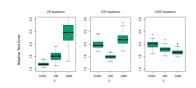
Introduction to Machine Learning

Feature Selection Feature Selection: Motivating Examples





Learning goals

- Understand the practical importance of feature selection
- Understand that models with integrated selection do not always work
- Know different categories of selection methods

MOTIVATING EXAMPLE 1: REGULARIZATION

In case of $p \gg n$, overfitting becomes increasingly problematic, as can be shown by the following simulation study:

- For each of 100 simulation iterations:
- Simulate 3 datasets with $n = 100, p \in \{20, 100, 1000\}$.
- ullet Features are drawn from a standard Gaussian with pairwise correlation ho=0.2.
- Target is simulated as $y = \sum_{j=1}^{p} x_j \theta_j + \sigma \varepsilon$, where ε and θ are both sampled from standard Gaussians, and σ is fixed such that the signal-to-noise ratio is $Var(\mathbb{E}[y|X])/\sigma^2 = 2$.
- Three ridge regression models with $\lambda \in \{0.001, 100, 1000\}$ are fitted to each simulated dataset.



MOTIVATING EX. 2: COMPARISON OF METHODS

Generalization performance of eight classification methods on micro-array data with $|\mathcal{D}_{train}|=$ 144, $|\mathcal{D}_{test}|=$ 54, p= 16, 063 genes and a categorical target encoding the type of cancer with 14 classes.

Methods	CV errors (SE) Out of 144	Test errors Out of 54	Number of Genes Used
1. Nearest shrunken centroids	35 (5.0)	17	6.520
2. L ₂ -penalized discriminant analysis	25 (4.1)	12	16,063
3. Support vector classifier	26 (4.2)	14	16,063
4. Lasso regression (one vs all)	30.7 (1.8)	12.5	1,429
 k-nearest neighbors 	41 (4.6)	26	16,063
6. L ₂ -penalized multinomial	26 (4.2)	15	16,063
 L₁-penalized multinomial 	17 (2.8)	13	269
8. Elastic-net penalized multinomial	22 (3.7)	11.8	384

Hastie (2009). The Elements of Statistical Learning

Methods need at least regularization or built-in FS to perform well. Possible to build good, small models which helps in interpretation



MOTIVATING EX. 3: INTEGRATED SELECTION

Set-up for simulated micro-array data:

- We generate n = 200 samples with p = 100 features drawn from a MV Gaussian
- 50% are relevant for the target and 50% have no influence
- Among informative features, 25 are positively and 25 negatively correlated with target, using weights {-1,1}
- Target is simulated from Bernoulli distribution using linear predictor as log-odds (linear decision boundary!)

