

CS4248  
AY 2012/13 Semester 1  
Problem Set 1

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1.  $(ab(a + \epsilon))^+$
2. Let the DFA be  $M = (Q, \Sigma, \delta, q_0, F)$ .

$$Q = \left\{ \begin{array}{ll} q_0, & \text{both even} \\ q_1, & \text{0s odd} \\ q_2, & \text{1s odd} \\ q_3 & \text{both odd} \end{array} \right\}$$

$$F = \{q_0\}$$

$$\delta(q_0, 0) = q_1$$

$$\delta(q_0, 1) = q_2$$

$$\delta(q_1, 0) = q_0$$

$$\delta(q_1, 1) = q_3$$

$$\delta(q_2, 0) = q_3$$

$$\delta(q_2, 1) = q_0$$

$$\delta(q_3, 0) = q_2$$

$$\delta(q_3, 1) = q_1$$

3. Let  $M' = (Q, \Sigma, \delta, q_0, F')$  be the DFA that produces the complement of  $L(M)$ , then  $F' = Q - F$ .

4. (a)

$$\begin{aligned} \left\{ \begin{array}{c} a \\ b \\ c \\ e \\ f \\ g \end{array} \right\} &\rightarrow \left\{ \begin{array}{c} a \\ b \\ c \\ e \\ f \\ g \end{array} \right\} / \_ \Sigma \\ \left\{ \begin{array}{c} a \\ e \end{array} \right\} &\rightarrow \epsilon / \Sigma \_ \Sigma \end{aligned}$$

(b)

$$\begin{aligned} b &\rightarrow 1 / \Sigma \_ \Sigma \\ c &\rightarrow 1 / \Sigma \_ \Sigma \\ f &\rightarrow 2 / \Sigma \_ \Sigma \\ g &\rightarrow 2 / \Sigma \_ \Sigma \end{aligned}$$

(c)  $x \rightarrow \epsilon / x \_ \Sigma$