

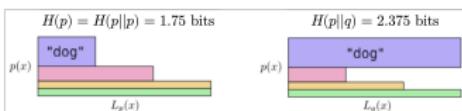
Introduction to Machine Learning

Information Theory Source Coding and Cross-Entropy



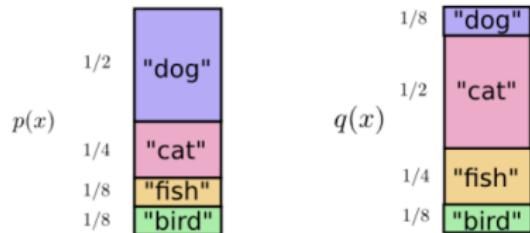
Learning goals

- Know connection between source coding and (cross-)entropy
- Know that the entropy of the source distribution is the lower bound for the average code length

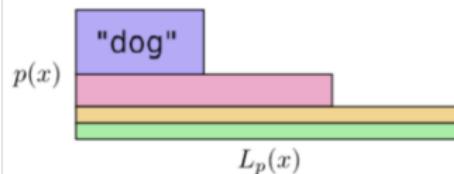


SOURCE CODING AND CROSS-ENTROPY

- For a random source / distribution p , the minimal number of bits to optimally encode messages from is the entropy $H(p)$.
- If the optimal code for a different distribution $q(x)$ is instead used to encode messages from $p(x)$, expected code length will grow.



$$H(p) = H(p||p) = 1.75 \text{ bits}$$



$$H(p||q) = 2.375 \text{ bits}$$

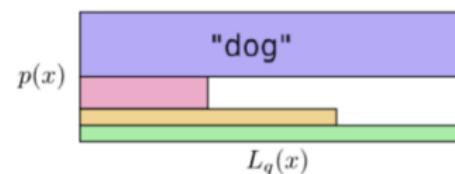


Figure: $L_p(x)$, $L_q(x)$ are the optimal code lengths for $p(x)$ and $q(x)$