Assignment 8

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Exercise 1. (478 and 578) Express the point (0,2,0) as a quaternion. Following the steps shown in class for computing the result of a rotation using quaternions, find the result of rotating this point 30 degrees around the line that passes through the origin and the point (1,1,1).

Proof.
$$\therefore q_p = (0, \vec{p}), \ q = [\cos(\phi/2); \sin(\phi/2)\vec{n}], \ q'_p = qq_pq^{-1}$$

Also, $\therefore \vec{p} = (0, 2, 0), \ \vec{n} = \frac{(1, 1, 1)}{\sqrt{1^2 + 1^2 + 1^2}}, \ \phi = 30^{\circ}$

$$\therefore q = (\frac{\sqrt{6} + \sqrt{2}}{4}, \frac{\sqrt{6} - \sqrt{2}}{4}\vec{n}), \ q_p = (0, (0, 2, 0)), \ q^{-1} = (\frac{\sqrt{6} + \sqrt{2}}{4}, (\frac{\sqrt{6} - 3\sqrt{2}}{12}, \frac{\sqrt{6} - 3\sqrt{2}}{12}))$$

$$\therefore qq_p = (\frac{\sqrt{6} - 3\sqrt{2}}{6}, (\frac{\sqrt{6} - 3\sqrt{2}}{6}, \frac{\sqrt{6} + \sqrt{2}}{2}, \frac{3\sqrt{2} - \sqrt{6}}{6}))$$

$$\therefore qq_pq^{-1} = (0, (\frac{2 - 2\sqrt{3}}{3}, \frac{2 + 2\sqrt{3}}{3}, \frac{2}{3}))$$

$$\therefore q'_p = (\frac{2 - 2\sqrt{3}}{3}, \frac{2 + 2\sqrt{3}}{3}, \frac{2}{3})$$