

Competitive Programming Reference

First, solve the problem. Then, write the code.

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Contents

Coding Resources

4

C++	4
Decimal Precision.cpp	4
Include All Libraries.cpp	4
Int To Binary.cpp	4
IO Optimization.cpp	4
Map Value To Int.cpp	4
Permutations.cpp	4
Print Vector.cpp	4
Priority Queue Of Object.cpp	4
Random.cpp	5
Read Line.cpp	5
Sort Pair.cpp	5
Sort Vector Of Object.cpp	5
Split String.cpp	5
Typedef.cpp	5
Python	5
Combinations.py	5
Fast IO.py	5
Permutations.py	5
Random.py	5
Sort List.py	6
Sort List Of Object.py	6

Data Structures

6

Geometry	6
K-D Tree.cpp	6
Graphs	6
UnionFind.cpp	6
Ranges	6
BIT.cpp	6
BIT Range Update.cpp	7
Segment Tree.cpp	7
Segment Tree Lazy Propagation.cpp	7
Sparse Table.cpp	8
Strings	9
Trie.cpp	9
Trees And Heaps	9
Treap.cpp	9

Geometry

9

Max Interval Overlap.cpp	9
--------------------------	---

Graphs

10

Articulation Points And Bridges.cpp	10
Connected Components.cpp	10
Flood Fill.cpp	11
Is Bipartite.cpp	11
LCA.cpp	11
MST Kruskal.cpp	12
MST Prim.cpp	12
Strongly Connected Components.cpp	13
Topological Sort.cpp	13
Cycles	14
Get All Simple Cycles.cpp	14
Get Some Cycles.cpp	14
Has Cycle.cpp	14

Flow	14
Max Flow Dinic.cpp	14
Maximum Bipartite Matching.cpp	15
ShortestPaths	15
Bellman Ford.cpp	15
Dijkstra.cpp	15

Maths

16

Number Theory	16
Divisibility Criterion.py	16
Extended Euclidean.cpp	17
GCD.cpp	17
LCM.cpp	17
Prime Check Miller Rabin.py	17
Prime Sieve.cpp	17

Strings

18

KMP.cpp	18
Rabin Karp.cpp	18

Techniques

18

Binary Search.cpp	18
Multiple Queries	18
Mo.cpp	18
SQRT Decomposition.cpp	19

Coding Resources

C++

Decimal Precision.cpp

```
// rounds up the decimal number
cout << setprecision(N) << n << endl;
// specify N fixed number of decimals
cout << fixed << setprecision(N) << n << endl;
```

Include All Libraries.cpp

```
#include <bits/stdc++.h>
using namespace std;
```

Int To Binary.cpp

```
typedef long long int lli;

lli bitsInInt(lli n) { // clz = count leading zeroes
    return sizeof(n) * 8 - __builtin_clzll(n);
}

vector<bool> intToBitsArray(lli n) {
    n = abs(n);
    if (!n) return {};
    int length = bitsInInt(n), lastPos = length - 1;
    vector<bool> v(length);
    for (lli i = lastPos, j = 0; i > -1LL; i--, j++)
        ↪ v[j] = (n >> i) & 1LL;
    return v;
}
```

IO Optimization.cpp

```
int main() {
    ios_base::sync_with_stdio(0);
    cin.tie(0);
}
```

Map Value To Int.cpp

```
// val = value
typedef string Val;
unordered_map<Val, int> intForVal;
unordered_map<int, Val> valForInt;
int mapId = 0;

int Map(Val val) {
    valForInt[mapId] = val;
    return intForVal.count(val) ? intForVal[val] :
        ↪ intForVal[val] = mapId++;
}
```

```
int IMap(int val) {
    return valForInt[val];
}
```

```
void initMapping() {
    mapId = 0;
    intForVal.clear();
    valForInt.clear();
}
```

Permutations.cpp

```
typedef vector<int> T; // typedef string T;

vector<T> permutations(T v) {
    vector<vector<int>>> ans;
    sort(v.begin(), v.end());
    do
        ans.push_back(v);
    while (next_permutation(v.begin(), v.end()));
    return ans;
}
```

Print Vector.cpp

```
void printv(vector<int> v) {
    if (v.size() == 0) {
        cout << "[]" << endl;
        return;
    }
    cout << "[" << v[0];
    for (int i = 1; i < v.size(); i++) cout << ", " <<
        ↪ v[i];
    cout << "]" << endl;
}
```

Priority Queue Of Object.cpp

```
struct Object {
    char first;
    int second;
};

int main() {
    auto cmp = [](const Object& a, const Object& b) {
        ↪ return a.second > b.second; };
    priority_queue<Object, vector<Object>,
        ↪ decltype(cmp)> pq(cmp);
    vector<Object> v = {{'c', 3}, {'a', 1}, {'b', 2}};
    sort(v.begin(), v.end(), cmp);
    return 0;
}
```

Random.cpp

```
int random(int min, int max) {
    return min + rand() % (max - min + 1);
}

int main() {
    srand(time(0));
    // code ...
}
```

Read Line.cpp

```
// when reading lines, don't mix 'cin' with
// 'getline' just use getline and split
string input() {
    string ans;
    // cin >> ws; // eats all whitespaces.
    getline(cin, ans);
    return ans;
}
```

Sort Pair.cpp

```
pair<int, int> p;
// sorts array on the basis of the first element
sort(p.begin(), p.end());
```

Sort Vector Of Object.cpp

```
struct Object {
    char first;
    int second;
};

bool cmp(const Object& a, const Object& b) {
    return a.second > b.second;
}

int main() {
    vector<Object> v = {{'c', 3}, {'a', 1}, {'b', 2}};
    sort(v.begin(), v.end(), cmp);
    printv(v);
    return 0;
}
```

Split String.cpp

```
vector<string> split(string str, char token) {
    stringstream test(str);
    string seg;
    vector<string> seglist;
    while (getline(test, seg, token))
        seglist.push_back(seg);
    return seglist;
}
```

Typedef.cpp

```
typedef TYPE ALIAS;
// example:
typedef int T;
```

Python

Combinations.py

```
import itertools
# from arr choose k = > combinations(arr, k)
print(list(itertools.combinations([1, 2, 3], 3)))
```

Fast IO.py

```
from sys import stdin, stdout

N = 10
# Reads N chars from stdin (it counts '\n' as char)
stdin.read(N)
# Reads until '\n' or EOF
line = stdin.readline()
# Reads all lines in stdin until EOF
lines = stdin.readlines()
# Writes a string to stdout, it doesn't add '\n'
stdout.write(line)
# Writes a list of strings to stdout
stdout.writelines(lines)
# Reads numbers separated by space in a line
numbers = list(map(int, stdin.readline().split()))
```

Permutations.py

```
import itertools
print(list(itertools.permutations([1, 2, 3])))
```

Random.py

```
import random
# Initialize the random number generator.
random.seed(None)
# Returns a random integer N such that a <= N <= b.
random.randint(a, b)
# Returns a random integer N such that 0 <= N < b
random.randrange(b)
# Returns a random integer N such that a <= N < b.
random.randrange(a, b)
# Returns and integer with k random bits.
random.getrandbits(k)
# shuffles a list
random.shuffle(li)
```

Sort List.py

```
li = ['a', 'c', 'b']
# sorts inplace in descending order
li.sort(reverse=True)
# returns sorted list ascending order
ol = sorted(li)
```

Sort List Of Object.py

```
class MyObject :
    def __init__(self, first, second, third):
        self.first = first
        self.second = second
        self.third = third

li = [MyObject('b', 3, 1), MyObject('a', 3, 2),
      ↪ MyObject('b', 3, 3)]
# returns list sorted by first then by second then by
↪ third in increasing order
ol = sorted(li, key = lambda x: (x.first, x.second,
↪ x.third), reverse=False)
# sorts inplace by first then by second then by third
↪ in increasing order
li.sort(key = lambda x: (x.first, x.second, x.third),
↪ reverse=False)
```

Data Structures

Geometry

K-D Tree.cpp

Graphs

UnionFind.cpp

```
struct UnionFind {
    vector<int> dad, size;
    int n;
    UnionFind(int N = 0) : n(N), dad(N), size(N, 1) {
        while (N--) dad[N] = N;
    }

    int root(int u) {
        if (dad[u] == u) return u;
        return dad[u] = root(dad[u]);
    }

    bool areConnected(int u, int v) {
        return root(u) == root(v);
    }
}
```

```
void join(int u, int v) {
    int Ru = root(u), Rv = root(v);
    if (Ru == Rv) return;
    --n, dad[Ru] = Rv;
    size[Rv] += size[Ru];
}

int getSize(int u) {
    return size[root(u)];
}

int numberOfSets() {
    return n;
}
};
```

Ranges

BIT.cpp

```
typedef long long int T;
T neutro = 0;
vector<T> bit;
void initVars(int n) {
    bit.assign(++n, neutro);
}

T F(T a, T b) {
    return a + b;
    // return a * b;
}

// Inverse of F
T I(T a, T b) {
    return a - b;
    // return a / b;
}

// O(N)
void build() {
    for (int i = 1; i < bit.size(); i++) {
        int j = i + (i & -i);
        if (j < bit.size()) bit[j] = F(bit[j], bit[i]);
    }
}

// O(lg(N))
void update(int i, T val) {
    for (i++; i < bit.size(); i += i & -i) bit[i] =
        ↪ F(bit[i], val);
}

// O(lg(N))
T query(int i) {
    T ans = neutro;
    for (i++; i; i -= i & -i) ans = F(ans, bit[i]);
    return ans;
}
```

```
// O(lg(N)), [l, r]
T query(int l, int r) {
    return I(query(r), query(--l));
}

void setValAt(T val, int i) {
    bit[++i] = val;
}

// O(lg(N)), [l, r]
void update(int l, int r, T val) {
    update(bit1, l, val);
    update(bit1, r + 1, -val);
    update(bit2, r + 1, val * r);
    update(bit2, l, -val * (l - 1));
}

// O(lg(N))
T query(vector<T> &bit, int i) {
    T ans = neutro;
    for (i++; i; i -= i & -i) ans += bit[i];
    return ans;
}

// O(lg(N))
T query(int i) {
    return query(bit1, i) * i + query(bit2, i);
}

// O(lg(N)), [l, r]
T query(int l, int r) {
    return query(r) - query(l - 1);
}
```

Segment Tree.cpp

```
// st = segment tree. st[1] = root;
// neutro = operation neutral value
// e.g. for sum is 0, for multiplication
// is 1, for gcd is 0, for min is INF, etc.
typedef int T;
T neutro = 0;
int N;
vector<T> st;
```

```
void initVars(int n) {
    st.assign(2 * (N = n), neutro);
}

T F(T a, T b) {
    return a + b;
    // return __gcd(a, b);
    // return a * b;
    // return min(a, b);
}

// O(2N)
void build() {
    for (int i = N - 1; i > 0; i--) st[i] = F(st[i << 1], st[i << 1 | 1]);
}

// O(lg(2N))
void update(int i, T val) {
    for (st[i += N] = val; i > 1; i >>= 1) st[i >> 1] = F(st[i], st[i ^ 1]);
}

// O(3N), [l, r]
void update(int l, int r, T val) {
    for (l += N, r += N; l <= r; l++) st[l] = val;
    build();
}

// O(lg(2N)), [l, r]
T query(int l, int r) {
    T ans = neutro;
    for (l += N, r += N; l <= r; l >>= 1, r >>= 1) {
        if (l & 1) ans = F(ans, st[l++]);
        if (~r & 1) ans = F(ans, st[r--]);
    }
    return ans;
}

void setValAt(T val, int i) {
    st[i + N] = val;
}
```

Segment Tree Lazy Propagation.cpp

```
// st = segment tree, st[1] = root, H = height of d
// u = updates, d = delayed updates
// neutro = operation neutral val
// e.g. for sum is 0, for multiplication
// is 1, for gcd is 0, for min is INF, etc.
```

```
template <class T>
struct SegmentTree {
    T neutro = 0;
    int N, H;
    vector<T> st, d;
    vector<bool> u;
```

```

SegmentTree(int n) : st(2 * n, neutro), d(n), u(n,
    ↪ 0) {
    H = sizeof(int) * 8 - __builtin_clz(N = n);
}

T F(T a, T b) {
    return a + b;
    // return __gcd(a, b);
    // return a * b;
    // return min(a, b);
}

void apply(int i, T val, int k) {
    st[i] = val * k; // sum
    // st[i] = val; // min, max, gcd
    // st[i] = pow(a, k); // multiplication
    if (i < N) d[i] = val, u[i] = 1;
}

void calc(int i) {
    if (!u[i]) st[i] = F(st[i << 1], st[i << 1 | 1]);
}

// O(2N)
void build() {
    for (int i = N - 1; i > 0; i--) calc(i);
}

// O(lg(N))
void build(int p) {
    while (p > 1) p >>= 1, calc(p);
}

// O(lg(N))
void push(int p) {
    for (int s = H, k = 1 << (H - 1); s > 0; s--, k
    ↪ >>= 1) {
        int i = p >> s;
        if (u[i]) {
            apply(i << 1, d[i], k);
            apply(i << 1 | 1, d[i], k);
            u[i] = 0, d[i] = neutro;
        }
    }
}

// O(lg(N)), [l, r]
void update(int l, int r, T val) {
    push(l += N);
    push(r += N);
    int ll = l, rr = r, k = 1;
    for (; l <= r; l >>= 1, r >>= 1, k <<= 1) {
        if (l & 1) apply(l++, val, k);
        if (~r & 1) apply(r--, val, k);
    }
    build(ll);
    build(rr);
}

```

```

// O(lg(2N)), [l, r]
T query(int l, int r) {
    push(l += N);
    push(r += N);
    T ans = neutro;
    for (; l <= r; l >>= 1, r >>= 1) {
        if (l & 1) ans = F(ans, st[l++]);
        if (~r & 1) ans = F(ans, st[r--]);
    }
    return ans;
}

void setValAt(T val, int i) {
    st[i + N] = val;
}
};

```

Sparse Table.cpp

```

// st = sparse table, Arith = Arithmetic
typedef int T;
int neutro = 0;
vector<vector<T>> st;

T F(T a, T b) {
    // return min(a, b);
    return __gcd(a, b);
    // return a + b; // Arith
    // return a * b; // Arith
}

// O(Nlg(N))
void build(vector<T> &arr) {
    st.assign(log2(arr.size()), vector<T>(arr.size()));
    st[0] = arr;
    for (int i = 1; (1 << i) <= arr.size(); i++)
        for (int j = 0; j + (1 << i) <= arr.size(); j++)
            ↪ st[i][j] = F(st[i - 1][j], st[i - 1][j + (1 <<
            ↪ (i - 1))]);
}

// O(1), [l, r]
T query(int l, int r) {
    int i = log2(r - l + 1);
    return F(st[i][l], st[i][r + 1 - (1 << i)]);
}

// O(lg(N)), [l, r]
T queryArith(int l, int r) {
    T ans = neutro;
    while (true) {
        int k = log2(r - l + 1);
        ans = F(ans, st[k][l]);
        l += 1 << k;
        if (l > r) break;
    }
    return ans;
}

```


Strings

Trie.cpp

```
// wpt = number of words passing through
// w = number of words ending in the node
// c = character
struct Trie {
    struct Node {
        // for lexicographical order use 'map'
        // map<char, Node *> ch;
        unordered_map<char, Node *> ch;
        int w = 0, wpt = 0;
    };

    Node *root = new Node();

    // O(STR.SIZE)
    void insert(string str) {
        Node *curr = root;
        for (auto &c : str) {
            curr->wpt++;
            if (!curr->ch.count(c)) curr->ch[c] = new
                ↪ Node();
            curr = curr->ch[c];
        }
        curr->wpt++;
        curr->w++;
    }

    // O(STR.SIZE)
    Node *find(string &str) {
        Node *curr = root;
        for (auto &c : str) {
            if (!curr->ch.count(c)) return nullptr;
            curr = curr->ch[c];
        }
        return curr;
    }

    // number of words with given prefix O(N)
    int prefixCount(string prefix) {
        Node *node = find(prefix);
        return node ? node->wpt : 0;
    }

    // number of words matching str O(N)
    int strCount(string str) {
        Node *node = find(str);
        return node ? node->w : 0;
    }

    // O(N)
    void getWords(Node *curr, vector<string> &words,
        ↪ string &word) {
        if (!curr) return;
        if (curr->w) words.push_back(word);
        for (auto &c : curr->ch) {
            getWords(c.second, words, word += c.first);
            word.pop_back();
        }
    }
}
```

```
// O(N)
vector<string> getWords() {
    vector<string> words;
    string word = "";
    getWords(root, words, word);
    return words;
}

// O(N)
vector<string> getWordsByPrefix(string prefix) {
    vector<string> words;
    getWords(find(prefix), words, prefix);
}

// O(STR.SIZE)
bool remove(Node *curr, string &str, int &i) {
    if (i == str.size()) {
        curr->wpt--;
        return curr->w ? !(curr->w = 0) : 0;
    }
    int c = str[i];
    if (!curr->ch.count(c)) return false;
    if (remove(curr->ch[c], str, ++i)) {
        if (!curr->ch[c]->wpt) curr->wpt--,
            ↪ curr->ch.erase(c);
        return true;
    }
    return false;
}

// O(STR.SIZE)
int remove(string str) {
    int i = 0;
    return remove(root, str, i);
}
};
```

Trees And Heaps

Treap.cpp

Geometry

Max Interval Overlap.cpp

```
typedef long long int T;
typedef pair<T, T> Interval;
```

```
// O(N * lg(N))
pair<int, T> maxOverlap(vector<Interval> &arr) {
    map<T, int> m;
    int maxI = 0, curr = 0;
    T idx = -1LL;
    for (auto &i : arr) m[i.first]++, m[i.second + 1]--;
    for (auto &p : m) {
        curr += p.second;
        if (curr > maxI) maxI = curr, idx = p.first;
    }
    return {maxI, idx};
}

// O(MaxPoint) maxPoint < vector::max_size
pair<int, int> maxOverlap(vector<Interval> &arr) {
    T maxPoint = 0;
    for (auto &i : arr)
        if (i.second > maxPoint) maxPoint = i.second;
    vector<int> x(maxPoint + 2);
    for (auto &i : arr) x[i.first]++, x[i.second + 1]--;
    int maxI = 0, curr = 0;
    T idx = -1LL;
    for (int i = 0; i < x.size(); i++) {
        curr += x[i];
        if (curr > maxI) maxI = curr, idx = i;
    }
    return {maxI, idx};
}
```

Graphs

Articulation Points And Bridges.cpp

```
// APB = articulation points and bridges
// ap = Articulation Point
// br = bridges, p = parent
// disc = discovery time
// low = lowTime, ch = children
typedef pair<int, int> Edge;
int Time;
vector<vector<int>>> ady;
vector<int> disc, low, ap;
vector<Edge> br;

void initVars(int N) {
    ady.assign(N, vector<int>());
}
```

```
int dfsAPB(int u, int p) {
    int ch = 0;
    low[u] = disc[u] = ++Time;
    for (int &v : ady[u]) {
        if (v == p) continue;
        if (!disc[v]) {
            ch++, dfsAPB(v, u);
            if (disc[u] <= low[v]) ap[u]++;
            if (disc[u] < low[v]) br.push_back({u, v});
            low[u] = min(low[u], low[v]);
        } else
            low[u] = min(low[u], disc[v]);
    }
    return ch;
}

// O(N)
void APB() {
    br.clear();
    ap = low = disc = vector<int>(ady.size());
    Time = 0;
    for (int u = 0; u < ady.size(); u++)
        if (!disc[u]) ap[u] = dfsAPB(u, u) > 1;
}

void addEdge(int u, int v) {
    ady[u].push_back(v);
    ady[v].push_back(u);
}
```

Connected Components.cpp

```
// comp = component
int compId;
vector<vector<int>>> ady;
vector<int> getComp;

void initVars(int N) {
    ady.assign(N, vector<int>());
    getComp.assign(N, -1);
    compId = 0;
}

void dfsCC(int u, vector<int> &comp) {
    if (getComp[u] > -1) return;
    getComp[u] = compId;
    comp.push_back(u);
    for (auto &v : ady[u]) dfsCC(v, comp);
}
```

```
// O(N)
vector<vector<int>>> connectedComponents() {
    vector<vector<int>>> comps;
    for (int u = 0; u < ady.size(); u++) {
        vector<int> comp;
        dfsCC(u, comp);
        if (!comp.empty()) comps.push_back(comp),
        ↪ compId++;
    }
    return comps;
}

void addEdge(int u, int v) {
    ady[u].push_back(v);
    ady[v].push_back(u);
}
```

Flood Fill.cpp

```
int n, m, oldColor = 0, color = 1;
vector<vector<int>>> mat;
vector<vector<int>>> movs = {{1, 0}, {0, 1}, {-1, 0},
    ↪ {0, -1}};

void floodFill(int i, int j) {
    if (i >= mat.size() || i < 0 || j >= mat[i].size()
    ↪ || j < 0 || mat[i][j] != oldColor) return;
    mat[i][j] = color;
    for (auto move : movs) floodFill(i + move[1], j +
    ↪ move[0]);
}

void floodFill() {
    for (int i = 0; i < n; i++)
        for (int j = 0; j < m; j++)
            if (mat[i][j] == oldColor) floodFill(i, j);
}
```

Is Bipartite.cpp

```
vector<vector<int>>> ady;

void initVars(int N) {
    ady.assign(N, vector<int>());
}
```

```
// O(N)
bool isBipartite() {
    vector<int> color(ady.size(), -1);
    for (int s = 0; s < ady.size(); s++) {
        if (color[s] > -1) continue;
        color[s] = 0;
        queue<int> q;
        q.push(s);
        while (!q.empty()) {
            int u = q.front();
            q.pop();
            for (int &v : ady[u]) {
                if (color[v] < 0) q.push(v), color[v] =
                ↪ !color[u];
                if (color[v] == color[u]) return false;
            }
        }
    }
    return true;
}
```

LCA.cpp

```
// st = sparse table
typedef pair<int, int> T;
int neutro = 0;
vector<vector<T>>> st;
vector<int> first;
vector<T> tour;
vector<vector<int>>> ady;

void initVars(int N) {
    ady.assign(N, vector<int>());
}

T F(T a, T b) {
    return a.first < b.first ? a : b;
}

void build() {
    st.assign(log2(tour.size()),
    ↪ vector<T>(tour.size()));
    st[0] = tour;
    for (int i = 1; (1 << i) <= tour.size(); i++)
        for (int j = 0; j + (1 << i) <= tour.size(); j++)
            ↪ st[i][j] = F(st[i - 1][j], st[i - 1][j + (1 <<
            ↪ (i - 1))]);
}
```

```

void eulerTour(int u, int p, int h) {
    first[u] = tour.size();
    tour.push_back({h, u});
    for (int v : ady[u])
        if (v != p) {
            eulerTour(v, u, h + 1);
            tour.push_back({h, u});
        }
}

// O(N * lg(N))
void preprocess() {
    tour.clear();
    first.assign(ady.size(), -1);
    eulerTour(0, 0, 0);
    build();
}

// O(1)
int lca(int u, int v) {
    int l = min(first[u], first[v]);
    int r = max(first[u], first[v]);
    int i = log2(r - l + 1);
    return F(st[i][l], st[i][r + 1 - (1 << i)]).second;
}

void addEdge(int u, int v) {
    ady[u].push_back(v);
    ady[v].push_back(u);
}

```

MST Kruskal.cpp

```

// N = number of nodes, Wedge = Weighted Edge
#include "../Data Structures/Graphs/UnionFind.cpp"
typedef int T;
typedef pair<int, int> Edge;
typedef pair<T, Edge> Wedge;
vector<Wedge> Wedges;
vector<Wedge> mst;
UnionFind uf(0);

void initVars(int N) {
    mst.clear();
    Wedges.clear();
    uf = UnionFind(N);
}

T kruskal() {
    T cost = 0;
    sort(Wedges.begin(), Wedges.end());
    // reverse(Wedges.begin(), Wedges.end());
    for (Wedge &wedge : Wedges) {
        int u = wedge.second.first, v =
            ↪ wedge.second.second;
        if (!uf.areConnected(u, v)) uf.join(u, v),
            ↪ mst.push_back(wedge), cost += wedge.first;
    }
    return cost;
}

```

```

void addEdge(int u, int v, T w) {
    Wedges.push_back({w, {u, v}});
}

```

MST Prim.cpp

```

// st = spanning tree, p = parent
// vis = visited, dist = distance
typedef int T;
typedef pair<int, int> Edge;
typedef pair<T, Edge> Wedge;
typedef pair<T, int> DistNode;
int INF = 1 << 30;
vector<vector<int>>> ady;
unordered_map<int, unordered_map<int, T>> weight;
vector<int> p, vis;
vector<T> dist;
vector<vector<Wedge>> msts;

void initVars(int N) {
    ady.assign(N, vector<int>());
    p.assign(N, 0);
    vis.assign(N, 0);
    dist.assign(N, INF);
    weight.clear();
    msts.clear();
}

// O(E * log(V))
T prim(int s) {
    vector<Wedge> mst;
    vector<set<Edge>::iterator> pos(ady.size());
    vector<T> dist(ady.size(), INF);
    set<Edge> q;
    T cost = dist[s] = 0;
    q.insert({0, s});
    while (q.size()) {
        int u = q.begin()->second;
        q.erase(q.begin());
        vis[u] = 1, cost += dist[u];
        mst.push_back({dist[u], {p[u], u}});
        for (int &v : ady[u]) {
            T w = weight[u][v];
            if (!vis[v] && w < dist[v]) {
                if (dist[v] != INF) q.erase(pos[v]);
                pos[v] = q.insert({dist[v] = w, v}).first;
            }
        }
    }
    msts.push_back(vector<Wedge>(mst.begin() + 1,
        ↪ mst.end()));
    return cost;
}

```

```
T primLazy(int s) {
    vector<Wedge> mst;
    vector<set<Edge>::iterator> pos(ady.size());
    vector<T> dist(ady.size(), INF);
    priority_queue<DistNode, vector<DistNode>,
        ⇨ greater<DistNode>> q;
    T cost = dist[s] = 0;
    q.push({0, s});
    while (q.size()) {
        pair<int, int> aux = q.top();
        int u = aux.second;
        q.pop();
        if (dist[u] < aux.first) continue;
        vis[u] = 1, cost += dist[u];
        mst.push_back({dist[u], {p[u], u}});
        for (int &v : ady[u]) {
            T w = weight[u][v];
            if (!vis[v] && w < dist[v]) q.push({dist[v] = w,
                ⇨ v});
        }
    }
    msts.push_back(vector<Wedge>(mst.begin() + 1,
        ⇨ mst.end()));
    return cost;
}
```

*// O(V + E * log(V))*

```
T prim() {
    T cost = 0;
    map<int, T> q;
    for (int i = 0; i < ady.size(); i++)
        if (!vis[i]) cost += prim(i);
    return cost;
}
```

```
void addEdge(int u, int v, T w) {
    ady[u].push_back(v);
    weight[u][v] = w;
    ady[v].push_back(u);
    weight[v][u] = w;
}
```

Strongly Connected Components.cpp

*// tv = top value from stack
 // sccs = strongly connected components
 // scc = strongly connected component
 // disc = discovery time, low = low time
 // s = stack, top = top index of the stack*

```
int Time, top;
vector<vector<int>> ady, sccs;
vector<int> disc, low, s;

void initVars(int N) {
    ady.assign(N, vector<int>());
}
```

```
void dfsSCCS(int u) {
    if (disc[u]) return;
    low[u] = disc[u] = ++Time;
    s[++top] = u;
    for (int &v : ady[u]) dfsSCCS(v), low[u] =
        ⇨ min(low[u], low[v]);
    if (disc[u] == low[u]) {
        vector<int> scc;
        while (true) {
            int tv = s[top--];
            scc.push_back(tv);
            low[tv] = ady.size();
            if (tv == u) break;
        }
        sccs.push_back(scc);
    }
}

// O(N)
void SCCS() {
    s = low = disc = vector<int>(ady.size());
    Time = 0, top = -1, sccs.clear();
    for (int u = 0; u < ady.size(); u++) dfsSCCS(u);
}
```

```
void addEdge(int u, int v) {
    ady[u].push_back(v);
}
```

Topological Sort.cpp

// vis = visited
 vector<vector<int>> ady;
 vector<int> vis, toposorted;

```
void initVars(int N) {
    ady.assign(N, vector<int>());
    vis.assign(N, 0);
    toposorted.clear();
}
```

// returns false if there is a cycle

```
bool toposort(int u) {
    vis[u] = 1;
    for (auto &v : ady[u])
        if (v != u && vis[v] != 2 && (vis[v] ||
            ⇨ !toposort(v))) return false;
    vis[u] = 2;
    toposorted.push_back(u);
    return true;
}
```

// O(N)

```
bool toposort() {
    vis.clear();
    for (int u = 0; u < ady.size(); u++)
        if (!vis[u] && !toposort(u)) return false;
    return true;
}
```

Cycles

Get All Simple Cycles.cpp

Get Some Cycles.cpp

```
// at least detects one cycle per component
vector<vector<int>> ady, cycles;
vector<int> vis, cycle;
bool flag = false, isDirected = false;
int root = -1;

void initVars(int N) {
    ady.assign(N, vector<int>());
    vis.assign(N, 0);
    cycles.clear();
    root = -1, flag = false;
}

// O(N)
bool hasCycle(int u, int prev) {
    vis[u] = 1;
    for (auto &v : ady[u]) {
        if (v == u || vis[v] == 2 || (!isDirected && v ==
            ↪ prev)) continue;
        if (flag) {
            if (!vis[v]) hasCycle(v, u);
            continue;
        }
        if (vis[v] || hasCycle(v, u)) {
            if (root == -1) root = v, flag = true;
            cycle.push_back(u);
            if (root == u) flag = false, root = -1,
                ↪ cycles.push_back(cycle), cycle.clear();
        }
    }
    vis[u] = 2;
    return flag;
}

// O(N)
bool hasCycle() {
    for (int u = 0; u < ady.size(); u++)
        if (!vis[u]) cycle.clear(), hasCycle(u, -1);
    return cycles.size() > 0;
}

void addEdge(int u, int v) {
    ady[u].push_back(v);
    if (!isDirected) ady[v].push_back(u);
}
```

Has Cycle.cpp

```
vector<vector<int>> ady;
vector<int> vis;
bool isDirected = false;
```

```
void initVars(int N) {
    ady.assign(N, vector<int>());
    vis.assign(N, 0);
}

bool hasCycle(int u, int prev) {
    vis[u] = 1;
    for (auto &v : ady[u])
        if (v != u && vis[v] != 2 && (isDirected || v !=
            ↪ prev) && (vis[v] || hasCycle(v, u))) return
            ↪ true;
    vis[u] = 2;
    return false;
}

// O(N)
bool hasCycle() {
    for (int u = 0; u < ady.size(); u++)
        if (!vis[u] && hasCycle(u, -1)) return true;
}

void addEdge(int u, int v) {
    ady[u].push_back(v);
    if (!isDirected) ady[v].push_back(u);
}
```

Flow

Max Flow Dinic.cpp

```
// cap[a][b] = Capacity from a to b
// flow[a][b] = flow occupied from a to b
// level[a] = level in graph of node a

typedef int T;
vector<int> level;
vector<vector<int>> ady;
unordered_map<int, unordered_map<int, T>> cap, flow;

void initVars(int N) {
    ady.assign(N, vector<int>());
    cap.clear();
    flow.clear();
}

bool levelGraph(int s, int t) {
    level = vector<int>(ady.size());
    level[s] = 1;
    queue<int> q;
    q.push(s);
    while (!q.empty()) {
        int u = q.front();
        q.pop();
        for (int &v : ady[u]) {
            if (!level[v] && flow[u][v] < cap[u][v]) {
                q.push(v);
                level[v] = level[u] + 1;
            }
        }
    }
    return level[t];
}
```

```

T blockingFlow(int u, int t, T currPathMaxFlow) {
    if (u == t) return currPathMaxFlow;
    for (int v : ady[u]) {
        T capleft = cap[u][v] - flow[u][v];
        if ((level[v] == (level[u] + 1)) && (capleft > 0))
            ↪ {
                T pathMaxFlow = blockingFlow(v, t,
                    ↪ min(currPathMaxFlow, capleft));
                if (pathMaxFlow > 0) {
                    flow[u][v] += pathMaxFlow;
                    flow[v][u] -= pathMaxFlow;
                    return pathMaxFlow;
                }
            }
    }
    return 0;
}

// O(E * V^2)
T dinicMaxFlow(int s, int t) {
    if (s == t) return -1;
    T maxFlow = 0;
    while (levelGraph(s, t))
        while (T flow = blockingFlow(s, t, 1 << 30))
            ↪ maxFlow += flow;
    return maxFlow;
}

void addEdge(int u, int v, T capacity) {
    cap[u][v] = capacity;
    ady[u].push_back(v);
}

```

Maximum Bipartite Matching.cpp

```
#include "Max Flow Dinic.cpp"
```

```

void addEdge(int u, int v) {
    cap[u][v] = 1;
    ady[u].push_back(v);
}

int main() {
    int n, s = 0, t = 1;
    cin >> n;
    initVars(n);
    while (n--) {
        int u, v;
        cin >> u >> v;
        addEdge(u += 2, v += 2);
        addEdge(s, u);
        addEdge(v, t);
    }
    cout << dinicMaxFlow(s, t) << endl;
    return 0;
}

```

ShortestPaths

Bellman Ford.cpp

```

// N = number of nodes
// returns {} if there is a negative weight cycle
typedef int T;
int MAXN = 20001, N, INF = 1 << 30, isDirected = true;
vector<vector<int>>> ady;
unordered_map<int, unordered_map<int, T>> weight;

void initVars(int N) {
    ady.assign(N, vector<int>());
    weight.clear();
}

// O(V * E)
vector<T> bellmanFord(int s) {
    vector<T> dist(ady.size(), INF);
    dist[s] = 0;
    for (int i = 1; i <= ady.size(); i++)
        for (int u = 0; u < ady.size(); u++)
            for (auto &v : ady[u]) {
                T w = weight[u][v];
                if (dist[u] != INF && dist[u] + w < dist[v]) {
                    if (i == ady.size()) return {};
                    dist[v] = dist[u] + w;
                }
            }
    return dist;
}

void addEdge(int u, int v, T w) {
    ady[u].push_back(v);
    weight[u][v] = w;
    if (isDirected) return;
    ady[v].push_back(u);
    weight[v][u] = w;
}

```

Dijkstra.cpp

```

typedef int T;
typedef pair<T, int> DistNode;
int MAXN = 20001, INF = 1 << 30, isDirected = false;
vector<vector<int>>> ady;
unordered_map<int, unordered_map<int, T>> weight;

void initVars(int N) {
    ady.assign(N, vector<int>());
    weight.clear();
}

```



```
// O(E * lg(V))
vector<int> dijkstra(int s) {
    vector<set<DistNode>::iterator> pos(ady.size());
    vector<T> dist(ady.size(), INF);
    set<DistNode> q;
    q.insert({0, s}), dist[s] = 0;
    while (q.size()) {
        int u = q.begin()->second;
        q.erase(q.begin());
        for (int &v : ady[u]) {
            T w = weight[u][v];
            if (dist[u] + w < dist[v]) {
                if (dist[v] != INF) q.erase(pos[v]);
                pos[v] = q.insert({dist[v] = dist[u] + w,
                                   ↪ v}).first;
            }
        }
    }
    return dist;
}

vector<int> dijkstraLazy(int s) {
    vector<int> dist(ady.size(), INF);
    priority_queue<DistNode, vector<DistNode>,
    ↪ greater<DistNode>> q;
    q.push({0, s}), dist[s] = 0;
    while (q.size()) {
        DistNode top = q.top(); q.pop();
        int u = top.second;
        if (dist[u] < top.first) continue;
        for (int &v : ady[u]) {
            T w = weight[u][v];
            if (dist[u] + w < dist[v]) q.push({dist[v] =
            ↪ dist[u] + w, v});
        }
    }
    return dist;
}

void addEdge(int u, int v, T w) {
    ady[u].push_back(v);
    weight[u][v] = w;
    if (isDirected) return;
    ady[v].push_back(u);
    weight[v][u] = w;
}
```

Maths

Number Theory

Divisibility Criterion.py

```
def divisorCriteria(n, lim):
    results = []
    tenElevated = 1
    for i in range(lim):
        # remainder = pow(10, i, n)
        remainder = tenElevated % n
        negremainder = remainder - n
        if (remainder <= abs(negremainder)):
            results.append(remainder)
        else:
            results.append(negremainder)
        tenElevated *= 10
    return results

def testDivisibility(dividend, divisor,
    ↪ divisor_criteria):
    dividend = str(dividend)
    addition = 0
    dividendSize = len(dividend)
    i = dividendSize - 1
    j = 0
    while j < dividendSize:
        addition += int(dividend[i]) *
        ↪ divisor_criteria[j]
        i -= 1
        j += 1
    return addition % divisor == 0

if __name__ == '__main__':
    dividend, divisor = map(int, input().split())
    divisor_criteria = divisorCriteria(divisor,
    ↪ len(str(dividend)))
    print(divisor_criteria)
    print(testDivisibility(dividend, divisor,
    ↪ divisor_criteria))
```


Extended Euclidean.cpp

```
// gcd(a, b) = ax + by
vector<long long int> extendedGCD(long long int a,
    ↪ long long int b) {
    if (a > 0LL && b == 0LL) {
        return {a, 1LL, 0LL};
    }
    long long int x = 1LL, y = 0LL, prevx = 0LL, prevy =
    ↪ 1LL, q, remainder;
    while (true) {
        q = a / b;
        remainder = a - b * q;
        if (remainder == 0LL) break;
        a = b;
        b = remainder;
        x = x - prevx * q;
        swap(x, prevx);
        y = y - prevy * q;
        swap(y, prevy);
    }
    // gcd = b, x = prevx, y = prevy
    return {b, prevx, prevy};
}
```

GCD.cpp

```
// recursive
int gcd(int a, int b) {
    return !b ? a : gcd(b, a % b);
}

// iterative
int gcd(int a, int b) {
    while (b) {
        a %= b;
        swap(a, b);
    }
    return a;
}
```

LCM.cpp

```
int lcm(int a, int b) {
    int c = gcd(a, b);
    return c ? a / c * b : 0;
}
```

Prime Check Miller Rabin.py

```
from random import randrange

def is_prime(p):
    k = 100
    if p == 2 or p == 3:
        return True
    if (p & 1) == 0 or p == 1:
        return False
    phi = p - 1
    d = phi
    r = 0
    while (d & 1) == 0:
        d = int(d >> 1)
        r += 1
    for i in range(k):
        a = randrange(2, p - 2)
        exp = pow(a, d, p)
        if exp == 1 or exp == p - 1:
            continue
        flag = False
        for j in range(r - 1):
            exp = pow(exp, 2, p)
            if exp == 1:
                return False
            if exp == p - 1:
                flag = True
                break
        if flag:
            continue
        else:
            return False
    return True
```

Prime Sieve.cpp

```
vector<int> primeSieve(int n) {
    vector<int> sieve(n + 1);
    for (int i = 4; i <= n; i += 2) sieve[i] = 2;
    for (int i = 3; i * i <= n; i += 2)
        if (!sieve[i])
            for (int j = i * i; j <= n; j += 2 * i)
                if (!sieve[j]) sieve[j] = i;
    return sieve;
}
```

Strings

KMP.cpp

```
// p = pattern, t = text
// f = error function, cf = create error function
// pos = positions where pattern is found in text

int MAXN = 1000000;
vector<int> f(MAXN + 1);

vector<int> kmp(string &p, string &t, int cf) {
    vector<int> pos;
    if (cf) f[0] = -1;
    for (int i = cf, j = 0; j < t.size(); i = f[i]) {
        while (i > -1 && p[i] != t[j]) i = f[i];
        i++, j++;
        if (cf) f[j] = i;
        if (!cf && i == p.size()) pos.push_back(j - i), i = f[i];
    }
    return pos;
}

vector<int> search(string &p, string &t) {
    kmp(p, p, -1); // create error function
    return kmp(p, t, 0); // search in text
}
```

Rabin Karp.cpp

```
class RollingHash {
public:
    vector<unsigned long long int> pow;
    vector<unsigned long long int> hash;
    unsigned long long int B;

    RollingHash(const string &text) : B(257) {
        int N = text.size();
        pow.resize(N + 1);
        hash.resize(N + 1);
        pow[0] = 1;
        hash[0] = 0;
        for (int i = 1; i <= N; ++i) {
            // in c++ an unsigned long long int is
            // automatically modulated by 2^64
            pow[i] = pow[i - 1] * B;
            hash[i] = hash[i - 1] * B + text[i - 1];
        }
    }

    unsigned long long int getWordHash() {
        return hash[hash.size() - 1];
    }

    unsigned long long int getSubstrHash(int begin,
        ↪ int end) {
        return hash[end] - hash[begin - 1] * pow[end -
        ↪ begin + 1];
    }
}
```

```
int size() {
    return hash.size();
}

};

vector<int> rabinKarp(RollingHash &rhStr, string
    ↪ &pattern) {
    vector<int> positions;
    RollingHash rhPattern(pattern);
    unsigned long long int patternHash =
        ↪ rhPattern.getWordHash();
    int windowSize = pattern.size(), end = windowSize;
    for (int i = 1; end < rhStr.size(); i++) {
        if (patternHash == rhStr.getSubstrHash(i, end))
            ↪ positions.push_back(i);
        end = i + windowSize;
    }
    return positions;
}
```

Techniques

Binary Search.cpp

Multiple Queries

Mo.cpp

```
// q = query
// qs = queries

struct Query {
    int l, r;
};

int blksize;
vector<Query> qs;
vector<int> arr;

void initVars(int N, int M) {
    arr = vector<int>(N);
    qs = vector<Query>(M);
}

bool cmp(Query &a, Query &b) {
    if (a.l == b.l) return a.r < b.r;
    return a.l / blksize < b.l / blksize;
}
```

```

void getResults() {
    blksize = (int)sqrt(arr.size());
    sort(qs.begin(), qs.end(), cmp);
    int prevL = 0, prevR = -1;
    int sum = 0;
    for (auto &q : qs) {
        int L = q.l, R = q.r;
        while (prevL < L) {
            sum -= arr[prevL]; // problem specific
            prevL++;
        }
        while (prevL > L) {
            prevL--;
            sum += arr[prevL]; // problem specific
        }
        while (prevR < R) {
            prevR++;
            sum += arr[prevR]; // problem specific
        }
        while (prevR > R) {
            sum -= arr[prevR]; // problem specific
            prevR--;
        }

        cout << "sum[" << L << ", " << R << "] = " << sum
              << endl;
    }
}

int main() {
    initVars(9, 2);
    arr = {1, 1, 2, 1, 3, 4, 5, 2, 8};
    qs = {{0, 8}, {3, 5}};
    getResults();
}

```

SQRT Decomposition.cpp

```

// sum of elements in range
int neutro = 0;
vector<int> arr;
vector<int> blks;
void initVars(int n) {
    arr.assign(n, neutro);
    blks.assign(sqrt(n), neutro);
}

void preprocess() {
    for (int i = 0, j = 0; i < arr.size(); i++) {
        if (i == blks.size() * j) j++;
        blks[j - 1] += arr[i]; // problem specific
    }
}

// problem specific
void update(int i, int val) {
    blks[i / blks.size()] += val - arr[i];
    arr[i] = val;
}

```

```

int query(int l, int r) {
    int sum = 0;
    int lblk = l / blks.size();
    if (l != blks.size() * lblk++)
        while (l < r && l != lblk * blks.size()) {
            sum += arr[l]; // problem specific
            l++;
        }

    while (l + blks.size() <= r) {
        sum += blks[l / blks.size()]; // problem specific
        l += blks.size();
    }
    while (l <= r) {
        sum += arr[l]; // problem specific
        l++;
    }
    return sum;
}

int main() {
    initVars(10);
    arr = {1, 5, 2, 4, 6, 1, 3, 5, 7, 10};
    preprocess();
    for (int i = 0; i < blks.size() + 1; i++) cout <<
        blks[i] << " ";
    // output: 8 11 15 10
    cout << endl;
    cout << query(3, 8) << " ";
    cout << query(1, 6) << " ";
    update(8, 0);
    cout << query(8, 8) << endl;
    // output: 26 21 0
    return 0;
}

```