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Matrix theory - Assignment4

Shreeprasad Bhat AI20MTECH14011

Abstract—This document illustrates proving properties triangles using linear algebra

Hence proved triangles on the same base and having equal areas lie between the same parallels.

Download all latex-tikz codes from

https://github.com/shreeprasadbhat/matrix-theory/blob/master/assignment4/

1 Problem

Triangles on the same base (or equal bases) and having equal areas lie between the same parallels.

2 Solution

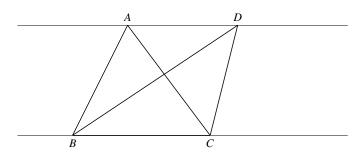


Fig. 0: $\triangle ABC$ and $\triangle BCD$ having common base BC

Given that,

Area of
$$\triangle ABC$$
 = Area of $\triangle BCD$ (2.0.1)

We know that, area of triangle can be obtained by cross product.

Area of
$$\triangle ABC = \frac{1}{2} \| (\mathbf{B} - \mathbf{A}) \times (\mathbf{B} - \mathbf{C}) \|$$
 (2.0.2)

$$= \frac{1}{2} \| [(\mathbf{B} - \mathbf{D}) + (\mathbf{D} - \mathbf{A})] \times (\mathbf{B} - \mathbf{C}) \|$$
 (2.0.3)

$$= \text{Area of } \triangle BCD + \frac{1}{2} \| (\mathbf{D} - \mathbf{A}) \times (\mathbf{B} - \mathbf{C}) \|$$
 (2.0.4)

From (2.0.1) and (2.0.4) we get,

$$(\mathbf{D} - \mathbf{A}) \times (\mathbf{B} - \mathbf{C}) = 0$$

$$(\mathbf{D} - \mathbf{A}) \times (\mathbf{B} - \mathbf{C}) = k(\mathbf{B} - \mathbf{C}) \times (\mathbf{B} - \mathbf{C})$$

$$(2.0.5)$$

$$\implies (\mathbf{D} - \mathbf{A}) = k(\mathbf{B} - \mathbf{C}) \tag{2.0.7}$$

$$\implies$$
 AD \parallel **BC** (2.0.8)