## Matrix theory - Assignment4

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Abstract—This document illustrates proving properties triangles using linear algebra

Download all latex-tikz codes from

https://github.com/shreeprasadbhat/matrix-theory/blob/master/assignment4/

## 1 Problem

Triangles on the same base (or equal bases) and having equal areas lie between the same parallels.

## 2 Solution

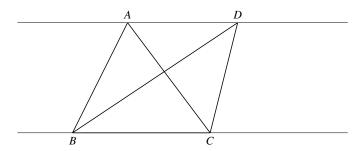


Fig. 0:  $\triangle ABC$  and  $\triangle BCD$  having common base BC

Given that,

Area of 
$$\triangle ABC$$
 = Area of  $\triangle BCD$  (2.0.1)

We know that, area of triangle can be obtained by cross product.

Area of 
$$\triangle ABC = \frac{1}{2} \times ((\mathbf{B} - \mathbf{C}) \times (\mathbf{B} - \mathbf{A}))$$
 (2.0.2)  

$$= \frac{1}{2} \times (\mathbf{B} - \mathbf{C}) \times ((\mathbf{B} - \mathbf{D}) + (\mathbf{D} - \mathbf{A}))$$
 (2.0.3)  

$$= \text{Area of } \triangle BCD + \frac{1}{2} \times (\mathbf{B} - \mathbf{C}) \times (\mathbf{D} - \mathbf{A})$$
 (2.0.4)

From (2.0.1) and (2.0.4) we get,

$$(\mathbf{B} - \mathbf{C}) \times (\mathbf{D} - \mathbf{A}) = 0 \implies \mathbf{AD} \parallel \mathbf{BC}$$
 (2.0.5)

Hence proved triangles on the same base and having equal areas lie between the same parallels.

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