Introduction to Machine Learning

Boosting
Gradient Boosting: CWB and GLMs

Parameter after 10000 Iterations
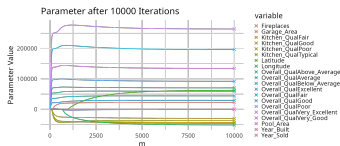
Learning goals

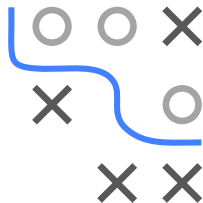- Understand relationship of CWB and GLM

RELATION TO GLM

In the simplest case we use linear models (without intercept) on single features as base learners:

$$b_j(x_j, \theta) = \theta x_j \quad \text{for } j = 1, 2, \ldots, p \quad \text{and with } b_j \in \mathcal{B}_j = \{\theta x_j \mid \theta \in \mathbb{R}\}.$$

This definition will result in an ordinary **linear regression** model.

- In the limit, boosting algorithm will converge to the maximum likelihood solution.

- By specifying loss as NLL of exponential family distribution with an appropriate link function, CWB is equivalent to (regularized) **GLM**.

EXAMPLE: LOGISTIC REGRESSION WITH CWB

Fitting a logistic regression (GLM with a Bernoulli distributed response) requires the specification of the loss as function as

$$L(y, f(\mathbf{x})) = -y \cdot f(\mathbf{x}) + \log(1 + \exp(f(\mathbf{x}))), \ y \in \{0, 1\}$$

Note that CWB (as gradient boosting in general) predicts a score $f(\mathbf{x}) \in \mathbb{R}$. Squashing the score $f(\mathbf{x})$ to $\pi(\mathbf{x}) = s(f(\mathbf{x})) \in [0, 1]$ corresponds to transforming the linear predictor of a GLM to the response domain with a link function s:

- $s(f(\mathbf{x})) = (1 + \exp(-f(\mathbf{x})))^{-1}$ for logistic regression.
- $s(f(\mathbf{x})) = \Phi(f(\mathbf{x}))$ for probit regression with Φ the CDF of the standard normal distribution.

EXAMPLE: CWB PARAMETER CONVERGENCE

The following figure shows the parameter values for $m \leq 10000$
iterations as well as the estimates from a linear model as crosses (GLM
with normally distributed errors):
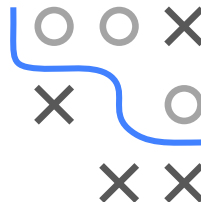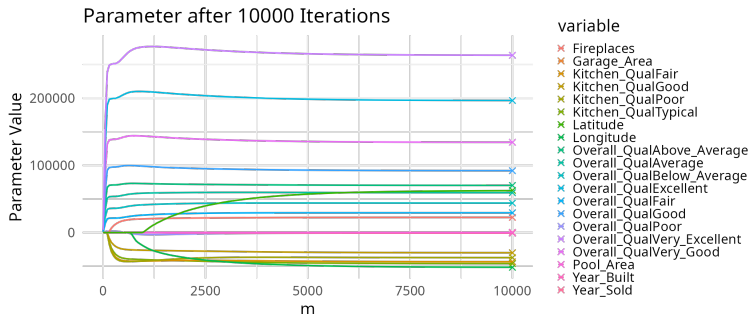
Throughout the fitting of CWB, the parameters estimated converge to
the GLM solution. The used data set is Ames Housing.