ACM-ICPC-REFERENCE

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Contents

1 Coding Resources

1.1 C++

1.1.1 Decimal Precision

```
// rounds up the decimal number
cout << setprecision(N) << n << endl;
// specify N fixed number of decimals
cout << fixed << setprecision(N) << n << endl;
```

1.1.2 IO Optimization

```
int main() {
  ios_base::sync_with_stdio(0);
  cin.tie(0);
}
```

1.1.3 Int To Binary

```
typedef long long int lli;

lli bitsInInt(lli n) {
  return floor(log2(n) + 1LL);
}

vector<int> intToBitsArray(lli n) {
  n = abs(n);
  if (!n) {
    vector<int> v;
    return v;
  }
  int length = bitsInInt(n);
  int lastPos = length - 1;
  vector<int> v(length);
  for (lli i = lastPos, j = 0; i > -1LL;
       i--, j++) {
    lli aux = (n >> i) & 1LL;
    v[j] = aux;
  }
  return v;
}
```

1.1.4 Map Value To Int

```
typedef string Key;
unordered_map<Key, int> val;
unordered_map<int, Key> getKey;
int mapId = 0;

int Map(Key key) {
  getKey[mapId] = key;
  return val.count(key) ? val[key]
                        : val[key] = mapId++;
}

void initMapping() {
  mapId = 0;
  val.clear();
}
```

1.1.5 Permutations

```
typedef vector<int> T;// typedef string T;
vector<T> permutations(T v) {
  vector<vector<int>> ans;
  sort(v.begin(), v.end());
  do
    ans.push_back(v);
  while (next_permutation(v.begin(), v.end()));
  return ans;
}
```

1.1.6 Print Vector

```
void printv(vector<int> v) {
  if (v.size() == 0) {
    cout << "[]" << endl;
    return;
  }
  cout << "[" << v[0];
  for (int i = 1; i < v.size(); i++) {
    cout << ", " << v[i];
  }
  cout << "]" << endl;
}
```

1.1.7 Priority Queue Of Object

```
struct Object {
  char first;
  int second;
};

int main() {
  auto cmp = [](const Object& a,
                const Object& b) {
    return a.second > b.second;
  };
  priority_queue<Object, vector<Object>,
                 decltype(cmp)>
      pq(cmp);
  vector<Object> v = {
      {'c', 3}, {'a', 1}, {'b', 2}};
  sort(v.begin(), v.end(), cmp);
  return 0;
}
```

1.1.8 Random

```
int random(int min, int max) {
  return min + rand() % (max - min + 1);
}

int main() {
  srand(time(0));
  // code
}
```

1.1.9 Read Line

```cpp
// when reading lines, don't mix 'cin' with
// 'getline' just use getline and split
string input() {
  string ans;
  // cin >> ws; // eats all whitespaces.
  getline(cin, ans);
  return ans;
}
```

1.1.10 Sort Pair

```cpp
pair<int, int> p;
sort(p.begin(), p.end());
// sorts array on the basis of the first element
```

1.1.11 Sort Vector Of Object

```cpp
struct Object {
  char first;
  int second;
};

bool cmp(const Object& a, const Object& b) {
  return a.second > b.second;
}

int main() {
  vector<Object> v = {
      {'c', 3}, {'a', 1}, {'b', 2}};
  sort(v.begin(), v.end(), cmp);
  printv(v);
  return 0;
}
```

1.1.12 Split String

```cpp
vector<string> split(string str, char token) {
  stringstream test(str);
  string seg;
  vector<string> seglist;
  while (getline(test, seg, token))
    seglist.push_back(seg);
  return seglist;
}
```

1.1.13 Typedef

```cpp
typedef TYPE ALIAS
// e.g.
typedef int T;
```

1.2 Python

1.2.1 Combinations

```python
import itertools
#from arr choose k = > combinations(arr, k)
print(list(itertools.combinations([1, 2, 3], 3)))
```

1.2.2 Fast IO

```python
from sys import stdin, stdout

N = 10
#Reads N chars from stdin(it counts '\n' as char)
stdin.read(N)
#Reads until '\n' or EOF
line = stdin.readline()
#Reads all lines in stdin until EOF
lines = stdin.readlines()
#Writes a string to stdout, it doesn 't adds '\n'
stdout.write(line)
#Writes a list of strings to stdout
stdout.writelines(lines)
#Reads numbers separated by space in a line
numbers = list(map(int, stdin.readline().split()))
```

1.2.3 Permutations

```python
import itertools
print(list(itertools.permutations([1, 2, 3])))
```

1.2.4 Random

```python
import random
# Initialize the random number generator.
random.seed(None)
# Returns a random integer N such that a <= N <=
↪  b.
random.randint(a, b)
# Returns a random integer N such that 0 <= N < b
random.randrange(b)
# Returns a random integer N such that a <= N <
↪  b.
random.randrange(a, b)
# Returns and integer with k random bits.
random.getrandbits(k)
# shuffles a list
random.shuffle(li)
```

1.2.5 Sort List Of Object

```python
class MyObject :
  def __init__(self, first, second, third):
    self.first = first
    self.second = second
    self.third = third

li = [MyObject('b', 3, 1), MyObject('a', 3, 2),
↪  MyObject('b', 3, 3)]
# returns list sorted by first then by second then
↪  by third in increasing order
ol = sorted(li, key = lambda x: (x.first,
↪  x.second, x.third), reverse=False)
# sorts inplace by first then by second then by
↪  third in increasing order
li.sort(key = lambda x: (x.first, x.second,
↪  x.third), reverse=False)
```

1.2.6 Sort List

```python
li = ['a', 'c', 'b']
# sorts inplace in descending order
li.sort(reverse=True)
# returns sorted list ascending order
ol = sorted(li)
```

2 Data Structures

2.1 BIT

2.2 Interval Tree

2.3 Segment Tree

```cpp
// st = segment tree. st[1] = root;
// neutro = operation neutral value
// e.g. for sum is 0, for multiplication
// is 1, for gcd is 0, for min is INF, etc.
int MAXN = 500000, N;
vector<int> st, arr;
typedef int T;
const T neutro = 0;

void initVars() {
  st = vector<int>(2 * MAXN, neutro);
}

const T F(T a, T b) {
  // return a + b;
  return __gcd(a, b);
  // return a * b;
  // return min(a, b);
}

// O(2N)
int build() {
  copy(arr.begin(), arr.end(), st.begin() + N);
  for (int i = N - 1; i > 0; i--)
    st[i] = F(st[i << 1], st[i << 1 | 1]);
}

// O(lg(2N))
void updateNode(int i, T val) {
  for (st[i += N] = val; i > 1; i >>= 1)
    st[i >> 1] = F(st[i], st[i ^ 1]);
}

// O(3N), [l, r)
void updateRange(int l, int r, T val) {
  for (int i = l; i < r; i++)
    arr[i] = val;
  build();
}

// O(lg(2N)), [l, r)
T query(int l, int r) {
  int ans = neutro;
  for (l += N, r += N; l < r; l >>= 1, r >>= 1) {
    if (l & 1) ans = F(ans, st[l++]);
    if (r & 1) ans = F(ans, st[--r]);
  }
  return ans;
}
```

2.4 Sparse Table

```cpp
#include <bits/stdc++.h>

using namespace std;
// st = sparse table
typedef int T;

int MAXN = 100, N;
vector<vector<T>> st;
vector<T> arr;

void initVars() {
  st = vector<vector<T>>(
      MAXN, vector<T>(log2(MAXN) + 1));
  arr = vector<T>(MAXN);
}

static T F1(T a, T b) {
  // return min(a, b);
  return __gcd(a, b);
}

static T F2(T a, T b) {
  return a + b;
  // return a * b;
}

// O(NlgN)
void buildSparseTabe(T F(T, T)) {
  st[0] = arr;
  for (int i = 1; (1 << i) <= N; i++)
    for (int j = 0; j + (1 << i) <= N; j++)
      st[i][j] = F(st[i - 1][j],
                   st[i - 1][j + (1 << (i - 1))]);
}

// O(1)
T query(int L, int R) {
  int i = log2(R - L + 1);
  return F1(st[i][L], st[i][R + 1 - (1 << i)]);
}

// O(lgN)
T queryArith(int L, int R) {
  // Neutral Element
  T ans = 0;  // for sum
  // T ans = 1; for multiplication
```

```
  while (true) {
    int k = log2(R - L + 1);
    ans = F2(ans, st[k][L]);
    L += 1 << k;
    if (L > R) break;
  }
  return ans;
}
int main() {
  initVars();
  N = 9;
  arr = {7, 2, 3, 0, 5, 10, 3, 12, 18};
  buildSparseTabe(F1);

  cout << query(0, 2) << endl;
  cout << query(1, 3) << endl;
  cout << query(4, 5) << endl;

  initVars();
  N = 6;
  arr = {3, 7, 2, 5, 8, 9};
  buildSparseTabe(F2);
  cout << queryArith(0, 5) << endl;
  cout << queryArith(3, 5) << endl;
  cout << queryArith(2, 4) << endl;
  return 0;
}
```

2.5 Trie

```
// wpt = number of words passing through
// w = number of words ending in the node
// c = character

struct Trie {
  struct Node {
    // for lexicographical order use 'map'
    // map<char, Node *> ch;
    unordered_map<char, Node *> ch;
    int w = 0, wpt = 0;
  };

  Node *root = new Node();

  // O(STR.SIZE)
  void insert(string str) {
    Node *curr = root;
    for (auto &c : str) {
      curr->wpt++;
      if (!curr->ch.count(c))
        curr->ch[c] = new Node();
      curr = curr->ch[c];
    }
    curr->wpt++;
    curr->w++;
  }

  Node *find(string &str) {
    Node *curr = root;
    for (auto &c : str) {
      if (!curr->ch.count(c)) return nullptr;
      curr = curr->ch[c];
    }
    return curr;
  }

  // number of words with given prefix O(N)
  int prefixCount(string prefix) {
    Node *node = find(prefix);
    return node ? node->wpt : 0;
  }
  // number of words matching str O(N)
  int strCount(string str) {
    Node *node = find(str);
    return node ? node->w : 0;
  }

  void getWords(Node *curr, vector<string> &words,
                string &word) {
    if (!curr) return;
    if (curr->w) words.push_back(word);
    for (auto &c : curr->ch) {
      getWords(c.second, words, word += c.first);
      word.pop_back();
    }
  }

  // O(N)
  vector<string> getWords() {
    vector<string> words;
    string word = "";
    getWords(root, words, word);
    return words;
  }

  // O(N)
  vector<string> getWordsByPrefix(string prefix) {
    vector<string> words;
    getWords(find(prefix), words, prefix);
  }

  // O(N)
  bool remove(Node *curr, string &str, int &i) {
    if (i == str.size()) {
      curr->wpt--;
      return curr->w ? !(curr->w = 0) : 0;
    }
    int c = str[i];
    if (!curr->ch.count(c)) return false;
    if (remove(curr->ch[c], str, ++i)) {
      if (!curr->ch[c]->wpt)
        curr->wpt--, curr->ch.erase(c);
      return true;
    }
    return false;
  }

  int remove(string str) {
    int i = 0;
```

```
    return remove(root, str, i);
  }
};
```

2.6 UnionFind

```
struct UnionFind {
  vector<int> dad, size;
  int n;
  UnionFind(int N) : n(N), dad(N), size(N, 1) {
    while (--N) dad[N] = N;
  }

  int root(int u) {
    if (dad[u] == u) return u;
    return dad[u] = root(dad[u]);
  }

  bool areConnected(int u, int v) {
    return root(u) == root(v);
  }

  void join(int u, int v) {
    int Ru = root(u), Rv = root(v);
    if (Ru == Rv) return;
    --n, dad[Ru] = Rv;
    size[Rv] += size[Ru];
  }

  int getSize(int u) {
    return size[root(u)];
  }

  int numberOfSets() {
    return n;
  }
};
```

2.7 try

```
#include <bits/stdc++.h>

using namespace std;

int main() {
  vector<int> arr = {1, 2, 3, 4, 5};
  vector<int> ar(10);
  // copy(arr.begin(), arr.end(), ar.begin() +
  ↪  5);
  for (auto &i : ar)
    cout << i << " ";
  cout << endl;
  return 0;
}
```

3 Geometry

4 Graphs

4.1 Articulation Points And Bridges

```
// APB = articulation points and bridges
// ap = Articulation Point
// br = bridges
// p = parent
// disc = discovery time
// low = lowTime
// ch = children

typedef pair<int, int> Edge;
int MAXN = 101, N = 7, Time;
vector<vector<int>> ady;
vector<int> disc, low, ap;
vector<Edge> br;

void initVars() {
  ady = vector<vector<int>>(MAXN, vector<int>());
}

int dfsAPB(int u, int p) {
  int ch = 0;
  low[u] = disc[u] = ++Time;
  for (int &v : ady[u]) {
    if (v == p) continue;
    if (!disc[v]) {
      ch++;
      dfsAPB(v, u);
      if (disc[u] <= low[v]) ap[u]++;
      if (disc[u] < low[v]) br.push_back({u, v});
      low[u] = min(low[u], low[v]);
    } else
      low[u] = min(low[u], disc[v]);
  }
  return ch;
}

// O(N)
void APB() {
  br.clear();
  ap = low = disc = vector<int>(MAXN);
  Time = 0;
  for (int u = 0; u < N; u++)
    if (!disc[u]) ap[u] = dfsAPB(u, u) > 1;
}

void addEdge(int u, int v) {
  ady[u].push_back(v);
  ady[v].push_back(u);
}
```

4.2 Connected Components

```
// comp = component
int MAXN = 26, N, compId = 1;
vector<vector<int>> ady;
```

```
vector<int> getComp;

void initVars() {
  ady = vector<vector<int>>(MAXN, vector<int>());
  getComp = vector<int>(MAXN);
}

void dfsCC(int u, vector<int> &comp) {
  if (getComp[u]) return;
  getComp[u] = compId;
  comp.push_back(u);
  for (auto &v : ady[u]) dfsCC(v, comp);
}

// O(N)
vector<vector<int>> connectedComponents() {
  vector<vector<int>> comps;
  for (int u = 0; u < N; u++) {
    vector<int> comp;
    dfsCC(u, comp);
    compId++;
    if (!comp.empty()) comps.push_back(comp);
  }
  return comps;
}

void addEdge(int u, int v) {
  ady[u].push_back(v);
  ady[v].push_back(u);
}
```

4.3 Cycle In Directed Graph

```
int n;                      // max node id >= 0
vector<vector<int>> ady;    // ady.resize(n)
vector<int> vis;            // vis.resize(n)
vector<vector<int>> cycles;
vector<int> cycle;
bool flag = false;
int rootNode = -1;

bool hasDirectedCycle(int u) {
  vis[u] = 1;
  for (auto &v : ady[u]) {
    if (v == u || vis[v] == 2) continue;
    if (vis[v] == 1 || hasDirectedCycle(v)) {
      if (rootNode == -1)
        rootNode = v, flag = true;
      if (flag) {
        cycle.push_back(u);
        if (rootNode == u) flag = false;
      }
      return true;
    }
  }
  vis[u] = 2;
  return false;
}

// O(N)
bool hasDirectedCycle() {
  vis.clear();
  for (int u = 0; u < n; u++)
    if (!vis[u]) {
      cycle.clear();
      if (hasDirectedCycle(u))
        cycles.push_back(cycle);
    }
  return cycles.size() > 0;
}
```

4.4 Cycle In Undirected Graph

```
int n;                      // max node id >= 0
vector<vector<int>> ady;    // ady.resize(n)
vector<bool> vis;           // vis.resize(n)
vector<vector<int>> cycles;
vector<int> cycle;
bool flag = false;
int rootNode = -1;

bool hasUndirectedCycle(int u, int prev) {
  vis[u] = true;
  for (auto &v : ady[u]) {
    if (v == u || v == prev) continue;
    if (vis[v] || hasUndirectedCycle(v, u)) {
      if (rootNode == -1)
        rootNode = v, flag = true;
      if (flag) {
        cycle.push_back(u);
        if (rootNode == u) flag = false;
      }
      return true;
    }
  }
  return false;
}

// O(N)
bool hasUndirectedCycle() {
  vis.clear();
  for (int u = 0; u < n; u++)
    if (!vis[u]) {
      cycle.clear();
      if (hasUndirectedCycle(u, -1))
        cycles.push_back(cycle);
    }
  return cycles.size() > 0;
}
```

4.5 Flood Fill

```
int n, m, oldColor = 0, color = 1;
vector<vector<int>> mat;

vector<vector<int>> movs = {
    {1, 0}, {0, 1}, {-1, 0}, {0, -1}};

void floodFill(int i, int j) {
```

```
  if (i >= mat.size() || i < 0 ||
      j >= mat[i].size() || j < 0 ||
      mat[i][j] != oldColor)
    return;
  mat[i][j] = color;
  for (auto move : movs)
    floodFill(i + move[1], j + move[0]);
}

void floodFill() {
  for (int i = 0; i < n; i++)
    for (int j = 0; j < m; j++)
      if (mat[i][j] == oldColor) floodFill(i, j);
}
```

4.6 Flow

4.6.1 Max Flow Dinic

```
// cap[a][b] = Capacity from a to b
// flow[a][b] = flow occupied from a to b
// level[a] = level in graph of node a
// Num = number
typedef int Num;
int N, MAXN = 101;
vector<int> level;
vector<vector<int>> ady, cap, flow;

void initVars() {
  ady = vector<vector<int>>(MAXN, vector<int>());
  cap = vector<vector<int>>(MAXN,
  ↪  vector<int>(MAXN));
  flow = vector<vector<int>>(MAXN,
  ↪  vector<int>(MAXN));
}

bool levelGraph(int s, int t) {
  level = vector<int>(MAXN);
  level[s] = 1;
  queue<int> q;
  q.push(s);
  while (!q.empty()) {
    int u = q.front();
    q.pop();
    for (int &v : ady[u]) {
      if (!level[v] && flow[u][v] < cap[u][v]) {
        q.push(v);
        level[v] = level[u] + 1;
      }
    }
  }
  return level[t];
}

Num blockingFlow(int u, int t,
                 Num currPathMaxFlow) {
  if (u == t) return currPathMaxFlow;
  for (int v : ady[u]) {
    Num capleft = cap[u][v] - flow[u][v];
    if ((level[v] == (level[u] + 1)) &&
        (capleft > 0)) {
      Num pathMaxFlow = blockingFlow(
          v, t, min(currPathMaxFlow, capleft));
      if (pathMaxFlow > 0) {
        flow[u][v] += pathMaxFlow;
        flow[v][u] -= pathMaxFlow;
        return pathMaxFlow;
      }
    }
  }
  return 0;
}

// O(E * V^2)
Num dinicMaxFlow(int s, int t) {
  if (s == t) return -1;
  Num maxFlow = 0;
  while (levelGraph(s, t))
    while (Num flow = blockingFlow(s, t, 1 << 30))
      maxFlow += flow;
  return maxFlow;
}

void addEdge(int u, int v, Num capacity) {
  cap[u][v] = capacity;
  ady[u].push_back(v);
}
```

4.7 Is Bipartite

```
int n;                      // max node id >= 0
vector<vector<int>> ady;    // ady.resize(n)

// O(N)
bool isBipartite() {
  vector<int> color(n, -1);
  for (int s = 0; s < n; s++) {
    if (color[s] > -1) continue;
    color[s] = 0;
    queue<int> q;
    q.push(s);
    while (!q.empty()) {
      int u = q.front();
      q.pop();
      for (int &v : ady[u]) {
        if (color[v] < 0)
          q.push(v), color[v] = !color[u];
        if (color[v] == color[u]) return false;
      }
    }
  }
  return true;
}
```

4.8 Kruskal MST

```
typedef int Weight;
typedef pair<int, int> Edge;
typedef pair<Weight, Edge> Wedge;
```

```
vector<Wedge> Wedges;  // gets filled from input;
vector<Wedge> mst;

int kruskal() {
  int cost = 0;
  sort(Wedges.begin(), Wedges.end());
  // reverse(Wedges.begin(), Wedges.end());
  UnionFind uf(N);
  for (Wedge &wedge : Wedges) {
    int u = wedge.second.first,
        v = wedge.second.second;
    if (!uf.areConnected(u, v))
      uf.join(u, v), mst.push_back(wedge),
          cost += wedge.first;
  }
  return cost;
}
```

4.9 LCA

4.10 Maximum Bipartite Matching

```
#include "Flow/Max Flow Dinic.cpp"

void addEdge(int u, int v) {
  cap[u][v] = 1;
  ady[u].push_back(v);
}

int main() {
  initVars();
  int m, s = 0, t = 1;
  cin >> m;
  while (m--) {
    int u, v;
    cin >> u >> v;
    addEdge(u += 2, v += 2);
    addEdge(s, u);
    addEdge(v, t);
  }
  cout << dinicMaxFlow(s, t) << endl;
  return 0;
}
```

4.11 ShortestPaths

4.11.1 Bellman Ford

```
typedef int Weight;
int MAXN = 20001, N, INF = 1 << 30,
    isDirected = true;
vector<vector<int>> ady, weight;

void initVars() {
  ady = vector<vector<int>>(MAXN, vector<int>());
  weight = vector<vector<int>>(
      MAXN, vector<int>(MAXN, INF));
}

// O(N^2)
vector<Weight> bellmanFord(int s) {
  vector<Weight> dist(MAXN, INF);
  dist[s] = 0;
  for (int i = 0; i <= N; i++)
    for (int u = 0; u < N; u++)
      for (auto &v : ady[u]) {
        Weight w = weight[u][v];
        if (dist[u] != INF &&
            dist[v] > dist[u] + w) {
          if (i == N) return vector<Weight>();
          dist[v] = dist[u] + w;
        }
      }
  return dist;
}

void addEdge(int u, int v, Weight w) {
  ady[u].push_back(v);
  weight[u][v] = w;
  if (isDirected) return;
  ady[v].push_back(u);
  weight[v][u] = w;
}
```

4.11.2 Dijkstra

```
typedef int Weight;
typedef pair<Weight, int> NodeDist;
int MAXN = 20001, INF = 1 << 30,
    isDirected = false;
vector<vector<int>> ady, weight;

void initVars() {
  ady = vector<vector<int>>(MAXN, vector<int>());
  weight = vector<vector<int>>(
      MAXN, vector<int>(MAXN, INF));
}

vector<Weight> dijkstra(int s) {
  vector<int> dist(MAXN, INF);
  set<NodeDist> q;
  q.insert({0, s});
  dist[s] = 0;
  while (!q.empty()) {
    NodeDist nd = *q.begin();
    q.erase(nd);
    int u = nd.second;
    for (int &v : ady[u]) {
      Weight w = weight[u][v];
      if (dist[v] > dist[u] + w) {
        if (dist[v] != INF) q.erase({dist[v], v});
        dist[v] = dist[u] + w;
        q.insert({dist[v], v});
      }
    }
  }
```

```
  return dist;
}

void addEdge(int u, int v, Weight w) {
  ady[u].push_back(v);
  weight[u][v] = w;
  if (isDirected) return;
  ady[v].push_back(u);
  weight[v][u] = w;
}
```

4.12 Strongly Connected Components

```
// tv = top value from stack
// sccs = strongly connected components
// scc = strongly connected component
// disc = discovery time
// low = low time
// s = stack
// top = top index of the stack

int MAXN = 101, N = 7, Time, top;
vector<vector<int>> ady, sccs;
vector<int> disc, low, s;

void initVars() {
  ady = vector<vector<int>>(MAXN, vector<int>());
}

void dfsSCCS(int u) {
  if (disc[u]) return;
  low[u] = disc[u] = ++Time;
  s[++top] = u;
  for (int &v : ady[u]) {
    dfsSCCS(v);
    low[u] = min(low[u], low[v]);
  }
  if (disc[u] == low[u]) {
    vector<int> scc;
    while (true) {
      int tv = s[top--];
      scc.push_back(tv);
      low[tv] = N;
      if (tv == u) break;
    }
    sccs.push_back(scc);
  }
}

// O(N)
void SCCS() {
  s = low = disc = vector<int>(MAXN);
  Time = 0, top = -1, sccs.clear();
  for (int u = 0; u < N; u++) dfsSCCS(u);
}

void addEdge(int u, int v) {
  ady[u].push_back(v);
}
```

4.13 Topological Sort

```
int n;                      // max node id >= 0
vector<vector<int>> ady;    // ady.resize(n)
vector<int> vis;            // vis.resize(n)
vector<int> toposorted;

bool toposort(int u) {
  vis[u] = 1;
  for (auto &v : ady[u]) {
    if (v == u || vis[v] == 2) continue;
    if (vis[v] == 1 || !toposort(v)) return false;
  }
  vis[u] = 2;
  toposorted.push_back(u);
  return true;
}

// O(N)
bool toposort() {
  vis.clear();
  for (int u = 0; u < n; u++)
    if (!vis[u])
      if (!toposort(u)) return false;
  return true;
}
```

5 Maths

5.1 Game Theory

5.2 Number Theory

5.2.1 Divisibility Criterion

```
def divisorCriteria(n, lim):
    results = []
    tenElevated = 1
    for i in range(lim):
        # remainder = pow(10, i, n)
        remainder = tenElevated % n
        negremainder = remainder - n
        if(remainder <= abs(negremainder)):
            results.append(remainder)
        else:
            results.append(negremainder)
        tenElevated *= 10
    return results


def testDivisibility(dividend, divisor,
↪  divisor_criteria):
    dividend = str(dividend)
    addition = 0
    dividendSize = len(dividend)
    i = dividendSize - 1
    j = 0
    while j < dividendSize:
```

```
        addition += int(dividend[i]) *
        ↪  divisor_criteria[j]
        i -= 1
        j += 1
    return addition % divisor == 0


if __name__ == '__main__':
    dividend, divisor = map(int, input().split())
    divisor_criteria = divisorCriteria(divisor,
    ↪  len(str(dividend)))
    print(divisor_criteria)
    print(testDivisibility(dividend, divisor,
    ↪  divisor_criteria))
```

5.2.2 Extended Euclidean

```
// gcd(a, b) = ax + by
vector<long long int> extendedGCD(
    long long int a, long long int b) {
  if (a > 0LL && b == 0LL) {
    return {a, 1LL, 0LL};
  }
  long long int x = 1LL, y = 0LL, prevx = 0LL,
                prevy = 1LL, q, remainder;
  while (true) {
    q = a / b;
    remainder = a - b * q;
    if (remainder == 0LL) break;
    a = b;
    b = remainder;
    x = x - prevx * q;
    swap(x, prevx);
    y = y - prevy * q;
    swap(y, prevy);
  }
  // gcd = b, x = prevx, y = prevy
  return {b, prevx, prevy};
}
```

5.2.3 GCD

```
int gcd(int a, int b) {
  return !b ? a : gcd(b, a % b);
}

int gcdI(int a, int b) {
  while (b) {
    a %= b;
    swap(a, b);
  }
  return a;
}
```

5.2.4 LCM

```
int lcm(int a, int b) {
  int c = gcd(a, b);
  return c ? a / c * b : 0;
}
```

5.2.5 Prime Check Miller Rabin

```
from random import randrange


def is_prime(p):
    k = 100
    if p == 2 or p == 3:
        return True
    if (p & 1) == 0 or p == 1:
        return False
    phi = p - 1
    d = phi
    r = 0
    while (d & 1) == 0:
        d = int(d >> 1)
        r += 1
    for i in range(k):
        a = randrange(2, p - 2)
        exp = pow(a, d, p)
        if exp == 1 or exp == p - 1:
            continue
        flag = False
        for j in range(r - 1):
            exp = pow(exp, 2, p)
            if exp == 1:
                return False
            if exp == p - 1:
                flag = True
                break
        if flag:
            continue
        else:
            return False
    return True
```

5.2.6 Prime Sieve

```
vector<int> primeSieve(int n) {
  vector<int> sieve(n + 1);
  for (int i = 4; i <= n; i += 2) sieve[i] = 2;
  for (int i = 3; i * i <= n; i += 2)
    if (!sieve[i])
      for (int j = i * i; j <= n; j += 2 * i)
        if (!sieve[j]) sieve[j] = i;
  return sieve;
}
```

5.3 Probability

5.3.1 Combinations

5.3.2 Permutations

6 Rare Topics

7 Strings

7.1 KMP

```
// f = error function
// cf = create error function
// p = pattern
// t = text
// pos = positions where pattern is found in text

int MAXN = 1000000;
vector<int> f(MAXN + 1);

vector<int> kmp(string &p, string &t, int cf) {
  vector<int> pos;
  if (cf) f[0] = -1;
  for (int i = cf, j = 0; j < t.size();) {
    while (i > -1 && p[i] != t[j]) i = f[i];
    i++, j++;
    if (cf) f[j] = i;
    if (!cf && i == p.size())
      pos.push_back(j - i), i = f[i];
  }
  return pos;
}

vector<int> search(string &p, string &t) {
  kmp(p, p, -1);        // create error function
  return kmp(p, t, 0);  // search in text
}
```

7.2 Rabin Karp

```
class RollingHash {
 public:
  vector<unsigned long long int> pow;
  vector<unsigned long long int> hash;
  unsigned long long int B;
  RollingHash(const string &text) : B(257) {
    int N = text.size();
    pow.resize(N + 1);
    hash.resize(N + 1);
    pow[0] = 1;
    hash[0] = 0;
    for (int i = 1; i <= N; ++i) {
      // in c++ an unsigned long long int is
      // automatically modulated by 2^64
      pow[i] = pow[i - 1] * B;
      hash[i] = hash[i - 1] * B + text[i - 1];
    }
  }

  unsigned long long int getWordHash() {
    return hash[hash.size() - 1];
  }

  unsigned long long int getSubstrHash(int begin,
                                       int end) {
    return hash[end] -
           hash[begin - 1] * pow[end - begin + 1];
  }

  int size() {
    return hash.size();
  }
};

vector<int> rabinKarp(RollingHash &rhStr,
                      string &pattern) {
  vector<int> positions;
  RollingHash rhPattern(pattern);
  unsigned long long int patternHash =
      rhPattern.getWordHash();
  int windowSize = pattern.size(),
      end = windowSize;
  for (int i = 1; end < rhStr.size(); i++) {
    if (patternHash ==
        rhStr.getSubstrHash(i, end))
      positions.push_back(i);
    end = i + windowSize;
  }
  return positions;
}
```

8 Techniques

8.1 Binary Search

8.2 DP

8.3 Multiple Queries

8.3.1 Mo

```
#include <bits/stdc++.h>

using namespace std;

// q = query
// qs = queries

struct Query {
  int l, r;
};

int N, M, blksize;
vector<Query> qs;
vector<int> arr;

void initVars() {
```

```
  qs = vector<Query>(M);
  arr = vector<int>(N);
}

bool cmp(Query &a, Query &b) {
  if (a.l == b.l) return a.r < b.r;
  return a.l / blksize < b.l / blksize;
}

void getResults() {
  blksize = (int)sqrt(N);
  sort(qs.begin(), qs.end(), cmp);
  int prevL = 0, prevR = -1;
  int sum = 0;
  for (auto &q : qs) {
    int L = q.l, R = q.r;
    while (prevL < L) {
      sum -= arr[prevL];  // problem specific
      prevL++;
    }
    while (prevL > L) {
      prevL--;
      sum += arr[prevL];  // problem specific
    }
    while (prevR < R) {
      prevR++;
      sum += arr[prevR];  // problem specific
    }
    while (prevR > R) {
      sum -= arr[prevR];  // problem specific
      prevR--;
    }

    cout << "sum[" << L << ", " << R
         << "] = " << sum << endl;
  }
}

int main() {
  arr = {1, 1, 2, 1, 3, 4, 5, 2, 8};
  N = arr.size();
  qs = {{0, 8}, {3, 5}};
  M = qs.size();
  getResults();
}
```

8.3.2 SQRT Decomposition

```
// sum of elements in range
#include <bits/stdc++.h>

using namespace std;

int N, blksize;
int MAXN = 100, MAXSQR = (int)sqrt(MAXN);

vector<int> arr(MAXN);
vector<int> blks(MAXSQR + 1);

void preprocess() {
  blksize = sqrt(N);
  for (int i = 0, j = 0; i < N; i++) {
    if (i == blksize * j) j++;
    blks[j - 1] += arr[i];  // problem specific
  }
}

// problem specific
void update(int i, int val) {
  blks[i / blksize] += val - arr[i];
  arr[i] = val;
}

int query(int l, int r) {
  int sum = 0;
  int lblk = l / blksize;
  if (l != blksize * lblk++)
    while (l < r && l != lblk * blksize) {
      sum += arr[l];  // problem specific
      l++;
    }

  while (l + blksize <= r) {
    sum += blks[l / blksize];  // problem
    ↪  specific
    l += blksize;
  }
  while (l <= r) {
    sum += arr[l];  // problem specific
    l++;
  }
  return sum;
}

int main() {
  N = 10;
  arr = {1, 5, 2, 4, 6, 1, 3, 5, 7, 10};
  preprocess();
  for (int i = 0; i < blksize + 1; i++)
    cout << blks[i] << " ";
  // 8 11 15 10
  cout << endl;
  cout << query(3, 8) << " ";
  cout << query(1, 6) << " ";
  update(8, 0);
  cout << query(8, 8) << endl;
  // 26 21 0
  return 0;
}
```

9 Faster But Longer

9.1 BellmanFerrari

```
// will be with queue
```

9.2 KMP