```
:- dynamic p/1.
1
     :- dynamic q/1.
2
     :- dynamic r/1.
3
     r(X) := q(X).
4
5
     q(X) :- p(X).
     p(t).
7
     :- dynamic qs/2.
8
     :- dynamic part/4.
9
     :- dynamic app/3.
10
11
     qs([],[]).
12
     qs([X|Xs],Ys) :-
        part(X,Xs,Littles,Bigs),
13
        qs(Littles,Ls),
14
15
        qs(Biqs,Bs),
16
        app(Ls,[X|Bs],Ys).
17
     part(_,[],[],[]).
18
     part(X,[Y|Xs],[Y|Ls],Bs) :- X > Y, part(X,Xs,Ls,Bs).
     part(X,[Y|Xs],Ls,[Y|Bs]) :- X =< Y, part(X,Xs,Ls,Bs).
19
20
21
     app([],Ys,Ys).
22
     app([X|Xs],Ys,[X|Zs]) :- app(Xs,Ys,Zs).
23
     solve(Pred,N):-
24
        setval(step_count,0),
25
26
        (solve_bt(Pred) ->
27
          write('Success.'),nl;
28
          write('Failed.'),nl),
29
        getval(step_count,N).
30
31
     solve_bt(true) :- !.
32
     solve_bt(A) :- arithmetic(A),incval(step_count), !,A.
     solve_bt((A,B)) :- !,solve_bt(A), solve_bt(B).
33
     solve_bt(H) :-
34
35
        clause(H,Body),
        incval(step_count),
36
37
        solve_bt(Body).
38
     arithmetic(_<_).</pre>
39
40
     arithmetic(_>_).
     arithmetic(_=<_).</pre>
41
42
     arithmetic(_>=_).
     arithmetic(_=:=_).
43
     arithmetic(\_=\=\_).
44
```

```
propagate(Cons, Doms, {NewDomains}):-
1
2
        arrayify(Cons, Constraints),
3
        arrayify(Doms, VarsDomains),
4
        var_dom(VarsDomains, Variables, Domains),
5
        domains(Variables, Domains, Constraints, NewDs),
6
           fromto( (Variables, NewDo, NewDomains),
7
                 ([V|RestVar],[D|RestDom],(V:D,RestDomains)),
8
9
                 (RestVar, RestDom, RestDomains),
10
                 ([VLast],[DomLast], VLast:DomLast)) do true
11
        ),!.
12
     domains(Variables, Domains, Constraints, Ranges) :-
13
        findall(A,all_solns(Variables,Domains,Constraints,A),Solutions),
14
15
16
           fromto( (Solutions, Ranges),
17
                 (Solns, [Range | RestRans]),
                (RestSolns, RestRans),
18
19
                 ([[]]_{-}],[])
           ) do minmax(Solns,Range),cutcolumn(Solns,RestSolns)
20
21
        ).
22
23
     all_solns(Variables, Domains, Constraints, A) :-
        length(Domains, N), length(A, N),
24
25
        (
26
           fromto( (Variables, Domains, A),
27
                   ([X|RestV],[D|RestD],[E|RestA]),
28
                 (RestV, RestD, RestA),
29
                   ([],[],[])
30
           ) do member(E,D), X is E
31
        ),(
32
           foreach(Con,Constraints) do Con
33
        ).
34
     minmax(List,(Min..Max)) :-
35
        findall(A,member([A|_],List),D),
36
37
        min(D,Min),
38
        max(D,Max).
39
     cutcolumn(List,Result) :-
40
41
        fromto( (List, Result),
42
              ([[_|RestVals]|RestList],[RestVals|RestResult]),
43
              (RestList, RestResult),
44
              ([],[])) do true.
45
     arrayify({G},Res) :-!, arrayify(G,Res).
46
47
     arrayify((X,Y),[X|Rest]) :-!, arrayify(Y,Rest).
```

```
48
     arrayify(Y,[Y]).
49
50
     consec(N,N,[N]).
     consec(N,M,[N|Rest]) :- N<M,N1 is N+1,consec(N1,M,Rest),!.</pre>
51
52
53
     var_dom([],[],[]).
54
     var_dom([Var:Start..End|Tail],[Var|VarRest],[Dom|DomRest]) :-
55
        consec(Start,End,Dom),
        var_dom(Tail, VarRest, DomRest).
56
```

```
solve(true,_) :- !.
1
     solve((A,B),Callstack) :- !,
2
       solve(A,Callstack),
3
       solve(B,Callstack).
4
5
     solve(H,Callstack) :-!,
       clause(H,Body),
6
       (strict_member(H,Callstack) ->
7
          write('Infinite loop detected, execution aborted'),nl;
8
           solve(Body,[H|Callstack])
9
10
       ).
11
12
13
     arithmetic(_<_).</pre>
     arithmetic(_>_).
14
15
     arithmetic(_=<_).</pre>
16
     arithmetic(_>=_).
17
     arithmetic(_=:=_).
18
     arithmetic(\_=\=\_).
19
20
     strict_member(H,[H1]) :- H==H1.
21
     strict_member(H,[H1|_]) :- H==H1,!.
22
     strict_member(H,[_|T]) :- strict_member(H,T).
23
24
     :- dynamic p/2.
25
     :- dynamic q/1.
     :- dynamic r/1.
26
27
28
     p(X,[X]).
     p(X,[H|T]) :- p(X,T).
29
30
31
```