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Unscented Kalman Filters

REVIEW

CODE REVIEW 6

HISTORY

▼ src/ukf.cpp 6

```
1 #include "ukf.h"
2 #include "Eigen/Dense"
3 #include <math.h>
4 #include <iostream>
5
6 using namespace std;
7 using Eigen::MatrixXd;
8 using Eigen::VectorXd;
9 using std::vector;
10
11 /**
12  * Initializes Unscented Kalman filter
13  * This is scaffolding, do not modify
14  */
15 UKF::UKF() {
16     // if this is false, laser measurements will be ignored (except during init)
17     use_laser_ = true;
18
19     // if this is false, radar measurements will be ignored (except during init)
20     use_radar_ = true;
21
22     // initial state vector
23     x_ = VectorXd(5);
24
25     // initial covariance matrix
26     P_ = MatrixXd(5, 5);
```

```

27
28 // Process noise standard deviation longitudinal acceleration in m/s^2
29 std_a_ = 2;

```



AWESOME

Good job tuning the **Longitudinal Acceleration Parameter** ! Other students have used values up to 3

```

30
31 // Process noise standard deviation yaw acceleration in rad/s^2
32 std_yawdd_ = 1;

```



AWESOME

Good job tuning the **Yaw Acceleration Noise Parameter** .Seems you have a good intuition and chose a

```

33
34 //DO NOT MODIFY measurement noise values below these are provided by the sen
35 // Laser measurement noise standard deviation position1 in m
36 std_laspx_ = 0.15;
37
38 // Laser measurement noise standard deviation position2 in m
39 std_laspy_ = 0.15;
40
41 // Radar measurement noise standard deviation radius in m
42 std_radr_ = 0.3;
43
44 // Radar measurement noise standard deviation angle in rad
45 std_radphi_ = 0.03; // Original value.
46
47 // Radar measurement noise standard deviation radius change in m/s
48 std_radr_ = 0.3; // Original value.
49 //DO NOT MODIFY measurement noise values above these are provided by the sen
50
51 // state vector: [pos1 pos2 vel_abs yaw_angle yaw_rate] in SI units and rad
52 x_ << 0.0, 0.0, 0.0, 0.0, 0.0;
53
54 ///< state covariance matrix
55 P_ << 10.0, 0.0, 0.0, 0.0, 0.0,
56      0.0, 10.0, 0.0, 0.0, 0.0,
57      0.0, 0.0, 10.0, 0.0, 0.0,
58      0.0, 0.0, 0.0, 10.0, 0.0,
59      0.0, 0.0, 0.0, 0.0, 10.0;
60
61 time_us_ = 0;
62 is_initialized_ = false;
63
64 ///< State dimension
65 n_x_ = 5;
66
67 // Augmented state dimension
68 n_aug_ = n_x_ + 2;
69
70 // Radar measurement dimension
71 n_z_ = 3;
72

```

```

73 // Lidar measurement dimension
74 n_l_ = 2;
75
76 // Initializing measurement noise matrix R.
77 R_radar_ = MatrixXd(n_z_, n_z_);
78 R_radar_.fill(0.0);
79 R_radar_(0, 0) = pow(std_radr_, 2);
80 R_radar_(1, 1) = pow(std_radphi_, 2);
81 R_radar_(2, 2) = pow(std_radrdrd_, 2);
82
83 // Initializing measurement noise matrix R.
84 R_lidar_ = MatrixXd(n_l_, n_l_);
85 R_lidar_.fill(0.0);
86 R_lidar_(0, 0) = pow(std_laspx_, 2);
87 R_lidar_(1, 1) = pow(std_laspy_, 2);
88
89 ///< Sigma point spreading parameter
90 lambda_ = 3 - static_cast<int>(n_aug_);
91
92 // Predicted sigma points. Need to be shared between prediction and radar me
93 Xsig_pred_ = MatrixXd(n_x_, 2 * n_aug_ + 1);
94
95 // Create and set vector for weights of sigma points.
96 weights_ = VectorXd(2 * n_aug_ + 1);
97 weights_(0) = lambda_ / (lambda_ + n_aug_);
98 float weight_other = 1 / (lambda_ + n_aug_) / 2;
99 for (unsigned i = 1; i < 2 * n_aug_ + 1; ++i) {
100     weights_(i) = weight_other;
101 }
102 }
103
104 UKF::~UKF() {}
105
106 /**
107  * @param {MeasurementPackage} meas_package The latest measurement data of
108  * either radar or laser.
109  */
110 void UKF::ProcessMeasurement(const MeasurementPackage & meas_package) {
111     /*****
112      * Initialization
113      *****/
114     if (!is_initialized_) {
115         // First measurement.
116         cout << "UKF: initializing..." << endl;
117
118         if (meas_package.sensor_type_ == MeasurementPackage::RADAR) {
119             /**
120              Convert radar from polar to Cartesian coordinates and initialize state.
121              */
122             float rho = meas_package.raw_measurements_[0];
123             float phi = meas_package.raw_measurements_[1];
124             //float delta_rho = meas_package.raw_measurements_[2];
125
126             x_(0) = rho * cos(phi);
127             x_(1) = rho * sin(phi);
128
129             x_(2) = 0;
130             x_(3) = 0;
131             x_(4) = 0;
132
133         }

```

```

134     else if (meas_package.sensor_type_ == MeasurementPackage::LASER) {
135         /**
136         Initialize state.
137         */
138         x_(0) = meas_package.raw_measurements_[0];
139         x_(1) = meas_package.raw_measurements_[1];
140     }
141 }
142
143 // Initializing time of the state vector.
144 time_us_ = meas_package.timestamp_;
145 // Done initializing, no need to predict or update.
146 is_initialized_ = true;
147 return;
148 }
149
150 /*****
151  * Prediction
152  *****/
153 float delta_t = (meas_package.timestamp_ - time_us_) / 1000000.0;
154 // Updating time-measurement state of KF.
155 time_us_ = meas_package.timestamp_;
156
157 // Updating state transition matrix based on elapsed time. For brevity, only
158 // elements that depend on time.
159
160 // Noise `ax` and `ay` are given as constants in this problem.
161 // Updating process covariance matrix based on elapsed time. For readability
162 Prediction(delta_t);
163
164 /*****
165  * Update
166  *****/
167
168 if (meas_package.sensor_type_ == MeasurementPackage::RADAR) {
169     // Radar updates.
170     UpdateRadar(meas_package);
171 } else {
172     // Laser updates.
173     UpdateLidar(meas_package);
174 }
175
176 // Print the output of the state and its covariance.
177 //cout << "x_ = " << x_ << endl;
178 //cout << "P_ = " << P_ << endl;
179 }
180
181 /**
182  * Predicts sigma points, the state, and the state covariance matrix.
183  * @param {double} delta_t the change in time (in seconds) between the last
184  * measurement and this one.
185  */
186 void UKF::Prediction(double delta_t) {
187     MatrixXd Xsig_aug;
188     // Create sigma point matrix.
189     Xsig_aug = MatrixXd(n_aug_, 2 * n_aug_ + 1);
190
191     GenerateSigmaPoints(Xsig_aug);
192     PredictSigmaPoints(Xsig_aug, Xsig_pred_, delta_t);
193     PredictMeanAndCovariance(Xsig_pred_);
194 }

```

```

195
196 /**
197  * Updates the state and the state covariance matrix using a laser measurement
198  * @param {MeasurementPackage} meas_package
199  */
200 void UKF::UpdateLidar(const MeasurementPackage & meas_package) {

```



AWESOME

Good job using the standard equations for the linear LIDAR case.

```

201
202   VectorXd z(2);
203   z(0) = meas_package.raw_measurements_[0];
204   z(1) = meas_package.raw_measurements_[1];
205
206   MatrixXd H_laser = MatrixXd(n_l_, n_x_);
207   H_laser << 1.0, 0.0, 0.0, 0.0, 0.0,
208              0.0, 1.0, 0.0, 0.0, 0.0;
209
210   VectorXd z_pred = H_laser * x_;
211   VectorXd y = z - z_pred;
212   MatrixXd S = H_laser * P_ * H_laser.transpose() + R_lidar_;
213   MatrixXd PHt = P_ * H_laser.transpose();
214   MatrixXd K = PHt * S.inverse();
215
216   // Updating estimate.
217   x_ = x_ + (K * y);
218   MatrixXd I = MatrixXd::Identity(n_x_, n_x_);
219   P_ = (I - K * H_laser) * P_;
220
221   // Calculating NIS value
222   float epsilon = y.transpose() * S.inverse() * y;
223   cout << "Lidar NIS value=" << epsilon << endl;
224 }
225
226 /**
227  * Updates the state and the state covariance matrix using a radar measurement
228  * @param {MeasurementPackage} meas_package
229  */
230 void UKF::UpdateRadar(const MeasurementPackage & meas_package) {
231
232   VectorXd z(n_z_), z_pred(n_z_);
233   float rho = meas_package.raw_measurements_[0];
234   float phi = meas_package.raw_measurements_[1];
235   float delta_rho = meas_package.raw_measurements_[2];
236   z << rho, phi, delta_rho;
237
238   // Predicted state covariance in the measurement space.
239   MatrixXd S = MatrixXd(n_z_, n_z_);
240
241   // Predicted sigma points in the radar measurement space.
242   MatrixXd Zsig = MatrixXd(n_z_, 2 * n_aug_ + 1);
243
244   PredictRadarMeasurement(Xsig_pred_, Zsig, z_pred, S);
245
246   // Matrix for cross-correlation Tc
247   MatrixXd Tc = MatrixXd(n_x_, n_z_);
248   Tc.fill(0.0);

```

```

249
250 for (unsigned i = 0; i < Zsig.cols(); ++i) {
251     // Calculating state difference.
252     VectorXd x_diff = Xsig_pred.col(i) - x_;
253     // Angle psi normalization to [-PI, PI].
254     while (x_diff(3) > M_PI) x_diff(3) -= 2. * M_PI;
255     while (x_diff(3) < -M_PI) x_diff(3) += 2. * M_PI;
256
257     // Calculating Z-residual.
258     VectorXd z_diff = Zsig.col(i) - z_pred;
259     // Angle phi normalization to [-PI, PI].
260     while (z_diff(1) > M_PI) z_diff(1) -= 2. * M_PI;
261     while (z_diff(1) < -M_PI) z_diff(1) += 2. * M_PI;
262
263     Tc += weights_(i) * x_diff * z_diff.transpose();
264 }
265
266 // Calculate Kalman gain K.
267 MatrixXd K = MatrixXd(n_x_, n_x_);
268 K.fill(0.0);
269 K = Tc * S.inverse();
270
271 // Calculate measurement residual.
272 VectorXd z_diff = z - z_pred;
273
274 // Angle phi normalization to [-PI, PI].
275 while (z_diff(1) > M_PI) z_diff(1) -= 2. * M_PI;
276 while (z_diff(1) < -M_PI) z_diff(1) += 2. * M_PI;
277
278 x_ = x_ + K * z_diff;
279 P_ = P_ - K * S * K.transpose();
280
281 // Calculating NIS value
282 float epsilon = z_diff.transpose() * S.inverse() * z_diff;
283 cout << "Radar NIS value=" << epsilon << endl;
284 }
285
286 /**
287  * Populates provided matrix with sigma points based on the current state and
288  * @param pointer to MatrixD matrix that will store results.
289  */
290 void UKF::GenerateSigmaPoints(MatrixXd & Xsig_aug) {
291     // Create augmented mean vector.
292     VectorXd x_aug = VectorXd(n_aug_);
293     x_aug.head(n_x_) = x_;
294     x_aug(n_x_) = 0;
295     x_aug(n_x_ + 1) = 0;
296
297     // Create augmented covariance matrix.
298     MatrixXd P_aug = MatrixXd(n_aug_, n_aug_);
299     P_aug.fill(0.0);
300     P_aug.topLeftCorner(n_x_, n_x_) = P_;
301     P_aug(n_x_, n_x_) = std_a_ * std_a_;
302     P_aug(n_x_ + 1, n_x_ + 1) = std_yawdd_ * std_yawdd_;
303     // Calculate square root of P_aug.
304     MatrixXd A = P_aug.llt().matrixL();
305     // Actually placing the values inside the matrix.
306     // 1. Assigning the mean vector as a first column.
307     Xsig_aug.col(0) = x_aug;
308     // 2. Assigning the values of the second and third group of sigmas.
309     for (unsigned i = 0; i < n_aug_; i++)

```

```

310 {
311     Xsig_aug.col(i + 1)      = x_aug + sqrt(lambda_ + n_aug_) * A.col(i);
312     Xsig_aug.col(i + 1 + n_aug_) = x_aug - sqrt(lambda_ + n_aug_) * A.col(i);
313 }
314
315 }
316
317 void UKF::PredictSigmaPoints(const MatrixXd & Xsig_aug, MatrixXd & Xsig_pred,
318     // Set state and augmented vector dimensions.
319     Xsig_pred.fill(0.0);
320
321     // Predict sigma points.
322     for (unsigned i = 0; i < 2* n_aug_ + 1; ++i) {
323         // The following five items of the vector is CTRV model vector
324         float px = Xsig_aug(0, i);
325         float py = Xsig_aug(1, i);
326         float v = Xsig_aug(2, i);
327         float psi = Xsig_aug(3, i);
328         float psi_dot = Xsig_aug(4, i);
329         // The following two items are noise vector nu for longitudinal accelera
330         float nu_a = Xsig_aug(5, i);
331         float nu_psi = Xsig_aug(6, i);
332
333         // Computing stochastic part common for both cases when psi is either 0
334         float px_stochastic = pow(delta_t, 2) * cos(psi) * nu_a / 2;
335         float py_stochastic = pow(delta_t, 2) * sin(psi) * nu_a / 2;
336         float v_stochastic = delta_t * nu_a;
337         float psi_stochastic = pow(delta_t, 2) * nu_psi / 2;
338         float psi_dot_stochastic = delta_t * nu_psi;
339
340         float px_gain = 0; // Initializing, re-defining below according to situa
341         float py_gain = 0; // Initializing, re-defining below according to situa
342         float v_gain = 0;
343         float psi_gain = psi_dot * delta_t;
344         float psi_dot_gain = 0;
345
346         // Computing gain factor between two states. Avoiding division by zero.
347         if (fabs(psi_dot) < 0.001) {

```



AWESOME

Good job checking for 0.

You could save the value `0.001` as a constant to enable the compiler to optimise the implementation.

If you want to optimise this even further, you can replace all constants in your code with MACROS.

Check out this [post](#) to learn more about MACROS.

```

348         px_gain = v * cos(psi) * delta_t;
349         py_gain = v * sin(psi) * delta_t;
350     }
351     else {
352         px_gain = v / psi_dot * (sin(psi + psi_dot * delta_t) - sin(psi));
353         py_gain = v / psi_dot * (-cos(psi + psi_dot * delta_t) + cos(psi));
354     }
355
356     Xsig_pred(0, i) = px + px_gain + px_stochastic;
357     Xsig_pred(1, i) = py + py_gain + py_stochastic;
358     Xsig_pred(2, i) = v + v_gain + v_stochastic;
359     Xsig_pred(3, i) = psi + psi_gain + psi_stochastic;

```

```

360     Xsig_pred(4, i) = psi_dot + psi_dot_gain + psi_dot_stochastic;
361 }
362
363 }
364
365 void UKF::PredictMeanAndCovariance(const MatrixXd & Xsig_pred){
366     // Create vector for predicted state.
367     VectorXd x = VectorXd(n_x_);
368     x.fill(0.0);
369
370     // Create covariance matrix for prediction.
371     MatrixXd P = MatrixXd(n_x_, n_x_);
372     P.fill(0.0);
373
374     // Predict state mean.
375     for (unsigned i = 0; i < Xsig_pred.cols(); ++i) {
376         x += weights_(i) * Xsig_pred.col(i);
377     }
378
379     // Predict state covariance matrix.
380     for (unsigned i = 0; i < Xsig_pred.cols(); ++i) {
381         VectorXd x_diff = Xsig_pred.col(i) - x;
382         // Angle normalization.
383         while (x_diff(3) > M_PI) x_diff(3) -= 2. * M_PI;
384         while (x_diff(3) < -M_PI) x_diff(3) += 2. * M_PI;
385         P += weights_(i) * x_diff * x_diff.transpose();
386     }
387
388     // Write result to existing state and covariance variables.
389     x_ = x;
390     P_ = P;
391 }
392
393 void UKF::PredictRadarMeasurement(const MatrixXd & Xsig_pred, MatrixXd & Zsig,
394     // Initializing measurement space sigma points matrix.
395     Zsig.fill(0.0);
396     // Transform predicted sigma points into measurement space.
397     for (unsigned i = 0; i < Zsig.cols(); ++i) {
398         VectorXd z_measurement = VectorXd(n_z_);
399         float px = Xsig_pred(0, i);
400         float py = Xsig_pred(1, i);
401         float v = Xsig_pred(2, i);
402         float yaw = Xsig_pred(3, i);
403
404         // Calculating rho.
405         z_measurement(0) = sqrt(pow(px, 2) + pow(py, 2));
406         // Calculating phi.
407         z_measurement(1) = atan2(py, px);

```



SUGGESTION

Be aware that `atan2(0.0, 0.0)` is undefined. You would want to prevent this case in a robust industry so

```

408     // Calculating rho_dot.
409     z_measurement(2) = (px * cos(yaw) * v + py * sin(yaw) * v) / z_measurement

```



SUGGESTION

You should make sure, that a zero measurement does not result in a divide by zero here. You could do so with a small epsilon.

```
410
411     Zsig.col(i) = z_measurement;
412
413 }
414
415 // Calculate predicted mean measurement vector.
416 z_pred.fill(0.0);
417 for (unsigned i = 0; i < Zsig.cols(); ++i){
418     z_pred += weights_(i) * Zsig.col(i);
419 }
420
421 // Calculate measurement covariance matrix S.
422 S.fill(0.0);
423 for (unsigned i = 0; i < Zsig.cols(); ++i) {
424     VectorXd z_diff = Zsig.col(i) - z_pred;
425     // Angle normalization for phi.
426     while (z_diff(1) > M_PI) z_diff(1) -= 2. * M_PI;
427     while (z_diff(1) < -M_PI) z_diff(1) += 2. * M_PI;
428     S += weights_(i) * z_diff * z_diff.transpose();
429 }
430
431 // Obtaining updated covariance matrix.
432 S += R_radar_;
433
434 }
435
```

► src/ukf.h

► src/tools.h

► src/tools.cpp

► src/stdout.txt

► src/radar_NIS.txt

► src/plot_NIS.py

► src/measurement_package.h

► src/main.cpp

► src/lidar_NIS.txt

► src/CMakeLists.txt

- ▶ `readme.txt`
- ▶ `install-ubuntu.sh`
- ▶ `install-mac.sh`
- ▶ `cmakepatch.txt`
- ▶ `README.md`
- ▶ `LICENSE`
- ▶ `CMakeLists.txt`

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