Matrix theory - Assignment4

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***Abstract*—This document illustrates finding determinant of matrix using properties of determinant**

Download all python codes from

https://github.com/shreeprasadbhat/matrix−theory/tree/master/assignment4/codes

and latex-tikz codes from

https://github.com/shreeprasadbhat/matrix−theory/blob/master/assignment4/

1 Problem

Triangles on the same base (or equal bases) and having equal areas lie between the same parallels.

2 Solution

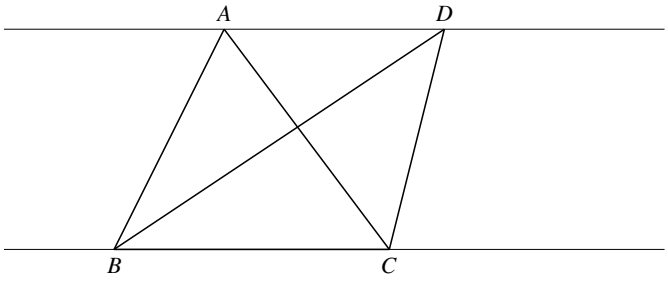

Fig. 0: $\triangle ABC$ and $\triangle BCD$ having common base BC

Given that,

$$\text{Area of } \triangle ABC = \text{Area of } \triangle BCD \tag{2.0.1}$$

$$\text{Area of } \triangle ABC = \frac{1}{2} \times ((\mathbf{B}-\mathbf{C}) \times (\mathbf{B}-\mathbf{A})) \tag{2.0.2}$$

$$= \frac{1}{2} \times (\mathbf{B}-\mathbf{C}) \times ((\mathbf{B}-\mathbf{D}) + (\mathbf{D}-\mathbf{A})) \tag{2.0.3}$$

$$= \text{Area of } \triangle BCD + \frac{1}{2} \times (\mathbf{B}-\mathbf{C}) \times (\mathbf{D}-\mathbf{A}) \tag{2.0.4}$$

From (2.0.1) and (2.0.4) we get,

$$(\mathbf{B}-\mathbf{C}) \times (\mathbf{D}-\mathbf{A}) = 0 \implies \mathbf{AD} \parallel \mathbf{BC} \tag{2.0.5}$$

Hence proved triangles on the same base and having equal areas lie between the same parallels.