

GRAPH THEORY NOTES

ERGZ:
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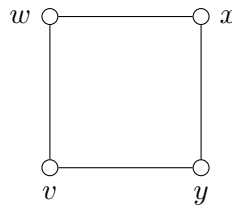
These set of notes are based on readings, excercises from the book Graph Theory by Chartrand and Zhang among other sources.

Among notes, questions that are arise will also be placed in appropriate sections of the notes, solutions to these will be added at appropriate sections as well, all of this will be documented for easy reading.

Definition: A Graph G consists of two sets. The first set V , called the vertex (nodes) set, is a nonempty finite set whose elements are objects called vertices or nodes. The second set E is a set consisting of 2 – *element* subsets of V , called e dges, we call E the *edge set*. We sometimes denote G as $G = (V, E)$ indicating its vertes and edge sets V and E respectively. Lastly we will use $V(G)$ and $E(G)$ to indicate the vertex set and edge set of G respectively.

Definition: Let G and H be both graph we say, G and H are equal, write $G = H$, if and only if $V(G) = V(H)$ and $E(G) = E(H)$.

We will generally be representing these graphs both symbolically as well as in the plane.



Graph G (Figure 1)

The figure above is also called a graph and is the plane representation of $G = (V, E)$. We can write out G symbolically as in the definition as follows:

$V(G) = \{x, y, v, w\}$ and $E(G) = \{(x, y), (y, v), (v, w), (w, x)\}$, note that the ordered pair $(x, y) = (y, x)$, and thus its repitition in the set $E(G)$ is redundant and left out.

Definition: Let G be a graph, it is customary to denote an edge (u, v) simply as uv . If uv is an edge of G then u and v are said to be **adjacent** in G . Moreover the number of vertices in G is the **order** of G (*i.e* $|V(G)|$ is the order of G). Similarly the number of edges is its **size**.