

Deep Learning for NLP

Training LLMs

Memory and Compute Requirements

32-bit float (FP32)

sign exponent (8 bits) significand (23 bits)

0 1 0 0 0 0 0 0 0 1 0 0 1 0 0 1 0 0 0 0 1 1 1 1 1 0 1 1 0 1 1

$$(-1)^0 \times 2^{100-127} \times 1.5707964 = 3.1415927$$

16-bit float (FP16)

sign exponent (5 bits) significand (10 bits)

0 1 0 0 0 0 1 0 0 1 0 0 0 0

$$(-1)^0 \times 2^{100-127} \times 1.571 = 3.141$$

Learning goals

- Learn about different contributions to compute requirements
- Learn how model size components influence memory requirements

COMPUTE REQUIREMENTS

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Basic equation: Cost to train a transformer (decoder) model:

$$C \approx \tau T = 6PD$$

► Source: Quentin et al., 2023

COMPUTE REQUIREMENTS $C \approx \tau T = 6PD$

where:

- τ is throughput of hardware: (No. GPUs) x (FLOPs/GPU)
- T is the time spent training the model, in seconds
- P is the number of parameters in the model
- D is the dataset size (in tokens)
- C : No. of floating-point operations to train the model:
$$C = C_{forward} + C_{backward}$$
- $C_{forward} \approx 2PD$; $C_{backward} \approx 4PD$
 - $2PD$: **2** comes from the multiply-accumulate operation used in matrix multiplication
 - $4PD$: backward pass approximately twice the compute of the forward pass
- In the backward pass at each layer, gradients have to be calculated for the weights at that layer and for the previous layers' outputs

COMPUTE UNITS

C (actually, C per time) can be measured in different units:

- FLOPs = FLOP-seconds which is [Floating Point Ops / Second]
 - We also use multiples:
GFLOP-seconds, TFLOP-seconds etc.
 - Other multiples like PFLOP-days are used in papers
 - 1 PFLOP-day = $10^{15} \cdot 24 \cdot 3600$ FLOP-seconds
 - Actual FLOPs are always lower than the advertised theoretical FLOPs
- GPU-hours
 - GPU model is also required, since they have different compute capacities

PARAMETERS VS DATASET

- Model performance depends on number of parameters P , but also on number of training tokens D
- One proposed optimal tradeoff between P and D is: $D = 20P$
 - This was true for Chinchilla models ► Hoffmann et al., 2022, not clear to what extent it still holds.
- Training an LLM on less than 200 billion tokens is not recommended
- One rule of thumb: First determine the uppermost inference cost, and then train the biggest model within that boundary
- Different ways to determine P : based on available data, compute budget or inference time

MEMORY REQUIREMENTS

MEMORY REQUIREMENTS

Common questions:

- How big is this model in bytes?
- Will it fit/train on my GPUs?

Model size components:

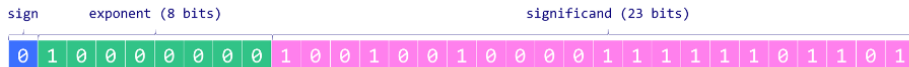
- Model parameters
- Optimizer states
- Gradients
- Activations

NUMBER REPRESENTATIONS

- Pure fp32: single precision floating point number as defined by ▶ IEEE 754 standard, takes 32 bits or 4 bytes
- fp16: half precision float number as defined by ▶ IEEE_754-2008, occupying 16 bits or 2 bytes
- bf16 or brain floating point 16, developed by Google Brain project, occupying 16 bits or 2 bytes
 - bf16 has a larger dynamic range than fp16 (8 exponent bits instead of 5)
 - bf16 is less precise, but also less likely to suffer from underflow or overflow
- INT8: integer from -128 to 127, occupying 8 bits or 1 byte

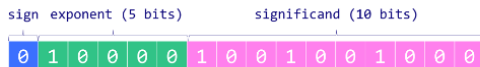
FP32/FP16 (▶ (MAXIME LABONNE))

32-bit float (FP32)



$$(-1)^0 \times 2^{128-127} \times 1.5707964 = 3.1415927$$

16-bit float (FP16)



$$(-1)^0 \times 2^{128-127} \times 1.571 = 3.141$$

You can represent every float like this: $(-1)^S \cdot 2^{e-bias} \cdot 1.m$

INT8 QUANTIZATION

It's hard to fit meaningful floats into 8 bits, but you can use integer quantization: INT8.

- $\text{Real_number} = \text{stored_integer} * \text{scaling_factor}$
- **Absmax quantization:**
 - $X_{\text{quant}} = \text{round} \left(\frac{127}{\max|\mathbf{X}|} \cdot \mathbf{X} \right)$
- **Zero-point quantization:**
 - $\text{scale} = \frac{255}{\max(\mathbf{X}) - \min(\mathbf{X})}$
 - $\text{zeropoint} = -\text{round}(\text{scale} \cdot \min(\mathbf{X})) - 128$
 - $X_{\text{quant}} = \text{round}(\text{scale} \cdot \mathbf{X} + \text{zeropoint})$
 - (draw example)

MODEL PARAMETERS

Parameter size depends on chosen representation:

- Pure fp32: $Mem_{model} = 4 \text{ bytes/param} \cdot N_{params}$
- fp16 or bf16: $Mem_{model} = 2 \text{ bytes/param} \cdot N_{params}$
- INT8: $Mem_{model} = 1 \text{ byte/param} \cdot N_{params}$

It is common to use mixed representations:

- fp32 + fp16
- fp32 + bf16

OPTIMIZER STATES

AdamW: $Mem_{AdamW} = 8 \text{ bytes/param} \cdot N_{params}$

- Momentum: 4 bytes/param
- Variance: 4 bytes/param

bitsandbytes (8-bit optimizer): $Mem_{optimizer} = 2 \text{ bytes/param} \cdot N_{params}$

- Momentum: 1 byte/param
- Variance: 1 byte/param

GRADIENTS

They are usually stored in the same datatype as the model parameters.

Their memory overhead contribution is:

- fp32: $Mem_{grad} = 4 \text{ bytes/param} \cdot N_{params}$
- fp16 or bf16: $Mem_{grad} = 2 \text{ bytes/param} \cdot N_{params}$
- INT8: $Mem_{grad} = 1 \text{ byte/param} \cdot N_{params}$

ACTIVATIONS

- GPUs are bottlenecked by memory, not FLOPs
- Save GPU memory by recomputing activations of certain layers
- Various schemes for how exactly this is implemented.

Total memory when training **without** activations:

$$Mem_{training} = Mem_{params} + Mem_{opt} + Mem_{grad}$$

Total memory when training **with** activations:

$$Mem_{training} = Mem_{params} + Mem_{opt} + Mem_{grad} + Mem_{activ}$$