   if (N > 2)
            break;
                                                                                       primes = \{2, 3\};
                                                                                   dic[0] = -1;
        primeFactors.push_back(sieveToMaxN[n]);
                                                                                   dic[1] = 1;
        n /= sieveToMaxN[n];
                                                                                   for (int i = 4; i < n; i += 2)
                                                                                       dic[i] = 2:
    return primeFactors;
                                                                                   for (int i = 9; i < n; i += 6)
}
                                                                                       dic[i] = 3;
                                                                                   int i = 5, w = 2, k = i * i;
                                                                                   while (k < n) {
void printv(vector<int> v) {
                                                                                       if (dic[i] == 0) {
    if (v.size() == 0) {
                                                                                           primes.push_back(i);
        cout << "[]" << endl;
                                                                                           // skip multiples of 2
        return;
                                                                                           int jump = 2 * i;
    }
                                                                                           for (long long int j = k; j < n; j += jump)
    cout << "[" << v[0];
                                                                                               dic[j] = i;
    for (int i = 1; i < v.size(); i++) {</pre>
                                                                                       }
```

```
i += w;
        w = 6 - w:
       k = i * i;
    // if you need primes bigger than the root of N
    while (i < n) {
        if (dic[i] == 0)
            primes.push_back(i);
       i += w;
        w = 6 - w;
    return {dic, primes};
void printv(vector<int> v) {
    if (v.size() == 0) {
        cout << "[]" << endl;
        return;
    }
    cout << "[" << v[0];
    for (int i = 1; i < v.size(); i++) {</pre>
       cout << ", " << v[i];
    }
    cout << "]" << endl;
}
int main() {
    int n;
    cin >> n;
    printv(mySieve(n).second);
}
    CodingResources
    priorityQueueOfClass
```

```
#include <bits/stdc++.h>
using namespace std;
struct Object {
    char first;
    int second;
};
```

```
template<typename T> void print_queue(T& q) {
    while(!q.empty()) {
        std::cout << "{" << q.top().first << " " << q.top().second << "}";
        q.pop();
    std::cout << '\n';
}
int main() {
    auto cmp = [](const Object& a, const Object& b) {return a.second >
    → b.second;};
    priority_queue<Object, vector<Object>, decltype(cmp)> pq(cmp);
    vector<0bject> v = \{\{'c',3\}, \{'a', 1\}, \{'b', 2\}\};
   for (auto i : v)
        pq.push(i);
    sort(v.begin(), v.end(), cmp);
    print_queue(pq);
   return 0;
}
5.2 printVector
#include <bits/stdc++.h>
using namespace std;
void printv(vector<int> v) {
    if (v.size() == 0) {
        cout << "[]" << endl;
        return;
   }
    cout << "[" << v[0];
    for (int i = 1; i < v.size(); i++) {</pre>
        cout << ", " << v[i];
   }
    cout << "]" << endl;
}
int main() {
    vector<int> v = \{1, 2, 3, 4, 5, 6\};
    printv(v);
   return 0;
}
```

```
5.3 splitString
#include <bits/stdc++.h>
using namespace std;
vector<string> split(string str, char token) {
    stringstream test(str);
    string segment;
    vector<std::string> seglist;
    while (std::getline(test, segment, token))
        seglist.push_back(segment);
    return seglist;
}
int main () {
    string str;
    getline(cin, str);
    vector<string> segments = split(str, ' ');
    for (string segment : segments)
        cout << segment << endl;</pre>
    return 0;
}
5.4 intToBinary
#include <bits/stdc++.h>
using namespace std;
typedef long long int lli;
lli bitsInInt(lli n) {
    return floor(log2(n) + 1LL);
}
void printv(vector <int> v) {
    cout << v[0];
    for (int i = 1; i < v.size(); i++) {</pre>
        cout << " " << v[i];
    cout << endl;</pre>
vector<int> intToBitsArray(lli n) {
    n = abs(n);
    if (!n) {
        vector<int> v;
```

```
return v;
    }
    int length = bitsInInt(n);
    int lastPos = length - 1;
    vector<int> v(length);
    for (lli i = lastPos, j = 0; i > -1LL; i--, j++) {
        lli aux = (n >> i) & 1LL;
        v[j] = aux;
    }
    return v;
}
int main() {
    lli n;
    cin >> n;
    printv(intToBitsArray(n));
    return 0;
}
5.5 readLineCpp
#include <bits/stdc++.h>
using namespace std;
string strInput() {
    string ans;
    cin >> ans;
    cin.ignore();
    return ans;
}
int intInput() {
    int ans:
    cin >> ans;
    cin.ignore();
    return ans;
}
double dInput() {
    double ans:
    cin >> ans;
    cin.ignore();
    return ans;
}
```

```
*/
string input() {
    string ans;
    cin >> ws;
    getline(cin, ans);
    return ans;
}
int main() {
    ios_base::sync_with_stdio(0);
    string ans;
    // cout << strInput() << endl;</pre>
    cin >> ans;
    cout << ans << endl;</pre>
    cout << input() << endl;</pre>
    return 0;
}
5.6 sortVectorOfClass
#include <bits/stdc++.h>
using namespace std;
struct Object {
    char first;
    int second;
};
void printv(vector<Object> v) {
    if (v.size() == 0) {
        cout << "[]" << endl;</pre>
        return;
    cout << "[{" << v[0].first << ", " << v[0].second << "}";</pre>
    for (int i = 1; i < v.size(); i++) {</pre>
        cout << ", {" << v[i].first << ", " << v[i].second << "}";</pre>
    cout << "]" << endl;
int main() {
    auto cmp = [](const Object& a, const Object& b) {return a.second >
     → b.second;};
    vector<Object> v = {{'c',3}, {'a', 1}, {'b', 2}};
    sort(v.begin(), v.end(), cmp);
```

```
printv(v);
   return 0;
}
5.7 sortListOfClass
class MyObject:
    def __init__(self, first, second):
        self.first = first
        self.second = second
1 = [MyObject('c', 3), MyObject('a', 1), MyObject('b', 2)]
for myObject in 1:
    print(myObject.first, myObject.second)
print()
l.sort(key=lambda x: x.first, reverse=False)
for myObject in sorted(1, key=lambda x: x.first, reverse=False):
    print(myObject.first, myObject.second)
print()
for myObject in 1:
    print(myObject.first, myObject.second)
```