

# Deep Learning for NLP

# Training LLMs

## Memory and compute requirements

## Learning goals

- Learn about different contributions to compute requirements
  - Learn how model size components influence memory requirements

```

32-bit float (FP32)
sign exponent (8 bits) significand (23 bits)
0 1 0 0 0 0 0 0 0 1 0 0 0 1 0 0 0 1 0 0 0 0 0 1 1 1 1 1 1 0 1 1 0 1 1
(-1)0 × 2(10-127) × 1.5707964 = 3.1415927

16-bit float (FP16)
sign exponent (5 bits) significand (10 bits)
0 1 0 0 0 0 1 0 0 1 0 0 1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0
(-1)0 × 2(10-127) × 1.571 = 3.141

```

# NUMBER OF PARAMETERS: NOTATION

- In this slide set, we use  $P$  for the number of parameters.
- (Unfortunately, we use  $N$  for the number of parameters in other slide sets.)

# COMPUTE REQUIREMENTS

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**Basic equation: Cost to train a transformer (decoder) model:**

$$C \approx \tau T = 6PD$$

► Source: Quentin et al., 2023

# COMPUTE REQUIREMENTS $C \approx \tau T = 6PD$

where:

- $\tau$  is throughput of hardware: (No. GPUs) x (FLOPs/GPU)
- $T$  is the time spent training the model, in seconds
- $P$  is the number of parameters in the model
- $D$  is the dataset size (in tokens)
- $C$ : No. of floating-point operations to train the model:  
$$C = C_{forward} + C_{backward}$$
- $C_{forward} \approx 2PD$ ;  $C_{backward} \approx 4PD$ 
  - **2PD**: 2 comes from the multiply-accumulate operation used in matrix multiplication
  - **4PD**: backward pass approximately twice the compute of the forward pass
- In the backward pass at each layer, gradients have to be calculated for the weights at that layer and for the previous layers' outputs

# COMPUTE UNITS

$C$  (actually,  $C$  per time) can be measured in different units:

- FLOPs = FLOP-seconds which is [Floating Point Ops / Second]
  - We also use multiples:  
GFLOP-seconds, TFLOP-seconds etc.
  - Other multiples like PFLOP-days are used in papers
  - $1 \text{ PFLOP-day} = 10^{15} \cdot 24 \cdot 3600 \text{ FLOP-seconds}$
  - Actual FLOPs are always lower than the advertised theoretical FLOPs
- GPU-hours
  - GPU model is also required, since they have different compute capacities

# PARAMETERS VS DATASET

- Model performance depends on number of parameters  $P$ , but also on number of training tokens  $D$
- One proposed optimal tradeoff between  $P$  and  $D$  is:  $D = 20P$ 
  - This was true for Chinchilla models ▶ Hoffmann et al., 2022, not clear to what extent it still holds.
- Training an LLM on less than 200 billion tokens is not recommended
- One rule of thumb: First determine the uppermost inference cost, and then train the biggest model within that boundary
- Different ways to determine  $P$ : based on available data, compute budget or inference time

# MEMORY REQUIREMENTS

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Common questions:

- How big is this model in bytes?
- Will it fit/train on my GPUs?

Model size components:

- Model parameters
- Optimizer states
- Gradients
- Activations

# NUMBER REPRESENTATIONS

- Pure fp32: single precision floating point number as defined by [IEEE 754](#) standard, takes 32 bits or 4 bytes
- fp16: half precision float number as defined by [IEEE\\_754-2008](#), occupying 16 bits or 2 bytes
- bf16 or brain floating point 16, developed by Google Brain project, occupying 16 bits or 2 bytes
  - bf16 has a larger dynamic range than fp16 (8 exponent bits instead of 5)
  - bf16 is less precise, but also less likely to suffer from underflow or overflow
- INT8: integer from -128 to 127, occupying 8 bits or 1 byte

## 32-bit float (FP32)

| sign | exponent (8 bits) | significand (23 bits)                         |
|------|-------------------|---|
| 0    | 1 0 0 0 0 0 0 0   | 1 0 0 1 0 0 1 0 0 0 0 0 1 1 1 1 1 1 0 1 1 0 1 |

$$(-1)^0 \times 2^{128-127} \times 1.5707964 = 3.1415927$$

## 16-bit float (FP16)

| sign | exponent (5 bits) | significand (10 bits) |
|------|-------------------|-----------------------|
| 0    | 1 0 0 0 0         | 1 0 0 1 0 0 1 0 0 0   |

$$(-1)^0 \times 2^{128-127} \times 1.571 = 3.141$$

You can represent every float like this:  $(-1)^S \cdot 2^{e-bias} \cdot 1.m$

# INT8 QUANTIZATION

*It's hard to fit meaningful floats into 8 bits, but you can use integer quantization: INT8.*

- Real\_number = stored\_integer \* scaling\_factor
- **Absmax quantization:**
  - $X_{quant} = \text{round}\left(\frac{127}{\max|\mathbf{X}|} \cdot \mathbf{X}\right)$
- **Zero-point quantization:**
  - $\text{scale} = \frac{255}{\max(\mathbf{X}) - \min(\mathbf{X})}$
  - $\text{zeropoint} = -\text{round}(\text{scale} \cdot \min(\mathbf{X})) - 128$
  - $X_{quant} = \text{round}(\text{scale} \cdot \mathbf{X} + \text{zeropoint})$
  - (draw example)

# MODEL PARAMETERS

Parameter size depends on chosen representation:

- Pure fp32:  $Mem_{model} = 4 \text{ bytes/param} \cdot N_{params}$
- fp16 or bf16:  $Mem_{model} = 2 \text{ bytes/param} \cdot N_{params}$
- INT8:  $Mem_{model} = 1 \text{ byte/param} \cdot N_{params}$

It is common to use mixed representations:

- fp32 + fp16
- fp32 + bf16

# OPTIMIZER STATES

AdamW:  $Mem_{\text{AdamW}} = 8 \text{ bytes/param} \cdot N_{\text{params}}$

- Momentum: 4 bytes/param
- Variance: 4 bytes/param

bitsandbytes (8-bit optimizer):  $Mem_{\text{optimizer}} = 2 \text{ bytes/param} \cdot N_{\text{params}}$

- Momentum: 1 byte/param
- Variance: 1 byte/param

# GRADIENTS

They are usually stored in the same datatype as the model parameters.

Their memory overhead contribution is:

- fp32:  $Mem_{grad} = 4 \text{ bytes/param} \cdot N_{params}$
- fp16 or bf16:  $Mem_{grad} = 2 \text{ bytes/param} \cdot N_{params}$
- INT8:  $Mem_{grad} = 1 \text{ byte/param} \cdot N_{params}$

# ACTIVATIONS

- GPUs are bottlenecked by memory, not FLOPs
- Save GPU memory by recomputing activations of certain layers
- Various schemes for how exactly this is implemented.

Total memory when training **without** activations:

$$Mem_{training} = Mem_{params} + Mem_{opt} + Mem_{grad}$$

Total memory when training **with** activations:

$$Mem_{training} = Mem_{params} + Mem_{opt} + Mem_{grad} + Mem_{activ}$$