## Competitive

## Programming

### Reference

First, solve the problem. Then, write the code.

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### 1 Coding Resources

### 1.1 C++

### 1.1.1 Decimal Precision

```
// rounds up the decimal number
cout << setprecision(N) << n << endl;
// specify N fixed number of decimals
cout << fixed << setprecision(N) << n << endl;</pre>
```

### 1.1.2 Int To Binary

### 1.1.3 IO Optimization

```
int main() {
  ios_base::sync_with_stdio(0);
  cin.tie(0);
}
```

### 1.1.4 Map Value To Int

```
1.1.5 Permutations
typedef vector<int> T;// typedef string T;
vector<T> permutations(T v) {
  vector<vector<int>> ans;
  sort(v.begin(), v.end());
    ans.push_back(v);
  while (next_permutation(v.begin(), v.end()));
  return ans;
}
1.1.6 Print Vector
void printv(vector<int> v) {
  if (v.size() == 0) {
    cout << "[]" << endl;
    return;
  }
  cout << "[" << v[0];
  for (int i = 1; i < v.size(); i++) cout << ", " <<</pre>

  v[i];
  cout << "]" << endl;
}
1.1.7 Priority Queue Of Object
struct Object {
  char first;
  int second;
};
int main() {
  auto cmp = [](const Object& a,
                const Object& b) {
    return a.second > b.second;
  priority_queue<Object, vector<Object>,
                  decltype(cmp)>
      pq(cmp);
  vector<Object> v = {
      {'c', 3}, {'a', 1}, {'b', 2}};
  sort(v.begin(), v.end(), cmp);
  return 0;
}
```

### 1.1.8 Random

```
int random(int min, int max) {
  return min + rand() % (max - min + 1);
}
int main() {
  srand(time(0));
  // code
}
```

### 1.1.9 Read Line

```
// when reading lines, don't mix 'cin' with
// 'getline' just use getline and split
string input() {
    string ans;
    // cin >> ws; // eats all whitespaces.
    getline(cin, ans);
    return ans;
}

1.1.10 Sort Pair

pair<int, int> p;
sort(p.begin(), p.end());
// sorts array on the basis of the first element

1.1.11 Sort Vector Of Object

struct Object {
    char first;
    int second;
```

# }; bool cmp(const Object& a, const Object& b) { return a.second > b.second; } int main() { vector<Object> v = { {'c', 3}, {'a', 1}, {'b', 2}};

sort(v.begin(), v.end(), cmp);

### 1.1.12 Split String

printv(v);

return 0;

```
vector<string> split(string str, char token) {
   stringstream test(str);
   string seg;
   vector<string> seglist;
   while (getline(test, seg, token))
      seglist.push_back(seg);
   return seglist;
}
```

### 1.1.13 Typedef

```
typedef TYPE ALIAS;
// example:
typedef int T;
```

### 1.2 Python

### 1.2.1 Combinations

```
import itertools
#from arr choose k = > combinations(arr, k)
print(list(itertools.combinations([1, 2, 3], 3)))
```

### 1.2.2 Fast IO

```
from sys import stdin, stdout

N = 10
#Reads N chars from stdin(it counts '\n' as char)
stdin.read(N)
#Reads until '\n' or EOF
line = stdin.readline()
#Reads all lines in stdin until EOF
lines = stdin.readlines()
#Writes a string to stdout, it doesn't add '\n'
stdout.write(line)
#Writes a list of strings to stdout
stdout.writelines(lines)
#Reads numbers separated by space in a line
numbers = list(map(int, stdin.readline().split()))
```

### 1.2.3 Permutations

```
import itertools
print(list(itertools.permutations([1, 2, 3])))
```

### 1.2.4 Random

```
import random
# Initialize the random number generator.
random.seed(None)
# Returns a random integer N such that a <= N <= b.
random.randint(a, b)
# Returns a random integer N such that 0 <= N < b
random.randrange(b)
# Returns a random integer N such that a <= N < b.
random.randrange(a, b)
# Returns and integer with k random bits.
random.getrandbits(k)
# shuffles a list
random.shuffle(li)</pre>
```

### 1.2.5 Sort List

```
li = ['a', 'c', 'b']
# sorts inplace in descending order
li.sort(reverse=True)
# returns sorted list ascending order
ol = sorted(li)
```

### 1.2.6 Sort List Of Object

```
class MyObject :
    def __init__(self, first, second, third):
        self.first = first
        self.second = second
        self.third = third

li = [MyObject('b', 3, 1), MyObject('a', 3, 2),
        MyObject('b', 3, 3)]
```

### 2 Data Structures

### 2.1 Geometry

### 2.1.1 K-D Tree

### 2.2 Graphs

### 2.2.1 UnionFind

```
struct UnionFind {
  vector<int> dad, size;
  int n;
 UnionFind(int N = 0): n(N), dad(N), size(N, 1) {
   while (N--) dad[N] = N;
  int root(int u) {
   if (dad[u] == u) return u;
   return dad[u] = root(dad[u]);
 bool areConnected(int u, int v) {
   return root(u) == root(v);
  void join(int u, int v) {
   int Ru = root(u), Rv = root(v);
   if (Ru == Rv) return;
   --n, dad[Ru] = Rv;
    size[Rv] += size[Ru];
  int getSize(int u) {
   return size[root(u)];
  int numberOfSets() {
   return n;
 }
};
```

### 2.3 Ranges

### 2.3.1 BIT

```
typedef long long int T;
T neutro = 0;
vector<T> bit;
```

```
void initVars(int n) {
  bit.assign(++n, neutro);
T F(T a, T b) {
  return a + b;
  // return a * b;
// Inverse of F
T I(T a, T b) {
 return a - b;
  // return a / b;
// O(N)
void build() {
  for (int i = 1; i < bit.size(); i++) {</pre>
    int j = i + (i \& -i);
    if (j < bit.size()) bit[j] = F(bit[j], bit[i]);</pre>
}
// O(lg(N))
void update(int i, T val) {
  for (i++; i < bit.size(); i += i & -i) bit[i] =

    F(bit[i], val);

}
// O(lg(N))
T query(int i) {
  T ans = neutro;
  for (i++; i; i-= i \& -i) ans = F(ans, bit[i]);
  return ans;
// O(lg(N)), [l, r]
T query(int 1, int r) {
  return I(query(r), query(--1));
void setValAt(T val, int i) {
  bit[++i] = val;
2.3.2 BIT Range Update
typedef long long int T;
T neutro = 0;
vector<T> bit1, bit2;
void initVars(int n) {
  bit1.assign(++n, neutro);
  bit2 = bit1;
// O(lg(N))
void update(vector<T> &bit, int i, T val) {
  for (i++; i < bit.size(); i += i & -i) bit[i] +=
  → val;
}
```

```
// O(lq(N)), [l, r]
void update(int 1, int r, T val) {
  update(bit1, 1, val);
  update(bit1, r + 1, -val);
 update(bit2, r + 1, val * r);
                                                         }
 update(bit2, 1, -val * (1 - 1));
// O(lg(N))
T query(vector<T> &bit, int i) {
  T ans = neutro;
 for (i++; i; i -= i & -i) ans += bit[i];
 return ans;
                                                         }
// O(lq(N))
T query(int i) {
                                                         }
 return query(bit1, i) * i + query(bit2, i);
// O(lg(N)), [l, r]
T query(int 1, int r) {
 return query(r) - query(l - 1);
2.3.3 Segment Tree
// st = segment tree. st[1] = root;
// neutro = operation neutral value
// e.g. for sum is 0, for multiplication
// is 1, for gcd is 0, for min is INF, etc.
typedef int T;
T neutro = 0;
int N;
vector<T> st;
void initVars(int n) {
  st.assign(2 * (N = n), neutro);
T F(T a, T b) {
 return a + b;
 // return __gcd(a, b);
  // return a * b;
  // return min(a, b);
// O(2N)
void build() {
 for (int i = N - 1; i > 0; i--) st[i] = F(st[i <<
  // O(lq(2N))
void update(int i, T val) {
  for (st[i += N] = val; i > 1; i >>= 1) st[i >> 1] =

    F(st[i], st[i ^ 1]);
```

```
// O(3N), [l, r]
void update(int 1, int r, T val) {
  for (1 += N, r += N; 1 <= r; 1++) st[1] = val;
  build();
// O(lg(2N)), [l, r]
T query(int 1, int r) {
  T ans = neutro;
  for (1 += N, r += N; 1 <= r; 1 >>= 1, r >>= 1) {
   if (l \& 1) ans = F(ans, st[l++]);
   if (r \& 1) ans = F(ans, st[r--]);
 return ans;
void setValAt(T val, int i) {
  st[i + N] = val;
2.3.4 Segment Tree Lazy Propagation
// st = segment tree, st[1] = root, H = height of d
// u = updates, d = delayed updates
// neutro = operation neutral val
// e.g. for sum is 0, for multiplication
// is 1, for gcd is 0, for min is INF, etc.
template <class T>
struct SegmentTree {
  T neutro = 0;
  int N, H;
  vector<T> st, d;
  vector<bool> u;
  SegmentTree(int n) : st(2 * n, neutro), d(n), u(n,
  → 0) {
   H = sizeof(int) * 8 - __builtin_clz(N = n);
  T F(T a, T b) {
   return a + b;
   // return __gcd(a, b);
   // return a * b;
   // return min(a, b);
  void apply(int i, T val, int k) {
   st[i] = val * k; // sum
    // st[i] = val; // min, max, gcd
   // st[i] = pow(a, k); // multiplication
   if (i < N) d[i] = val, u[i] = 1;</pre>
  void calc(int i) {
    if (!u[i]) st[i] = F(st[i << 1], st[i << 1 | 1]);</pre>
  // O(2N)
  void build() {
    for (int i = N - 1; i > 0; i--) calc(i);
  // O(lg(N))
  void build(int p) {
    while (p > 1) p >>= 1, calc(p);
```

```
// O(lq(N))
  void push(int p) {
    for (int s = H, k = 1 \ll (H - 1); s > 0; s--, k

→ >>= 1) {

      int i = p \gg s;
      if (u[i]) {
        apply(i << 1, d[i], k);
        apply(i << 1 | 1, d[i], k);
        u[i] = 0, d[i] = neutro;
      }
    }
  }
  // O(lg(N)), [l, r]
  void update(int 1, int r, T val) {
    push(1 += N);
    push(r += N);
    int ll = 1, rr = r, k = 1;
    for (; 1 <= r; 1 >>= 1, r >>= 1, k <<= 1) {
      if (1 & 1) apply(1++, val, k);
      if (~r & 1) apply(r--, val, k);
    }
    build(11);
    build(rr);
  }
  // O(lg(2N)), [l, r]
  T query(int 1, int r) {
    push(1 += N);
    push(r += N);
    T ans = neutro;
    for (; 1 <= r; 1 >>= 1, r >>= 1) {
      if (1 & 1) ans = F(ans, st[1++]);
      if (~r & 1) ans = F(ans, st[r--]);
    }
    return ans;
  void setValAt(T val, int i) {
    st[i + N] = val;
};
2.3.5 Sparse Table
// st = sparse table, Arith = Arithmetic
typedef int T;
int neutro = 0;
vector<vector<T>>> st;
T F(T a, T b) {
 // return min(a, b);
 return __gcd(a, b);
  // return a + b; // Arith
  // return a * b; // Arith
```

```
// O(Nlq(N))
void build(vector<T> &arr) {
  st.assign(log2(arr.size()), vector<T>(arr.size()));
  st[0] = arr;
  for (int i = 1; (1 << i) <= arr.size(); i++)
    for (int j = 0; j + (1 << i) <= arr.size(); j++)
    \Rightarrow st[i][j] = F(st[i - 1][j], st[i - 1][j + (1 <<

    (i - 1))]);
}
// O(1), [l, r]
T query(int 1, int r) {
  int i = log2(r - l + 1);
  return F(st[i][l], st[i][r + 1 - (1 << i)]);</pre>
// O(lg(N)), [l, r]
T queryArith(int 1, int r) {
  T ans = neutro;
  while (true) {
    int k = log2(r - 1 + 1);
    ans = F(ans, st[k][1]);
    1 += 1 << k;
    if (1 > r) break;
  return ans;
}
2.4
    Strings
2.4.1 Trie
// wpt = number of words passing through
// w = number of words ending in the node
// c = character
struct Trie {
  struct Node {
    // for lexicographical order use 'map'
    // map<char, Node *> ch;
   unordered_map<char, Node *> ch;
    int w = 0, wpt = 0;
  };
  Node *root = new Node();
  // O(STR.SIZE)
  void insert(string str) {
    Node *curr = root;
    for (auto &c : str) {
      curr->wpt++;
      if (!curr->ch.count(c)) curr->ch[c] = new
      → Node();
      curr = curr->ch[c];
    curr->wpt++;
    curr->w++;
  }
```

```
// O(STR.SIZE)
Node *find(string &str) {
 Node *curr = root;
 for (auto &c : str) {
   if (!curr->ch.count(c)) return nullptr;
   curr = curr->ch[c];
 }
 return curr;
// number of words with given prefix O(N)
int prefixCount(string prefix) {
 Node *node = find(prefix);
  return node ? node->wpt : 0;
// number of words matching str O(N)
int strCount(string str) {
 Node *node = find(str);
 return node ? node->w : 0;
}
void getWords(Node *curr, vector<string> &words,

    string &word) {

 if (!curr) return;
 if (curr->w) words.push_back(word);
 for (auto &c : curr->ch) {
    getWords(c.second, words, word += c.first);
    word.pop_back();
}
// O(N)
vector<string> getWords() {
 vector<string> words;
 string word = "";
 getWords(root, words, word);
 return words;
}
// O(N)
vector<string> getWordsByPrefix(string prefix) {
 vector<string> words;
  getWords(find(prefix), words, prefix);
// O(STR.SIZE)
bool remove(Node *curr, string &str, int &i) {
  if (i == str.size()) {
    curr->wpt--;
   return curr->w ? !(curr->w = 0) : 0;
 }
  int c = str[i];
  if (!curr->ch.count(c)) return false;
  if (remove(curr->ch[c], str, ++i)) {
   if (!curr->ch[c]->wpt) curr->wpt--,

    curr→ch.erase(c);

   return true;
 }
  return false;
```

```
// O(STR.SIZE)
int remove(string str) {
  int i = 0;
  return remove(root, str, i);
};
```

### 2.5 Trees And Heaps

### 2.5.1 Treap

### 3 Graphs

### 3.1 Articulation Points And Bridges

```
// APB = articulation points and bridges
// ap = Articulation Point
// br = bridges, p = parent
// disc = discovery time
// low = lowTime, ch = children
typedef pair<int, int> Edge;
int Time;
vector<vector<int>> ady;
vector<int> disc, low, ap;
vector<Edge> br;
void initVars(int N) {
  ady.assign(N, vector<int>());
}
int dfsAPB(int u, int p) {
  int ch = 0;
  low[u] = disc[u] = ++Time;
  for (int &v : ady[u]) {
    if (v == p) continue;
    if (!disc[v]) {
      ch++, dfsAPB(v, u);
      if (disc[u] <= low[v]) ap[u]++;</pre>
      if (disc[u] < low[v]) br.push_back({u, v});</pre>
      low[u] = min(low[u], low[v]);
      low[u] = min(low[u], disc[v]);
  return ch;
// O(N)
void APB() {
  br.clear();
  ap = low = disc = vector<int>(ady.size());
  Time = 0;
  for (int u = 0; u < ady.size(); u++)</pre>
    if (!disc[u]) ap[u] = dfsAPB(u, u) > 1;
void addEdge(int u, int v) {
  ady[u].push_back(v);
  ady[v].push_back(u);
}
```

### 3.2 Connected Components

```
// comp = component
int compId;
vector<vector<int>> ady;
vector<int> getComp;
void initVars(int N) {
  ady.assign(N, vector<int>());
  getComp.assign(N, -1);
  compId = 0;
void dfsCC(int u, vector<int> &comp) {
  if (getComp[u] > -1) return;
  getComp[u] = compId;
  comp.push_back(u);
 for (auto &v : ady[u]) dfsCC(v, comp);
// O(N)
vector<vector<int>>> connectedComponents() {
  vector<vector<int>> comps;
  for (int u = 0; u < ady.size(); u++) {</pre>
    vector<int> comp;
    dfsCC(u, comp);
    if (!comp.empty()) comps.push_back(comp),

→ compId++;

 }
 return comps;
void addEdge(int u, int v) {
  ady[u].push_back(v);
  ady[v].push_back(u);
```

### 3.3 Cycles

### 3.3.1 Get All Simple Cycles

### 3.3.2 Get Some Cycles

```
// at least detects one cycle per component
vector<vector<int>> ady, cycles;
vector<int>> vis, cycle;
bool flag = false, isDirected = false;
int root = -1;

void initVars(int N) {
   ady.assign(N, vector<int>());
   vis.assign(N, 0);
   cycles.clear();
   root = -1, flag = false;
}
```

```
// O(N)
bool hasCycle(int u, int prev) {
  vis[u] = 1;
  for (auto &v : ady[u]) {
    if (v == u | | vis[v] == 2 | | (!isDirected && v ==
    → prev)) continue;
    if (flag) {
      if (!vis[v]) hasCycle(v, u);
      continue;
    }
    if (vis[v] || hasCycle(v, u)) {
      if (root == -1) root = v, flag = true;
      cycle.push_back(u);
      if (root == u) flag = false, root = -1,

    cycles.push_back(cycle), cycle.clear();

    }
  }
  vis[u] = 2;
  return flag;
// O(N)
bool hasCycle() {
  for (int u = 0; u < ady.size(); u++)</pre>
    if (!vis[u]) cycle.clear(), hasCycle(u, -1);
  return cycles.size() > 0;
}
void addEdge(int u, int v) {
  ady[u].push_back(v);
  if (!isDirected) ady[v].push_back(u);
}
3.3.3 Has Cycle
vector<vector<int>> ady;
vector<int> vis;
bool isDirected = false;
void initVars(int N) {
  ady.assign(N, vector<int>());
  vis.assign(N, 0);
bool hasCycle(int u, int prev) {
  vis[u] = 1;
  for (auto &v : ady[u])
    if (v != u && vis[v] != 2 && (isDirected || v !=

→ prev) && (vis[v] | hasCycle(v, u))) return

    true;

  vis[u] = 2;
  return false;
// O(N)
bool hasCycle() {
  for (int u = 0; u < ady.size(); u++)</pre>
    if (!vis[u] && hasCycle(u, -1)) return true;
void addEdge(int u, int v) {
  ady[u].push_back(v);
  if (!isDirected) ady[v].push_back(u);
}
```

### 3.4 Flood Fill

### 3.5 Flow

### 3.5.1 Max Flow Dinic

```
// cap[a][b] = Capacity from a to b
// flow[a][b] = flow occupied from a to b
// level[a] = level in graph of node a
typedef int T;
vector<int> level;
vector<vector<int>> ady;
unordered_map<int, unordered_map<int, T>> cap, flow;
void initVars(int N) {
  ady.assign(N, vector<int>());
  cap.clear();
 flow.clear();
bool levelGraph(int s, int t) {
  level = vector<int>(ady.size());
  level[s] = 1;
  queue<int> q;
  q.push(s);
  while (!q.empty()) {
    int u = q.front();
    q.pop();
    for (int &v : ady[u]) {
      if (!level[v] && flow[u][v] < cap[u][v]) {</pre>
        q.push(v);
        level[v] = level[u] + 1;
      }
    }
  }
 return level[t];
```

```
T blockingFlow(int u, int t, T currPathMaxFlow) {
  if (u == t) return currPathMaxFlow;
  for (int v : ady[u]) {
    T capleft = cap[u][v] - flow[u][v];
    if ((level[v] == (level[u] + 1)) && (capleft > 0))
      T pathMaxFlow = blockingFlow(v, t,

→ min(currPathMaxFlow, capleft));
      if (pathMaxFlow > 0) {
        flow[u][v] += pathMaxFlow;
        flow[v][u] -= pathMaxFlow;
        return pathMaxFlow;
    }
  }
  return 0;
// O(E * V^2)
T dinicMaxFlow(int s, int t) {
  if (s == t) return -1;
  T \max Flow = 0;
  while (levelGraph(s, t))
    while (T flow = blockingFlow(s, t, 1 << 30))</pre>

→ maxFlow += flow;

  return maxFlow;
}
void addEdge(int u, int v, T capacity) {
  cap[u][v] = capacity;
  ady[u].push_back(v);
}
3.5.2 Maximum Bipartite Matching
#include "Max Flow Dinic.cpp"
void addEdge(int u, int v) {
  cap[u][v] = 1;
  ady[u].push_back(v);
}
int main() {
  int n, s = 0, t = 1;
  cin >> n;
  initVars(n);
  while (n--) {
    int u, v;
    cin >> u >> v;
    addEdge(u += 2, v += 2);
    addEdge(s, u);
    addEdge(v, t);
  cout << dinicMaxFlow(s, t) << endl;</pre>
  return 0;
}
     Is Bipartite
```

vector<vector<int>> ady;

```
void initVars(int N) {
                                                           void eulerTour(int u, int p, int h) {
  ady.assign(N, vector<int>());
                                                             first[u] = tour.size();
                                                             tour.push_back({h, u});
                                                             for (int v : ady[u])
                                                               if (v != p) {
// O(N)
                                                                 eulerTour(v, u, h + 1);
bool isBipartite() {
                                                                 tour.push_back({h, u});
  vector<int> color(ady.size(), -1);
  for (int s = 0; s < ady.size(); s++) {</pre>
                                                           }
    if (color[s] > -1) continue;
    color[s] = 0;
                                                           void preprocess() {
    queue<int> q;
                                                             tour.clear();
    q.push(s);
                                                             first.assign(ady.size(), -1);
    while (!q.empty()) {
                                                             eulerTour(0, 0, 0);
      int u = q.front();
                                                             build();
      q.pop();
                                                           }
      for (int &v : ady[u]) {
                                                           // 0(1)
        if (color[v] < 0) q.push(v), color[v] =</pre>
                                                           int lca(int u, int v) {
        int l = min(first[u], first[v]);
        if (color[v] == color[u]) return false;
                                                             int r = max(first[u], first[v]);
                                                             int i = log2(r - 1 + 1);
    }
                                                             return F(st[i][1], st[i][r + 1 - (1 << i)]).second;</pre>
  }
                                                           }
  return true;
                                                           void addEdge(int u, int v) {
                                                             ady[u].push_back(v);
                                                             ady[v].push_back(u);
3.7 LCA
                                                           }
// st = sparse table
                                                                 MST Kruskal
                                                           3.8
typedef pair<int, int> T;
int neutro = 0;
                                                           // N = number of nodes, Wedge = Weighted Edge
vector<vector<T>> st;
                                                           #include "../Data Structures/Graphs/UnionFind.cpp"
                                                           typedef int T;
vector<int> first;
                                                           typedef pair<int, int> Edge;
vector<T> tour;
                                                           typedef pair<T, Edge> Wedge;
vector<vector<int>> ady;
                                                           vector<Wedge> Wedges;
                                                           vector<Wedge> mst;
void initVars(int N) {
                                                           UnionFind uf(0);
  ady.assign(N, vector<int>());
                                                           void initVars(int N) {
                                                             mst.clear();
T F(T a, T b) {
                                                             Wedges.clear();
                                                             uf = UnionFind(N);
  return a.first < b.first ? a : b;</pre>
                                                           T kruskal() {
void build() {
                                                             T cost = 0;
  st.assign(log2(tour.size()),
                                                             sort(Wedges.begin(), Wedges.end());

    vector<T>(tour.size()));
                                                             // reverse(Wedges.begin(), Wedges.end());
  st[0] = tour:
                                                             for (Wedge &wedge : Wedges) {
  for (int i = 1; (1 << i) <= tour.size(); i++)
                                                               int u = wedge.second.first, v =
    for (int j = 0; j + (1 << i) <= tour.size(); j++)

    wedge.second.second;

    \rightarrow st[i][j] = F(st[i - 1][j], st[i - 1][j + (1 <<
                                                               if (!uf.areConnected(u, v)) uf.join(u, v),

    (i - 1))]);

→ mst.push_back(wedge), cost += wedge.first;

}
                                                             }
                                                             return cost;
```

void addEdge(int u, int v, T w) {
 Wedges.push\_back({w, {u, v}});

}

### 3.9 MST Prim

```
// st = spanning tree, p = parent
// vis = visited, dist = distance
typedef int T;
typedef pair<int, int> Edge;
typedef pair<T, Edge> Wedge;
typedef pair<T, int> DistNode;
int MAXN = 20001, INF = 1 << 30;
vector<vector<int>> ady;
unordered_map<int, unordered_map<int, T>> weight;
vector<int> p, vis;
vector<T> dist;
vector<vector<Wedge>> msts;
void initVars(int N) {
  ady.assign(N, vector<int>());
  p.assign(N, 0);
  vis.assign(N, 0);
  dist.assign(N, INF);
  weight.clear();
 msts.clear();
// O(E * log(V))
T prim(int s) {
  vector<Wedge> mst;
  vector<set<Edge>::iterator> pos(ady.size());
  vector<T> dist(ady.size(), INF);
  set<Edge> q;
  T cost = dist[s] = 0;
  q.insert({0, s});
  while (q.size()) {
    int u = q.begin()->second;
    q.erase(q.begin());
    vis[u] = 1, cost += dist[u];
    mst.push_back({dist[u], {p[u], u}});
    for (int &v : ady[u]) {
      T w = weight[u][v];
      if (!vis[v] && w < dist[v]) {</pre>
        if (dist[v] != INF) q.erase(pos[v]);
        pos[v] = q.insert({dist[v] = w, v}).first;
      }
    }
  msts.push_back(vector<Wedge>(mst.begin() + 1,

→ mst.end()));
 return cost;
```

```
T primLazy(int s) {
  vector<Wedge> mst;
  vector<set<Edge>::iterator> pos(ady.size());
  vector<T> dist(ady.size(), INF);
  priority queue DistNode, vector DistNode,

    greater<DistNode>> q;

  T cost = dist[s] = 0;
  q.push({0, s});
  while (q.size()) {
    pair<int, int> aux = q.top();
    int u = aux.second;
    q.pop();
    if (dist[u] < aux.first) continue;</pre>
    vis[u] = 1, cost += dist[u];
    mst.push_back({dist[u], {p[u], u}});
    for (int &v : ady[u]) {
      T w = weight[u][v];
      if (!vis[v] && w < dist[v]) q.push({dist[v] = w,</pre>

    v});
    }
  msts.push_back(vector<Wedge>(mst.begin() + 1,

→ mst.end()));
  return cost;
}
// O(V + E * log(V))
T prim() {
  T cost = 0;
  map<int, T> q;
  for (int i = 0; i < ady.size(); i++)</pre>
    if (!vis[i]) cost += prim(i);
  return cost;
}
void addEdge(int u, int v, T w) {
  ady[u].push_back(v);
  weight[u][v] = w;
  ady[v].push_back(u);
  weight[v][u] = w;
}
3.10
       ShortestPaths
3.10.1 Bellman Ford
//N = number of nodes
// returns {} if there is a negative weight cycle
typedef int T;
int MAXN = 20001, N, INF = 1 << 30, isDirected = true;</pre>
vector<vector<int>> ady;
unordered_map<int, unordered_map<int, T>> weight;
void initVars(int N) {
  ady.assign(N, vector<int>());
```

weight.clear();

}

```
// O(V * E)
vector<T> bellmanFord(int s) {
  vector<T> dist(ady.size(), INF);
  dist[s] = 0;
  for (int i = 1; i <= adv.size(); i++)</pre>
    for (int u = 0; u < ady.size(); u++)</pre>
      for (auto &v : ady[u]) {
        T w = weight[u][v];
        if (dist[u] != INF && dist[u] + w < dist[v]) {</pre>
          if (i == ady.size()) return {};
          dist[v] = dist[u] + w;
  return dist;
void addEdge(int u, int v, T w) {
  ady[u].push_back(v);
  weight[u][v] = w;
  if (isDirected) return;
  ady[v].push_back(u);
  weight[v][u] = w;
3.10.2 Dijkstra
typedef int T;
typedef pair<T, int> DistNode;
int MAXN = 20001, INF = 1 << 30, isDirected = false;</pre>
vector<vector<int>> ady;
unordered_map<int, unordered_map<int, T>> weight;
void initVars(int N) {
  ady.assign(N, vector<int>());
  weight.clear();
// O(E * lg(V))
vector<int> dijkstra(int s) {
  vector<set<DistNode>::iterator> pos(ady.size());
  vector<T> dist(ady.size(), INF);
  set<DistNode> q;
  q.insert({0, s}), dist[s] = 0;
  while (q.size()) {
    int u = q.begin()->second;
    q.erase(q.begin());
    for (int &v : ady[u]) {
      T w = weight[u][v];
      if (dist[u] + w < dist[v]) {</pre>
        if (dist[v] != INF) q.erase(pos[v]);
        pos[v] = q.insert({dist[v] = dist[u] + w,
        → v}).first;
      }
    }
  }
 return dist;
```

```
vector<int> dijkstraLazy(int s) {
  vector<int> dist(ady.size(), INF);
  priority_queue<DistNode, vector<DistNode>,

    greater<DistNode>> q;

  q.push(\{0, s\}), dist[s] = 0;
  while (q.size()) {
    DistNode top = q.top(); q.pop();
    int u = top.second;
    if (dist[u] < top.first) continue;</pre>
    for (int &v : ady[u]) {
      T w = weight[u][v];
      if (dist[u] + w < dist[v]) q.push({dist[v] =</pre>
       \rightarrow dist[u] + w, v});
    }
  }
  return dist;
void addEdge(int u, int v, T w) {
  ady[u].push_back(v);
  weight[u][v] = w;
  if (isDirected) return;
  ady[v].push_back(u);
  weight[v][u] = w;
}
```

### 3.11 Strongly Connected Components

```
// tv = top value from stack
// sccs = strongly connected components
// scc = strongly connected component
// disc = discovery time
// low = low time
// s = stack
// top = top index of the stack
int Time, top;
vector<vector<int>> ady, sccs;
vector<int> disc, low, s;
void initVars(int N) {
  ady.assign(N, vector<int>());
}
void dfsSCCS(int u) {
  if (disc[u]) return;
  low[u] = disc[u] = ++Time;
  s[++top] = u;
  for (int &v : ady[u]) dfsSCCS(v), low[u] =

    min(low[u], low[v]);
  if (disc[u] == low[u]) {
    vector<int> scc;
   while (true) {
      int tv = s[top--];
      scc.push_back(tv);
      low[tv] = ady.size();
      if (tv == u) break;
    sccs.push_back(scc);
}
```

```
// O(N)
void SCCS() {
    s = low = disc = vector<int>(ady.size());
    Time = 0, top = -1, sccs.clear();
    for (int u = 0; u < ady.size(); u++) dfsSCCS(u);
}
void addEdge(int u, int v) {
    ady[u].push_back(v);
}</pre>
```

### 3.12 Topological Sort

```
// vis = visited
vector<vector<int>> ady;
vector<int> vis, toposorted;
void initVars(int N) {
 ady.assign(N, vector<int>());
 vis.assign(N, 0);
 toposorted.clear();
// returns false if there is a cycle
bool toposort(int u) {
 vis[u] = 1;
 for (auto &v : ady[u])
   if (v != u && vis[v] != 2 && (vis[v] ||
    vis[u] = 2;
 toposorted.push_back(u);
 return true;
// O(N)
bool toposort() {
 vis.clear();
 for (int u = 0; u < ady.size(); u++)</pre>
   if (!vis[u] && !toposort(u)) return false;
 return true;
```

### 4 Maths

### 4.1 Number Theory

### 4.1.1 Divisibility Criterion

```
def divisorCriteria(n, lim):
    results = []
    tenElevated = 1
    for i in range(lim):
        \# remainder = pow(10, i, n)
        remainder = tenElevated % n
        negremainder = remainder - n
        if(remainder <= abs(negremainder)):</pre>
            results.append(remainder)
        else:
            results.append(negremainder)
        tenElevated *= 10
    return results
def testDivisibility(dividend, divisor,

    divisor_criteria):

    dividend = str(dividend)
    addition = 0
    dividendSize = len(dividend)
    i = dividendSize - 1
    j = 0
    while j < dividendSize:</pre>
        addition += int(dividend[i]) *

    divisor_criteria[j]

        i -= 1
        j += 1
    return addition % divisor == 0
if __name__ == '__main__':
    dividend, divisor = map(int, input().split())
    divisor_criteria = divisorCriteria(divisor,
    → len(str(dividend)))
    print(divisor_criteria)
    print(testDivisibility(dividend, divisor,

→ divisor_criteria))
4.1.2 Extended Euclidean
// qcd(a, b) = ax + by
vector<long long int> extendedGCD(long long int a,
→ long long int b) {
 if (a > OLL && b == OLL) {
    return {a, 1LL, 0LL};
  }
  long long int x = 1LL, y = 0LL, prevx = 0LL, prevy =
  \hookrightarrow 1LL, q, remainder;
  while (true) {
    q = a / b;
    remainder = a - b * q;
    if (remainder == OLL) break;
    a = b;
    b = remainder;
    x = x - prevx * q;
    swap(x, prevx);
    y = y - prevy * q;
    swap(y, prevy);
  // gcd = b, x = prevx, y = prevy
  return {b, prevx, prevy};
}
```

### 4.1.3 GCD

```
// recursive
int gcd(int a, int b) {
  return !b ? a : gcd(b, a % b);
}

// iterative
int gcd(int a, int b) {
  while (b) {
    a %= b;
    swap(a, b);
  }
  return a;
}

4.1.4 LCM

int lcm(int a, int b) {
```

### 4.1.5 Prime Check Miller Rabin

return c ? a / c \* b : 0;

int c = gcd(a, b);

```
from random import randrange
def is_prime(p):
   k = 100
    if p == 2 or p == 3:
       return True
    if (p \& 1) == 0 or p == 1:
       return False
    phi = p - 1
    d = phi
   r = 0
    while (d & 1) == 0:
        d = int(d >> 1)
        r += 1
    for i in range(k):
        a = randrange(2, p - 2)
        exp = pow(a, d, p)
        if exp == 1 or exp == p - 1:
            continue
        flag = False
        for j in range(r - 1):
            exp = pow(exp, 2, p)
            if exp == 1:
                return False
            if exp == p - 1:
                flag = True
                break
        if flag:
            continue
        else:
            return False
    return True
```

### 4.1.6 Prime Sieve

```
vector<int> primeSieve(int n) {
  vector<int> sieve(n + 1);
  for (int i = 4; i <= n; i += 2) sieve[i] = 2;
  for (int i = 3; i * i <= n; i += 2)
    if (!sieve[i])
     for (int j = i * i; j <= n; j += 2 * i)
        if (!sieve[j]) sieve[j] = i;
  return sieve;
}</pre>
```

### 5 Strings

### 5.1 KMP

```
// f = error function
// cf = create error function
// p = pattern
// t = text
// pos = positions where pattern is found in text
int MAXN = 1000000;
vector<int> f(MAXN + 1);
vector<int> kmp(string &p, string &t, int cf) {
  vector<int> pos;
  if (cf) f[0] = -1;
  for (int i = cf, j = 0; j < t.size();) {
    while (i > -1 \&\& p[i] != t[j]) i = f[i];
   i++, j++;
   if (cf) f[j] = i;
   if (!cf && i == p.size()) pos.push_back(j - i), i
    \rightarrow = f[i];
  return pos;
vector<int> search(string &p, string &t) {
  kmp(p, p, -1);
                   // create error function
  return kmp(p, t, 0); // search in text
}
```

### 5.2 Rabin Karp

```
class RollingHash {
  public:
    vector<unsigned long long int> pow;
    vector<unsigned long long int> hash;
    unsigned long long int B;
```

```
RollingHash(const string &text) : B(257) {
    int N = text.size();
    pow.resize(N + 1);
   hash.resize(N + 1);
   pow[0] = 1;
   hash[0] = 0;
   for (int i = 1; i <= N; ++i) {
      // in c++ an unsigned long long int is
      // automatically modulated by 2^64
     pow[i] = pow[i - 1] * B;
     hash[i] = hash[i - 1] * B + text[i - 1];
   }
 unsigned long long int getWordHash() {
   return hash[hash.size() - 1];
  }
  unsigned long long int getSubstrHash(int begin, int
   return hash[end] - hash[begin - 1] * pow[end -
      begin + 1];
  int size() {
   return hash.size();
 }
};
vector<int> rabinKarp(RollingHash &rhStr, string
vector<int> positions;
 RollingHash rhPattern(pattern);
 unsigned long long int patternHash =

¬ rhPattern.getWordHash();
  int windowSize = pattern.size(), end = windowSize;
  for (int i = 1; end < rhStr.size(); i++) {</pre>
    if (patternHash == rhStr.getSubstrHash(i, end))
    \rightarrow positions.push_back(i);
   end = i + windowSize;
 }
 return positions;
}
    Techniques
```

### 6.1 Binary Search

### 6.2 Multiple Queries

```
6.2.1 Mo
// q = query
```

// qs = queries

```
int 1, r;
};
int blksize;
vector<Query> qs;
vector<int> arr;
void initVars(int N, int M) {
  arr = vector<int>(N);
  qs = vector<Query>(M);
}
bool cmp(Query &a, Query &b) {
  if (a.1 == b.1) return a.r < b.r;
  return a.l / blksize < b.l / blksize;</pre>
}
void getResults() {
  blksize = (int)sqrt(arr.size());
  sort(qs.begin(), qs.end(), cmp);
  int prevL = 0, prevR = -1;
  int sum = 0;
  for (auto &q : qs) {
    int L = q.1, R = q.r;
    while (prevL < L) {</pre>
      sum -= arr[prevL]; // problem specific
      prevL++;
    while (prevL > L) {
      prevL--;
      sum += arr[prevL]; // problem specific
    while (prevR < R) {</pre>
      prevR++;
      sum += arr[prevR]; // problem specific
    while (prevR > R) {
      sum -= arr[prevR]; // problem specific
      prevR--;
    cout << "sum[" << L << ", " << R << "] = " << sum
     }
int main() {
  initVars(9, 2);
  arr = \{1, 1, 2, 1, 3, 4, 5, 2, 8\};
  qs = \{\{0, 8\}, \{3, 5\}\};
  getResults();
}
6.2.2 SQRT Decomposition
// sum of elements in range
int neutro = 0;
vector<int> arr;
vector<int> blks;
```

struct Query {

```
void initVars(int n) {
  arr.assign(n, neutro);
 blks.assign(sqrt(n), neutro);
void preprocess() {
 for (int i = 0, j = 0; i < arr.size(); i++) {
    if (i == blks.size() * j) j++;
    blks[j - 1] += arr[i]; // problem specific
}
// problem specific
void update(int i, int val) {
 blks[i / blks.size()] += val - arr[i];
 arr[i] = val;
int query(int 1, int r) {
  int sum = 0;
  int lblk = 1 / blks.size();
  if (l != blks.size() * lblk++)
    while (1 < r && 1 != lblk * blks.size()) {</pre>
      sum += arr[1]; // problem specific
      1++;
    }
  while (l + blks.size() <= r) {</pre>
    sum += blks[l / blks.size()]; // problem specific
    1 += blks.size();
  while (1 <= r) {
    sum += arr[1]; // problem specific
    1++;
  }
  return sum;
int main() {
  initVars(10);
  arr = \{1, 5, 2, 4, 6, 1, 3, 5, 7, 10\};
 preprocess();
  for (int i = 0; i < blks.size() + 1; i++) cout <<</pre>

    blks[i] << " ";
</pre>
  // output: 8 11 15 10
  cout << endl;</pre>
  cout << query(3, 8) << " ";
  cout << query(1, 6) << " ";</pre>
  update(8, 0);
  cout << query(8, 8) << endl;</pre>
  // output: 26 21 0
 return 0;
```