# Comparative Effectiveness and Personalized Medicine Research Using Real-World Data

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## 1 Preface

Thomas Debray (Smart Data Analysis and Statistics B.V.)

This book provides practical guidance for estimating the effectiveness of treatments in real-world populations. It explains how real-world data can directly be used or combined with other data sources to derive overall and individualized estimates of treatment effect. The book explains statistical methods for implementing bias adjustments, conducting evidence synthesis and individualizing treatment effect, whilst also providing illustrative examples and supporting software. The chapters and contents of the book are written by leading experts, with a track record in the generation and/or evaluation of real-world evidence.

This book is intended as a pivotal textbook for statisticians, epidemiologists, methodologists, regulators and/or regulatory scientists considering, undertaking or appraising the real-world evidence of treatment effectiveness. It covers key concepts and stages to derive and evaluate treatment effect estimates for entire populations and specific individuals. The book offers a conceptual framework towards estimating treatment effects at both the population and individualized level, where modelling methods may include traditional regression-based and machine learning methods.

#### **Motivation**

Although randomized clinical trials traditionally form the cornerstone of comparative effectiveness research, there is a growing demand to consider evidence from "real-world data" (RWD) in clinical decision-making. These data are often available from observational cohort studies, administrative databases, and patient registries, and may offer additional insights into the comparative effectiveness and safety of treatments. Yet, the analysis of RWD and the evaluation of real-world evidence face many operational and methodological challenges.

In this book, we aim to address three current needs. First, this book will offer the guidance that is currently lacking on assessing the quality of RWD and on implementing appropriate statistical methods to reduce bias of single study estimates of treatment effects. Second, this book will provide researchers with advanced approaches to pooling estimates from multiple non-randomized studies for which traditional evidence synthesis methods are not suitable.

Finally, to answer the growing need to translate average estimates of treatment effects to individualized clinical decision-making, this book will present recent methods for more tailored approaches where patient characteristics are used to derive their individualized prognosis and treatment benefit.

This book aims to explain key principles and state-of-the-art methods for deriving treatment effects in entire populations and specific individuals using RWD. It will not only discuss statistical theory by key experts in the field; it will also provide illustrative examples and practical guidance for implementation in R. In short, the book aims to prepare a new generation of researchers who wish to generate and integrate evidence from both randomized and non-randomized data sources to investigate the real-world effectiveness of treatments in populations and individual patients.

#### Contents

The book is divided into six sections:

- 1. **Introduction**. This section introduces the relevance of real-world data for conducting comparative effectiveness research, and discusses various concerns regarding their use.
- 2. Principles of treatment effect estimation using real-world data. In this section, we discuss key principles of treatment effect estimation in non-randomized data sources. We explain methods to adjust for confounding (including propensity score analysis and disease risk score analysis) and missing data when estimating the treatment effect for a specific (sub)population.
- 3. Principles of evidence synthesis. In this section, we discuss statistical methods for estimating the treatment effect using (individual participant and/or aggregate) data from multiple studies. To this purpose, key principles of meta-analysis are introduced and explained, including the standard fixed effect and random effects meta-analysis models, methods for individual patient data (IPD) meta-analysis, methods for network meta-analysis, and methods for data-driven and tailored bias adjustment.
- 4. Advanced modelling issues for dealing with additional bias in both randomized and non-randomized data sources. In this section, we discuss advanced statistical and machine learning methods for dealing with time-varying confounding, informative visit schedules, and measurement error.
- 5. **Individualizing treatment effects for personalized medicine**. In this section, we discuss statistical methods to estimate and evaluate individualized treatment effects.
- 6. Closing

## 2 Validity control and quality assessment of real-world data and real-world evidence

Christina ReadThomas Debray (Smart Data Analysis and Statistics B.V.)

```
library(readxl)
library(robvis)
```

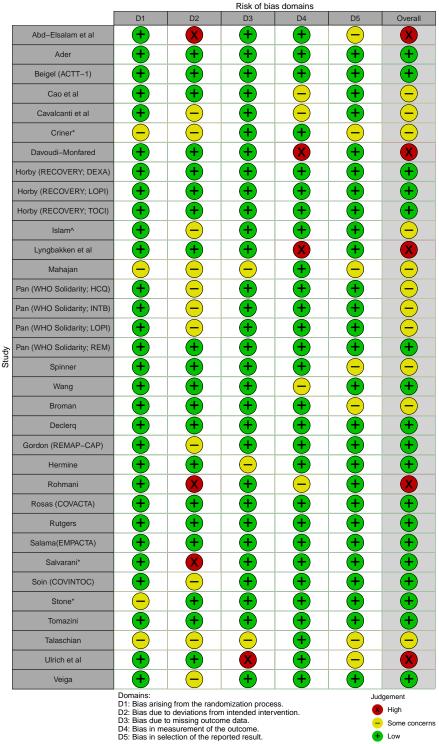
The quality of real-world data is often suboptimal and can therefore lead to bias when generating real-world evidence (RWE). In this chapter, we will introduce key quality concerns of RWD, including their accuracy, completeness, and timeliness. Subsequently, we will discuss which steps can be taken to assess the quality of RWD, and determine their fitness for use. The chapter will also introduce directed acyclic graphs to explain how the analysis of RWD may be affected by different types of bias. We will put particular focus on confounding bias, selection bias, and information bias, and explain how these biases can be addressed by referring to specific chapters from the book. Finally, the chapter presents common quality appraisal tools that can be used to assess the quality of real-world evidence (for instance when conducting a systematic review).

## 2.1 Example code

A risk of bias assessment was conducted in the COVID-NMA review. We can create a summary table of risk of bias assessment and produce a traffic light plot as follows:

```
Risk_of_Bias <- read_excel("resources/RoB-covid.xlsx")

#creation of traffic light plot
trafficlight_rob <- rob_traffic_light(data = Risk_of_Bias, tool = "ROB2")
trafficlight_rob</pre>
```





## 3 Confounding adjustment using propensity score methods

```
Tammy Jiang (Biogen)
Thomas Debray (Smart Data Analysis and Statistics B.V.)
```

The purpose of this document is to provide example R code that demonstrates how to estimate the propensity score and implement matching, stratification, weighting, and regression adjustment for the continuous propensity score. In this example using simulated data, we have two disease modifying therapies (DMT1 and DMT0) and the outcome is the number of post-treatment multiple sclerosis relapses during follow-up. We will estimate the average treatment effect in the treated (ATT) using propensity score matching, stratification, and weighting. We will estimate the average treatment effect in the population (ATE) using regression adjustment for the continuous propensity score. The treatment effects can be interpreted as annualized relapse rate ratios (ARR).

We consider an example dataset with the following characteristics:

```
head(dat)
```

```
age female prevDMTefficacy premedicalcost numSymptoms prerelapse_num
    50
1:
                           None
                                        3899.61
                                        9580.51
2:
    51
             0
                           None
                                                            1
                                                                            0
    56
                                        4785.89
                                                            1
                                                                            0
3:
                           None
4:
    44
             1
                           None
                                        8696.80
                                                            1
                                                                            1
5:
    63
             0
                           None
                                        2588.03
                                                            1
                                                                            0
6:
    28
                                        5435.57
                                                            1
                                                                            0
                           None
   treatment y
                     years
                                  Iscore
1:
        DMT1 0 1.78507871 Moderate A1
2:
        DMT1 0 0.01368925
                                High A1
        DMT1 2 3.25530459
3:
                                High A1
4:
        DMT1 2 5.73853525
                                Neutral
5:
        DMT1 0 1.31143053
                                High A1
6:
        DMT1 0 0.59137577 Moderate A0
```

### 3.1 Comparing baseline characteristics

- DMT1 is the treatment group and DMT0 is the control group
- prevDMTefficacy is previous DMT efficacy (none, low efficacy, and medium/high efficacy)
- prerelapse\_num is the number of previous MS relapses

	DMT0	DMT1
n	2300	7700
age (mean (SD))	51.39(8.32)	44.25 (9.79)
female = 1 (%)	$1671\ (72.65)$	5915 (76.82)
prevDMTefficacy (%)		
None	1247 (54.22)	3171 (41.18)
Low_efficacy	$261\ (11.35)$	858 (11.14)
Medium_high_efficacy	792 (34.43)	3671 (47.68)
prerelapse_num (mean (SD))	0.39 (0.62)	0.46 (0.68)

## 3.2 Estimating the propensity score

#### 3.2.1 Logistic regression

We sought to restore balance in the distribution of baseline covariates in patients treated with DMT1 (index treatment) and DMT0 (control tratment). We fit a multivariable logistic regression model in which treatment was regressed on baseline characteristics including age, sex, previous DMT efficacy, and previous number of relapses.

```
Call:
```

```
glm(formula = treatment ~ age + female + prevDMTefficacy + prerelapse_num,
    family = binomial(), data = dat)
```

Deviance Residuals:

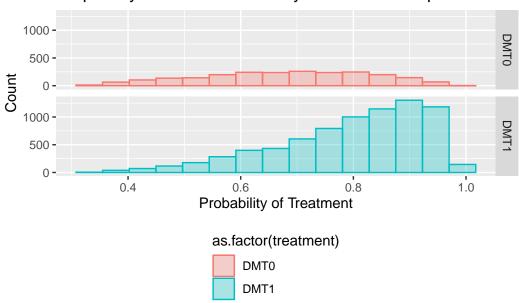
```
Median
                                3Q
    Min
              1Q
                                       Max
-2.7949
          0.2585
                   0.5220
                           0.7478
                                     1.5033
Coefficients:
                                    Estimate Std. Error z value Pr(>|z|)
                                    4.809473
                                               0.157127 30.609 < 2e-16 ***
(Intercept)
                                    -0.086708
                                               0.002996 -28.939 < 2e-16 ***
age
female1
                                    0.253611
                                               0.057664
                                                          4.398 1.09e-05 ***
prevDMTefficacyLow_efficacy
                                               0.083022
                                                          3.739 0.000185 ***
                                    0.310394
prevDMTefficacyMedium_high_efficacy 0.660266
                                               0.054393 12.139 < 2e-16 ***
                                               0.039288 3.979 6.93e-05 ***
prerelapse_num
                                     0.156318
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for binomial family taken to be 1)
    Null deviance: 10786 on 9999 degrees of freedom
Residual deviance: 9597 on 9994 degrees of freedom
AIC: 9609
Number of Fisher Scoring iterations: 5
  # Extract propensity scores
  dat$ps <- predict(ps.model, data = dat, type = "response")</pre>
```

#### 3.2.2 Assessing overlap

We examined the degree of overlap in the distribution of propensity scores across treatment groups using histograms and side-by-side box plots.

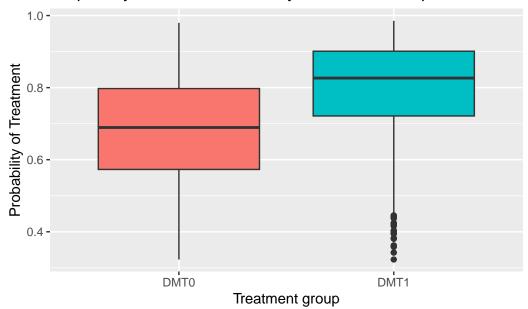
```
# Histogram
ggplot(dat, aes(x = ps, fill = as.factor(treatment), color = as.factor(treatment))) +
    geom_histogram(alpha = 0.3, position='identity', bins = 15) +
    facet_grid(as.factor(treatment) ~ .) +
    xlab("Probability of Treatment") +
    ylab("Count") +
    ggtitle("Propensity Score Distribution by Treatment Group") +
    theme(legend.position = "bottom", legend.direction = "vertical")
```

### Propensity Score Distribution by Treatment Group



```
# Side-by-side box plots
ggplot(dat, aes(x=as.factor(treatment), y=ps, fill=as.factor(treatment))) +
    geom_boxplot() +
    ggtitle("Propensity Score Distribution by Treatment Group") +
    ylab("Probability of Treatment") +
    xlab("Treatment group") +
    theme(legend.position = "none")
```

## Propensity Score Distribution by Treatment Group



```
# Distribution of propensity scores by treatment groups
summary(dat$ps[dat$treatment == "DMT1"])
```

```
Min. 1st Qu. Median Mean 3rd Qu. Max. 0.3230 0.7214 0.8265 0.7970 0.9010 0.9854
```

```
summary(dat$ps[dat$treatment == "DMTO"])
```

Min. 1st Qu. Median Mean 3rd Qu. Max. 0.3230 0.5730 0.6894 0.6795 0.7975 0.9799

## 3.3 Propensity score matching

#### 3.3.1 1:1 Optimal full matching without replacement

```
call:
matchit(formula = treatment ~ age + female + prevDMTefficacy +
    prerelapse_num, data = dat, method = "full", estimand = "ATT")
```

Summary of Balance for All Data:

	Means Treated	Means Control	Std. Mean Diff.
distance	0.7970	0.6795	0.8943
age	44.2496	51.3883	-0.7289
female0	0.2318	0.2735	-0.0987
female1	0.7682	0.7265	0.0987
${\tt prevDMTefficacyNone}$	0.4118	0.5422	-0.2649
<pre>prevDMTefficacyLow_efficacy</pre>	0.1114	0.1135	-0.0065

<pre>prevDMTefficacyMedium_high_efficacy</pre>	0.4768		0.3443	0.2651
prerelapse_num	0.4595		0.3930	0.0976
1 -	Var. Ratio eC	DF Mean		
distance	0.7873	0.1917	0.3379	
age	1.3868	0.1519	0.3085	
female0		0.0417	0.0417	
female1		0.0417	0.0417	
prevDMTefficacyNone	•	0.1304	0.1304	
prevDMTefficacyLow_efficacy		0.0020	0.0020	
<pre>prevDMTefficacyMedium_high_efficacy</pre>		0.1324	0.1324	
prerelapse_num	1.1990	0.0133	0.0383	
Summary of Balance for Matched Data			a a	M D: CC
34 -4	Means Treated			
distance	0.7970		0.7970	0.0003
age	44.2496		44.3185	-0.0070
female0	0.2318		0.2275	0.0101
female1	0.7682		0.7725	-0.0101
prevDMTefficacyNone	0.4118		0.4130	-0.0024
prevDMTefficacyLow_efficacy	0.1114		0.0893	0.0703
prevDMTefficacyMedium_high_efficacy			0.4977	-0.0419
prerelapse_num	0.4595	DE Mass	0.4399	0.0288
diatores	Var. Ratio eCl			
distance	0.9976 1.0392	0.0005 0.0038	0.0075 0.0153	
age femaleO	1.0392			
female1	•	0.0043		
	•	0.0043 0.0012		
<pre>prevDMTefficacyNone prevDMTefficacyLow_efficacy</pre>	•	0.0012		
prevDMTefficacyMedium_high_efficacy	•	0.0221	0.0221	
	1.1319	0.0209	0.0209	
prerelapse_num	Std. Pair Dis		0.0229	
distance	0.00			
age female0	0.0667 0.1775			
female1	0.1775			
prevDMTefficacyNone	0.1173			
prevDMTefficacyLow_efficacy	0.1100			
prevDMTefficacyMedium_high_efficacy				
prerelapse_num	0.10			
brororabso_nam	0.21			

Sample Sizes:

Control Treated

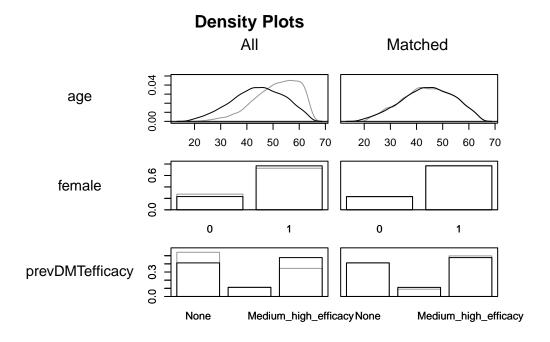
```
All 2300. 7700
Matched (ESS) 307.06 7700
Matched 2300. 7700
Unmatched 0. 0
Discarded 0. 0
```

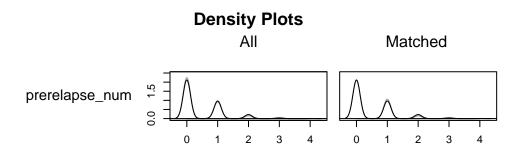
plot(summary(opt))

```
distance
age
female0
female1
prevDMTefficacyNone
prevDMTefficacyLow_efficacy
prerelapse_num

0.0 0.4 0.8
Absolute Standardized
Mean Difference
```

```
# black line is treated group, grey line is control group
plot(opt, type = "density", which.xs = vars)
```





#### 3.3.3 Estimating the ATT

We can estimate the ATT in the matched sample using Poisson regression in which the number of post-treatment relapses is regressed on treatment status and follow-up time for each patient (captured by the variable years). More details are provided at <a href="https://cran.r-project.org/web/packages/MatchIt/vignettes/estimating-effects.html">https://cran.r-project.org/web/packages/MatchIt/vignettes/estimating-effects.html</a>.

```
# Matched data
  matched.data <- match.data(opt)</pre>
  # Poisson regression model
  opt.fit <- glm(y ~ treatment + offset(log(years)),</pre>
              family = poisson(link = "log"),
               data = matched.data,
               weights = weights)
  # Treatment effect estimation
  opt.comp <- comparisons(opt.fit,</pre>
                           variables = "treatment",
                           vcov = ~subclass,
                           newdata = subset(matched.data, treatment == "DMT1"),
                           wts = "weights",
                           transform_pre = "ratio")
  opt.comp |> tidy()
# A tibble: 1 x 8
            contrast
                         estimate std.error statistic p.value conf.low conf.high
  term
                            <dbl>
                                       <dbl>
                                                 <dbl>
                                                           <dbl>
                                                                    <dbl>
                                                                               <dbl>
  <chr>
            <chr>
                            0.804
                                                  7.88 3.25e-15
                                                                    0.604
1 treatment mean(DMT1)~
                                      0.102
                                                                                1.00
```

As indicated in the summary output above, the annualized relapse rate ratio for DMT1 vs DMT0 among patients treated with DMT0 (ATT) is given as 0.8 with a 95% confidence interval ranging from 0.6 to 1.

## 3.4 Propensity score stratification

#### 3.4.1 Divide sample into quintiles of propensity scores

We will form five mutually exclusive groups of the estimated propensity score.

```
1 2 3 4 5
2002 2015 1991 1997 1995
```

#### 3.4.2 Assess balance within each propensity score stratum

Within each propensity score stratum, treated and control patients should have similar values of the propensity score and the distribution of baseline covariates should be approximately balanced between treatment groups.

#### 3.4.2.1 Propensity Score Stratum #1

	DMT0	DMT1	SMD
n	901	1101	
age (mean (SD))	58.38 (3.67)	57.45(3.73)	0.251
female = 1 (%)	605 (67.15)	775 (70.39)	0.070
prevDMTefficacy (%)			0.056
None	650 (72.14)	771 (70.03)	
Low_efficacy	$106 \ (11.76)$	$130 \ (11.81)$	
Medium_high_efficacy	$145 \ (16.09)$	$200 \ (18.17)$	
prerelapse_num (mean (SD))	$0.29 \ (0.53)$	$0.33 \ (0.56)$	0.074

#### 3.4.2.2 Propensity Score Stratum #2

	DMT0	DMT1	SMD
n	617	1398	
age (mean (SD))	52.18(4.35)	51.97(4.22)	0.049
female = 1 (%)	458 (74.23)	1048 (74.96)	0.017
prevDMTefficacy (%)			0.054
None	292 (47.33)	624 (44.64)	
Low_efficacy	69 (11.18)	162 (11.59)	
Medium_high_efficacy	256 (41.49)	612 (43.78)	
prerelapse_num (mean (SD))	$0.40 \ (0.64)$	$0.41 \ (0.66)$	0.004

#### 3.4.2.3 Propensity Score Stratum #3

	DMT0	DMT1	SMD
n	392	1599	
age (mean (SD))	46.73(4.06)	46.36(4.08)	0.092
female = 1 (%)	305 (77.81)	$1193 \ (74.61)$	0.075
prevDMTefficacy (%)			0.041
None	168 (42.86)	687 (42.96)	
Low_efficacy	52 (13.27)	$191\ (11.94)$	
Medium_high_efficacy	172 (43.88)	721 (45.09)	
prerelapse_num (mean (SD))	$0.49 \ (0.68)$	$0.47 \ (0.66)$	0.031

#### 3.4.2.4 Propensity Score Stratum #4

	DMT0	DMT1	SMD
n	269	1728	
age (mean (SD))	41.07 (4.11)	40.88(4.29)	0.046
female = $1 (\%)$	203 (75.46)	1356 (78.47)	0.071
prevDMTefficacy (%)			0.084
None	105 (39.03)	634 (36.69)	
Low_efficacy	22 (8.18)	$181\ (10.47)$	
Medium_high_efficacy	142 (52.79)	913 (52.84)	
prerelapse_num (mean (SD))	$0.50 \ (0.69)$	$0.51 \ (0.71)$	0.012

#### 3.4.2.5 Propensity Score Stratum #5

	DMT0	DMT1	SMD
n	121	1874	
age (mean (SD))	33.26(4.95)	32.04(5.58)	0.233
female = 1 (%)	100 (82.64)	1543 (82.34)	0.008
prevDMTefficacy (%)			0.050
None	32(26.45)	455 (24.28)	
Low_efficacy	12 ( 9.92)	194 (10.35)	
Medium_high_efficacy	77(63.64)	1225 (65.37)	
$prerelapse\_num~(mean~(SD))$	$0.52 \ (0.66)$	$0.52 \ (0.73)$	0.004

#### 3.4.3 Estimating and pooling of stratum-specific treatment effects

The overall ATT across strata can be estimated by weighting stratum-specific estimates by the proportion of treated patients in each stratum over all treated patients in the sample.

We first define a function att.strata.function() to calculate stratum-specific estimates of the treatment effect:

```
att.strata.function <- function(data, stratum, confint = TRUE) {</pre>
    fit <- glm("y ~ treatment + offset(log(years))",</pre>
        family = poisson(link = "log"),
        data = data %>% filter(ps.strata == stratum))
    arr <- round(as.numeric(exp(coef(fit)["treatmentDMT1"])), digits = 3)</pre>
    11 <- ul <- NA
    if (confint) {
      11 <- round(exp(confint(fit))["treatmentDMT1",1], digits = 3)</pre>
      ul <- round(exp(confint(fit))["treatmentDMT1",2], digits = 3)</pre>
    }
    return(c("stratum" = stratum,
              "arr" = arr,
              "ci lower" = 11,
              "ci_upper" = ul))
  }
  arr.strata <- as.data.frame(t(sapply(1:5, att.strata.function, data = dat)))
  arr.strata
            arr ci_lower ci_upper
  stratum
1
        1 0.904
                    0.760
                             1.076
2
        2 0.822
                    0.696
                             0.975
3
        3 0.798
                    0.666
                             0.961
        4 0.716
                    0.587
                             0.881
        5 0.589
                    0.463
                             0.761
```

Subsequently, we define a function weights.strata.function() to calculate the weights for each stratum. The weight is the proportion of treated patients in each stratum over all treated patients in the sample:

```
weights.strata.function <- function(data, stratum) {</pre>
    n_DMT1_stratum <- nrow(data %>% filter(ps.strata == stratum & treatment == "DMT1"))
    n_DMT1_all <- nrow(data %>% filter(treatment == "DMT1"))
    weight <- n_DMT1_stratum/n_DMT1_all</pre>
    return(c("stratum" = stratum, "weight" = weight))
  }
  weights.strata <- as.data.frame(t(sapply(1:5, weights.strata.function, data = dat)))</pre>
  weights.strata
  stratum
             weight
        1 0.1429870
2
        2 0.1815584
3
        3 0.2076623
        4 0.2244156
5
        5 0.2433766
  # Create table with ARRs and weights for each PS stratum
  arr.weights.merged <- merge(arr.strata, weights.strata, by = "stratum")
  # Calculate the weighted ARR for each stratum
  arr.weights.merged <- arr.weights.merged %>%
    mutate(weighted.arr = as.numeric(arr) * weight)
  # Sum the weighted ARRs across strata to get the overall ATT
  sum(arr.weights.merged$weighted.arr)
```

#### [1] 0.7482462

We now define a new function ps.stratification.bootstrap() that integrates estimation of the ATT and the PS weights for bootstrapping purposes:

```
arr.strata <- as.data.frame(t(sapply(1:5, att.strata.function,</pre>
                                           data = d, confint = FALSE)))
    weights.strata <- as.data.frame(t(sapply(1:5, weights.strata.function, data = d)))</pre>
    return(arr.strata$arr[1] * weights.strata$weight[1] +
              arr.strata$arr[2] * weights.strata$weight[2] +
              arr.strata$arr[3] * weights.strata$weight[3] +
              arr.strata$arr[4] * weights.strata$weight[4] +
              arr.strata$arr[5] * weights.strata$weight[5])
  }
We can now estimate the treatment effect and its confidence interval using the bootstrap
procedure:
  library(boot)
Attaching package: 'boot'
The following object is masked from 'package:survival':
    aml
  set.seed(1854)
  arr.stratification.boot <- boot(data = dat,</pre>
                                    statistic = ps.stratification.bootstrap,
                                    R = 1000
  # Bootstrapped ARR
  median(arr.stratification.boot$t)
[1] 0.7558609
  # Bootstrapped ARR 95% CI
  quantile(arr.stratification.boot$t[,1], c(0.025, 0.975))
     2.5%
              97.5%
```

0.6835885 0.8362947

## 3.5 Propensity score weighting

#### 3.5.1 Calculate propensity score weights for ATT

Propensity score weighting reweights the study sample to generate an artificial population (i.e., pseudo-population) in which the covariates are no longer associated with treatment, thereby removing confounding by measured covariates. For the ATT, the weight for all treated patients is set to one. Conversely, the weight for patients in the control group is set to the propensity score divided by one minus the propensity score, that is, (PS/(1 - PS)). We estimated stabilized weights to address extreme weights.

```
library(WeightIt)
  w.out <- weightit(treatment ~ age + female + prevDMTefficacy + prerelapse_num,
                    data = dat,
                    method = "ps",
                    estimand = "ATT")
                    #stabilize = TRUE)
  w.out
A weightit object
 - method: "glm" (propensity score weighting with GLM)
 - number of obs.: 10000
 - sampling weights: none
 - treatment: 2-category
 - estimand: ATT (focal: DMT1)
 - covariates: age, female, prevDMTefficacy, prerelapse_num
  summary(w.out)
                Summary of weights
- Weight ranges:
        Min
                                             Max
DMTO 0.4772 |----- 48.6856
DMT1 1.0000 ||
                                          1.0000
- Units with the 5 most extreme weights by group:
```

9492 8836 6544 9610 4729

DMTO 32.1027 32.1027 34.3126 38.1817 48.6856

8 7 4 2 1

DMT1 1 1 1 1 1

### - Weight statistics:

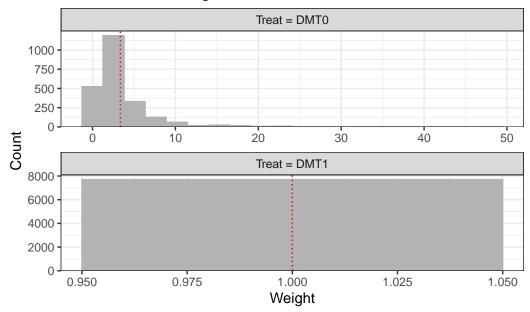
Coef of Var MAD Entropy # Zeros
DMT0 1.098 0.673 0.383 0
DMT1 0.000 0.000 -0.000 0

#### - Effective Sample Sizes:

DMT0 DMT1 Unweighted 2300. 7700 Weighted 1043.16 7700

plot(summary(w.out))

## Distribution of Weights



#### 3.5.2 Assess balance in the weighted sample

```
bal.tab(w.out, stats = c("m", "v"), thresholds = c(m = .05))
Balance Measures
                                         Type Diff.Adj
                                                           M.Threshold
                                     Distance -0.0045 Balanced, <0.05
prop.score
                                      Contin.
                                                0.0054 Balanced, <0.05
age
female
                                       Binary
                                                0.0005 Balanced, < 0.05
prevDMTefficacy_None
                                       Binary -0.0003 Balanced, <0.05
prevDMTefficacy_Low_efficacy
                                       Binary 0.0023 Balanced, <0.05
prevDMTefficacy_Medium_high_efficacy
                                       Binary -0.0020 Balanced, <0.05
                                      Contin. -0.0034 Balanced, <0.05
prerelapse_num
                                     V.Ratio.Adj
                                          0.9926
prop.score
age
                                          1.0102
female
prevDMTefficacy_None
prevDMTefficacy_Low_efficacy
prevDMTefficacy_Medium_high_efficacy
prerelapse_num
                                          1.0941
Balance tally for mean differences
                    count
Balanced, <0.05
Not Balanced, >0.05
Variable with the greatest mean difference
 Variable Diff.Adj
                       M.Threshold
            0.0054 Balanced, <0.05
Effective sample sizes
              DMTO DMT1
Unadjusted 2300.
                   7700
Adjusted
           1043.16 7700
```

#### 3.5.3 Estimate the ATT

One way to estimate the ATT is to use the survey package. The function <code>svyglm()</code> generates model-robust (Horvitz-Thompson-type) standard errors by default, and thus does not require additional adjustments.

```
library(survey)
  weighted.data <- svydesign(ids = ~1, data = dat, weights = ~w.out$weights)</pre>
  weighted.fit <- svyglm(y ~ treatment + offset(log(years)),</pre>
                           family = poisson(link = "log"),
                           design = weighted.data)
  exp(coef(weighted.fit)["treatmentDMT1"])
treatmentDMT1
    0.7083381
  exp(confint(weighted.fit))["treatmentDMT1",]
    2.5 %
           97.5 %
0.6245507 0.8033662
As indicated above, propensity score weighting yielded an ATT estimate of 0.71 (95% CI: 0.62;
0.8).
An alternative approach is to use glm() to estimate the treatment effect and calculate robust
standard errors.
  # Alternative way to estimate treatment effect
  weighted.fit2 <- glm(y ~ treatment + offset(log(years)),</pre>
                  family = poisson(link = "log"),
                  data = dat,
                  weights = w.out$weights)
  # Extract the estimated ARR
  exp(coef(weighted.fit2))["treatmentDMT1"]
```

treatmentDMT1

0.7083381

```
# Calculate robust standard error and p-value of the log ARR
coeftest(weighted.fit2, vcov. = vcovHC)["treatmentDMT1",]
```

Using this approach, the ATT estimate was 0.71 (95% CI: 0.62; 0.8).

### 3.6 Regression adjustment for the propensity score for the ATE

In this approach, a regression model is fitted to describe the observed outcome as a function of the received treatment and the estimated propensity score:

```
ps.reg.fit <- glm(y ~ treatment + ps + offset(log(years)),</pre>
                    family = poisson(link = "log"),
                    data = dat)
  summary(ps.reg.fit)
Call:
glm(formula = y ~ treatment + ps + offset(log(years)), family = poisson(link = "log"),
    data = dat)
Deviance Residuals:
              1Q
                  Median
                                3Q
                                        Max
-2.0160 -0.7336 -0.4441 -0.1352
                                     4.2634
Coefficients:
              Estimate Std. Error z value Pr(>|z|)
                          0.10359 -19.266 < 2e-16 ***
(Intercept)
              -1.99585
                          0.04431 -5.777 7.60e-09 ***
treatmentDMT1 -0.25598
                         0.13878 7.748 9.36e-15 ***
               1.07521
ps
___
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
(Dispersion parameter for poisson family taken to be 1)
    Null deviance: 7514.7 on 9999 degrees of freedom
Residual deviance: 7443.0 on 9997 degrees of freedom
AIC: 12378
Number of Fisher Scoring iterations: 6
  # ATE
  exp(coef(ps.reg.fit))["treatmentDMT1"]
treatmentDMT1
    0.7741606
Waiting for profiling to be done...
Waiting for profiling to be done...
Bootstrapped confidence intervals can be obtained as follows:
  # Function to bootstrap for 95% CIs
  ps.reg.bootstrap <- function(data, inds) {</pre>
    d <- data[inds,]</pre>
    fit <- glm(y ~ treatment + ps + offset(log(years)),</pre>
                 family = poisson(link = "log"),
                 data = d
    return(exp(coef(fit))["treatmentDMT1"])
  }
  set.seed(1854)
  # Generate 1000 bootstrap replicates
  arr.boot <- boot(dat, statistic = ps.reg.bootstrap, R = 1000)</pre>
  # Extract the median annualized relapse rate across 1000 bootstrap replicates
  median(arr.boot$t)
```

```
# Take 2.5th and 97.5th percentiles to be 95% CI quantile(arr.boott[,1], c(0.025, 0.975))
```

2.5% 97.5% 0.7010540 0.8545169

#### 3.7 Overview

Estima	nd Estimate	95% CI (lower)	95% CI (upper)
ATT	0.8039901	0.6040414	1.0039388
ATT	0.7482462	NA	NA
ATT	0.7558609	0.6835885	0.8362947
ATT	0.7083381	0.6245507	0.8033662
ATT	0.7083381	0.6243094	0.8036767
ATE	0.7741606	0.7101080	0.8448218
ATE	0.7750426	0.7010540	0.8545169
	ATT ATT ATT ATT ATT ATT ATE	ATT 0.7482462 ATT 0.7558609 ATT 0.7083381 ATT 0.7083381 ATE 0.7741606	Estimand Estimate       (lower)         ATT       0.8039901       0.6040414         ATT       0.7482462       NA         ATT       0.7558609       0.6835885         ATT       0.7083381       0.6245507         ATT       0.7083381       0.6243094         ATE       0.7741606       0.7101080

#### **Version info**

This chapter was developed using the following version of R and its packages:

R version 4.2.3 (2023-03-15 ucrt)

Platform: x86\_64-w64-mingw32/x64 (64-bit)
Running under: Windows 10 x64 (build 19044)

Matrix products: default

#### locale:

- [1] LC\_COLLATE=Dutch\_Netherlands.utf8 LC\_CTYPE=Dutch\_Netherlands.utf8
- [3] LC\_MONETARY=Dutch\_Netherlands.utf8 LC\_NUMERIC=C
- [5] LC\_TIME=Dutch\_Netherlands.utf8

#### attached base packages:

- [1] grid stats graphics grDevices utils datasets methods
- [8] base

### other attached packages:

[1]	WeightIt_0.14.1	boot_1.3-28.1	MatchIt_4.5.3
[4]	sandwich_3.0-2	truncnorm_1.0-9	tableone_0.13.2
[7]	survey_4.2-1	survival_3.5-5	Matrix_1.5-4
[10]	MASS_7.3-58.3	${\tt marginaleffects\_0.12.0}$	<pre>lmtest_0.9-40</pre>
[13]	zoo_1.8-12	knitr_1.42	ggplot2_3.4.2
[16]	data.table 1.14.8	cobalt 4.5.1	dplyr 1.1.1

## loaded via a namespace (and not attached):

[1]	tidyselect_1.2.0	xfun_0.39	mitools_2.4	splines_4.2.3
[5]	haven_2.5.2	lattice_0.21-8	labelled_2.11.0	<pre>colorspace_2.1-0</pre>
[9]	vctrs_0.6.1	generics_0.1.3	htmltools_0.5.5	yaml_2.3.7
[13]	utf8_1.2.3	rlang_1.1.0	e1071_1.7-13	pillar_1.9.0
[17]	glue_1.6.2	withr_2.5.0	DBI_1.1.3	lifecycle_1.0.3
[21]	munsell_0.5.0	gtable_0.3.3	codetools_0.2-19	evaluate_0.21
[25]	labeling_0.4.2	forcats_1.0.0	fastmap_1.1.1	class_7.3-22
[29]	fansi_1.0.4	optmatch_0.10.6	Rcpp_1.0.10	checkmate_2.2.0
[33]	backports_1.4.1	scales_1.2.1	jsonlite_1.8.4	farver_2.1.1
[37]	chk_0.8.1	hms_1.1.3	digest_0.6.31	insight_0.19.1
[41]	cli_3.6.1	tools_4.2.3	magrittr_2.0.3	proxy_0.4-27
[45]	tibble_3.2.1	crayon_1.5.2	pkgconfig_2.0.3	rlemon_0.2.1
[49]	rmarkdown_2.21	rstudioapi_0.14	R6_2.5.1	compiler_4.2.3

## 3.8 References

## 4 Effect Modification Analysis within the Propensity score Framework

Mohammad Ehsanul Karim (University of British Columbia)

Observational comparative effectiveness studies often adopt propensity score analysis to adjust for confounding. Although this approach is relatively straightforward to implement, careful thought is needed when treatment effect heterogeneity is present. This chapter illustrates the estimation of subgroup-specific treatment effects using (traditional) covariate adjustment methods, propensity score matching, propensity score weighting, propensity score stratification, and covariate adjustment using propensity scores.

First, we need to install the R package simcausal, which can be obtained from GitHub:

```
devtools::install_github('osofr/simcausal', build_vignettes = FALSE)
```

We will use the following data-generation model:

```
require(simcausal)
D <- DAG.empty()
D <- D +
  node("age", distr = "rnorm",
       mean = 2, sd = 4) +
  node("gender", distr = "rbern",
       prob = plogis(4)) +
  node("education", distr = "rbern",
       prob = plogis(3 + 5 * age)) +
  node("diet", distr = "rbern",
       prob = plogis(1 - 3 * education)) +
  node("income", distr = "rbern",
       prob = plogis(2 - 5 * education - 4 * age)) +
  node("smoking", distr = "rbern",
       prob = plogis(1 + 1.2 * gender + 2 * age)) +
  node("hypertension", distr = "rbern",
```

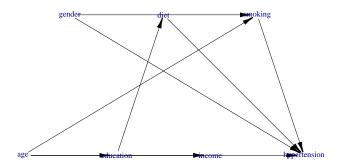
Below is the diagram, with pink lines representing open backdoor path.

using the following vertex attributes:

NAdarkbluenone100.50

using the following edge attributes:

black0.210.60.5



We can now generate an example dataset:

```
Obs.Data <- sim(DAG = Dset, n = 50000, rndseed = 123)
Obs.Data$smoking <- as.character(Obs.Data$smoking)
Obs.Data$income <- as.factor(Obs.Data$income)
```

```
Obs.Data$income <- relevel(Obs.Data$income, ref = "1")
```

Sample data from the hypothetical example of association between hypertension and smoking, where other variables such as income, age [centered], gender, education and diet also plays a role in the data generation process.

	age	gender	education	diet	income	smoking	hypertension
34901	12.29	1	1	1	0	1	1
149	10.40	1	1	0	0	1	1
10060	2.99	1	1	0	0	1	0
22220	-4.31	0	0	0	1	0	1
9979	-6.44	0	0	0	1	0	1

### 4.1 Covariate adjustment

#### 4.1.1 Interaction approach

Below, we estimate a logistic regression model to assess whether the effect of smoking (the exposure) on hypertension is modified by income levels. This model considers the following variables:

• Outcome: hypertension

• Exposure variables: smoking and income

• Confounders: age and gender

Results indicate that the interaction between smoking status and income level is statistically significant (p = 0.02).

If we expand previous model to adjust for an additional confounder education, we have:

	$\exp(\text{Est.})$	2.5%	97.5%	z val.	p
(Intercept)	5.46	4.37	6.82	14.97	0.00
smoking1	2.93	2.60	3.30	17.69	0.00
income0	0.48	0.41	0.57	-8.28	0.00
age	1.29	1.27	1.31	36.77	0.00
gender	0.54	0.43	0.67	-5.55	0.00
smoking 1: income 0	1.27	1.04	1.56	2.33	0.02

results.int.model <- summ(fit.w.int, exp = TRUE)

	$\exp(\text{Est.})$	2.5%	97.5%	z val.	p
(Intercept)	5.69	4.56	7.11	15.31	0.00
smoking1	3.35	2.95	3.79	18.85	0.00
income0	1.09	0.85	1.40	0.68	0.49
age	1.30	1.28	1.32	37.32	0.00
gender	0.54	0.43	0.67	-5.58	0.00
education smoking1:income0	$0.42 \\ 1.10$	$0.35 \\ 0.90$	$0.51 \\ 1.35$	-8.87 $0.93$	$0.00 \\ 0.35$

The interaction term between income and smoking is no longer statistically significant (p = 0.35).

We can generate a summary report from aforementioned effect modification analysis.

The table below depicts the adjusted odds ratios for income levels (high = 0, and low = 1). The variables CI.ll and CI.ul depict the lower and upper limits of the 95 percent confidence intervals,  $\mathtt{OR11} = OR_{A=1,M=1}$ ,  $\mathtt{OR10} = OR_{A=1}$ ,  $\mathtt{OR01} = OR_{M=1}$  and  $\mathtt{OR00}$  captures the reference.

Similarly, for the analysis adjusting for an additional confounder education, we have:

Table 4.1: Summary report from an interaction analysis when investigating association between two exposure variables (smoking and income) and hypertension.

Measures	Estimates	CI.ll	CI.ul
OR00	1.00	NA	NA
OR01	2.93	2.60	3.30
OR10	0.48	0.41	0.57
OR11	1.80	1.63	1.98
OR(smoking1 on outcome [income0==0]	2.93	2.60	3.30
OR(smoking1 on outcome [income0==1]	3.72	3.14	4.41
Multiplicative scale	1.27	1.04	1.56
RERI	-0.61	-0.98	-0.29

Table 4.2: Summary report from an interaction analysis when investigating association between two exposure variables (smoking and income) and hypertension.

Measures	Estimates	CI.ll	CI.ul
OR00	1.00	NA	NA
OR01	1.09	0.85	1.40
OR10	3.35	2.95	3.79
OR11	4.02	3.29	4.92
OR(income0 on outcome [smoking1==0]	1.09	0.85	1.40
OR(income0 on outcome [smoking1==1]	1.20	1.00	1.45
OR(smoking1 on outcome [income0==0]	3.35	2.95	3.79
OR(smoking1 on outcome [income0==1]	3.69	3.11	4.37
Multiplicative scale	1.10	0.90	1.35
RERI	0.59	0.03	1.27
AP	0.15	0.00	0.26
SI	1.24	1.01	1.53

#### JOHNSON-NEYMAN INTERVAL

When income is INSIDE the interval [-3.27, 16.87], the slope of smoking is p < .05.

Note: The range of observed values of income is [0.00, 1.00]

SIMPLE SLOPES ANALYSIS

Slope of smoking when income = 0.00 (0):

Slope of smoking when income = 1.00(1):

#### 4.1.2 Stratification

This approach involves estimating a regression model in different strata of the discrete effect modifier income:

The table below summarizes the adjusted odds ratios for smoking across the different income levels (low = 1, and high = 0) as obtained using the stratified approach.

Note that we can obtain the same results by estimating a regression model with an interaction term between the modifier and all covariates:

Value of income	Estimate	2.5 %	97.5 %	z value	p value
1	3.07	2.71	3.47	17.65	0
0	3.59	3.02	4.26	14.57	0

# 4.2 Propensity score matching

#### 4.2.1 Stratification with exact matching within subgroups

We simulate another example dataset using aforementioned DAG, but restrict the sample size to 5000 individuals to reduce computational burden.

```
set.seed(123)
Obs.Data <- sim(DAG = Dset, n = 5000, rndseed = 123)</pre>
```

We first estimate the propensity of smoking in the high-income group (income == 0):

Below, we draw a sample from the high-income group based on the hypothetical example of an association between hypertension and smoking. Here age [centered], gender, education, and diet are covariates.

```
age gender education diet income smoking hypertension distance
657
      6.0810120
                     0
                               1
                                            0
                                                    1
                                                                 1 0.9999874
4932 1.6109860
                     1
                               1
                                            0
                                                    1
                                                                 0 0.9943155
252 -0.2475055
                                    1
                                            0
                                                    0
                                                                 1 0.8525107
                     1
                               1
2693 -0.2511048
                     1
                               1
                                     0
                                            0
                                                    1
                                                                 1 0.8516785
                               0
                                    1
1646 -0.2836155
                     1
                                            0
                                                    1
                                                                 1 0.8439843
        weights subclass
657 1.00000000
                      36
4932 1.00000000
                      50
252 0.03296089
                      25
2693 1.00000000
                      25
1646 1.00000000
                       4
```

Now, we do the same for the low-income group (income == 1):

We estimated the exposure effect from a weighted outcome model for the matched data. While the weights are essential for estimating the point estimate from the outcome model, the subclass variable assists in calculating the robust variance of the exposure effect estimate.

```
cluster = "subclass",
confint = TRUE)
```

Table 4.3: Subgroup-specific treatment effect estimates (expressed in log-OR) from the hypothetical example using the stratified approach.

Value of income	Est.	2.5%	97.5%	z val.	p
		-37.58			
1	1.39	0.94	1.85	6.04	0.00

## 4.2.2 Joint approach without exact matching within subgroups

Here, entire cohort data is used to estimate the propensity scores, and the effect modifier income is considered as a covariate in the propensity score model:

```
ps.formula <- as.formula("smoking ~ age + gender + income")</pre>
match.obj.j <- matchit(ps.formula, data = Obs.Data,</pre>
                       method = "full",
                       distance = "glm",
                       link = "logit")
match.data.j <- match.data(match.obj.j)</pre>
fit.joint.no.exact <- glm(hypertension ~ smoking*income + age + gender,</pre>
                            data = match.data.j,
                            weights = weights,
                            family = binomial("logit"))
require(interactions)
nem.nexp.adj.res <- sim_slopes(fit.joint.no.exact,</pre>
                                 pred = smoking,
                                 modx = income,
                                 robust = "HC1",
                                 cluster = "subclass",
                                 johnson neyman = TRUE,
                                 confint = TRUE,
                                 data = match.data.j)
```

#### 4.2.3 Joint approach with exact matching within subgroups

We specify the moderator variable's name in the exact argument of the matchit function.

Table 4.4: Subgroup-specific treatment effect estimates (expressed in log-OR) from the hypothetical example using the joint approach.

Value of income	Est.	S.E.	2.5%	97.5%	z val.	р
0	3.85	1.00	1.89	5.82	3.84	0
1	1.40	0.28	0.85	1.95	4.99	0

Table 4.5: Subgroup-specific exposure effect estimates (expressed in log-OR) from the hypothetical example using the Joint model, separate matching approach.

Value of income	Est.	S.E.	2.5%	97.5%	z val.	p
0	3.89	1.01	1.92	5.87	3.87	0
1	1.38	0.28	0.84	1.93	4.95	0

#### 4.2.4 Interaction approach without exact matching within subgroups

Analysts incorporate relevant moderator-covariate interactions into the propensity score model that align with biological plausibility. For instance, in the case study we considered an interaction between age (a covariate) and income (a moderator), but did not include other interactions terms.

Table 4.6: Subgroup-specific exposure effect estimates (expressed in log-OR) from the hypothetical example using the interaction approach.

Value of income	Est.	S.E.	2.5%	97.5%	z val.	p
0	3.87	1.00	1.90	5.83	3.86	0
1	1.39	0.28	0.84	1.94	4.95	0

## 4.2.5 Interaction approach with exact matching within subgroups

This method bears resemblance to the interaction approach for propensity score estimation. However, when it comes to matching, researchers match within each moderator subgroup.

# 4.3 Propensity Score Weighting

#### 4.3.1 Common model

This approach adds confounder-moderator interactions in the common weight model.

Table 4.7: Subgroup-specific exposure effect estimates (expressed in log-OR) from the hypothetical example using the interaction model, separate matching approach.

Value of income	Est.	S.E.	2.5%	97.5%	z val.	р
0	3.86	1.00	1.90	5.83	3.85	0
1	1.40	0.28	0.85	1.95	4.99	0

Table 4.8: Subgroup-specific exposure effect estimates (expressed in log-OR) from the hypothetical example using the weighting approach.

Value of income	Est.	S.E.	2.5%	97.5%	t val.	p
0	2.66	0.63	1.42	3.89	4.23	0
1	1.32	0.25	0.83	1.82	5.24	0

We can adjust previous analysis model to adopt stabilized weights for the propensity score (stabilize = TRUE):

Table 4.9: Subgroup-specific exposure effect estimates (expressed in log-OR) from the hypothetical example using stabilized propensity score weights.

Value of income	Est.	S.E.	2.5%	97.5%	t val.	р
0	2.27	0.73	0.84	3.69	3.12	0
1	1.32	0.25	0.83	1.82	5.23	0

## 4.3.2 Separate models

Propensity score weighting approach with weights estimated separately from each subgroup:

Table 4.10: Weight summaries before and after truncation.

Weight	Min.	1st Qu.	Median	Mean	3rd Qu.	Max.
Raw weights	0	0.01	0.11	0.45	1	11.69
1% truncated weights	0	0.01	0.11	0.44	1	7.61

```
family = binomial("logit"))

fit.exp.adj.res1 <- summ(fit2unadj1, confint = TRUE)
fit.exp.adj.res0 <- summ(fit2unadj0, confint = TRUE)</pre>
```

Table 4.11: Subgroup-specific exposure effect estimates (expressed in log-OR) from the hypothetical example using the propensity score weighting approach (Separate weight models).

Value of income	Est.	2.5%	97.5%	t val.	p
0	2.21	1.27	3.15	4.60	0
1	1.34	0.85	1.83	5.36	0

## 4.3.3 Weights from the subgroup balancing propensity scores

Subgroup balancing propensity scores for propensity score weighting:

Table 4.12: Subgroup-specific exposure effect estimates (expressed in log-OR) from the hypothetical example using the subgroup balancing weighting approach.

Value of income	Est.	S.E.	2.5%	97.5%	t val.	p
0	2.68	0.64	1.44	3.92	4.22	0
1	1.32	0.25	0.82	1.82	5.22	0

# 4.4 Covariate adjustment for the propensity score

#### 4.4.1 As continuous covariate

An implementation of propensity scores as a continuous covariate in the outcome model:

```
# Separate models for each subgroup
# For subgroup income = 1
Obs.Data$ps[Obs.Data$income == 1] <- glm(ps.formula,
                                           data = subset(Obs.Data, income == 1),
                                          family = "binomial")$fitted.values
fit2adj1 <- glm(hypertension ~ smoking + age + gender,</pre>
                family = binomial("logit"),
                data = subset(Obs.Data, income == 1))
# For subgroup income = 0
Obs.Data$ps[Obs.Data$income == 0] <- glm(ps.formula,
                                           data = subset(Obs.Data, income == 0),
                                          family = "binomial")$fitted.values
fit2adj0 <- glm(hypertension ~ smoking + age + gender,</pre>
                family = binomial("logit"),
                data = subset(Obs.Data, income == 0))
fit.nexp.adj.res1 <- summ(fit2adj1, robust = TRUE, confint = TRUE)</pre>
fit.nexp.adj.res0 <- summ(fit2adj0, robust = TRUE, confint = TRUE)</pre>
```

Table 4.13: Subgroup-specific exposure effect estimates (expressed in log-OR) from the hypothetical example using Propensity Score as a covariate adjustment approach (considering separate models for each subgroup).

Value of income	Est.	2.5%	97.5%	z val.	p
0	1.16	0.56	1.75	3.83	0
1	1.37	0.96	1.77	6.61	0

Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred

Table 4.14: Subgroup-specific exposure effect estimates (expressed in log-OR) from the hypothetical example using Propensity Score as a covariate adjustment approach (considering a common model).

Value of income	Est.	S.E.	2.5%	97.5%	z val.	р
0	1.17	0.29	0.61	1.74	4.07	0
1	1.43	0.23	0.98	1.87	6.30	0

## 4.4.2 As quantiles

The propensity scores as a categorical covariate, broken by quintiles, in the outcome model.

```
Obs.Data$ps <- glm(ps.formula.with.int,</pre>
                    data = Obs.Data,
                    family = "binomial")$fitted.values
quintiles <- quantile(Obs.Data$ps,
                       prob = seq(from = 0, to = 1, by = 0.2),
                       na.rm = T)
Obs.Data$psq <- cut(Obs.Data$ps, breaks = quintiles,
                    labels = seq(1,5), include.lowest = T)
Obs.Data$psq <- as.factor(Obs.Data$psq)</pre>
fit2adjq <- glm(hypertension ~ (smoking*psq)*income,</pre>
                 family = binomial("logit"),
                 data = Obs.Data)
cq.nexp.adj.res <- sim_slopes(fit2adjq,</pre>
                               pred = smoking,
                                modx = income,
                                confint = TRUE,
                                data = Obs.Data)
```

Table 4.15: Subgroup-specific exposure effect estimates (expressed in log-OR) from the hypothetical example using Propensity Score as a covariate adjustment approach (as quintiles).

Value of income	Est.	S.E.	2.5%	97.5%	z val.	р
0	3.08	0.63	1.85	4.32	4.91	0
1	2.60	0.47	1.68	3.51	5.56	0

# 4.5 Propensity Score Stratification

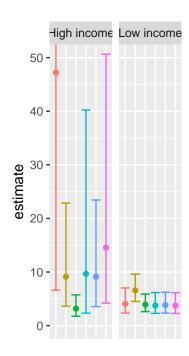
Here is an implementation of propensity score stratification approach by using the marginal mean weighting through stratification (MMWS):

Table 4.16: Subgroup-specific exposure effect estimates (expressed in log-OR) from the hypothetical example using propensity score stratification approach.

Value of income	Est.	S.E.	2.5%	97.5%	z val.	р
0	2.21	0.47	1.29	3.13	4.71	0
1	1.89	0.19	1.51	2.26	9.78	0

# 4.6 Summary

The marginal odds ratios for smoking are summarized below



# method

- PS joint approach (without exact matching)
- PS stratification
- PS stratification with exact matching within subgroups
- PS weighting (common model with stabilized weights)
- PS weighting (separate models)
- PS weighting (weights from the subgroup balancing)

# 5 Dealing with missing data

Johanna Munoz (Julius Center for Health Sciences and Primary Care) Thomas Debray (Smart Data Analysis and Statistics B.V.)

In this example, we consider the estimation of comparative treatment effects in the absence of treatment-effect heterogeneity.

## 5.0.1 Prepare R environment

```
library(mice)
library(dplyr)
library(ggmice)
library(MatchThem)
```

#### 5.0.2 Generating an observational dataset

We can simulate an observational dataset of N = 3000 patients as follows:

```
data_noHTE <- generate_data(n = 3000, seed = 1234)</pre>
```

This dataset does not (yet) contain any missing values;

The simulated dataset contains two treatment groups with differences in baseline characteristics. For example, the figure below shows that we have baseline imbalance in age.

#### 5.0.3 Generating missing values

Missing values can be generated using the function getmissdata(), which considers the following patterns of missingness for the previous number of relapses (prerelapse\_num):

1. MAR: missingness depends on age and sex

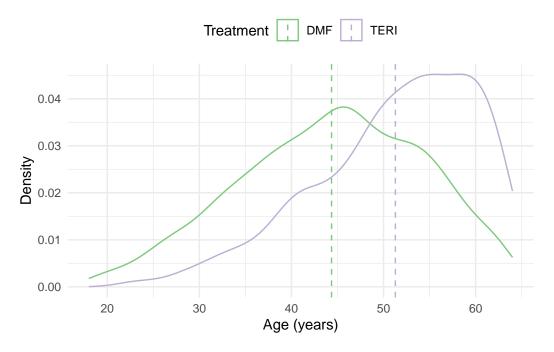


Figure 5.1: Distribution of the EDSS score at each time point

- 2. MART: missingness depends on age, sex and the treatment variable treatment
- 3. MARTY: missingness depends on age, sex, treatment and the outcome variable y
- 4. MNAR: missingness depends on age, sex and prerelapse\_num

```
mdata_noHTE <- getmissdata(data_noHTE, "MART")</pre>
```

After introducing missing values, we only have complete data for N = 946 patients.

# 5.1 Analysis of incomplete data

## 5.1.1 Complete Case Analysis

Below, we describe how to estimate the ATE using propensity score matching.

Table 5.1: Baseline characteristics of the incomplete dataset.

	DMF	TERI	Overall
	(N=2265)	(N=735)	(N=3000)
Age (years)			
Mean (SD)	44.4 (10.0)	51.3 (8.72)	46.2 (10.1)
Median [Min, Max]	45.0 [18.0, 64.0]	53.0 [23.0, 64.0]	47.0 [18.0, 64.0]
Missing	$248 \ (10.9\%)$	57 (7.8%)	$305\ (10.2\%)$
Female Sex			
Yes	$1740 \ (76.8\%)$	526 (71.6%)	2266~(75.5%)
No	525~(23.2%)	209 (28.4%)	$734\ (24.5\%)$
Efficacy of previous	$\mathbf{DMT}$		
None	740 (32.7%)	325 (44.2%)	1065 (35.5%)
Low	190 (8.4%)	59 (8.0%)	249 (8.3%)
Medium or High	830 (36.6%)	246 (33.5%)	1076 (35.9%)
Missing	$505\ (22.3\%)$	$105 \ (14.3\%)$	$610\ (20.3\%)$
Prior medical costs			
Mean (SD)	9970 (10700)	25500 (35400)	13900 (21200)
Median [Min, Max]	6530 [164, 102000]	12500 [259, 337000]	7450 [164, 337000]
Missing	$257 \ (11.3\%)$	52 (7.1%)	$309\ (10.3\%)$
Number of prior sys	mptoms		
0	157 (6.9%)	58 (7.9%)	215 (7.2%)
1	1169 (51.6%)	411 (55.9%)	$1580 \ (52.7\%)$
>=2	435 (19.2%)	159 (21.6%)	594 (19.8%)
Missing	$504\ (22.3\%)$	$107 \ (14.6\%)$	$611\ (20.4\%)$
Number of prior rel	apses		
Mean (SD)	$0.453 \ (0.671)$	$0.408 \; (0.646)$	$0.436 \ (0.662)$
Median [Min, Max]	0 [0, 4.00]	0 [0, 3.00]	0 [0, 4.00]
Missing	1365~(60.3%)	$152\ (20.7\%)$	$1517 \ (50.6\%)$

```
family = binomial,
                   method = "full",
                   caliper = 0.2,
                   estimand = "ATE",
                   replace = FALSE)
  mdata <- as.data.table(match.data(mout))</pre>
  match_mod <- glm("y ~ DMF + offset(log(years))",</pre>
                    family = poisson(link = "log"),
                    data = mdata,
                    weights = weights)
  # Estimate robust variance-covariance matrix
  tx_var <- vcovCL(match_mod, cluster = ~ subclass, sandwich = TRUE)</pre>
We can extract the treatment effect estimate as follows:
  # Treatment effect estimate (log rate ratio)
  coef(match_mod)["DMF"]
       DMF
-0.3685717
  # Standard error
  sqrt(tx_var["DMF", "DMF"])
[1] 0.1521243
```

#### **5.1.2** Multiple Imputation (within method)

In this approach, we will generate m=5 imputed datasets and perform matching within each imputed dataset. We first need to specify how the variables prevDMTefficacy, premedicalcost, numSymptoms, prerelapse\_num and age will be imputed:

```
premedicalcost ~ age + female + logyears + prevDMTefficacy + numSymptoms +
                  treatment + prerelapse_num + y,
                numSymptoms ~ age + female + premedicalcost + logyears + prevDMTefficacy +
                  prerelapse_num + treatment + y,
                prerelapse_num ~ age + female + premedicalcost + logyears + prevDMTefficacy
                  numSymptoms + treatment + y,
                age ~ prerelapse_num + female + premedicalcost + logyears + prevDMTefficacy
                  numSymptoms + treatment + y)
form_y <- name.formulas(form_y)</pre>
# Adopt predictive mean matching for imputing the incomplete variables
imp0 <- mice(impdata, form = form_y, maxit = 0)</pre>
method <- imp0$method</pre>
method["numSymptoms"] <- "pmm"</pre>
method["prevDMTefficacy"] <- "pmm"</pre>
# Generate 5 imputed datasets
imp <- mice(impdata, form = form_y, method = method, m = 5, maxit = 100)</pre>
```

We can now estimate the ATE using propensity score analysis in each of the imputed datasets. We here adopt full matching without replacement.

The results are then combined using Rubin's rules. We adopt robust standard errors to account for clustering of matched individuals.

We can extract the treatment effect estimate and corresponding standard error as follows:

```
# Treatment effect estimate (log rate ratio)
  (match_mod %>% filter(term == "DMF"))$estimate

[1] -0.1554094

# Standard error
  (match_mod %>% filter(term == "DMF"))$std.error

[1] 0.2202132
```

## 5.1.3 Multiple Imputation (across method)

The results are then combined using Rubin's rules. We adopt robust standard errors to account for clustering of matched individuals.

We can extract the treatment effect estimate and corresponding standard error as follows:

```
# Treatment effect estimate (log rate ratio)
(match_mod %>% filter(term == "DMF"))$estimate
```

[1] -0.3461563

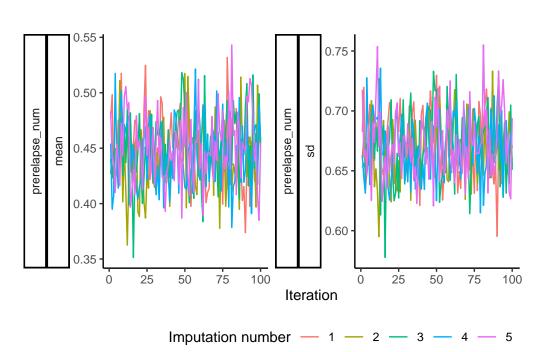
```
# Standard error
(match_mod %>% filter(term == "DMF"))$std.error
```

[1] 0.1351187

# 5.2 Convergence checking

We can inspect convergence for the imputed variable prerelapse\_num using a trace plot:

```
plot_trace(imp, vrb = "prerelapse_num")
```

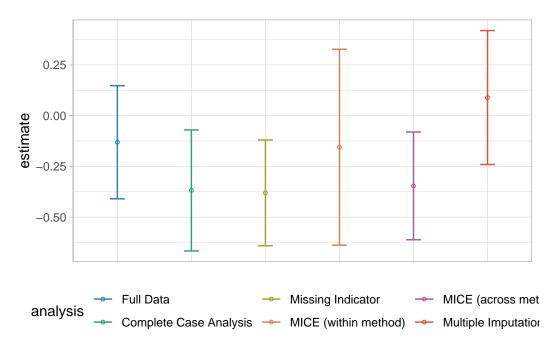


# 5.3 Results

Analysis methods:

• Full Data: The treatment effect is estimated in the original data of N=3000 patients where no missing values are present. This estimate can be used as a benchmark to compare the missing data methods.

- Complete Case Analysis: The treatment effect is estimated using all data from N = 946 patients that do not have any missing values.
- Missing Indicator: The treatment effect is estimated in the incomplete dataset of N=3000 patients. The propensity score model includes a missing indicator variable for each incomplete covariate.
- MICE (within method): A treatment effect is estimated within each imputed dataset using propensity score analysis. Using Rubin's rule, the five treatment effects are combined into a single treatment effect.
- MICE (ITE method): The missing covariates and potential outcomes are imputed simultaneously. Treatment effect estimates are derived by taking the average of the individualized treatment effect estimates Y|DMF Y|TERI.



## Version info

This chapter was developed using the following version of R and its packages:

R version 4.2.3 (2023-03-15 ucrt)

Platform: x86\_64-w64-mingw32/x64 (64-bit) Running under: Windows 10 x64 (build 19044)

Matrix products: default

#### locale:

- [1] LC\_COLLATE=Dutch\_Netherlands.utf8 LC\_CTYPE=Dutch\_Netherlands.utf8
- [3] LC\_MONETARY=Dutch\_Netherlands.utf8 LC\_NUMERIC=C
- [5] LC\_TIME=Dutch\_Netherlands.utf8

#### attached base packages:

- [1] grid stats graphics grDevices utils datasets methods
- [8] base

#### other attached packages:

- [1] ggmice\_0.0.1 table1\_1.4.3 kableExtra\_1.3.4 ggplot2\_3.4.2 [5] missForest\_1.5  $sandwich_3.0-2$ PSweight\_1.1.8 MatchThem\_1.0.1 [9] mice\_3.15.0 cobalt\_4.5.1 WeightIt\_0.14.1 MatchIt\_4.5.3 [13] optmatch\_0.10.6 truncnorm\_1.0-9 MASS\_7.3-58.3 survey\_4.2-1 [17] survival\_3.5-5 Matrix\_1.5-4 data.table\_1.14.8 tidyr\_1.3.0
- [21] dplyr\_1.1.1

[67] gtable\_0.3.3

[70] SuperLearner\_2.0-28 broom\_1.0.4

#### loaded via a namespace (and not attached):

Toda	ca via a namespace (an	na nou autachea).	
[1]	nlme_3.1-162	webshot_0.5.4	RColorBrewer_1.1-3
[4]	httr_1.4.6	numDeriv_2016.8-1.1	tools_4.2.3
[7]	backports_1.4.1	doRNG_1.8.6	utf8_1.2.3
[10]	R6_2.5.1	DBI_1.1.3	colorspace_2.1-0
[13]	nnet_7.3-19	withr_2.5.0	gbm_2.1.8.1
[16]	tidyselect_1.2.0	compiler_4.2.3	cli_3.6.1
[19]	rvest_1.0.3	see_0.7.5	xm12_1.3.3
[22]	labeling_0.4.2	scales_1.2.1	nnls_1.4
[25]	${\tt randomForest\_4.7-1.1}$	systemfonts_1.0.4	stringr_1.5.0
[28]	digest_0.6.31	minqa_1.2.5	rmarkdown_2.21
[31]	svglite_2.1.1	pkgconfig_2.0.3	htmltools_0.5.5
[34]	lme4_1.1-32	fastmap_1.1.1	itertools_0.1-3
[37]	rlang_1.1.0	rstudioapi_0.14	generics_0.1.3
[40]	farver_2.1.1	zoo_1.8-12	jsonlite_1.8.4
[43]	magrittr_2.0.3	Formula_1.2-5	Rcpp_1.0.10
[46]	munsell_0.5.0	fansi_1.0.4	lifecycle_1.0.3
[49]	stringi_1.7.12	chk_0.8.1	<pre>yaml_2.3.7</pre>
[52]	parallel_4.2.3	crayon_1.5.2	lattice_0.21-8
[55]	splines_4.2.3	knitr_1.42	pillar_1.9.0
[58]	boot_1.3-28.1	rngtools_1.5.2	codetools_0.2-19
[61]	glue_1.6.2	evaluate_0.21	mitools_2.4
[64]	vctrs_0.6.1	nloptr_2.0.3	foreach_1.5.2

purrr\_1.0.1

 $xfun_0.39$ 

viridisLite\_0.4.2

[73] tibble\_3.2.1 iterators\_1.0.14 gam\_1.22-2 [76] rlemon\_0.2.1

# 6 Systematic review and meta-analysis of Real-World Evidence

Dimitris Mavridis (University of Ioannina) Thomas Debray (Smart Data Analysis and Statistics B.V.)

We first load the required packages

```
library(dplyr)
library(gemtc)
library(netmeta)
```

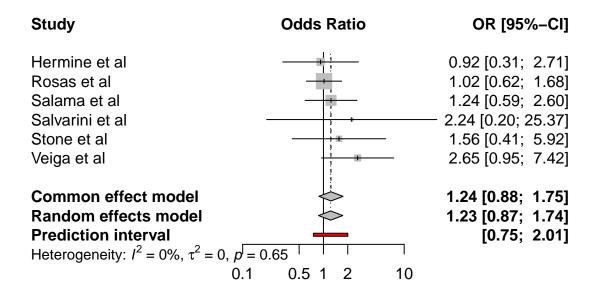
# 6.1 Pairwise meta-analysis of clinical trials

#### 6.1.1 Toculizumab for coronavirus disease 2019

In this example, we consider the results from a systematic literature review of clinical trials investigating any pharmacological in hospitalized patients with coronavirus disease 2019 (Selvarajan et al. 2022). A total of 23 randomized controlled trials were included and studied seven different interventions: dexamethasone, remdesivir, tocilizumab, hydroxychloroquine, combination of lopinavir/ritonavir, favipiravir and interferon. We here focus on the synthesis of 7 trials that comparted toculizumab (TOCI) to standard care (STD) and collected mortality data.

studlab	treat1	treat2	event1	n1	event2	n2
Hermine et al	TOCI	STD	7	63	8	67
Rosas et al	TOCI	STD	58	294	28	144
Salama et al	TOCI	STD	26	249	11	128
Salvarini et al	TOCI	STD	2	60	1	66
Stone et al	TOCI	STD	9	161	3	82
Veiga et al	TOCI	STD	14	65	6	64

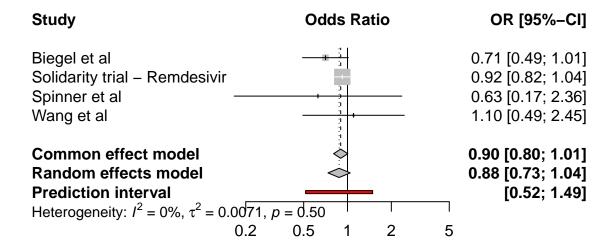
We now conduct a pairwise meta-analysis to assess the pooled effect of tocilizumab versus standard care. For each study, the log odds ratio and corresponding standard error is derived after which the corresponding estimates are pooled using the Mantel-Haenszel method.



Altough a random effects meta-analysis was conducted, no heterogeneity was found ( $\tau$ =0, with a 95% confidence interval ranging from 0 to 0.85).

#### 6.1.2 Remdesivir for coronavirus disease 2019

In aforementioned example, a total of 4 trials compared remdesivir to standard care:



# 6.2 Network meta-analysis of clinical trials

We here use the R packages netmeta for conducting a frequentist network meta-analysis. A detailed tutorial on the use of netmeta is available from the book Doing Meta-Analysis with R: A Hands-On Guide.

#### 6.2.1 Interventions for coronavirus disease 2019

We here consider data from a study which aimed to assess the comparative effectiveness of remdesivir and tocilizumab for reducing mortality in hospitalised COVID-19 patients. 80 trials were identified from two published network meta-analyses (Selvarajan et al. 2022), (Siemieniuk et al. 2020), a living COVID-19 trial database (COVID-NMA Initiative) [Covid-NMA.com], and a clinical trial database [clinicaltrials.gov]. Trials were included in this study if the patient population included hospitalized COVID-19 patients, active treatment was remdesivir or tocilizumab, comparator treatment was placebo or standard care, short-term mortality data was available, and the trial was published. 21 trials were included. For included trials, a risk of bias score was extracted from the COVID-NMA Initiative.

studlab	treat1	treat2	event1	n1	event2	n2
Ader	REM	STD	34	414	37	418
Beigel (ACTT-1)	REM	STD	59	541	77	521
Broman	TOCI	STD	1	57	0	29
Criner	REM	STD	4	384	4	200
Declerq (COV-AID)	TOCI	STD	10	81	9	74
Gordon (REMAP-CAP)	TOCI	STD	83	353	116	358
Hermine (CORIMUNO)	TOCI	STD	7	63	8	67
Horby (RECOVERY)	TOCI	STD	621	2022	729	2094
$\operatorname{Islam}$	REM	STD	0	30	0	30
Mahajan	REM	STD	5	34	3	36
Pan (WHO Solidarity)	REM	STD	602	4146	643	4129
Rosas (COVACTA)	TOCI	STD	58	294	28	144
Rutgers	TOCI	STD	21	174	34	180
Salama (EMPACTA)	TOCI	STD	26	249	11	128
Salvarani	TOCI	STD	2	60	1	63
Soin (COVINTOC)	TOCI	STD	11	92	15	88
Spinner	REM	STD	5	384	4	200
Stone (BACC-BAY)	TOCI	STD	9	161	4	82
Talaschian	TOCI	STD	5	17	4	19
Veiga (TOCIBRAS)	TOCI	STD	14	65	6	64
Wang	REM	STD	22	158	10	78

The corresponding network is displayed below:

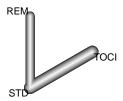


Figure 6.1: Evidence network of the 21 coronavirus-19 trials

We use the following command to calculate the log odds ratios and corresponding standard errors for each study:

# covid <- pairwise(treat = treat, event = event, n = n, studlab = studlab, sm = "OR") head(covid)</pre>

TE	seTE	studlab	treat1	treat2	event1	n1	event2	n2	incr	alls
-0.0819293	0.2483849	Ader	REM	STD	34	414	37	418	0.0	FAI
-0.3483875	0.1851030	Beigel (ACTT-1)	REM	STD	59	541	77	521	0.0	FAI
0.4487619	1.6487159	Broman	TOCI	STD	1	57	0	29	0.5	FAI
-0.6620566	0.7125543	Criner	REM	STD	4	384	4	200	0.0	FAI
0.0170679	0.4904898	Declerq (COV-AID)	TOCI	STD	10	81	9	74	0.0	FAI
-0.4442338	0.1688337	Gordon (REMAP-CAP)	TOCI	STD	83	353	116	358	0.0	FAI

Below, we conduct a random effects network meta-analysis where we consider standard care (STD) as the control treatment. Note that we have one study where zero cell counts occur, this study will not contribute to the NMA as the log odds ratio and its standard error cannot be determined.

```
NMA.covid <- netmeta(TE = TE, seTE = seTE, treat1 = treat1, treat2 = treat2,
                       studlab = studlab, data = covid, sm = "OR", ref = "STD",
                       comb.random = TRUE, common = FALSE, warn = FALSE)
  NMA.covid
Number of studies: k = 20
Number of pairwise comparisons: m = 20
Number of treatments: n = 3
Number of designs: d = 2
Random effects model
Treatment estimate (sm = 'OR', comparison: other treatments vs 'STD'):
                      95%-CI
                                 z p-value
REM 0.8999 [0.8067; 1.0039] -1.89 0.0588
STD
TOCI 0.8301 [0.7434; 0.9268] -3.31 0.0009
Quantifying heterogeneity / inconsistency:
tau^2 = 0; tau = 0; I^2 = 0\% [0.0\%; 48.9\%]
Tests of heterogeneity (within designs) and inconsistency (between designs):
                    Q d.f. p-value
                        18 0.5663
Total
                16.38
Within designs 16.38
                        18 0.5663
Between designs 0.00
```

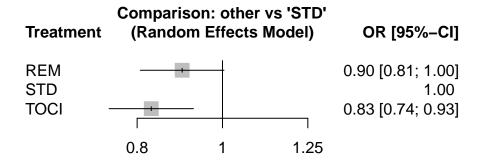
A league table of the treatment effect estimates is given below:

```
netleague(NMA.covid)
```

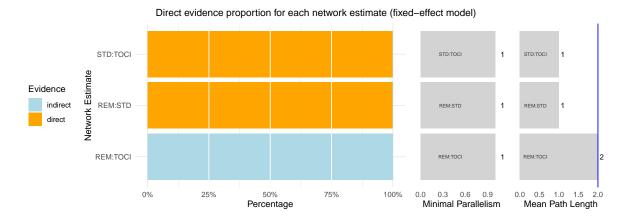
League table (random effects model):

```
REM 0.8999 [0.8067; 1.0039] .
0.8999 [0.8067; 1.0039] STD 1.2047 [1.0789; 1.3451]
1.0842 [0.9282; 1.2663] 1.2047 [1.0789; 1.3451] TOCI
```

We can also present the results in a forest plot:



The figure below shows the percentage of direct and indirect evidence used for each estimated comparison.



We now consider a Bayesian random effects network meta-analysis that analyzes the observed event counts using a binomial link function.

```
bdata <- data.frame(study = studlab,</pre>
                       treatment = treat,
                       responders = event,
                       sampleSize = n)
  network <- mtc.network(data.ab = bdata)</pre>
  model <- mtc.model(network,</pre>
                      likelihood = "binom",
                      link = "log",
                      linearModel = "random",
                      n.chain = 3)
  # Adaptation
  mcmc1 <- mtc.run(model, n.adapt = 1000, n.iter = 1000, thin = 10)
Compiling model graph
  Resolving undeclared variables
  Allocating nodes
Graph information:
   Observed stochastic nodes: 42
   Unobserved stochastic nodes: 45
   Total graph size: 930
```

```
# Sampling
mcmc2 <- mtc.run(model, n.adapt = 10000, n.iter = 100000, thin = 10)</pre>
```

Compiling model graph

Resolving undeclared variables

Allocating nodes

Graph information:

Observed stochastic nodes: 42 Unobserved stochastic nodes: 45

Total graph size: 930

#### Initializing model

We can extract the pooled treatment effect estimates from the posterior distribution. When using STD as control group, we have:

```
summary(relative.effect(mcmc2, t1 = "STD"))
```

Results on the Log Risk Ratio scale

Iterations = 10010:110000
Thinning interval = 10
Number of chains = 3
Sample size per chain = 10000

1. Empirical mean and standard deviation for each variable, plus standard error of the mean:

```
MeanSDNaive SE Time-series SEd.STD.REM-0.10830.098050.00056610.0008072d.STD.TOCI-0.11090.083150.00048000.0008498sd.d0.11340.088830.00051290.0018761
```

2. Quantiles for each variable:

```
2.5% 25% 50% 75% 97.5% d.STD.REM -0.31694 -0.16154 -0.10534 -0.05205 0.08566 d.STD.TOCI -0.25663 -0.16159 -0.11886 -0.06907 0.08273 sd.d 0.00275 0.04497 0.09498 0.16190 0.33112
```

The corresponding odds ratios are as follows:

Comparison	95% CrI
REM vs. STD	0.9 (0.73; 1.09)
TOCI vs. STD	0.89 (0.77; 1.09)
REM vs. TOCI	1.01 (0.74; 1.27)

Finally, we expand the COVID-19 network with trials investigating the effectiveness of hydroxychloroquine (HCQ), lopinavir/ritonavir (LOPI), dexamethasone (DEXA) or interferon- $\beta$  (INTB) (Selvarajan et al. 2022). The corresponding network is displayed below:

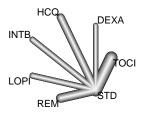


Figure 6.2: Evidence network of the 33 coronavirus-19 trials

We conducted a random effects network meta-analysis, results are depicted below:

```
Number of studies: k = 33

Number of pairwise comparisons: m = 33

Number of treatments: n = 7

Number of designs: d = 6
```

Random effects model

```
Treatment estimate (sm = 'OR', comparison: other treatments vs 'STD'):
         OR
                      95%-CI
                                 z p-value
                                                      95%-PI
DEXA 0.8557 [0.7558; 0.9688] -2.46
                                   0.0139
                                           [0.7463; 0.9812]
HCQ 1.1809 [0.8934; 1.5610]
                                           [0.8786; 1.5872]
                             1.17
                                   0.2428
INTB 1.1606 [0.9732; 1.3841]
                             1.66
                                   0.0973
                                            [0.9604; 1.4026]
LOPI 1.0072 [0.8906; 1.1392] 0.11
                                            [0.8794; 1.1537]
                                   0.9085
REM 0.8983 [0.8014; 1.0070] -1.84 0.0658
                                           [0.7913; 1.0199]
```

We can calculate the P score for each treatment as follows:

```
P-score
TOCI 0.9070
DEXA 0.8357
REM 0.7143
STD 0.4027
LOPI 0.3899
HCQ 0.1336
INTB 0.1166
```

## 6.2.2 Pharmacologic treatments for chronic obstructive pulmonary disease

In this example, we consider the resuls from a systematic review of randomized controlled trials on pharmacologic treatments for chronic obstructive pulmonary disease (Baker, Baker, and Coleman 2009). The primary outcome, occurrence of one or more episodes of COPD exacerbation, is binary (yes / no). For this outcome, five drug treatments (fluticasone, budesonide, salmeterol, formoterol, tiotropium) and two combinations (fluticasone + salmeterol, budesonide + formoterol) were compared to placebo. The authors considered the two combinations as separate treatments instead of evaluating the individual components.

```
data(Baker2009)
```

study	year	id	treatment	exac	total
Llewellyn-Jones 1996	1996	1	Fluticasone	0	8
Llewellyn-Jones 1996	1996	1	Placebo	3	8
Boyd 1997	1997	2	Salmeterol	47	229
Boyd 1997	1997	2	Placebo	59	227
Paggiaro 1998	1998	3	Fluticasone	45	142
Paggiaro 1998	1998	3	Placebo	51	139

Warning: Comparisons with missing TE / seTE or zero seTE not considered in network meta-analysis.

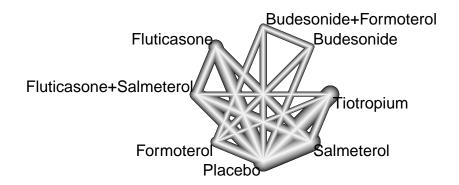
```
Comparisons not considered in network meta-analysis:
studlab treat1 treat2 TE seTE

39 Fluticasone+Salmeterol Placebo NA NA

39 Fluticasone+Salmeterol Salmeterol NA NA

39 Salmeterol Placebo NA NA
```

```
netgraph(NMA.COPD)
```



#### 6.2.3 Advanced Therapies for Ulcerative Colitis

In this example, we consider a systematic literature review of Phase 3 randomized controlled trials investigating the following advanced therapies: infliximab, adalimumab, vedolizumab, golimumab, tofacitinib, ustekinumab, filgotinib, ozanimod, and upadacitinib (Panaccione et al. 2023). This review included 48 RCTs, from which 23 were found eligible for inclusion in a network meta-analysis. The included RCT populations were largely comparable in their baseline characteristics, though some heterogeneity was noted in weight, disease duration, extent of disease, and concomitant medications. A risk of bias assessment showed a low risk of bias for all included RCTs, which were all industry sponsored.

We here focus on the synthesis of 18 trials that contributed efficacy data for induction in bionaive populations. The following FDA- and/or EMA-approved biologic or SMD doses were investigated:

- Adalimumab subcutaneous 160 mg at week 0, 80 mg at week 2, and 40 mg at week 4
   (ADA160/80)
- Infliximab intravenous 5 mg/kg (INF5) at weeks 0, 2, and 6 then every 8 weeks
- Infliximab intravenous 10 mg/kg (INF10) at weeks 0, 2, and 6 then every 8 weeks
- Filgotinib oral 100 mg once daily (FIL100)
- Filgotinib oral 200 mg once daily (FIL200)
- Golimumab subcutaneous 200 mg at week 0 and 100 mg at week 2 (GOL200/100)

- Ozanimod oral 0.23 mg once daily for 4 days, 0.46 mg once daily for 3 days, then 0.92 mg once daily (OZA0.92)
- Tofacitinib oral 10 mg twice daily for 8 weeks (TOF10)
- Upadacitinib oral 45 mg once daily for 8 weeks (UPA45)
- Ustekinumab intravenous 6 mg/kg at week 0 (UST6)
- Vedolizumab intravenous 300 mg at weeks 0, 2, and 6 (VED300)

The reference treatment is placebo (PBO).

Table 6.4: Efficacy outcomes (i.e., clinical remission) data of induction bio-naïve populations

studlab	treat1	treat2	event1	n1	event2	n2
ACT-1	INF10	INF5	39	122	47	121
ACT-1	INF10	PBO	39	122	18	121
ACT-1	INF5	PBO	47	121	18	121
ACT-2	INF10	INF5	33	120	41	121
ACT-2	INF10	PBO	33	120	7	123
ACT-2	INF5	PBO	41	121	7	123
GEMINI 1	VED300	PBO	30	130	5	76
Japic CTI-060298	INF5	PBO	21	104	11	104
Jiang 2015	INF5	PBO	22	41	9	41
M10-447	ADA160/80	PBO	9	90	11	96
NCT01551290	INF5	PBO	11	50	5	49
NCT02039505	VED300	PBO	22	79	6	41
OCTAVE 1	TOF10	PBO	56	222	9	57
OCTAVE 2	TOF10	PBO	43	195	4	47
PURSUIT-SC	GOL200/100	PBO	45	253	16	251
SELECTION	FIL100	FIL200	47	277	60	245
SELECTION	FIL100	PBO	47	277	17	137
SELECTION	FIL200	PBO	60	245	17	137
TRUE NORTH	OZA0.92	PBO	66	299	10	151
U-ACCOMPLISH	UPA45	PBO	54	166	3	81
U-ACHIEVE Study 2	UPA45	PBO	41	145	4	72
ULTRA-1	ADA160/80	PBO	24	130	12	130
ULTRA-2	ADA160/80	PBO	32	150	16	145
UNIFI	UST6	PBO	27	147	15	151

The corresponding network is displayed below:

Below, we conduct a random effects network meta-analysis of the reported study effects (expressed as odds ratio) and consider placebo (treat = "PBO") as the control treatment.

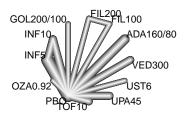


Figure 6.3: Evidence network of 18 trials that contributed efficacy data for induction in bionaive populations

All treatments except FIL100 and UST6 are significantly more efficacious than PBO at inducing clinical remission. We can now estimate the probabilities of each treatment being at each possible rank and the SUCRAs (Surface Under the Cumulative RAnking curve):

```
ADA160/80 FIL100 FIL200 GOL200/100 INF10 INF5 OZA0.92
0.25909091 0.15272727 0.44090909 0.67363636 0.56636364 0.74727273 0.77090909
PBO TOF10 UPA45 UST6 VED300
0.01636364 0.37909091 0.97909091 0.38909091 0.62545455
```

These results indicate that 97.9% of the evaluated treatments are worse than UPA45.

#### Version info

This chapter was developed using the following version of R and its packages:

R version 4.2.3 (2023-03-15 ucrt)

Platform: x86\_64-w64-mingw32/x64 (64-bit)
Running under: Windows 10 x64 (build 19044)

Matrix products: default

#### locale:

- $\hbox{\tt [1] LC\_COLLATE=Dutch\_Netherlands.utf8} \quad \hbox{\tt LC\_CTYPE=Dutch\_Netherlands.utf8} \\$
- [3] LC\_MONETARY=Dutch\_Netherlands.utf8 LC\_NUMERIC=C
- [5] LC\_TIME=Dutch\_Netherlands.utf8

#### attached base packages:

[1] stats graphics grDevices utils datasets methods base

#### other attached packages:

[64] igraph\_1.4.2

[70] abind\_1.4-5

[67] boot\_1.3-28.1

- [1] dmetar\_0.0.9000 netmeta\_2.8-2 meta\_6.2-1 gemtc\_1.0-1
- [5] coda\_0.19-4 dplyr\_1.1.1 kableExtra\_1.3.4

#### loaded via a namespace (and not attached):

[1]	httr_1.4.6	magic_1.6-1	jsonlite_1.8.4
[4]	<pre>viridisLite_0.4.2</pre>	splines_4.2.3	stats4_4.2.3
[7]	metafor_4.0-0	slam_0.1-50	yaml_2.3.7
[10]	robustbase_0.95-1	ggrepel_0.9.3	numDeriv_2016.8-1.1
[13]	pillar_1.9.0	lattice_0.21-8	glue_1.6.2
[16]	digest_0.6.31	rvest_1.0.3	minqa_1.2.5
[19]	colorspace_2.1-0	MuMIn_1.47.5	htmltools_0.5.5
[22]	Matrix_1.5-4	plyr_1.8.8	pkgconfig_2.0.3
[25]	mvtnorm_1.1-3	Rglpk_0.6-5	scales_1.2.1
[28]	webshot_0.5.4	svglite_2.1.1	rjags_4-14
[31]	metadat_1.2-0	lme4_1.1-32	tibble_3.2.1
[34]	farver_2.1.1	<pre>generics_0.1.3</pre>	ggplot2_3.4.2
[37]	withr_2.5.0	nnet_7.3-19	cli_3.6.1
[40]	magrittr_2.0.3	mclust_6.0.0	evaluate_0.21
[43]	fansi_1.0.4	nlme_3.1-162	MASS_7.3-58.3
[46]	truncnorm_1.0-9	forcats_1.0.0	xml2_1.3.3
[49]	class_7.3-22	tools_4.2.3	lifecycle_1.0.3
[52]	stringr_1.5.0	kernlab_0.9-32	munsell_0.5.0
[55]	cluster_2.1.4	fpc_2.2-10	compiler_4.2.3
[58]	systemfonts_1.0.4	rlang_1.1.0	grid_4.2.3
[61]	nloptr_2.0.3	rstudioapi_0.14	CompQuadForm_1.4.3

labeling\_0.4.2

 $flexmix_2.3-19$ 

gtable\_0.3.3

rmarkdown\_2.21
codetools\_0.2-19

R6\_2.5.1

[73] gridExtra_2.3	knitr_1.42	prabclus_2.3-2
[76] fastmap_1.1.1	utf8_1.2.3	mathjaxr_1.6-0
[79] poibin_1.5	modeltools_0.2-23	stringi_1.7.12
[82] parallel_4.2.3	Rcpp_1.0.10	vctrs_0.6.1
[85] DEoptimR_1.0-13	<pre>tidyselect_1.2.0</pre>	xfun_0.39
[88] diptest_0.76-0		

# References

# 7 Dealing with irregular and informative visits

We first load the required packages

```
library(dplyr)
library(broom)
library(ggplot2)
library(mice)
```

## 7.1 Example dataset

Below, we generate an example dataset that contains information on the treatment allocation x and three baseline covariates age, sex and edss (EDSS at treatment start). The discrete outcome y represents the Expanded Disability Status Scale (EDSS) score after time months of treatment exposure. Briefly, the EDSS is a semi-continuous measure that varies from 0 (no disability) to 10 (death).

```
set.seed(9843626)
dataset <- sim_data_EDSS(npatients = 500,</pre>
                          ncenters = 10,
                          follow_up = 12*5, # Total follow-up (number of months)
                          sd_a_t = 0.5,  # DGM - Within-visit variation in EDSS scores
                          baseline_EDSS = 1.3295,
                                                     # DGM - Mean baseline EDDS score
                          sd_alpha_ij = 1.46,  # DGM - Between-subject variation in base
                                              # DGM - Between-site variation in baseline
                          sd_beta1_j = 0.20,
                          mean_age = 42.41,
                          sd_age = 10.53,
                          min_age = 18,
                          beta_age = 0.05, # DGM - prognostic effect of age
                          beta_t = 0.014,  # DGM - prognostic effect of time
                          beta_t2 = 0,  # DGM - prognostic effect of time squared
                          delta_xt = 0, # DGM - interaction treatment time
                          delta_xt2 = 0, # 0.0005
                                                   # DGM - interaction treatment time2
```

```
p_female = 0.75,
beta_female = -0.2 , ## DGM - prognostic effect of male sex
delta_xf = 0, ## DGM - interaction sex treatment
rho = 0.8, # DGM - autocorrelation of between alpha_
corFUN = corAR1, # DGM - correlation structure of the late
tx_alloc_FUN = treatment_alloc_confounding_v2 ) ## or treatment_
```

# **EDSS Prognosis**

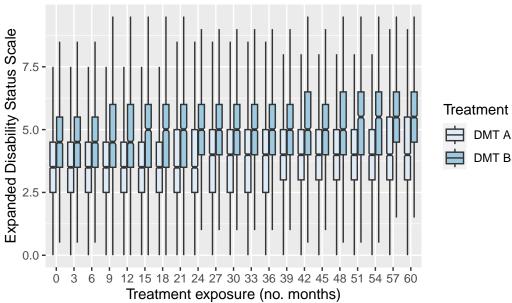


Figure 7.1: Distribution of the EDSS score at each time point

We remove the outcome y according to the informative visit process that depends on the received treatment, gender, and age.

```
dataset_visit <- censor_visits_a5(dataset, seed = 12345) %>%
  dplyr::select(-y) %>%
  mutate(time_x = time*x)
```

In the censored data, a total of 17 out of 5000 patients have a visit at time=60.

### 7.2 Estimation of treatment effect

We will estimate the marginal treatment effect at time time=60.

#### 7.2.1 Original data

#### 7.2.2 Doubly-weighted marginal treatment effect

#### 7.2.3 Multilevel multiple imputation

We impute the entire vector of y\_obs for all 61 potential visits and generate 10 imputed datasets. Note: mlmi currently does not support imputation of treatment-covariate interaction terms.

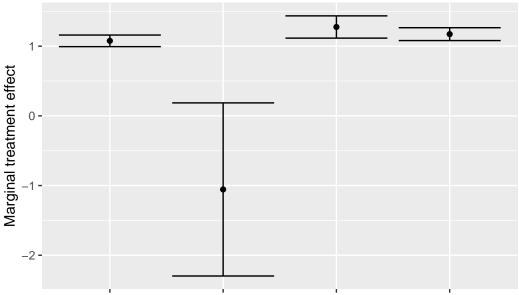
```
imp <- impute_y_mice_31(dataset_visit, seed = 12345)</pre>
```

We can now estimate the treatment effect in each imputed dataset

# 7.3 Reproduce the results using all data to compute the marginal effect with IIV-weighted

#### 7.3.1 Doubly -weighted marginal treatment effect total

#### 7.4 Results



Doubly weighted all times combuitbedweighteMt#60vel Multiple Imputation t=60Reference method

# 8 Prediction of individual treatment effect using data from multiple studies

Orestis Efthimiou (Institute of Social and Preventive Medicine (ISPM))

In this chapter, we discuss statistical methods for developing models to predict patient-level treatment effects using data from multiple randomized and non-randomized studies. We will first present prediction models that assume a constant treatment effect and discuss how to address heterogeneity in baseline risk. Subsequently, we will discuss approaches that allow for treatment effect modification by adopting two different approaches in an IPD-MA context, namely the risk modelling and the effect modelling approach. For both approaches, we will first discuss how to combine IPD from RCTs comparing the same two treatments. We will then discuss how these methods can be extended to include randomized data from multiple treatments, real-world data, and published aggregate data. We will discuss statistical software to implement these approaches and provide example code as supporting information. Real examples will be used throughout to illustrate the main methods.

We hereby provide code for estimating patient-level treatment effects for the case when we have patient-level data from multiple randomized trials.

#### 8.0.1 Example of a continuous outcome

#### 8.0.1.1 Simulate data

We start by simulating an artificial dataset using the R package **bipd**:

```
library(bipd)
ds <- generate_ipdma_example(type = "continuous")</pre>
```

Let us have a look at the dataset:

```
head(ds)
```

Table 8.1: The simulated dataset with a continuous outcome

	0	1	Overall
	(N=280)	(N=320)	(N=600)
z1			
Mean (SD)	0.00453 (1.05)	$0.0842 \ (0.996)$	0.0470 (1.02)
Median [Min, Max]	0.0424 [-3.32, 3.60]	0.0932 [-2.42, 2.99]	0.0670 [-3.32, 3.60]
z2			
Mean (SD)	-0.0129 (1.02)	-0.0320 (0.994)	-0.0231 (1.01)
Median [Min, Max]	-0.0189 [-2.57, 3.43]	-0.0832 [-2.95, 2.92]	-0.0351 [-2.95, 3.43]
$\operatorname{studyid}$			
1	$46 \ (16.4\%)$	54 (16.9%)	$100 \ (16.7\%)$
2	51 (18.2%)	49 (15.3%)	100 (16.7%)
3	47 (16.8%)	53 (16.6%)	100 (16.7%)
4	50 (17.9%)	50 (15.6%)	100 (16.7%)
5	40 (14.3%)	60 (18.8%)	100 (16.7%)
6	46 (16.4%)	54 (16.9%)	100 (16.7%)

	studyid	treat	z1	<b>z</b> 2	у
1	1	0	0.9753016	-0.2599767	11
2	1	1	0.5335720	-0.5522604	6
3	1	0	-0.9011067	1.5785622	11
4	1	0	-1.3821428	0.9132537	11
5	1	0	0.5272515	0.6478884	11
6	1	0	0.7369785	0.9802165	11

The simulated dataset contains information on the following variables:

- the treatment indicator treat, which takes the values 0 for control and 1 for active treatment
- $\bullet$  two prognostic variables z1 and z2
- the continuous outcome y
- a trial indicator studyid

#### 8.0.1.2 Perform analysis

We synthesize the evidence using a Bayesian random effects meta-analysis model. The model is given in Equation 16.7 of the book. First we need set up the data and create the model:

The JAGS model can be accessed as follows:

```
ipd$model.JAGS
function ()
    for (i in 1:Np) {
        y[i] ~ dnorm(mu[i], sigma)
        mu[i] <- alpha[studyid[i]] + inprod(beta[], X[i, ]) +</pre>
            (1 - equals(treat[i], 1)) * inprod(gamma[], X[i,
                ]) + d[studyid[i], treat[i]]
    }
    sigma ~ dgamma(0.001, 0.001)
    for (j in 1:Nstudies) {
        d[j, 1] \leftarrow 0
        d[j, 2] ~ dnorm(delta[2], tau)
    }
    sd \sim dnorm(0, 1)
    T(0,)
    tau <- pow(sd, -2)
    delta[1] <- 0
    delta[2] ~ dnorm(0, 0.001)
    for (j in 1:Nstudies) {
        alpha[j] ~ dnorm(0, 0.001)
    }
    for (k in 1:Ncovariate) {
        beta[k] ~ dnorm(0, 0.001)
    }
    for (k in 1:Ncovariate) {
        gamma[k] ~ dnorm(0, 0.001)
    }
}
<environment: 0x0000024dbefe6c10>
```

We can fit the treatment effect model as follows:

Compiling model graph
Resolving undeclared variables
Allocating nodes
Graph information:

Observed stochastic nodes: 600 Unobserved stochastic nodes: 19

Total graph size: 6034

Initializing model

Here are the estimated model parameters:

```
summary(samples)
```

Iterations = 2001:2020
Thinning interval = 1
Number of chains = 2
Sample size per chain = 20

1. Empirical mean and standard deviation for each variable, plus standard error of the mean:

```
Mean
                      SD Naive SE Time-series SE
alpha[1] 10.9627 0.05398 0.008535
                                        0.011004
alpha[2] 7.9897 0.05497 0.008692
                                        0.008720
alpha[3] 10.4637 0.05789 0.009153
                                        0.010889
alpha[4] 9.6431 0.04469 0.007067
                                        0.007159
alpha[5] 12.9361 0.07083 0.011199
                                        0.015200
alpha[6] 15.9006 0.05371 0.008493
                                        0.017285
beta[1]
         0.2052 0.01704 0.002694
                                        0.002532
beta[2]
         0.2901 0.02161 0.003418
                                        0.005191
delta[1] 0.0000 0.00000 0.000000
                                        0.000000
delta[2] -2.3707 0.80802 0.127759
                                        0.106608
gamma[1] -0.5404 0.02647 0.004186
                                        0.004095
gamma[2] 0.5927 0.03136 0.004958
                                        0.006968
sd
         2.0794 0.41767 0.066040
                                        0.119153
```

#### 2. Quantiles for each variable:

```
2.5%
                    25%
                            50%
                                   75%
                                         97.5%
alpha[1] 10.8564 10.9210 10.9737 11.0017 11.0558
        7.8940 7.9466 7.9908 8.0393 8.0704
alpha[3] 10.3824 10.4262 10.4575 10.4981 10.5943
alpha[4] 9.5589 9.6231 9.6441 9.6700 9.7093
alpha[5] 12.8068 12.8937 12.9368 12.9683 13.0748
alpha[6] 15.8038 15.8681 15.9028 15.9361 15.9894
beta[1]
         0.1691 0.1966 0.2045 0.2166 0.2369
beta[2]
         0.2520 0.2807 0.2923 0.3027 0.3241
delta[1] 0.0000 0.0000 0.0000 0.0000 0.0000
delta[2] -4.1413 -2.7365 -2.3399 -1.9803 -1.0305
gamma[1] -0.5852 -0.5564 -0.5362 -0.5219 -0.5008
gamma[2] 0.5390 0.5688 0.5904 0.6129 0.6539
sd
         1.3300 1.8293 2.0270 2.3425 2.8810
```

We can now predict treatment effects for a new patient with covariate values z1=1 and z2=0.5.

We can also predict treatment benefit for all patients in the sample, and look at the distribution of predicted benefit.

```
library(dplyr)
library(ggplot2)

ds <- ds %>% mutate(benefit = NA)

for (i in seq(nrow(ds))) {
   newpat <- as.matrix(ds[i, c("z1", "z2")])
   ds$benefit[i] <- treatment.effect(ipd, samples, newpatient = newpat)["0.5"]
}

ggplot(ds, aes(x = benefit)) + geom_histogram() + facet_wrap(~studyid) +
   xlab("Predicted treatment benefit")</pre>
```

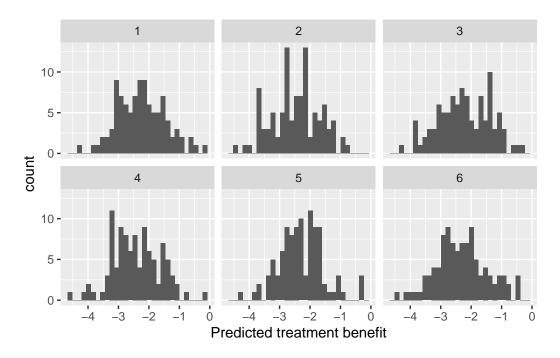


Figure 8.1: Distribution of predicted treatment benefit in each trial

Let us repeat the analysis, but this time while penalizing the treatment-covariate coefficients using a Bayesian LASSO prior.

The model is as follows:

```
for (j in 1:Nstudies) {
        d[j, 1] \leftarrow 0
        d[j, 2] ~ dnorm(delta[2], tau)
    sd \sim dnorm(0, 1)
    T(0,)
    tau \leftarrow pow(sd, -2)
    delta[1] <- 0
    delta[2] ~ dnorm(0, 0.001)
    for (j in 1:Nstudies) {
        alpha[j] ~ dnorm(0, 0.001)
    for (k in 1:Ncovariate) {
        beta[k] ~ dnorm(0, 0.001)
    tt <- lambda * sigma
    lambda <- pow(lambda.inv, -1)</pre>
    lambda.inv ~ dunif(0, 5)
    for (k in 1:Ncovariate) {
        gamma[k] ~ ddexp(0, tt)
    }
}
<environment: 0x0000024dc5069118>
To do the analysis we run:
  samples <- ipd.run(ipd, n.chains=2, n.iter=20,</pre>
                      pars.save = c("alpha", "beta", "delta", "sd", "gamma"))
Compiling model graph
   Resolving undeclared variables
   Allocating nodes
Graph information:
   Observed stochastic nodes: 600
   Unobserved stochastic nodes: 20
   Total graph size: 6039
Initializing model
  round(treatment.effect(ipd, samples, newpatient = c(1,0.5)), 2)
```

#### Example of a binary outcome

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