Report on Homework 2

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1 PCA algorithm

Algorithm 1: A variant of k-means

Input: The number of clusters K

Output: $\pi_k, \mu_k, \Sigma_k, (k = 1, 2, ..., K)$

- 1 Initialize the means μ_k , covariances Σ_k , mixing coefficients π_k and threshold Thres;
- 2 Evaluating the initial value of the log likelihood;
- 3 while the convergence criterion of parameters or log likelihood is not satisfied do
- **E step.** Evaluate the responsibilities with the current parameter values:

$$\omega \leftarrow \frac{\pi_k \mathcal{N}(x_n | \mu_k, \Sigma_k)}{\sum\limits_{j=1}^K \pi_j \mathcal{N}(x_n | \mu_j, \Sigma_j)} \quad , \quad \gamma(z_{nk}) \leftarrow \begin{cases} \omega & \omega > Thres \\ 0 & \omega \leq Thres \end{cases}$$

$$z_n \leftarrow \frac{e^{z_{n_i}}}{\sum\limits_{i=1}^K e^{z_{n_j}}}$$

M step. Re-estimate the parameters with the current responsibilities:

$$N_k \leftarrow \sum_{n=1}^N \gamma(z_{nk})$$
 , $\mu_k^{new} \leftarrow \frac{1}{N_k} \sum_{n=1}^N \gamma(z_{nk}) x_n$

$$\Sigma_k^{new} \leftarrow \frac{1}{N_k} \sum_{n=1}^N \gamma(z_{nk}) (x_n - \mu_k^{new}) (x_n - \mu_k^{new})^T$$

$$\pi_k^{new} \leftarrow \frac{N_k}{N}$$

Evaluate the log likelihood:

$$\ln p(X|\mu, \Sigma, \pi) \leftarrow \sum_{k=1}^{K} \ln \left\{ \sum_{k=1}^{K} \pi_k \mathcal{N}(x_n | \mu_k, \Sigma_k) \right\}.$$

5 return $\pi_k, \mu_k, \Sigma_k, (k = 1, 2, ..., K);$

2 Factor Analysis (FA)

pass

3 Independent Component Analysis (ICA)

pass

4 Causal discovery algorithms

pass

5 Causal tree reconstruction

pass