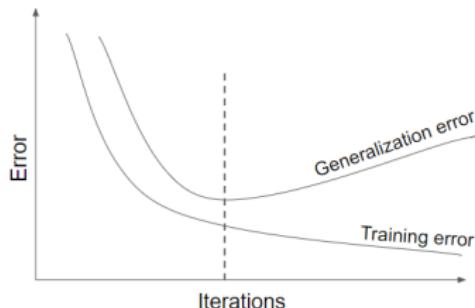


Introduction to Machine Learning

Regularization Early Stopping



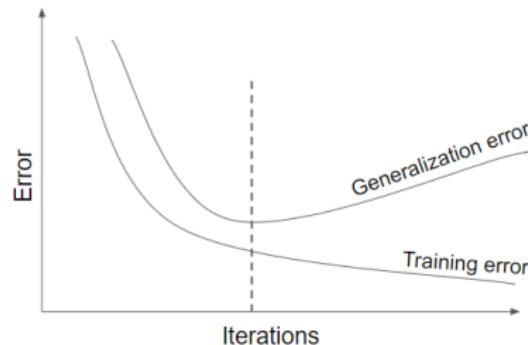
Learning goals

- Know how early stopping works
- Understand how early stopping acts as a regularizer

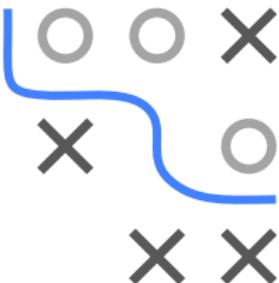


EARLY STOPPING

- Especially for complex nonlinear models we can easily overfit
- In optimization: Often, after a certain number of iterations, generalization error begins to increase even though training error continues to decrease



| Strengths | Weaknesses |
|---|--|
| Effective and simple | Periodical evaluation of validation error |
| Applicable to almost any model without adjustment | Temporary copy of θ (we have to save the whole model each time validation error improves) |
| Combinable with other regularization methods | Less data for training \rightarrow include \mathcal{D}_{val} afterwards |

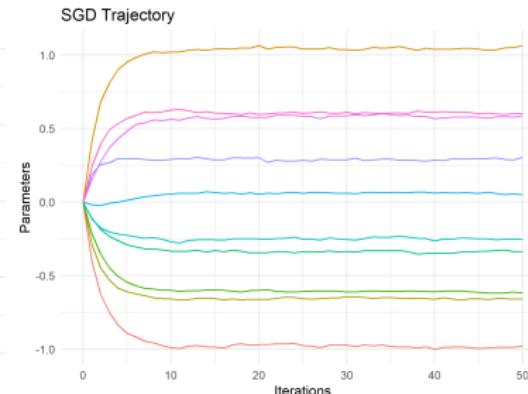
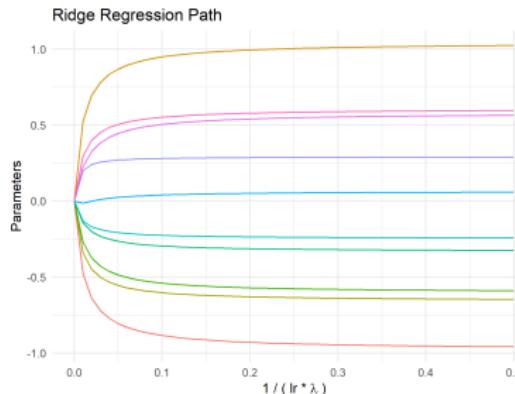
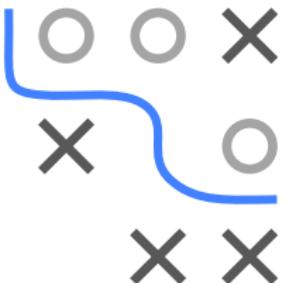


- For simple case of LM with squared loss and GD optim initialized at $\theta = 0$: Early stopping has exact correspondence with L_2 regularization/WD: optimal early-stopping iter T_{stop} inversely proportional to λ scaled by step-size α

$$T_{\text{stop}} \approx \frac{1}{\alpha\lambda} \Leftrightarrow \lambda \approx \frac{1}{T_{\text{stop}}\alpha}$$

- Small λ (regu. \downarrow) \Rightarrow large T_{stop} (complexity \uparrow) and vice versa

Solution paths for L_2 regularized linear model closely matches SGD trajectory of unregularized LM initialized at $\theta = 0$



Caveat: Initialization at the origin is crucial for this equivalence to hold, which is almost never exactly used in practice in ML/DL applications