ACM-ICPC-REFERENCE

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1 Coding Resources

1.1 C++

1.1.1 IOoptimizationCPP

```
int main() {
  ios_base::sync_with_stdio(0);
  cin.tie(0);
}
```

1.1.2 IntToBinary

```
typedef long long int lli;
lli bitsInInt(lli n) {
 return floor(log2(n) + 1LL);
vector<int> intToBitsArray(lli n) {
 n = abs(n);
  if (!n) {
   vector<int> v;
    return v;
  int length = bitsInInt(n);
  int lastPos = length - 1;
 vector<int> v(length);
  for (lli i = lastPos, j = 0; i > -1LL;
       i--, j++) {
   lli aux = (n \gg i) & 1LL;
   v[j] = aux;
 return v;
```

1.1.3 MapValueToInt

1.1.4 PrintVector

```
void printv(vector<int> v) {
  if (v.size() == 0) {
    cout << "[]" << endl;
    return;
}</pre>
```

```
cout << "[" << v[0];
for (int i = 1; i < v.size(); i++) {
   cout << ", " << v[i];
}
cout << "]" << endl;
}</pre>
```

1.1.5 PriorityQueueOfClass

```
struct Object {
  char first;
  int second;
};
int main() {
  auto cmp = [](const Object& a,
                const Object& b) {
    return a.second > b.second;
  priority_queue<Object, vector<Object>,
                 decltype(cmp)>
      pq(cmp);
  vector<Object> v = {
      {'c', 3}, {'a', 1}, {'b', 2}};
  sort(v.begin(), v.end(), cmp);
  return 0;
}
```

1.1.6 ReadLineCpp

```
// when reading lines, don't mix 'cin' with
// 'getline' just use getline and split
string input() {
   string ans;
   // cin >> ws; // eats all whitespaces.
   getline(cin, ans);
   return ans;
}
```

1.1.7 SortPair

```
pair<int, int> p;
sort(p.begin(), p.end());
// sorts array on the basis of the first element
```

1.1.8 SortVectorOfClass

```
struct Object {
  char first;
  int second;
};

bool cmp(const Object& a, const Object& b) {
  return a.second > b.second;
}

int main() {
  vector<Object> v = {
      {'c', 3}, {'a', 1}, {'b', 2}};
  sort(v.begin(), v.end(), cmp);
```

1.2 Python 2 DATA STRUCTURES

```
printv(v);
return 0;
}
```

1.1.9 SplitString

```
vector<string> split(string str, char token) {
   stringstream test(str);
   string seg;
   vector<string> seglist;
   while (getline(test, seg, token))
      seglist.push_back(seg);
   return seglist;
}
```

1.2 Python

1.2.1 Combinations

```
import itertools
#from arr choose k = > combinations(arr, k)
print(list(itertools.combinations([1, 2, 3], 3)))
```

1.2.2 Fast IO

```
from sys import stdin, stdout

N = 10
#Reads N chars from stdin(it counts '\n' as char)
stdin.read(N)
#Reads until '\n' or EOF
line = stdin.readline()
#Reads all lines in stdin until EOF
lines = stdin.readlines()
#Writes a string to stdout, it doesn 't adds '\n'
stdout.write(line)
#Writes a list of strings to stdout
stdout.writelines(lines)
#Reads numbers separated by space in a line
numbers = list(map(int, stdin.readline().split()))
```

1.2.3 Permutations

```
import itertools
print(list(itertools.permutations([1, 2, 3])))
```

1.2.4 SortListOfClass

2 Data Structures

2.1 BIT

2.2 SegmentTree

2.3 Trie

```
// wpt = number of words passing through
// w = number of words ending in the node
// c = character
struct Trie {
  struct Node {
    // for lexicographical order use 'map'
    // map<char, Node *> ch;
    unordered_map<char, Node *> ch;
    int w = 0, wpt = 0;
  Node *root = new Node();
  void insert(string str) {
    Node *curr = root;
    for (auto &c : str) {
      curr->wpt++;
      if (!curr->ch.count(c))
        curr->ch[c] = new Node();
      curr = curr->ch[c];
    curr->wpt++;
    curr->w++;
  Node *find(string &str) {
    Node *curr = root;
    for (auto &c : str) {
      if (!curr->ch.count(c)) return nullptr;
      curr = curr->ch[c];
    }
    return curr;
  }
  // number of words with given prefix
  int prefixCount(string prefix) {
    Node *node = find(prefix);
    return node ? node->wpt : 0;
  // number of words matching str
  int strCount(string str) {
    Node *node = find(str);
    return node ? node->w : 0;
  }
  void getWords(Node *curr, vector<string> &words,
                string &word) {
```

2.4 UnionFind 4 GRAPHS

```
int Ru = root(u), Rv = root(v);
    if (!curr) return;
    if (curr->w) words.push_back(word);
                                                          if (Ru == Rv) return;
    for (auto &c : curr->ch) {
                                                          --n, dad[Ru] = Rv;
      getWords(c.second, words, word += c.first);
                                                          size[Rv] += size[Ru];
      word.pop_back();
                                                        int getSize(int u) {
                                                          return size[root(u)];
  vector<string> getWords() {
    vector<string> words;
    string word = "";
                                                        int numberOfSets() {
    getWords(root, words, word);
                                                          return n;
                                                        }
    return words;
                                                      };
  vector<string> getWordsByPrefix(string prefix) {
    vector<string> words;
                                                      3
                                                           Geometry
    getWords(find(prefix), words, prefix);
                                                           Graphs
  bool remove(Node *curr, string &str, int &i) {
    if (i == str.size()) {
                                                            ArticulationPointsAndBridges
      curr->wpt--;
      return curr->w ? !(curr->w = 0) : 0;
                                                      // APB = articulation points and bridges
    }
                                                      // ap = Articulation Point
    int c = str[i];
                                                      // br = bridges
    if (!curr->ch.count(c)) return false;
                                                      // p = parent
    if (remove(curr->ch[c], str, ++i)) {
                                                      // disc = discovery time
      if (!curr->ch[c]->wpt)
                                                      // low = lowTime
        curr->wpt--, curr->ch.erase(c);
                                                      // ch = children
      return true;
    }
                                                      typedef pair<int, int> Edge;
    return false;
                                                      int MAXN = 101, N = 7, Time;
                                                      vector<vector<int>> ady;
                                                      vector<int> disc, low, ap;
  int remove(string str) {
                                                      vector<Edge> br;
    int i = 0;
    return remove(root, str, i);
                                                      void initVars() {
  }
                                                        ady = vector<vector<int>>(MAXN, vector<int>());
};
      UnionFind
                                                      int dfsAPB(int u, int p) {
                                                        int ch = 0;
struct UnionFind {
                                                        low[u] = disc[u] = ++Time;
  vector<int> dad, size;
                                                        for (int &v : ady[u]) {
                                                          if (v == p) continue;
  UnionFind(int N) : n(N), dad(N), size(N, 1) {
                                                          if (!disc[v]) {
    while (--N) dad[N] = N;
                                                            ch++;
                                                            dfsAPB(v, u);
                                                            if (disc[u] <= low[v]) ap[u]++;
  int root(int u) {
                                                            if (disc[u] < low[v]) br.push_back({u, v});</pre>
    if (dad[u] == u) return u;
                                                            low[u] = min(low[u], low[v]);
    return dad[u] = root(dad[u]);
                                                          } else
                                                            low[u] = min(low[u], disc[v]);
  bool areConnected(int u, int v) {
                                                        return ch;
                                                      }
    return root(u) == root(v);
                                                      void APB() {
  void join(int u, int v) {
                                                        br.clear();
```

```
if (vis[v] == 1 || hasDirectedCycle(v)) {
  ap = low = disc = vector<int>(MAXN);
  Time = 0;
                                                            if (rootNode == -1)
  for (int u = 0; u < N; u^{++})
                                                              rootNode = v, flag = true;
    if (!disc[u]) ap[u] = dfsAPB(u, u) > 1;
                                                            if (flag) {
}
                                                              cycle.push_back(u);
                                                              if (rootNode == u) flag = false;
void addEdge(int u, int v) {
                                                            }
  ady[u].push_back(v);
                                                            return true;
  ady[v].push_back(u);
                                                          }
}
                                                        vis[u] = 2;
                                                        return false;
4.2
      ConnectedComponents
                                                      }
// comp = component
                                                      bool hasDirectedCycle() {
int MAXN = 26, N, compId = 1;
                                                        vis.clear();
vector<vector<int>> ady;
                                                        for (int u = 0; u < n; u++)
vector<int> getComp;
                                                          if (!vis[u]) {
                                                            cycle.clear();
void initVars() {
                                                            if (hasDirectedCycle(u))
  ady = vector<vector<int>>(MAXN, vector<int>());
                                                              cycles.push_back(cycle);
  getComp = vector<int>(MAXN);
                                                        return cycles.size() > 0;
                                                      }
void dfsCC(int u, vector<int> &comp) {
  if (getComp[u]) return;
  getComp[u] = compId;
                                                            CycleInUndirectedGraph
  comp.push_back(u);
  for (auto &v : ady[u]) dfsCC(v, comp);
}
                                                                                 // max node id >= 0
                                                      int n;
                                                      vector<vector<int>> ady;
                                                                                // ady.resize(n)
vector<vector<int>>> connectedComponents() {
                                                      vector<bool> vis;
                                                                                 // vis.resize(n)
  vector<vector<int>> comps;
                                                      vector<vector<int>> cycles;
  for (int u = 0; u < N; u^{++}) {
                                                      vector<int> cycle;
    vector<int> comp;
                                                      bool flag = false;
    dfsCC(u, comp);
                                                      int rootNode = -1;
    compId++;
    if (!comp.empty()) comps.push_back(comp);
                                                      bool hasUndirectedCycle(int u, int prev) {
                                                        vis[u] = true;
  return comps;
                                                        for (auto &v : ady[u]) {
}
                                                          if (v == u || v == prev) continue;
                                                          if (vis[v] | hasUndirectedCycle(v, u)) {
void addEdge(int u, int v) {
                                                            if (rootNode == -1)
  ady[u].push_back(v);
                                                              rootNode = v, flag = true;
  ady[v].push_back(u);
                                                            if (flag) {
}
                                                              cycle.push_back(u);
                                                              if (rootNode == u) flag = false;
                                                            }
4.3
     CycleInDirectedGraph
                                                            return true;
                                                          }
                           // max node id >= 0
                                                        }
vector<vector<int>> ady;
                         // ady.resize(n)
vector<int> vis;
                          // vis.resize(n)
                                                        return false;
vector<vector<int>> cycles;
                                                      }
vector<int> cycle;
```

bool hasUndirectedCycle() {

if (!vis[u]) {

cycle.clear();

for (int u = 0; u < n; u^{++})

if (hasUndirectedCycle(u, -1))

cycles.push_back(cycle);

vis.clear();

bool flag = false;

int rootNode = -1;

vis[u] = 1;

bool hasDirectedCycle(int u) {

if $(v == u \mid \mid vis[v] == 2)$ continue;

for (auto &v : ady[u]) {

4.5 FloodFill 4 GRAPHS

```
}
  return cycles.size() > 0;
                                                      Num blockingFlow(int u, int t,
                                                                        Num currPathMaxFlow) {
                                                         if (u == t) return currPathMaxFlow;
                                                         for (int v : ady[u]) {
4.5
     FloodFill
                                                          Num capleft = cap[u][v] - flow[u][v];
                                                           if ((level[v] == (level[u] + 1)) &&
int n, m, oldColor = 0, color = 1;
                                                               (capleft > 0)) {
vector<vector<int>> mat;
                                                             Num pathMaxFlow = blockingFlow(
                                                                 v, t, min(currPathMaxFlow, capleft));
vector<vector<int>> movs = {
                                                            if (pathMaxFlow > 0) {
    \{1, 0\}, \{0, 1\}, \{-1, 0\}, \{0, -1\}\};
                                                               flow[u][v] += pathMaxFlow;
                                                               flow[v][u] -= pathMaxFlow;
void floodFill(int i, int j) {
                                                               return pathMaxFlow;
  if (i >= mat.size() || i < 0 ||
                                                            }
      j >= mat[i].size() || j < 0 ||</pre>
                                                          }
      mat[i][j] != oldColor)
                                                        }
    return;
                                                        return 0;
 mat[i][j] = color;
  for (auto move : movs)
    floodFill(i + move[1], j + move[0]);
                                                      Num dinicMaxFlow(int s, int t) {
}
                                                         if (s == t) return -1;
                                                        Num maxFlow = 0;
void floodFill() {
                                                        while (levelGraph(s, t))
  for (int i = 0; i < n; i++)
                                                           while (Num flow = blockingFlow(s, t, 1 << 30))
    for (int j = 0; j < m; j++)
                                                            maxFlow += flow;
      if (mat[i][j] == oldColor) floodFill(i, j);
                                                        return maxFlow;
4.6
     Flow
                                                      void addEdge(int u, int v, Num capacity) {
                                                         cap[u][v] = capacity;
4.6.1 MaxFlowDinic
                                                         ady[u].push_back(v);
// cap[a][b] = Capacity from a to b
// flow[a][b] = flow occupied from a to b
// level[a] = level in graph of node a
// Num = number
                                                      4.7
                                                            IsBipartite
typedef int Num;
int N, MAXN = 101;
vector<int> level;
                                                      int n;
                                                                                 // max node id >= 0
                                                      vector<vector<int>> ady; // ady.resize(n)
vector<vector<int>>> ady(MAXN, vector<int>),
    cap(MAXN, vector<int>(MAXN)),
    flow(MAXN, vector<int>(MAXN));
                                                      bool isBipartite() {
                                                        vector<int> color(n, -1);
bool levelGraph(int s, int t) {
                                                        for (int s = 0; s < n; s++) {
  level = vector<int>(MAXN);
                                                          if (color[s] > -1) continue;
  level[s] = 1;
                                                           color[s] = 0;
  queue<int> q;
                                                          queue<int> q;
  q.push(s);
                                                          q.push(s);
  while (!q.empty()) {
                                                          while (!q.empty()) {
    int u = q.front();
                                                             int u = q.front();
    q.pop();
                                                             q.pop();
    for (int &v : ady[u]) {
                                                             for (int &v : ady[u]) {
      if (!level[v] && flow[u][v] < cap[u][v]) {
                                                               if (color[v] < 0)</pre>
                                                                 q.push(v), color[v] = !color[u];
        q.push(v);
        level[v] = level[u] + 1;
                                                               if (color[v] == color[u]) return false;
      }
                                                            }
    }
                                                          }
  return level[t];
                                                        return true;
                                                      }
```

4.8 KruskalMST GRAPHS

KruskalMST 4.8

```
typedef int Weight;
typedef pair<int, int> Edge;
typedef pair<Weight, Edge> Wedge;
vector<Wedge> Wedges; // gets filled from input;
vector<Wedge> mst;
int kruskal() {
  int cost = 0;
  sort(Wedges.begin(), Wedges.end());
  // reverse(Wedges.begin(), Wedges.end());
 UnionFind uf(N);
  for (Wedge &wedge : Wedges) {
    int u = wedge.second.first,
        v = wedge.second.second;
    if (!uf.areConnected(u, v))
      uf.join(u, v), mst.push_back(wedge),
          cost += wedge.first;
  }
  return cost;
```

4.9 **ShortestPaths**

4.9.1 BellmanFord

```
typedef int Weight;
int MAXN = 20001, N, INF = 1 << 30,
    isDirected = true;
vector<vector<int>>> ady, weight;
void initVars() {
  ady = vector<vector<int>>(MAXN, vector<int>());
  weight = vector<vector<int>>(
      MAXN, vector<int>(MAXN, INF));
}
vector<Weight> bellmanFord(int s) {
  vector<Weight> dist(MAXN, INF);
  dist[s] = 0;
  for (int i = 0; i \le N; i++)
    for (int u = 0; u < N; u++)
      for (auto &v : ady[u]) {
        Weight w = weight[u][v];
        if (dist[u] != INF &&
            dist[v] > dist[u] + w) {
          if (i == N) return vector<Weight>();
          dist[v] = dist[u] + w;
      }
  return dist;
}
void addEdge(int u, int v, Weight w) {
  ady[u].push_back(v);
  weight[u][v] = w;
  if (isDirected) return;
  ady[v].push_back(u);
```

```
weight[v][u] = w;
4.9.2 Dijkstra
typedef int Weight;
typedef pair<Weight, int> NodeDist;
int MAXN = 20001, INF = 1 << 30,
    isDirected = false;
vector<vector<int>> ady, weight;
void initVars() {
  ady = vector<vector<int>>(MAXN, vector<int>());
  weight = vector<vector<int>>>(
      MAXN, vector<int>(MAXN, INF));
}
vector<Weight> dijkstra(int s) {
  vector<int> dist(MAXN, INF);
  set<NodeDist> q;
  q.insert({0, s});
  dist[s] = 0;
  while (!q.empty()) {
    NodeDist nd = *q.begin();
    q.erase(nd);
    int u = nd.second;
    for (int &v : ady[u]) {
      Weight w = weight[u][v];
      if (dist[v] > dist[u] + w) {
        if (dist[v] != INF) q.erase({dist[v], v});
        dist[v] = dist[u] + w;
        q.insert({dist[v], v});
      }
    }
  }
 return dist;
}
void addEdge(int u, int v, Weight w) {
  ady[u].push_back(v);
  weight[u][v] = w;
  if (isDirected) return;
  ady[v].push_back(u);
  weight[v][u] = w;
}
4.10
       StronglyConnectedComponents
// tv = top value from stack
// sccs = strongly connected components
// scc = strongly connected component
// disc = discovery time
// low = low time
// s = stack
// top = top index of the stack
```

```
int MAXN = 101, N = 7, Time, top;
vector<vector<int>>> ady, sccs;
vector<int> disc, low, s;
```

4.11 TopologicalSort 5 MATHS

```
void initVars() {
  ady = vector<vector<int>>(MAXN, vector<int>());
void dfsSCCS(int u) {
  if (disc[u]) return;
  low[u] = disc[u] = ++Time;
  s[++top] = u;
  for (int &v : ady[u]) {
    dfsSCCS(v);
    low[u] = min(low[u], low[v]);
  }
  if (disc[u] == low[u]) {
    vector<int> scc;
    while (true) {
      int tv = s[top--];
      scc.push_back(tv);
      low[tv] = N;
      if (tv == u) break;
    }
    sccs.push_back(scc);
}
void SCCS() {
  s = low = disc = vector<int>(MAXN);
  Time = 0, top = -1, sccs.clear();
  for (int u = 0; u < N; u++) dfsSCCS(u);
}
void addEdge(int u, int v) {
  ady[u].push_back(v);
```

4.11 TopologicalSort

```
int n;
                           // max node id >= 0
                          // ady.resize(n)
vector<vector<int>> ady;
vector<int> vis;
                           // vis.resize(n)
vector<int> toposorted;
bool toposort(int u) {
  vis[u] = 1;
  for (auto &v : ady[u]) {
    if (v == u || vis[v] == 2) continue;
    if (vis[v] == 1 || !toposort(v)) return false;
  }
  vis[u] = 2;
  toposorted.push_back(u);
  return true;
bool toposort() {
  vis.clear();
  for (int u = 0; u < n; u^{++})
    if (!vis[u])
      if (!toposort(u)) return false;
  return true;
```

5 Maths

5.1 Game Theory

5.2 Number Theory

5.2.1 DivisibilityCriterion

```
def divisorCriteria(n, lim):
    results = []
    tenElevated = 1
    for i in range(lim):
        \# remainder = pow(10, i, n)
        remainder = tenElevated % n
        negremainder = remainder - n
        if(remainder <= abs(negremainder)):</pre>
            results.append(remainder)
            results.append(negremainder)
        tenElevated *= 10
    return results
def testDivisibility(dividend, divisor,

    divisor_criteria):

    dividend = str(dividend)
    addition = 0
    dividendSize = len(dividend)
    i = dividendSize - 1
    j = 0
    while j < dividendSize:</pre>
        addition += int(dividend[i]) *

    divisor_criteria[j]

        i -= 1
        j += 1
    return addition % divisor == 0
if __name__ == '__main__':
    dividend, divisor = map(int, input().split())
    divisor_criteria = divisorCriteria(divisor,
    → len(str(dividend)))
    print(divisor_criteria)
    print(testDivisibility(dividend, divisor,

→ divisor_criteria))
5.2.2 ExtendedEuclidean
// \gcd(a, b) = ax + by
vector<long long int> extendedGCD(
```

5.3 Probability 8 STRINGS

```
if (remainder == OLL) break;
    a = b;
    b = remainder;
   x = x - prevx * q;
    swap(x, prevx);
    y = y - prevy * q;
    swap(y, prevy);
  // gcd = b, x = prevx, y = prevy
  return {b, prevx, prevy};
5.2.3 GCD
int gcd(int a, int b) {
  return b == 0 ? a : gcd(b, a % b);
int gcdI(int a, int b) {
  while (b) {
    a %= b;
    swap(a, b);
 return a;
}
```

5.2.4 PrimeCheckMillerRabin

from random import randrange

```
def is_prime(p):
    k = 100
    if p == 2 or p == 3:
       return True
    if (p \& 1) == 0 or p == 1:
       return False
    phi = p - 1
    d = phi
    r = 0
    while (d \& 1) == 0:
        d = int(d >> 1)
        r += 1
    for i in range(k):
        a = randrange(2, p - 2)
        exp = pow(a, d, p)
        if exp == 1 or exp == p - 1:
            continue
        flag = False
        for j in range(r - 1):
            exp = pow(exp, 2, p)
            if exp == 1:
                return False
            if exp == p - 1:
                flag = True
                break
        if flag:
            continue
        else:
            return False
```

```
return True
```

5.2.5 PrimeSieve

```
vector<int> primeSieve(int n) {
  vector<int> sieve(n + 1);
  for (int i = 4; i <= n; i += 2) sieve[i] = 2;
  for (int i = 3; i * i <= n; i += 2)
    if (!sieve[i])
      for (int j = i * i; j <= n; j += 2 * i)
        if (!sieve[j]) sieve[j] = i;
  return sieve;
}</pre>
```

5.3 Probability

- 5.3.1 Combinations
- 5.3.2 Permutations

6 Multiple Queries

6.1 Mo

#include <bits/stdc++.h>

6.2 SqrtDecomposition

#include <bits/stdc++.h>

7 Rare Topics

8 Strings

8.1 KMP

```
// f = error function
// cf = create error function
// p = pattern
// t = text
// pos = positions where pattern is found in text
int MAXN = 1000000;
vector<int> f(MAXN + 1);
vector<int> kmp(string &p, string &t, int cf) {
  vector<int> pos;
  if (cf) f[0] = -1;
  for (int i = cf, j = 0; j < t.size();) {
    while (i > -1 \&\& p[i] != t[j]) i = f[i];
    i++, j++;
    if (cf) f[j] = i;
    if (!cf && i == p.size())
      pos.push_back(j - i), i = f[i];
 }
 return pos;
vector<int> search(string &p, string &t) {
```

8.2 RabinKarp 9 FASTER BUT LONGER

```
kmp(p, p, -1);  // create error function
return kmp(p, t, 0); // search in text
}
```

9 Faster But Longer

9.1 BellmanFerrari

// will be with queue

9.2 KMP

8.2 RabinKarp

```
class RollingHash {
 public:
  vector<unsigned long long int> pow;
  vector<unsigned long long int> hash;
  unsigned long long int B;
  RollingHash(const string &text) : B(257) {
    int N = text.size();
    pow.resize(N + 1);
    hash.resize(N + 1);
    pow[0] = 1;
    hash[0] = 0;
    for (int i = 1; i \le N; ++i) {
      // in c++ an unsigned long long int is
      // automatically modulated by 2^64
      pow[i] = pow[i - 1] * B;
      hash[i] = hash[i - 1] * B + text[i - 1];
  unsigned long long int getWordHash() {
    return hash[hash.size() - 1];
  unsigned long long int getSubstrHash(int begin,
    return hash[end] -
           hash[begin - 1] * pow[end - begin + 1];
  }
  int size() {
    return hash.size();
  }
vector<int> rabinKarp(RollingHash &rhStr,
                      string &pattern) {
  vector<int> positions;
  RollingHash rhPattern(pattern);
  unsigned long long int patternHash =
      rhPattern.getWordHash();
  int windowSize = pattern.size(),
      end = windowSize;
  for (int i = 1; end < rhStr.size(); i++) {</pre>
    if (patternHash ==
        rhStr.getSubstrHash(i, end))
      positions.push_back(i);
    end = i + windowSize;
  return positions;
```