



# UNIVERSITAT POLITÈCNICA DE VALÈNCIA

## Fuzzy Modelling Toolbox for Aircraft Systems

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## USER MANUAL

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# 1 Introduction

Nowadays, there is an important reliance on automatic control systems in aviation. Some of the critical phases of the flight, like the final approach, induce that many variables should be controlled simultaneously. Therefore, the improvement of control algorithms combined with navigation systems, directly contributes to have a secure flight. These results have a common source before being implemented: a reliable aircraft dynamic model.

The classic aircraft dynamic models are on the most part composed by 15 non-linear differential equations, which are not the best option in order to adjust the control laws. The most common solution for this model identification, is by transfers functions methods, but there are also some inconvenient. These methods work due to a model linearisation from an equilibrium point, and for a normal flight, there are many different stages with one equilibrium point for each one. The outcome is a considerable number of different controllers.

This is the main fact for investigate a different dynamic model using a methodology based on fuzzy logic. These Fuzzy Models, have a considerable advantage in front of classic model, because it can be implemented one unified control system for all the model. They are composed by a combination of consequent and membership functions, which turn out into a sum of rules. Therefore this method is better than classic ones as it reduces computing costs.

The main objective will be the research of another version of conventional aircraft dynamic model, using Fuzzy Logic methods.

The main goal of this toolbox is to provide a general dynamic model based on fuzzy logic for aircraft systems, using a clear interface to maximize the user experience. The toolbox provides a complete definition and simulation environment for Fuzzy Aircraft Models based on Takagi-Sugeno structure.

In *doc* folder, user will find a detailed description of the classic aircraft dynamic models based on 15 non-linear differential equations.

## 2 Toolbox Installation and Uninstalling

The installation is straightforward and it does not require any changes to your system settings. The user should create a sub-directory to copy into all the toolbox files. If the toolbox was provided as a zip file, unzip it in this directory. Once all ready, the user should run MAIN.m script for begin to work with the GUI. It is indispensable to run it with Matlab program as it expected. Once all is copied into your work-space folder, it should look as showed in figure 1.

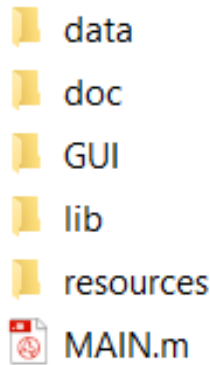


Figure 1: Toolbox directory

For uninstalling is as simple as installation procedure. The only step is to delete the directory mentioned before.

## 3 Aircraft Input Parameters Panel

First of all, for create any Aircraft fuzzy model, it should be defined some variables as defined in the *Model Description pdf*. It is important to understand which are the variables composing this system. As shown in figure 2, there are some components in these panel which are divided by Selection buttons, controller buttons and others.

### 3.1 Parameter Selection Buttons

These buttons are charged to select which input parameter of the aircraft would be introduced by the user to define an aircraft model. There are 5 different classes:

- **mig**: Mass and Geometry aircraft parameters.
- **coef**: Aerodynamic aircraft coefficients. There is a coefficient pop-up added to the panel, any type of coefficient can be chosen. In figure 2, this case is shown.
- **atm**: Atmospheric, altitudes and temperature conditions.
- **eng**: Engines parameters.
- **act**: Control Surface parameters (Aileron, Elevator and Rudder).

Of course, each of these panels or tabs, present an input parameter name label and its parameter value input which can be edited by the user. The labels can be confuse due to controller buttons (described in the next section), there is a "Model Description" button, where all the information about the model and input parameters is described.

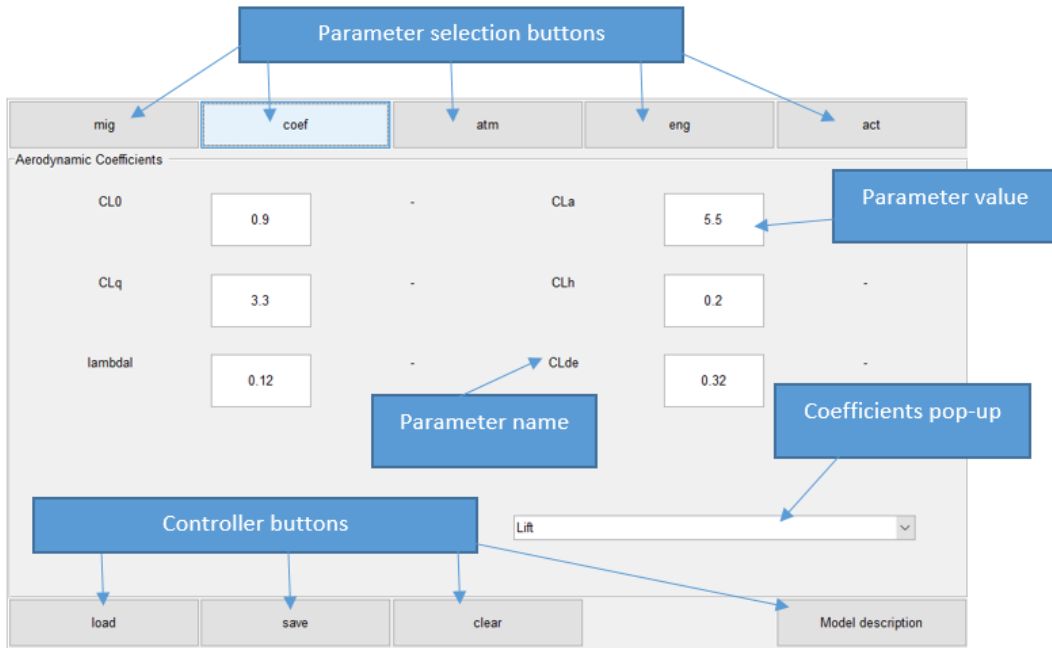


Figure 2: Aircraft Input Parameters Panel

### 3.2 Controller Buttons

In this section, a description of action buttons for showing, saving and loading is presented. In fact, there are four actions that can be execute with these controllers.

- **load**: Open browse window to select a .mat file with all the input data. In figure 3 is shown an example to load data saved in folder *SavedData*.
- **save**: Save in a .mat file the current input parameters introduced in all the aircraft input parameters panel.
- **clear**: Set all the parameters value to 0.
- **Model Description**: Show a document with detail model description for better understanding of each variable.

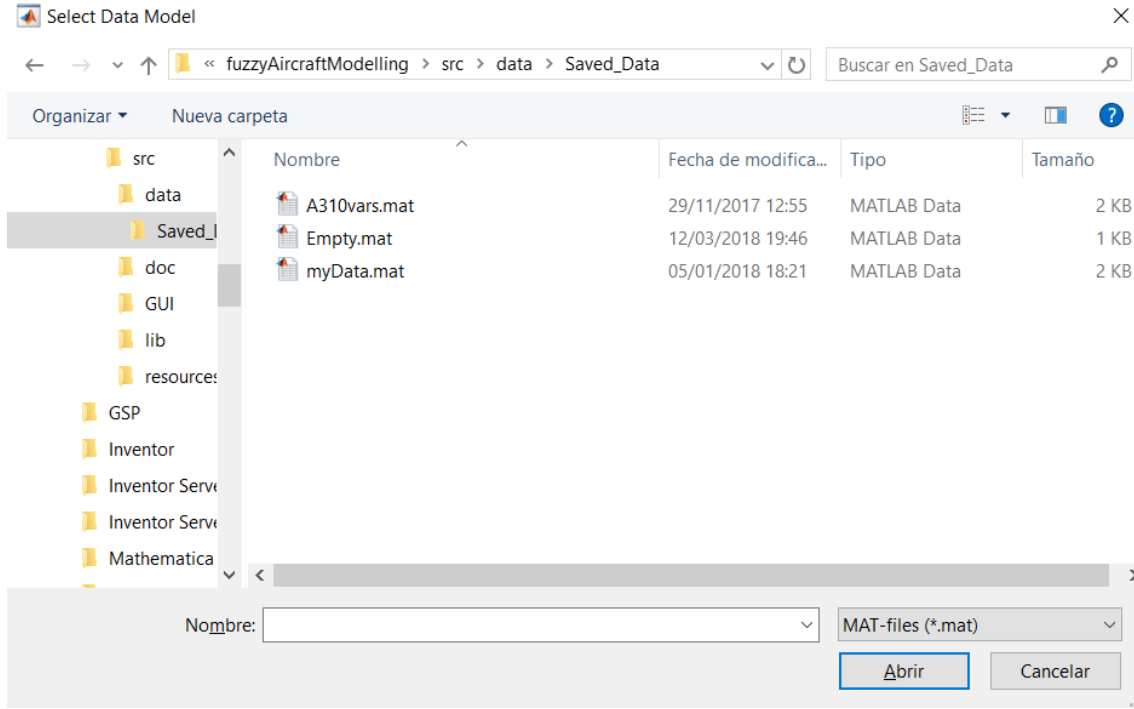


Figure 3: Select Data window

## 4 Fuzzy Model Limits Panel

The user have to define a set o variable limits to create the aircraft dynamic fuzzy model. Obviously, it is important to understand which is the meaning of each limit. In table 1, there is a description of the fuzzy limits variables that affect in this section. How it can be supposed, for some variables it is difficult to know what value should be set. For that reason, there is a *Default* button, to get the default values decided by the developer.

Table 1: Fuzzy limits description

Fuzzy Limits [min] [max]	
alpha	angle-of-attack
beta	sideslip angle
pVa	$\frac{p}{V_a}$
qVa	$\frac{q}{V_a}$
rVa	$\frac{r}{V_a}$
Va2	$V_a^2$
VazVax	$\frac{V_{az}}{V_{ax}}$
VayVa	$\frac{V_{ay}}{V_a}$
Hlg	Distance of the landing gear to the ground

Once the fuzzy limits are clear, there is two columns for each variable. Left column is designated to set the Minimum value and the right column for the Maximum value. After that, *Create* button generates the custom fuzzy aircraft model. All of these values are saved by default in data for get more comfortable usage. In the following figure 4, an example of the general fuzzy model limits panel can be shown. If user can not define which are the meaning of the variables described in table 1, then it is recommendable to get more information about at *Model Description.pdf*.

The screenshot shows a software interface titled "Fuzzy Model Limits". It contains several input fields for defining the limits of various variables. Each variable is listed on the left, followed by two input boxes for minimum and maximum values, and a unit label on the right. The variables and their limits are:

- alpha**: -1 to 1, unit: rad
- beta**: -1.5708 to 1.5708, unit: rad
- pVa**: -1 to 1, unit: rad/m
- qVa**: -1 to 1, unit: rad/m
- rVa**: -1 to 1, unit: rad/m
- Va2**: 1 to 500, unit: m<sup>2</sup>/s<sup>2</sup>
- VazVax**: -40 to 40, unit: -
- VayVa**: -1 to 1, unit: -
- Hlg**: 0 to 8000, unit: m

At the bottom right, there are two buttons: "Default" and "Create".

Figure 4: Fuzzy Limits Panel

## 5 Membership Function Plot Panel

This panel is only available once the fuzzy model is created and It is composed by 3 elements as figure 5 shows.

- **Non-linear terms pop-up:** User can select the non-linear term membership function to plot. The variables included in this pop-up are described in table 2. For more information, see *Toolbox Documentation.pdf*.
- **Plot Membership Button:** Once the non-linear term is selected, a figure containing all the membership functions that the non-linear term computes in the fuzzy model. For more information about the membership types description and nomenclature, see *Toolbox Documentation.pdf*. An example is shown in figure 6.
- **Model Rule nomenclature:** General composition diagram of the fuzzy model rule with the membership function.

Table 2: Non-Linear Variables  
Non-Linear Variables

alpha	angle-of-attack
beta	side-slip angle
Va	airspeed
CL1	first lift coefficient non-lineal term
CL2	second lift coefficient non-lineal term
CD2	first drag coefficient non-lineal term
Cl1	first roll coefficient non-lineal term
Cl2	second roll coefficient non-lineal term
Cm1	first pitch coefficient non-lineal term
Cm2	second pitch coefficient non-lineal term
Cn1	first yaw coefficient non-lineal term
Cn2	second yaw coefficient non-lineal term
Cn3	third yaw coefficient non-lineal term

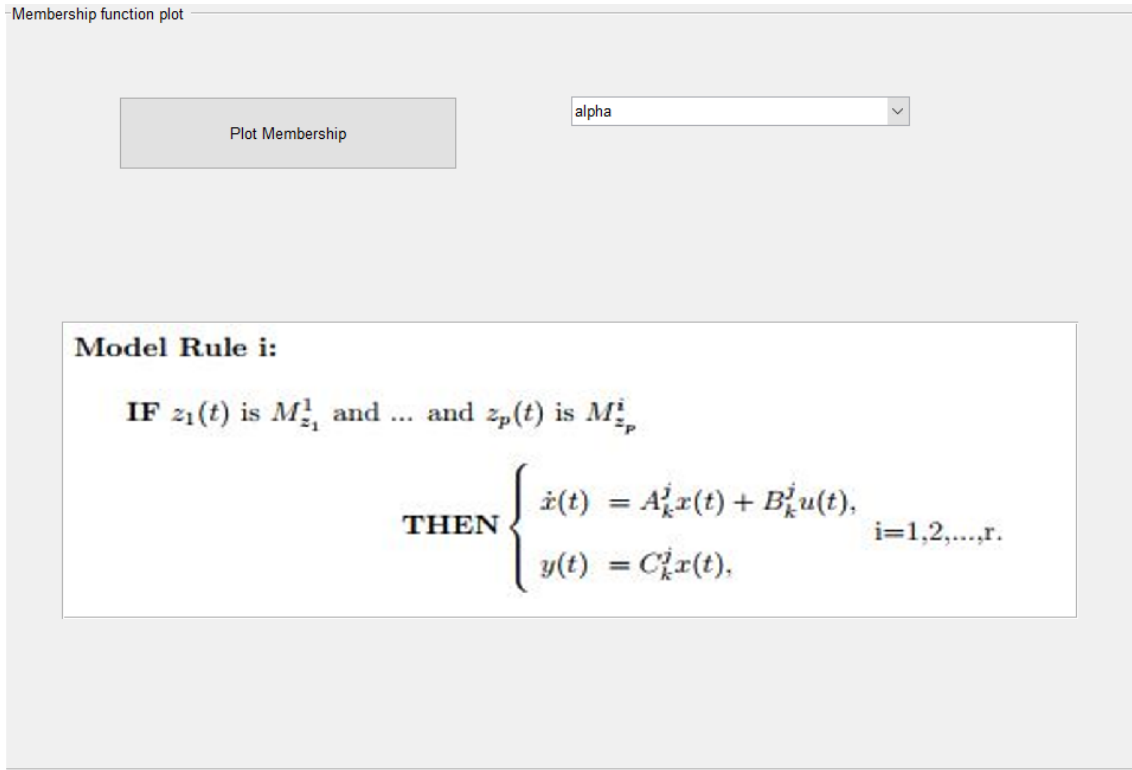


Figure 5: Membership Plot Panel

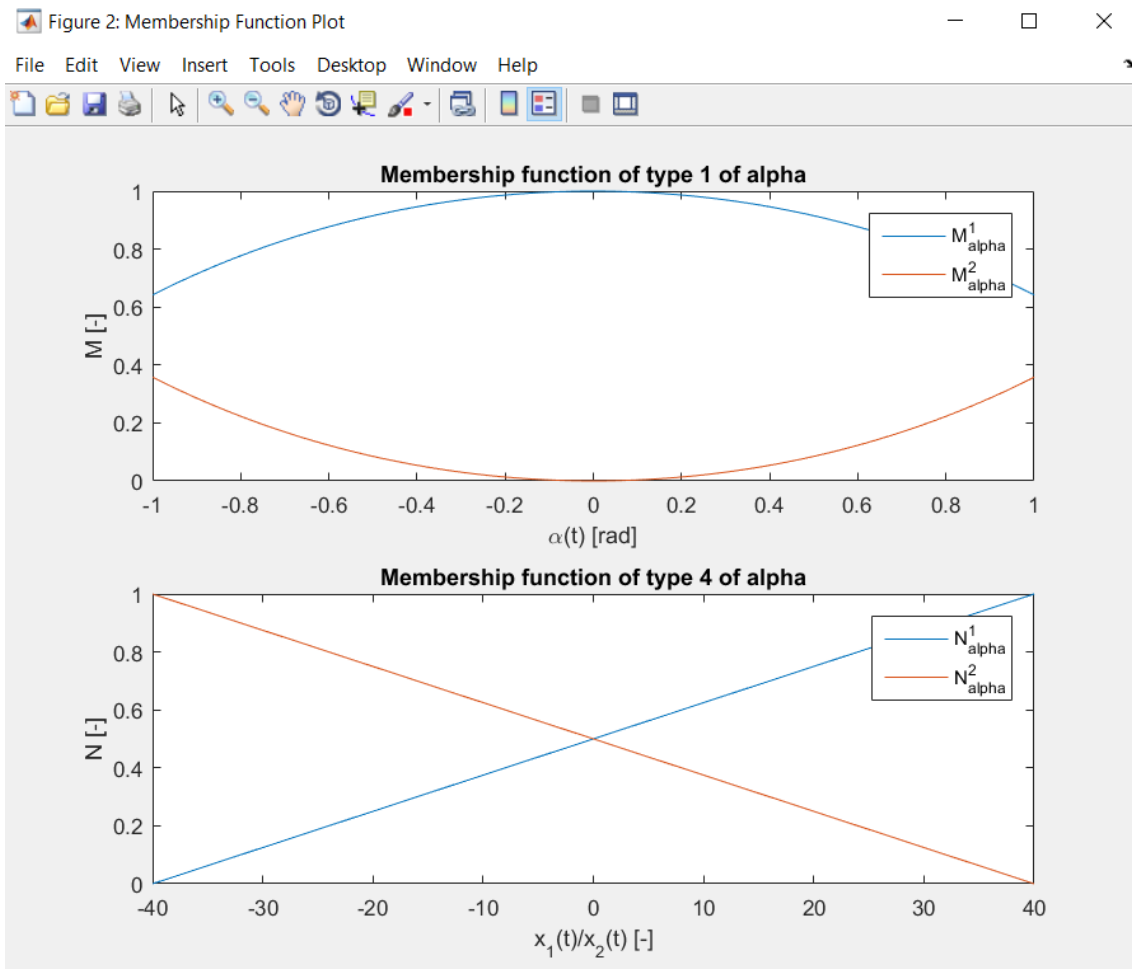


Figure 6: Membership functions figure

## 6 Simulation Panel

As the figure 7 shows, this panel is divided in three components: Inputs, Outputs and General Components. In the last of these, there is the Simulation *Time(s)* duration, where the user should introduce the maximum simulation time. On the other hand, Simulation button will start the evaluation of the fuzzy model. Note that, in some scenarios, the simulation can take few minutes due to the complexity of the system and the defuzzification procedure before to obtain the simulation results.

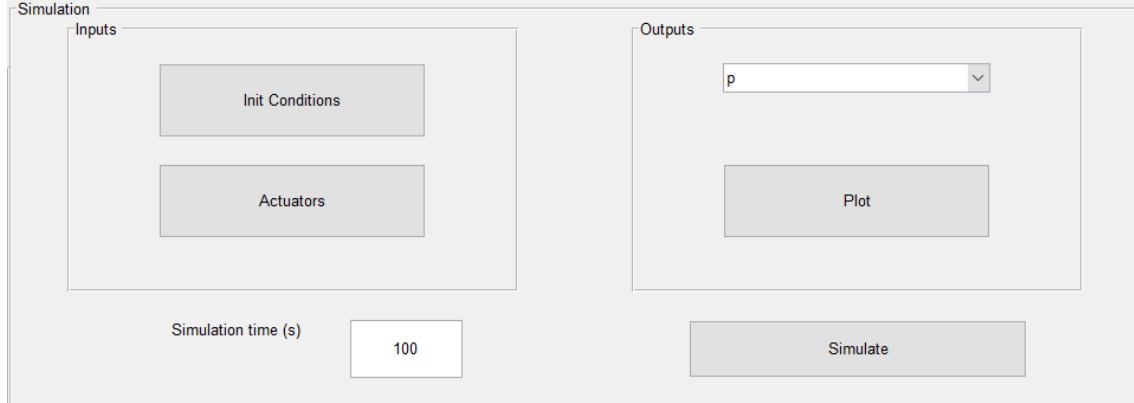


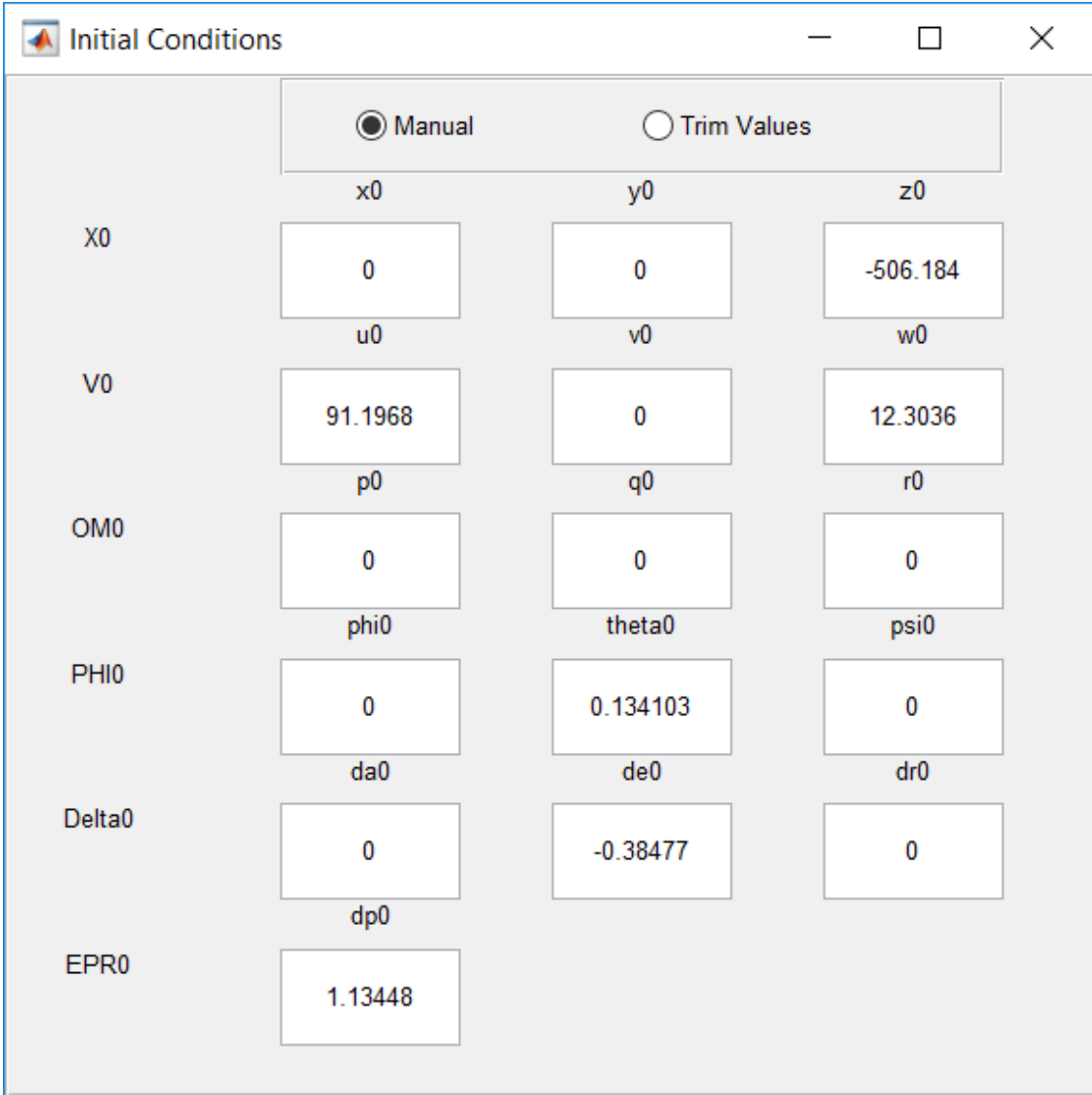
Figure 7: Simulation Panel

### 6.1 Inputs

To maximize the user experience, some variables should be declared. For this reason, this panel includes the functionality to define initial conditions for internal variables and control actions (control surfaces).

- **Init Conditions:** By clicking on this button, a configuration window (figure 8) is visualized. All the values for the state variables have to be defined. Further information about nomenclature, please check *Model Description.pdf*. On the other hand, two ways to introduce initial values: manually or trimmed. First option allows the user to study a particular case or flight scenario. The second option, trimmed, the toolbox automatically will calculate the values of the aircraft to start the simulation in an equilibrium point.
- **Actuators:** In this window, the user can define the amplitude of the action of the actuator, the step time (when the control surface is modified) and how much time their will be at this value (Step Duration). Figure 9 shows an example of control inputs.



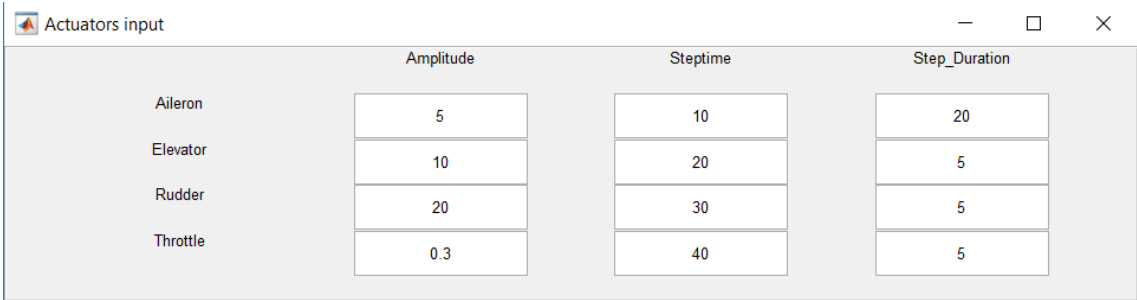


Initial Conditions

☒ Manual
 ☐ Trim Values

	x0	y0	z0
X0	0	0	-506.184
	u0	v0	w0
V0	91.1968	0	12.3036
	p0	q0	r0
OM0	0	0	0
	phi0	theta0	psi0
PHI0	0	0.134103	0
	da0	de0	dr0
Delta0	0	-0.38477	0
	dp0		
EPR0	1.13448		

Figure 8: Initial conditions window



Actuators input

	Amplitude	Step time	Step_Duration
Aileron	5	10	20
Elevator	10	20	5
Rudder	20	30	5
Throttle	0.3	40	5

Figure 9: Actuators inputs window

## 6.2 Outputs

Finally, in this panel, once the simulation has finished (indicated by the progress bar), the time response of the state variables is *plotted* in figure. This panel is composed by two elements: a state variable selection pop-up and a Plot button. Once the user has selected the state variable to display, the correspond figure is generated by clicking in the Plot button (figure 10), where the selected state variable and actuators time response will be represented.

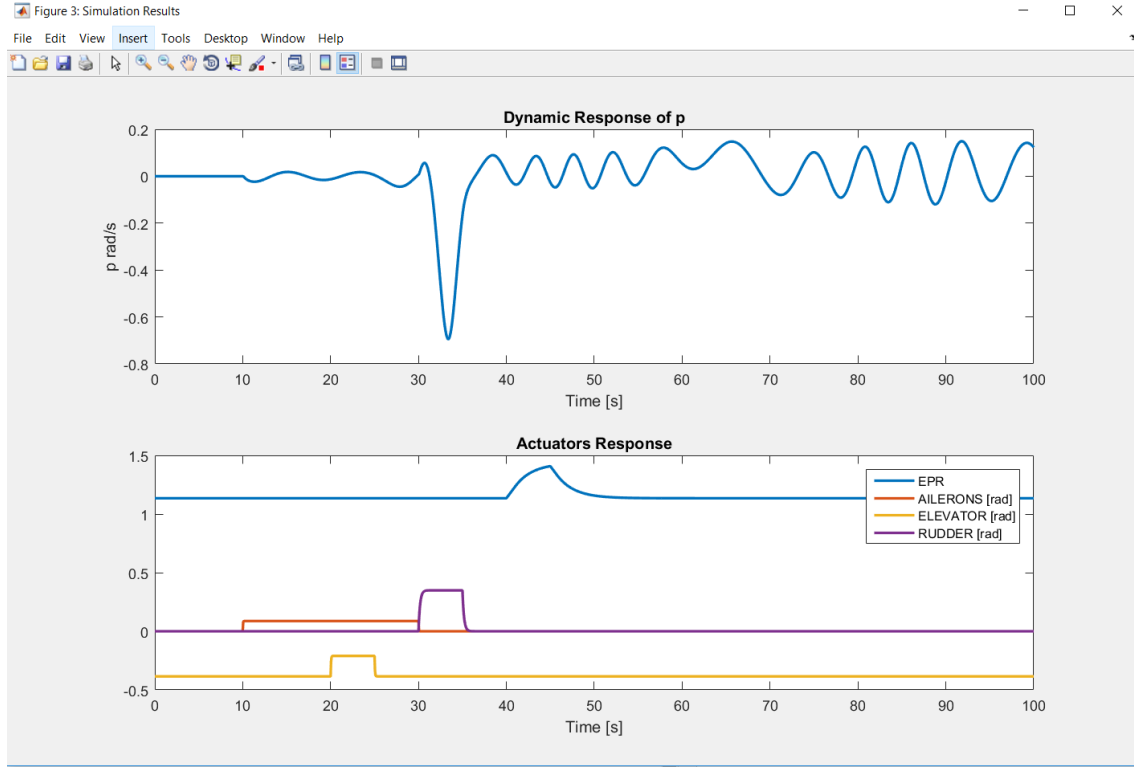


Figure 10: Simulation Results figure

## 7 External Example: Airbus A310

The functions implemented in this toolbox can be used without the GUI window, using the functions developed directly. To illustrate this functionality, the folder *doc* contains the Matlab script "*DemoA310.m*", which executes the same example that the main GUI (Airbus A310 aircraft fuzzy dynamic model) but shows how to use the functions without the graphical environment.

In this script, first it begins calculating the trim values for the initial conditions that they should be an input of the ode's solvers. There is a SolveODEs path that includes some solvers for the differential equations. In this case it gonna be used ode1 that it is a simple solver using Euler's method. After calculate the initial conditions, it initialize the parameters as a function ParamsInput. This function only create the param struct explained before. Next, it is time to define the inputs values, the actuators and engines in front of the time. It is important for simulate to know the actuators of the aircraft. It follows as the fuzzy modelling, with all the aircraft parameters it creates the FIS struct including the fuzzy model of the non-linear terms. Then it can be calculated the response of the non-linear dynamic and the fuzzy model dynamic of the aircraft.

Them on the figure 11 it can be observed one of the validation variable state parameter. Also it has been plotted the membership functions of each variable as it shows the illustration 12.

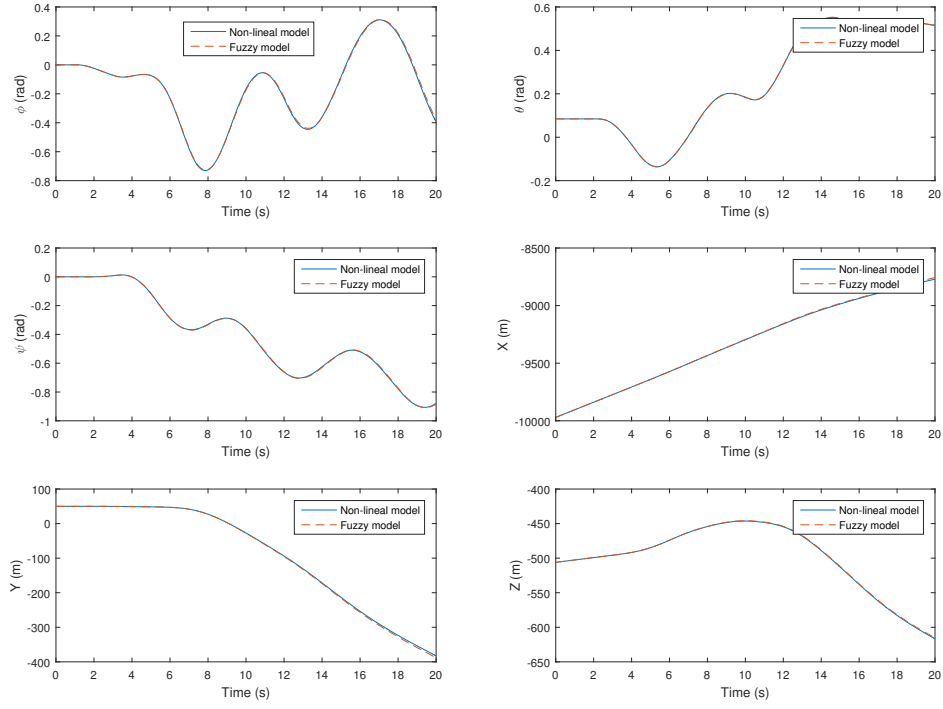


Figure 11: Validation of the system state variables

## 8 Data and Functions Reference

### 8.1 Data Structures

#### 8.1.1 param

The aerodynamic coefficients are governed by the following equations:

$$\begin{aligned}
 C_L &= C_{L0} + C_{L\alpha}\alpha(t) + \frac{\bar{c}}{V_a(t)}C_{Lq}q(t) + C_{L\delta_e}\delta_e + C_{LH}e^{-\lambda_L H_{LG}(t)} \\
 C_Y &= C_{Y\beta}\beta(t) + C_{Yr}\delta_r \\
 C_D &= C_{D0} + C_{D\alpha}\alpha(t) + C_{D\alpha_2}\alpha(t)^2
 \end{aligned} \tag{1}$$

$$\begin{aligned}
 C_l &= C_{l\beta}\beta(t) + \frac{\bar{c}}{V_a(t)}(C_{lp}p(t) + (C_{lr0} + C_{lr\alpha}\alpha(t))r(t)) + C_{l\delta_a}\delta_a + C_{l\delta_r}\delta_r \\
 C_m &= C_{m0} + C_{m\alpha}\alpha(t) + \frac{\bar{c}}{V_a(t)}C_{mq}q(t) + C_{m\delta_e}\delta_e + (C_{mH0} + C_{mH\alpha}\alpha(t))e^{-\lambda_m H_{LG}(t)} \\
 C_n &= (C_{n\beta_0} + C_{n\beta_\alpha}\alpha(t))\beta(t) + \frac{\bar{c}}{V_a(t)}(C_{nr}r + (C_{np0} + C_{np\alpha}\alpha(t))p(t)) + C_{n\delta_a}\delta_a + C_{n\delta_r}\delta_r
 \end{aligned} \tag{2}$$

Table 3: param.coef structure

Aerodynamic Coefficients (param.coef)					
.CL0	.CLa	.CLq	.CLh	.lambdal	.CLde
.CYb	.CYdr	.CD0	.CDa	.CDa2	.Clb
.Clp	.Clr0	.Clra	.Clda	.Clldr	.Cm0
.Cma	.Cmq	.Cmh0	.Cmha	.lambdam	.Cmde
.Cnb0	.Cnba	.Cnp0	.Cnpa	.Cnr	.Cnda
.Cndr					

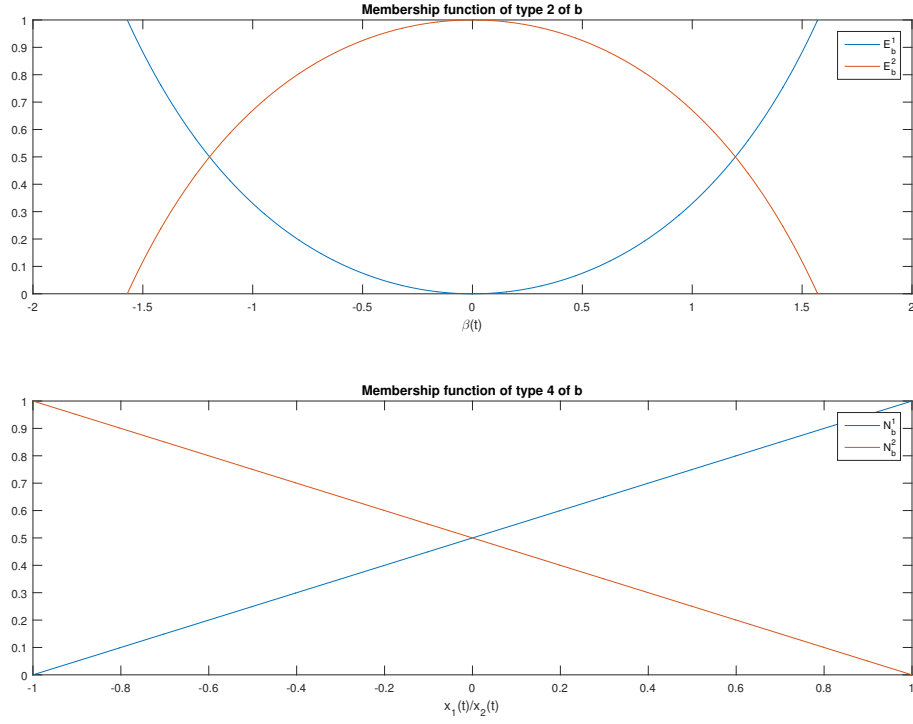


Figure 12: Example of the membership function plot

Table 4: param.mig structure

Mass and Geometry (param.mig)	
.Sref	Reference surface, $m^2$
.Lref	Aircraft mean chord, m
.mass	aircraft mass, kg
.I	Aircraft matrix of inertia, $kg/m^2$
.J	Inverse of the matrix of inertia
.dxg	distance in x axis of the aerodynamic center, m
.dze	distance in z axis of the engines thrust, m

Table 5: param.atm struct

Mass and Geometry (param.mig)	
.To	Reference temperature, K
.rho	air density, $kg/m^3$

Table 6: param.eng structure

Engines (param.eng)	
.Ga	Coefficient of thrust equation
.Gb	Coefficient of thrust equation
.tau	time constant, s
.RL	rate limit

Table 7: param.act structure

Actuators (param.act)	
.tau	1x3 vector with time constants
.RL	1x3 vector with rate limits

Table 8: param.lim structure

Input limits (param.lim = [max,min])	
.a	angle-of-attack
.b	sideslip angle
.pVa	$\frac{p}{V_a}$
.qVa	$\frac{q}{V_a}$
.rVa	$\frac{r}{V_a}$
.Va2	$V_a^2$
.VazVax	$\frac{V_{az}}{V_{ax}}$
.VayVa	$\frac{V_{ay}}{V_a}$
.Hlg	Distance of the landing gear to the ground

### 8.1.2 FIS

This struct is composed by all the non-linear terms of the classic aircraft dynamic model. The non-linear terms are described on the following table 9. In each variable mentioned, there is always

Table 9: FIS. structure	
Non-linear variables (FIS.)	
.a	angle-of-attack
.b	sideslip angle
.Va	airspeed
.CL1	first lift coefficient non-linear term
.CL2	second lift coefficient non-linear term
.CD2	first drag coefficient non-linear term
.Cl1	first roll coefficient non-linear term
.Cl2	second roll coefficient non-linear term
.Cm1	first pitch coefficient non-linear term
.Cm2	second pitch coefficient non-linear term
.Cn1	first yaw coefficient non-linear term
.Cn2	second yaw coefficient non-linear term
.Cn3	third yaw coefficient non-linear term

the same structure which define the fuzzy model.

**.mf:** In this struct it will be defined the membership function where it gonna be an nx3 matrix where n are the different types of membership function matrix. The first column of the matrix define the type of membership function. There are 5 types where:

- 1 =  $\text{atan}(x)$  type
- 2 =  $\text{asin}(x)$  type
- 3 =  $\sqrt{x}$  type
- 4 =  $\frac{x_1}{x_2}$  type
- 5 =  $e^{-x}$  type

The other two columns are the maximums and minimums of the membership function. If there are Global sector, this values are only use to plot the membership function.

**.c:** This struct define the fuzzy model consequent for each rule and it is an rxm matrix where r are the number of rules. The first column define if the consequent is 'constant' or if it is 'linear'. On the first case, m=2 and the second column takes the constant value. For the second case, m=3 and the second and third column are a and b coefficients respectively of an  $y = ax + b$  equation.

**.r:** This struct is an entire number which define the number of rules of the fuzzy model system.

## 8.2 Fuzzy Library

### 8.2.1 actuators.m

#### Purpose

This function returns the differential equation of the actuators dynamics of ailerons, elevators and rudder. They are been modeled as first-order differential equation.

#### Function

[ ddeltadt ] = actuators(t, delta, input_t, input_u, param)
---

#### Description

t = instant time value, sec  
 delta = 1x3 vector with the actuators deflections as delta=[da,de,dr]  
 input\_t = column time input vector, sec  
 input\_u = column actuators deflection input vector  
 param = struct with actuators parameters

For this function, param should be defined by the time constant and rates limits of the actuators dynamics as param.act.tau and param.act.RL respectively. This function will return the derivative of the actuators with respect the time in 1x3 vector  $[\frac{dda}{dt}, \frac{dde}{dt}, \frac{ddr}{dt}]$

#### See Also

param, engines.m, dFuzzyModeldt.m

### 8.2.2 calcc.m

#### Purpose

This function calculate the consequent of a fuzzy model with the function input. The consequents can be constants or lineal, it depends of the fuzzy model consequent matrix.

#### Function

`[ C ] = calcc ( c , u , n )`

#### Description

c = Consequent Matrix of the FIS struct  
 u = input values of the model system, is a column vector  
 n = Number of rules (number of consequents), include in the FIS struct.

The function output is the calculated consequent of the model included in the FIS struct. The output C is a nxm matrix where n has the same length that the input vector u and m is the number of rules.

#### See Also

FIS, calcfuzzy.m, calcmf.m

### 8.2.3 calcfuzzy.m

#### Purpose

This function calculate the defuzzyfication using the FIS struct model with the membership functions and consequent matrix information.

#### Function

`[ yout ] = calcfuzzy ( fisvar , x , u )`

#### Description

fisvar = FIS struct of the variable model with mfs and c matrix struct  
 x = Input variables of the membership functions  
 u = Input variables of the consequent functions (optional).

The function output will be the defuzzyfication of the system model. It uses the functions calcc.m and calcmf to calculate consequent and membership function respectively. The input of the consequent are optional for the reason that in many times, there are constant.

#### See Also

FIS, calcc.m, calcmf.m

#### 8.2.4 calcmf.m

##### Purpose

This function returns the value of each membership function of the model introducing the input variable of the membership function.

##### Function

$[M] = \text{calcmf}(\text{mf}, x, n)$

##### Description

mf = membership matrix of the FIS struct  
x = membership input  
n = number of membership types

The function output will be the membership function values where it is an struct for each membership function type. Each strut will have two columns for the reason of the pairs of the memberships function into each type.

##### See Also

FIS, calcc.m, calcfuzzy.m, plotmf.m

#### 8.2.5 DefaultMaxMin.m

##### Purpose

With this function, the intention is to set defaults maximums and minimums values for the fuzzy model system when the user has not defined it.

##### Function

$[param] = \text{DefaultMaxMin}(param)$

##### Description

param = aircraft parameters values.

The output will be an actualisation of the input param. The function has the objective of read all the param struct searching the limits and if they are not defined, it set the default values.

##### See Also

param, NoLin2Fis.m

#### 8.2.6 dFuzzyModeldt.m

##### Purpose

This function joins all the aircraft dynamic model with the differential equations based on fuzzy models of the non-linear terms and based on quaternions.

##### Function

$[dYoutdt] = \text{dFuzzyModeldt}(t, Y, input\_t, input\_u, param)$

##### Description



t	=	instant time (seconds)
Y	=	initial conditions of the variables states [OM, V, Quat, X]
input_t	=	time vector column of system inputs, sec
input_u	=	values vector column of the system inputs
param	=	aircraft parameters values, on this case it should be included param.FIS with the FIS struct of the aircraft.
OM	=	angular rates vector, rad/s
V	=	aircraft velocity vector, m/s
Quat	=	quaternions vector
X	=	aircraft position vector, m

The output of this function will be the derivative of the states variables of the system as dY-outdt =  $[\frac{dOM}{dt}, \frac{dV}{dt}, \frac{dQuat}{dt}, \frac{dX}{dt}]$ , and it will be an 1x13 vector.

#### See Also

param, dNoLindt.m, NoLin2FIS

### 8.2.7 dNoLindt.m

#### Purpose

This function joins all the differential equations of the classic aircraft dynamic model. Its structure is similar to the dFuzzyModeldt.m structure.

#### Function

[ dYoutdt ] = dNoLindt( t , Y , input\_t , input\_u , param )

#### Description

t	=	instant time (seconds)
Y	=	initial conditions of the variables states [OM, V, PHI, X]
input_t	=	time vector column of system inputs, sec
input_u	=	values vector column of the system inputs
param	=	aircraft parameters values, it is not necessary to include param.FIS
OM	=	angular rates vector, rad/s
V	=	aircraft velocity vector, m/s
PHI	=	euler angles, rad
X	=	aircraft position vector, m

The output of this function will be the derivative of the states variables of the system as dY-outdt =  $[\frac{dOM}{dt}, \frac{dV}{dt}, \frac{dPHI}{dt}, \frac{dX}{dt}]$ , and it will be an 1x12 vector.

#### See Also

param, dFuzzyModeldt.m, NoLin2FIS

### 8.2.8 engines.m

#### Purpose

This function returns the differential equation of the engines dynamics of the exhaust pressure ratio. It has been modelated as first-order differential equation.

#### Function

[ deprdt ] = engines( t , epr , input\_t , input\_u , param )

#### Description

t = instant time value, sec  
 epr = Exhaust pressure ratio, initial condition  
 input\_t = column time input vector, sec  
 input\_u = column EPR input vector  
 param = struct with engine parameters

For this function, param should be defined by the time constant and rates limits of the engines dynamics as param.eng.tau and param.eng.RL respectively. This function will return the derivative of the EPR with respect the time.

#### See Also

param, actuators.m, dFuzzyModeldt.m

### 8.2.9 mfplot.m

#### Purpose

This function plot the input membership function with the FIS.mfs matrix structure. It recognize the set limits in the conversion to FIS from non-linear.

#### Function

mfplot( mf, varname )
-----------------------

#### Description

mf = membership function matrix.  
 varname = name of the variable of the fuzzy model (optional)

Introducing the membership function matrix struct from a variable of the FIS, it returns one figure with one or two plots, it depends of the number of membership function types of the variable.

#### See Also

FIS, NoLin2FIS.m

### 8.2.10 NoLin2FIS.m

#### Purpose

This function gives the FIS struct including all the information of the fuzzy models merged from the aircraft specifications. FIS gives the information of the nonlinear terms of the classic model that it has been converted on fuzzy model.

#### Function

[ FIS ] = NoLin2FIS(param)
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#### Description

param = aircraft parameters values.

As aircraft parameter values inputs, this function calculates al the membership functions and consequents of the fuzzy model for each non-lineal term of the aircraft dynamic system. It returns a FIS struct.

#### See Also

param, FIS, calcfuzzy.m

## 9 Further Information

Please do not hesitate to contact us for any comments, questions or clarifications via email at [pabbrufe@upv.es](mailto:pabbrufe@upv.es) or [sgnieto@isa.upv.es](mailto:sgnieto@isa.upv.es).